The Syntax Definition Formalism SDF

-Reference Manual

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Depariment of Software Technology, Centre for Mathematics and Computer Science P.O. Box 4079, 1009 AB Amsterdam, The Netherlands SDF is a formalism for the definition of syntax which is comparable to BNF in some respects, but has a wider scope in that it also covers the definition of lexical and abstract syntax. Its design and implementation are tailored towards the language designer who wants to develop new languages as well as implement existing ones in a highly interactive manner. It emphasizes compactness of syntax definitions by offering (a) a standard interface between lexical and context-free syntax; (b) a standard correspondence between context-free and abstract syntax; (c) powerful disambiguation and list constructs; and (d) an efficient incremental implementation which accepts arbitrary context-free syntax definitions. SDF can be combined with a variety of programming and specification languages. In this way these obtain fully general user-definable

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1. INTRODUCTION

1.1 General design considerations

Since good notations may improve the readability of programs and other formal specifications considerably, many programming and specification languages give the user some control over the syntax that can be used. We refer the interested reader to Section 11.4 of this manual for a brief survey of the development of user-definable syntax. Although an issue of general importance, user-definable syntax becomes a sine qua non if a language is to be used for defining other languages. A language definition expressed in such a meta-language might consist of the following

• a definition of the concrete (i.e., lexical and context-free) as well as abstract syntax of the language to be defined;

a definition of its static semantics; and

a definition of its dynamic semantics.

In the GIPE project (Generation of Interactive Programming Environments - ESPRIT Project 348 [HKKL85]) we are constructing an environment for the interactive development and implementation of languages and it is in this context that we designed SDF to handle the syntax part of languages.

Although the static and dynamic semantics parts of language definitions do not concern us in this manual, coupling semantics to syntax does, and this is one of the points where abstract syntax comes in. From the viewpoint of concrete syntax it is natural to describe this coupling in terms of string or text matching. A string pattern containing variables is matched to the program text. If the matching succeeds at some point in the text, the corresponding string values of the variables are transmitted to the semantic rule attached to the pattern. In practice, however, the use of string matching gives rise to ambiguities that are difficult to control. We therefore decided that semantic should be coupled to syntax by means of tree matching, which is much less susceptible to unintended ambiguities.

Now the question arises whether the parse tree or the abstract syntax tree of the program text should be used. The parse tree is the derivation showing how the text in question can be derived from the start symbol of the grammar. Its interior nodes are non-terminals of the grammar and its leaves are the lexical tokens, such as keywords, operator symbols, identifiers, etc., making up the original text. The abstract syntax tree only contains the essential information describing the text; its interior nodes are the constructors (also called operators) of the language and the direct descendants of each node are its operands. The leaves of the abstract syntax tree are identifiers, integer constants, etc. The main argument in favor of performing matching on the basis of abstract syntax trees rather than parse trees is that the latter may contain many "unnecessary" nodes that can be omitted in the abstract syntax tree.

SDF supports patterns with variables by allowing the declaration of a (possibly infinite) number of variables with user-defined names in the variables-section of a syntax definition. A text containing variables (a text pattern) corresponds to an abstract syntax tree with variables (a tree pattern or an open term). The actual matching uses the abstract syntax tree pattern. Texts with variables may also be viewed as being incomplete, the variables playing the role of gaps that have yet to be fill. A in.

It should be emphasized that a coupling of semantics to syntax based on abstract syntax tree matching does not preclude the use of concrete syntax in the semantics parts of a language definition. In fact, we are very much in favor of doing this. The price to be paid is a discrepancy between the text matching viewpoint, which is strongly suggested by the use of concrete syntax and the abstract syntax tree matching viewpoint, which is the one actually intended. To minimize the gap separating both viewpoints, SDF implicitly defines a standard translation from contextine

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free to abstract syntax, i.e., the translation from context-free to abstract syntax is the same for all definition formalism Metal [KLMM83]. The abstract and context-free syntax defined by a Metal specification may differ from each other in important respects not reproducible in SDF. For example, the order of the arguments of the abstract and concrete forms of a function need not be the same in Metal. For the reason given above, we believe a uniform and predictable relationship between abstract and context-free syntax to be a distinct advantage. If required, transformation of ubstract syntax trees to some "deeper" form has to be expressed in the programming or specification language in which SDF is embedded. In our case this is the algebraic specification formalism SDF-definitions. This implies that SDF has less expressive power than, for instance, the syntax ASF [BHK89, Chapter 1], in which we express the static and dynamic semantics of languages.

guage definition [Log88, DK89a,b] and this is a second point where abstract syntax comes in. Syntax-directed movements through the text can be performed much more efficiently on the basis of the corresponding abstract syntax tree than on the basis of the parse tree. As explained above, the latter generally contains many redundant nodes which give rise to void text movements that may be quite irritating. On the other hand, text movements on the basis of abstract syntax cannot become too unpredictable due to the fixed correspondence between abstract and context-free syn-In the GIPE environment a syntax-directed editor is generated from the syntax part of a lantax enforced by SDF.

means that context-free and abstract syntax may bear a closer resemblance to each other, which is free power is available, syntax definitions no longer have to be brought into an acceptable, but often unnatural form that obeys the restrictions imposed by the implementation. This in turn developed independently from each other should be facilitated. Using SDF, the language designer We therefore adopted the viewpoint that SDF would not only have to allow definition of all context-free languages (BNF also permits this), but that its implementation would have to support this feature without reserve and impose no additional LR- or LL-like constraints. This is an advantage in another respect as well which has nothing to do with modularization. If full context-Although we do not discuss modular SDF-definitions in this manual, modularity has been an important design issue from the outset. In particular, putting together SDF-definitions that were should be able to borrow parts of already existing language definitions without undue difficulty. exactly what SDF requires.

An important question remains, however: what about ambiguous syntax definitions? This is a Usually, ambiguous definitions are eliminated by applying the LR- or LL-constraints we just dismissed as too limiting for the language designer. In the general case supported by our implementation, ambiguous definitions are handled correctly in the sense that all parses of an ambiguous sentence are returned, but freedom from ambiguities can no longer be guaranteed in advance due to the fact that it is no longer decidable. Obviously, unexpected ambiguities may cause fatal run-time errors. On the other hand, allowing syntactic ambiguities leaves room for semantic disambiguation schemes, similar perhaps to some of the ones people use to disambiguate sentences difficult problem, which is not solved by SDF but which has had implications for its design.

problem of unexpected syntactic ambiguities, of course. It only helps the language designer to parse trees (if any) are compared using a multiset ordering derived from the priority rules given in Whereas semantic disambiguation falls outside its scope, SDF attempts to alleviate the problem of syntactic disambiguation by offering a powerful priority construct. This does not solve the eliminate sources of ambiguity he is already aware of. Syntactic disambiguation proceeds in two phases: (1) all parse trees containing internal priority conflicts are rejected, and (2) the remaining The power of the priority mechanism is such that unambiguous SDF-definitions can be given for the SDF-definition. Unlike the first phase (which handles ordinary arithmetical expressions, for instance), the second phase allows parses that are totally different to be compared with each other.

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biguous context-free grammar. This does not mean, however, that every desired disambiguation can be obtained by adding appropriate priorities to a given ambiguous SDF-definition without some inherently ambiguous context-free languages, i.e., languages that do not have an unam-

The availability of a separate disambiguation construct means that disambiguation need not be tioned before, this is an important reason why the fixed correspondence between context-free and expressed in terms of the syntax rules themselves. As a result, parse trees will be much smaller and closer to abstract syntax trees. In addition to the availability of full context-free syntax menabstract syntax offered by SDF turns out to be satisfactory.

text-free level, but is primarily based on giving precedence to the longest lexemes and to literals occurring in the context-free syntax. Any remaining ambiguities are passed on to the context-free In addition to context-free and abstract syntax, lexical syntax can also be defined in SDF. Lexical disambiguation cannot be controlled by means of the priority mechanism available at the con-

disambiguation and list constructs, and (d) an efficient incremental implementation which accepts Its design and implementation are tailored towards the language designer who wants to develop new languages as well as implement existing ones in a highly interactive manner. It emphasizes compactness of syntax definitions by offering (a) a standard interface between lexical and contextarbitrary context-free syntax definitions. It can be combined with a variety of programming and In summary, SDF allows the definition of concrete and abstract syntax in a single framework. free syntax; (b) a standard correspondence between context-free and abstract syntax; (c) powerful specification languages. In this way these obtain fully general user-definable syntax.

1.2. A first example

An SDF definition consists of five sections and has the following overall structure:

```
names of domains or non-terminals to be used in the other sections of the specification
                                                                                                                                                     definition of priority relations between rules of the context-free syntax
                                                                                             text-free syntax
the rules of the concrete and abstract syntax
                                                                                                                                                                                                                 naming schemes for variables
                                               lexical syntax
the rules of the lexical syntax
                                                                                             context-free
                                                                                                                                          priorities
                                                                                                                                                                                             variables
sorts
```

We introduce the most significant features of SDF by means of an example in which we define the lexical, concrete and abstract syntax of a simple programming language (see Figure 1.1.).

In the sorts section, six names are declared. These names can be interpreted in two ways: as non-terminals of a lexical or a context-free grammar, and

- as names of the domains used to construct abstract syntax trees.

We will use this dual interpretation of sorts to achieve an automatic mapping between sentences and abstract syntax trees.

In the lexical syntax section, we define a space, a tabulation, and a newline character as layout characters (line 3). In addition, the form of identifiers (line 4) and numeric constants (line is defined.

In the context-free syntax section, the concrete and abstract syntax are defined:

- The concrete syntax is obtained by using the "non-terminal" interpretation of sorts and reading the rules from "right to left" as ordinary grammar rules.
- The abstract syntax is obtained by using the "domain" interpretation of sorts and reading the rules from left to right as definitions of (typed) constructor functions for abstract syntax

trees. The sort names appearing in function definitions define the types of the arguments as well as of the result of these functions.

Some other features illustrated by the context-free syntax in Figure 1.1 are:

- Rules can define lists with or without separators (line 9).
- Rules may have a bracket attribute. Such rules are used only for grouping language constructs, but do not contribute to the abstract syntax (lines 8 and 17).
- Rules may have various attributes defining their associativity properties (lines 13-16). We allow the definition of associative and left-, right-, or non-associative operators.

In the priorites section, priority relations between rules in the context-free syntax are defined as well as the associativity of groups of different operators. As shown here, the operators * and / have a higher priority than the operators + and -.

Finally, in the wartables section, naming schemes for variables are given. These variables can be used in two ways:

- as variables in semantics definitions added to the SDF definition,
- as "holes" in programs during syntax-directed editing.

```
non-assoc}
left}
                                                                                        non-assoc}
                                       SERIES (bracket)
                                                                                              bracket)
                                                                        left)
                                                                                                                   EXP) >
                                                       STATEMENT
STATEMENT
                                                  STATEMENT
                                  PROGRAM
           --> LAYOUT
                                             SERIES
                                                                                                                    "/" EXP ->
                       -> NAT
                                                                        EXP
EXP
EXP
EXP
EXP
                                                                                                   EXP
sorts ID NAT PROGRAM STATEMENT SERIES EXP
                                  <u>^</u> ^
                Ŷ
                                             Ŷ
                                                        ^ ^
                                                 Ŷ
                                                                        ^ ^ ^ ^
                                                                                        Ŷ
                                                                                              Ŷ
                                                                                                                    EXP
                                                 ":=" EXP
EXP then SERIES else SERIES
                                                                                                                    EXP, 1
                                                                                                                    ^ ^
                                                                                                                                          SERIES
                            context-free syntax
                                                             SERIES
                                                                                                                    EXP
                                           ( STATEMENT ";" )*
                                                                                                                                     EXP
                                program SERIES
begin SERIES end
  [a-z] [a-z0-9]*
                                                                                                                   (left: EXP "*" (left: EXP "+"
                                                                                                                                     ^ ^
                                                             until EXP do
                                                                                  "*" EXP
                                                                             EXP
                                                                                                              priorities
                                                                             EXP "-" |
EXP "*" |
EXP "/" |
                                                                                                                               variables
                                                                            +[6-0]
      lexical
                                                                                                                                          Series
                                                  ΩI
  13.
```

Figure 1.1. A simple programming language.1

1.3. Organization of this manual

The chapters of this manual can be divided in three groups, Chapters I and 2 have an introductory character; the main issues in the design of SDF are discussed and basic concepts and notations are introduced.

The second group of chapters contains the actual description of SDF. Each of the Chapters 3, 4, 5, 6 and 7 is devoted to a detailed description of one of the five sections of an SDF definition. Chapter 8 contains a summary of these definitions.

In the last group, miscellaneous subjects are addressed. In Chapter 9, we show how semantic rules can be attached to SDF definitions. This leads to specification formalisms with considerable syntactic freedom. In Chapter 10, the techniques required to implement SDF are sketched. A discussion of the results obtained and a comparison with related work is given in Chapter 11.

Two appendices complete this manual: they present SDF definitions of SDF itself and of erkeley Pascal.

2. PRELIMINARY DEFINITIONS

In this Chapter we introduce the basic notions to be used in the definition of SDF: regular grammars (Section 2.1), context-free grammars (Section 2.2), and signatures (Section 2.3). In Section 2.4 follows a motivation for these definitions, and in Section 2.5 we give an overview of the SDF definition and show how the basic notions are used in it.

2.1. Regular grammars

Regular expressions over a given alphabet Σ have the usual meaning [ASU85]. With each regular expression r, we associate a language L(r) of lexemes accepted by r:

- (1) The empty string ε is a regular expression with associated language $L(\varepsilon) = \emptyset$.
- (2) If $a \in \Sigma$, then "a" is a regular expression with associated language $L("a") = \{a\}$.
- Suppose r and s are regular expressions with associated languages L(r) and L(s), then (a) $(r) \mid (s)$ is a regular expression with the associated language $L(r) \cup L(s)$ of lexemes that are either in L(r) or in L(s).
- (b) (c) (s) is a regular expression with the associated language L(r) L(s) of lexemes consisting of a concatenation of two parts: the first part in L(r) and the second part in L(s).
- (c) $(r)^*$ is a regular expression with the associated language $L(r)^*$ of lexemes consisting of zero or more concatenations of lexemes in L(r).
- (e) (r) is a regular expression with associated language L(r), i.e., parentheses may be placed around a regular expression without changing its meaning.

We will extend this definition in the following ways:

- (r)+ is a regular expression with the associated language L(r)+ of lexemes consisting of one or more concatenations of lexemes in L(r). Note that (r)+ = (r) (r)*.
- Parentheses may be omitted by using the following priorities for the operators (going from high to low priority): * and +, concatenation, and |. In addition to this, the concatenation and |-operator are left-associative.
 - We will use string constants to abbreviate sequences of concatenations of single characters
 of the alphabet, i.e., "a," "a," "will be abbreviated to "a10," a,".
 - of the alphabet, i.e., " a_1 " " a_2 " ... " a_n " will be abbreviated to " a_1a_2 ... a_n ". A lexical non-terminal of the form < N > is also a regular expression (see below).

A regular grammar is now defined as an ordered list of named regular expressions. To emphasize the fact that they are similar to non-terminals in context-free grammars, we call names of regular expressions *lexical non-terminals*. The occurrence of a lexical non-terminal in a regular expression is to be interpreted as an abbreviation for the regular expression associated with it earlier in the list. The general form of a regular grammar is thus:

$$\langle N_1 \rangle = r_1$$

$$\langle N_2 \rangle = r_2$$
...
$$\langle N_k \rangle = r_k$$

v,

the all examples, we will add *line numbers* to SDF definitions for ease of reference in the text. They are not a part of the SDF definition proper.

grammar is the union of the languages associated with each r_I . We will use lexical non-terminals where $\langle N_i \rangle$ may only occur in r_j provided that i < j. The language associated with this regular to identify the lexical category of lexemes and call a (lexical non-terminal, lexeme)-pair a lexical

mar are written between angle brackets < and >. They may consist of arbitrary symbols except < We will use a variant of the well-known BNF notation to define the grammars corresponding to rules between double quotes ("), or lexical non-terminals. Lexemes are strings over a given charand >. We will use the convention that lexical non-terminals have the suffix -LEX. A grammar rule consists of a non-terminal, the symbol :: =, and a list of zero or more rule-elements. An acter alphabet and have to be defined by a separate regular grammar. Non-terminals of the gram-SDF definitions. The terminals of a grammar are either literal strings, which appear in grammar empty list of rule-elements is denoted by the symbol E. A rule-element is either

- a terminal or non-terminal, or
- (<non-terminal> sep)⊗, where sep is an optional terminal and ⊗ is either * or +. This rated by sep. When sep is not present, the brackets may be omitted and the rule-element is denotes a list of zero or more (*) or one or more (+) repetitions of the non-terminal sepaabbreviated to <non-terminal>⊗

We will use the symbol | to abbreviate rules with the same right-hand side, i.e.

```
<N> :: " Rhs1 | Rhs2,
```

is equivalent to

<N> ::= Rhs1

Each non-terminal in the grammar acts as a start symbol.

A parse tree for a combination of a given regular grammar and a given BNF grammar is an Nodes are either labeled with a lexical non-terminal, a non-terminal, or a list. This is described in ordered labeled tree. Leaves of the tree are either literals of the grammar or characters of lexemes. more detail in the following definition.

An ordered labeled tree P is a parse tree for a given regular grammar and BNF grammar if

- (i) the root of P is labeled with L, where L is a lexical non-terminal, all its children are labeled with characters from the lexical alphabet, and the characters together form a lexeme accepted by the regular expression associated with L in the regular grammar, or
- the root of P is labeled with <non-terminal>, has children $C_1,...,C_n$ (n ≥ 0) whose root is labeled with $X_1, ..., X_n$, the rule <non-terminal>::= $X_1...X_n$ is a rule of the grammar and all Ci's are either parse trees or literals, or (5)
- (3) the root of P is labeled with $\{\text{cnon-terminal} > \text{sep}\} \otimes$, has children $G_1,...,G_n$ $(n \ge 0)$ if $\otimes =^*$, $n \ge 1$ if $\otimes =+$) and either
- (a) sep is empty and all n children are parse trees labeled with <non-terminal> or (b) sep is not empty, n is either zero or odd, all odd-numbered children are parse trees whose root is labeled with <non-terminal>, while all even-numbered children are equal to

Consider, for instance, the following BNF grammar

::= "decl" (<ID> ",")+ ":" <TYPE> ::= "integer" ::= "real" ::= <ID-LEX> <TYPE><TYPE><ID> <DECL>

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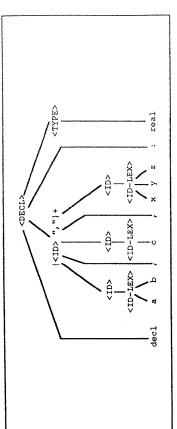


Figure 2.1, Parse tree for the sentence: decl ab, c, xyz : real.

and the regular grammar

= "a" | ... | "z" = <LETTER-LEX>+ <LETTER-LEX>

the sentence decl ab, c, xyz : real is shown in Figure 2.1. Note that the lexeme for each The literals of the BNF grammar are: "dec1", ", ", "; ", "integer", and "real". <1D-LEX> is the only lexical token. The non-terminals are <DECL>, <ID> and <TYPE>. The parse tree for <ID-LEX> is represented by a sequence of characters. Any structure appearing in the rules defining <ID-LEX> is lost in the parse tree.

In the sequel, we will add all literals occurring in the BNF grammar to the regular grammar and will identify an occurrence of the literal with an occurrence of the corresponding lexical non-terminal (see Section 5.2).

2.3. Signatures

The abstract syntax corresponding to an SDF definition will be described by a signature, which defines a set of abstract syntax trees (also known as terms). It consists of three parts:

- Declarations of sorts defining the basic domains of trees. For each declared sort s (basic implicitly defined (list sorts)1. They denote lists of, respectively, zero or more and one or sort), the sorts (S sep)* and (S sep)+, with sep an arbitrary identifier or empty, are more elements of sort s. The symbol sep is part of the list constructor and lists with elements of the same sort but different separators are distinct. Like before, we will use the abbreviation ⊗ to denote either * or +.
- A strict (i.e., non-reflexive) partial order on sorts defining inclusion relations between sorts (subsorts). This partial order is obtained by taking the transitive closure of the subsort declarations in the signature. In addition to this, the following subsort relations hold automatically:
 - (a) (s sep)+ < (s sep)* for all basic sorts s;
- (b) {s sep}⊗ < {s' sep}⊗ for all basic sorts s and s' with s < s'. Note that the relations s < s+ or s < s * do not hold automatically!
- Declarations of functions defining nodes in the tree by giving for each function a name, the number and sort of its children (arguments), and its result sort. The result sort of a function must always be a basic sort. Only the argument sorts may be list sorts. Functions without

To Chapter 7 we will also use lexical non-terminals with the suffix -VAR; they denote the contributions of ariable declarations to the lexical grammar.

¹ An occurrence of (S sep)* or (S sep)+ thus implicitly declares sep as a (varyadic) constructor function for lists with elements of sort s.

arguments are also called constants. The attribute assoc denotes an associative function and may be attached to binary functions with identical argument and result sorts.

We will adopt the convention that names of sorts, functions and separators in signatures either consist solely of alphanumeric characters and hyphens (e.g., a-sort-name) or, if not, are surrounded by double quotes (e.g., "/").

are implicitly defined and they are denoted by a sort, followed by a hyphen, followed by a Signatures do not contain a separate section for the declaration of variables. Instead, variables (possibly quoted) identifier (e.g., NAT-x denotes a variable of sort NAT, and (ID ",")+-Ids denotes a variable of sort (ID ",")+). Note that variables may range both over basic sorts as well

Trees can be constructed by combining functions and variables in ways compatible with their definition, i.e., each child of each node in the tree should be of a sort that is identical to or smaller than the one appearing in the declaration of the function corresponding to the node. There is one exception to this general rule: lists may contain list variables of the same or a smaller list sort with the same separators.

An abstract syntax tree (or term) t for a given signature is defined inductively as follows:

- (1) If t=c, where c is a constant of basic sort s, i.e., a function without arguments with result sort s, then t is a term of basic sort s.
- (2) If $t=\nu$, where ν is a variable of (basic or list) sort s, then t is a term of sort s. (3) If $t=f(t_1,...,t_n)$, where f is a function with arguments of sorts $s_1,...,s_n$, $(n\geq 1)$ and the basic sort s as result sort, and $t_1,...,t_n$, are terms of sort $s_1,...,s_n$ with $s'_1 \leq s_i$, then t is a term
- If $t=s[sep:t_1,...,t_n]$, where s is a basic sort, sep is a separator or empty, $n\geq 0$, and t_i is either (2)
 - (a) a term of basic sort s_i , with $s_i' \le s$, or
- (b) a variable of list sort $\{s_i'sep\}\otimes$, with $s_i' \leq s$,
- (i) t is a term of list sort $\{s \ sep\}^*$ if n=0 or all t_i are variables of sort $\{s_i \ sep\}^*$ $(s_i \le s)$,
 - (ii) otherwise, t is a term of list sort {s sep}+.

Note that this definition does not always associate the smallest possible sort with each term.

Consider, for example, the following signature:

sorts ID TYPE DECL NAT EXP ARG-LIST subsorts ID < EXP NAT < EXP (EXP ",")* < ARG-LIST functions TYPE # (ID ",")+ EXP # EXP EXP # EXP ID # ARG-LIST integer decl sacc real

in ARG-LIST. Next, the functions a, b, integer, real, decl, 0, succ, "*", "/", and The basic sorts in this signature are ID, TYPE, DECL, NAT, EXP and ARG-LIST. The partial order on sorts is defined such that both ID and NAT are included in EXP and that (EXP ",") * is included all are defined with the type of their arguments and that of their result. Some examples of ab-

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stract syntax trees over this signature are shown graphically in Figure 2.2. In prefix notation, the trees in these figures can be written as

```
ID[";":a, (ID ";")+-x,a, ID-1d,a])
                                 "*"(succ(NAT-n), "/"(0, ID-id))
                                                                                                                      EXP[",": (EXP ",")*-e,
                                                                                                                                         (ID ",")+-y])
                                                    decl(TYPE-t, (ID ";")+-x)
                   succ (NAT-n)
                                                                   (e') decl(real,
                                                                                                      (f) call (a,
(a,)
                                 g
G
                  (b) succ(0)
(c) "*"(succ(0), "/"(0,b))
(d) decl(real,ID[";": a,b])
(e) decl(real,ID[";":a,b,b,a,b,a])
                                                                                                            call(a, EXP[",":])
                                                                                                          \epsilon
```

The following variables appear in these examples:

Sort	NAT	ID	TYPE	+{'., QI}	+("," dI)	(EXP ",")+
Variable	NAT-n	ID-id	TYPE-t	(ID ";")+-x	γ-+("," dI)	(EXP ",")+-e

Observe that the list sort (ID ",")+ does not appear explicitly in the signature given in the example, but that the use of variables of this sort is permitted.

We also need the notion of selective substitution of variables in abstract syntax trees. A subset of the occurrences of a variable may be replaced by a tree of a sort that is identical to or smaller than the sort of the variable. Since a variable may occur more than once in an abstract tree, we assume that the occurrences that are to be affected by the substitution are explicitly marked.

List variables occurring as elements of lists are treated in a special way during substitution: when replacing such variables by a list of elements, those elements are inserted directly as elements of the original list, instead of producing a list with a nested structure.

For a given term t containing marked occurrences of a variable x of sort s, and a term t' of sort s's, we define the selective substitution of t' for x in t (denoted by t[x=t]) as follows:

- (1) If t=c, then t[x:=t]=c.
- (2) If t=x with x marked, then t[x:=t]=t'.
- (3) If $t=f(t_1,...,t_n)$ ($n\geq 1$), then $t(x:=t']=f(t_1[x:=t'],...,t_n[x:=t'])$. (4) If $t=s[sep:t_1,...,t_n]$ ($n\geq 0$), define substitution by induction on the length of the list:

 - The result of the substitution for $s[sep:12,...,t_n]$ is always a list of the form (i) If t=s[sep:] (the empty list), define t[x:=t]=s[sep:].
 (ii) The result of the substitution for s[sep:t2,...,t_n] is alwa
 - $s[sep:u_1,...,u_m]$ ($m \ge 0$). Now distinguish two cases:
- The result of the substitution $t_1[x:=t]$ is a list. In that case t_1 is a marked variable of sort $\{s_1 sep\} \otimes \text{with } s_1 \le s$, and $t_1[x:=t]=s_1[sep:e_1,...,e_k] \ (k \ge 0)$ and define $t[x:=t']=s[sep:e_1,...,e_k,u_1,...,u_m].$
- Otherwise, the result of the substitution $t_1[x:=t']$ is a term of sort s'(s'< s), define $t[x:=t]=s[sep:t_1[x:=t],u_1,...,u_m].$ 9
- (5) Otherwise, t[x:=t]=t.

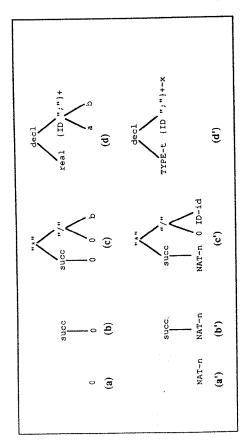


Figure 2.2(a-d). Examples of abstract syntax trees without (a-d) and with (a'-d') variables.

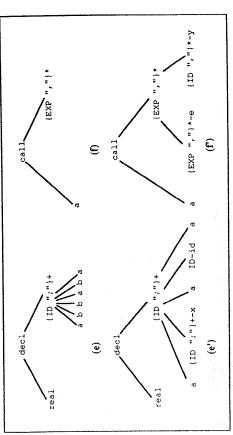


Figure 2.2(e-f). Examples of abstract syntax trees without (e,f) and with (e',f') variables.

The trees in Figure 2.2a-2.2e can be obtained from the corresponding trees in Figure 2.2a'-2.2e' by the following variable substitutions (assuming that all occurrences of variables are marked):

- NAT-n := 0 3
- NAT-n := 0 **(P**)
- NAT-n := 0, ID-id := b ઉ
- TYPE-t := real, {ID ","}+-x := ID{",": a,b} € €
- (EXP.",")*-e := EXP[",":], (ID ",")*-y := ID[",":]. $q =: pi-qi \cdot (q \cdot (q \cdot (u \cdot u)) =: x-+(u \cdot (u)) di)$

2

2.4. Rationale for the definitions of context-free grammar and signature

The definitions of the notions introduced in the previous sections differ, in some respects, from the usual ones. Here, we give the arguments for the particular choices we made.

2.4.1. BNF grammars

- All non-terminals act as start symbol. This is desirable from the perspective of syntax-directed editing, where the need arises to parse only parts of programs
 - The terminal alphabet consists of literal strings as well as of lexical non-terminals.
- can define parse trees in such a way that all list elements are treated symmetrically. An then have to be translated to a symmetrical representation in the abstract syntax tree, in order Because our notion of BNF grammars directly support list constructs with separators, we alternative approach would have been to use left- or right-recursive grammar rules, leading to a correspondingly biased representation of lists. This asymmetrical representation would to avoid the asymmetry becoming visible during the syntax-directed editing of list elements.

2.4.2. Signatures

- For each basic sort, we implicitly define different list sorts for all possible separators (constructor functions). In this way, lists with elements of equal type but different separators can be distinguished.
- Subsorts serve the purpose of eliminating chain rules of the form <N> ::= <M> in the BNF grammar. These would otherwise give rise to many void text movements in the syntax-directed editor.
- holds automatically for all sorts and separators. The inclusion S < {S sep}+ does not hold There is an interaction between subsorts and lists. The relation (S sep)+< (S sep)* automatically, however, since — from the perspective of syntax-directed editing — the distinction between a single element and a list consisting of one element would disappear (sec, for instance, Figure 5.9 in Chapter 5).
- We allow the declaration of associative functions in the signature (by means of the attribute solve by always choosing a left-associative parse from all possible (associatively equivalent) parses (see Section 6.2). Declaring a function in the signature to be associative allows assoc). At the syntactic level, associative functions may cause ambiguities which we rethe reconstruction of all these variants using the associative law.
 - Variables are not explicitly declared, but we use a general naming scheme for generating infinitely many variables. We need this generality to describe the naming schemes for variables in SDF variable declarations.
- The naming convention for sorts and functions is more general than normally found: we trary characters but surrounded by double quotes. This allows us great flexibility when allow names either consisting of alphanumeric characters and hyphens, or containing arbigenerating names for sorts and functions.

Finally, some comments on substitution are in order:

- We have chosen to define substitution for selected occurrences of a variable and not for all variable and then applying our notion of selective substitution. On the other hand, selective occurrences. Clearly, the latter can easily be defined by first marking all occurrences of a substitution is the fundamental operation used during syntax-directed editing.
 - The sort of a term may become smaller after substitution. In particular, a list of sort (8 sep) *may become a list of sort (\$ sep) + after substitution.
- The sorts of the elements in a list may all become smaller than the original element sort of that list as a result of substitution.

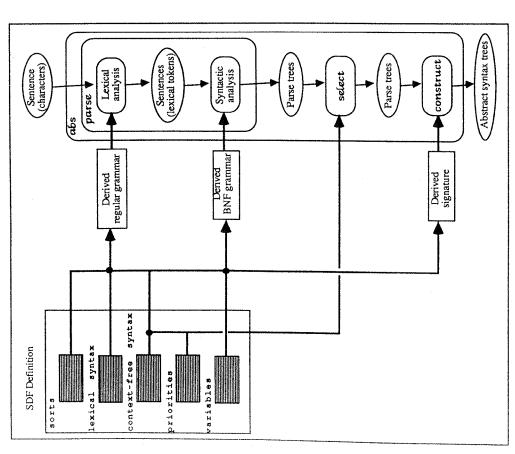


Figure 2.3. From sentence to abstract syntax tree(s).

2.5. Overview of the SDF definition

- An SDF definition consists of five sections, defining
 - sorts,
- lexical syntax,
- context-free syntax,
 - priorities, and

As a whole, the SDF definition has the purpose to define

- A set of sentences (strings).
- A set of abstract syntax trees.
- A relation between (parse trees of) sentences and abstract syntax trees

A derived regular grammar and a derived BNF grammar, defining a set of sentences. To this end, we can derive the following information from an SDF definition:

- A derived signature, defining a set of abstract syntax trees.
- A mapping from parse trees over the derived BNF grammar to abstract syntax trees over the derived signature. This is a fixed mapping that is part of the definition of SDF. Other mappings can only be obtained by adding semantic rules to SDF definitions (see Chapter 9).

The relation between the different sections of an SDF definition and the information derived from it is shown in Figure 2.3. This figure also shows the function abs that converts an input sentence into (one or more) abstract syntax trees, together with the three auxiliary functions parse, select and construct. We will return to this figure in the following chapters.

3. SORTS

Sorts are declared by listing their name in the sorts section of the SDF definition. Some constraints are imposed on the use of sorts:

- The sort LAYOUT is predefined and may not be redeclared. It may only be used as result sort of functions in the lexical syntax (see Sections 4.1 and 4.4).
 - The sort CHAR is predefined and may not be redeclared either. It may only be used in declarations of variables (see Chapter 7).

Each declared sort s becomes a non-terminal with the name <s> in the derived BNF grammar. If a sort appears as result sort of a lexical function, it will also be added to the derived regular grammar. A declaration for the predefined sort CHAR as well as declarations for all sorts declared in the SDF definition will be added to the derived signature. This is described by rules R1, G1, S1 and S2 in Chapter 8.

4. LEXICAL SYNTAX

4.1. Introduction

lexical tokens. A lexical token is a pair consisting of a sort name and a lexeme. The former is used to distinguish classes of lexical tokens such as, e.g., identifiers and numbers. The latter is the Lexical syntax describes the low level structure of sentences (sequences of characters) in terms of actual text of the token. The lexical syntax also defines which substrings of the sentence are layout symbols or comments and are to be skipped.

The definition of lexical syntax consists of a set of one or more function declarations, each consisting of a regular expression and a result sort. All function declarations with a given output sort together define the lexical syntax of lexemes of that sort. The layout symbols are defined by functions that have the predefined sort LAYOUT as result sort.

From a given SDF definition, one can derive a regular grammar. This derived regular grammar is obtained as follows:

- Regular expressions are extracted from the lexical syntax (described in this chapter).
 - All literals appearing in the context-free syntax are enumerated (Section 5.2).
- Regular expressions are extracted from variable declarations (Chapter 7).
- Regular expressions defining the complete alphabet are added when variables of sort CHAR are declared (Chapter 7).

will present tokens of other sorts as input to the syntactic analysis phase. As a result, an input Lexical analysis based on this derived regular grammar will skip tokens of the sort LAYOUT, and

sentence will be subdivided in a unique sequence of lexemes. However, more than one sort may be associated with each lexeme. The situation is shown in Figure 2.3.

erals are discussed in Section 4.6. The disambiguation rules we use are given in Section 4.7. A The organization of this chapter is as follows. In Section 4.2. elementary lexical functions are tition operators (Section 4.5). The definition of layout functions is described in Section 4.4. Litdescribed. Lexical function definitions may also contain character classes (Section 4.3) and reperationale for the way in which we define lexical syntax concludes this chapter (Section 4.8)

emes. In their simplest form, lexical function declarations consist of one or more literal strings or The lexical syntax contains declarations of lexical functions defining the syntactic form of lexnames of sorts, and their result sort.

The effects on the derived regular grammar, BNF grammar and signature are as follows. For each sort I (with I≠LAYOUT) that appears as result sort of a lexical function:

- and as terminal symbol in the derived BNF grammar. (For the sort LAYOUT we only define Define the symbol <L-LEX> both as lexical non-terminal in the derived regular grammar
 - Add to the derived BNF grammar a rule of the form: the lexical non-terminal <LAYOUT-LEX>).

```
<L> ::= <L-LEX>,
```

where <L-Lex> is the name associated with L in the derived regular grammar.¹

Add to the derived signature declarations of constants of sort CHAR for all characters in the alphabet as well as declarations for lexical constructor functions of the form

where 1 is the name L written in lower case letters. This definition reflects the fact that lexemes appear as strings of characters in the abstract syntax tree. regular expression associated with each symbol <L-LEX> consists of the or of all left-hand sides of lexical function declarations for sort 1. Sort names appearing in these left-hand sides are replaced by the symbol defined in the previous step. Note that, since we want to extract a regular grammar from the SDF definition, no cyclic dependency may exist between lexical function declarations

The above step leads to rules R1, G2, G3, S1, S4, and S5 in Chapter 8.

```
VOWEL
                   VOWEL VOWEL
           VOWEL
       VOWEL
       ٨
    syntax
           Ą.
               4444
VOWEL
```

Figure 4.1. Vowels.

In Figure 4.1 one sort (VOWEL) and six lexical functions, are defined. All functions have result SOUT VOWEL. The derived regular grammar of this example is:

<u>"</u>

```
<VOWEL-LEX> = "a" | "e" | "i" | "o" | "u" | "y" | "y
```

Given this definition, the following three tokens will be associated with the input sentence "aio": (<VOWEL-LEX>,

```
.0")
(<VOWEL-LEX>,
```

4.3. Character classes

using character classes enclosed by the symbols (and). A character class contains a list of zero as an abbreviation for the characters 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. A character range of the form Enumerations of characters occur frequently in lexical definitions. They can be abbreviated by or more characters (which stand for themselves) or character ranges such as, for instance, (0-9) c1-c2 should satisfy the following restrictions:

- c_1 and c_2 are both lower case letters and c_1 precedes c_2 in the alphabet, or c_1 and c_2 are both upper case letters and c_1 precedes c_2 in the alphabet, or
- c_1 and c_2 are both digits and the numeric value of c_1 is smaller than that of $c_2,$ or
- c_1 and c_2 are both escaped non-printable characters (see below) and the character code of c_1 is smaller than that of c2.

Character classes may also be complemented. This is denoted by the prefix operator ~. A complemented character class accepts all characters not listed in it.

In the derived regular grammar, character classes are replaced by an or of all characters in the class. See rule R3 in Chapter 8.

```
-> VOWEL
 [aeiouy]
sorts VOWEL
```

Figure 4.2. Shorter version of vowels using a character class.

The definition of vowels in Figure 4.2 is equivalent to the one in Figure 4.1, but has been abbreviated by using a character class.

```
-> DIGIT
-> OTHER
                        VOWEL
sorts VOWEL DIGIT OTHER
                        Ŷ
               lexical syntax
                                               ~[aeiouy0-9]
                         [aeiouy]
```

Figure 4.3. Vowels, digits and other characters.

Given the lexical syntax in Figure 4.3, the input sentence "3 aios", will be subdivided in the following sequence of tokens:

```
(<DIGIT-LEX>,
                 (<OTHER-LEX>, (<VOWEL-LEX>,
                                              (<VOWEL-LEX>,
                                                                             (<OTHER-LEX>,
                                                              (<VOWEL-LEX>,
```

Note that the space character occurring between the characters 3 and a as well as the character s at the end of the input string are classified as <0THER-LEX>. The proper treatment of layout characters is discussed in Section 4.4.

Therefore, three different entities may be associated with a sort: (a) <L-LEX> denotes all lexical functions with result sort L; (b) <L-VAR> denotes all variables of sort L (see Chapter 7); (c) <L> denotes all entities with result 1We will allow context-free functions with a lexical sort as output sort as well as variables over lexical sorts. on i. (i.e., lexical and context-free functions, and variables).

needed as ordinary characters in the definition. The backslash character (1) is used as escape character for the quoting of special characters. Thus the sequence \circ should be used whenever Several characters have a special meaning in SDF and may cause problems when they are special character c is needed as ordinary character in the definition. In character classes, the following characters have a special meaning:

begin of character class end of character class escape character. character range

In literal strings, the following characters have a special meaning:

escape character. double quote

The literal strings containing one double quote or one backslash are thus written as "\" and "\\", respectively.

In addition to this escape convention, abbreviations exist for some frequently used layout characters as well as for arbitrary, non-printable, characters:

newline character carriage return

horizontal tabulation رد

a non-printable character with three digit (octal) character code ddd. These abbreviations can be used both in character classes and in literal strings. \ddd

4.4. Layout

another result sort, the interpretation as layout symbol is ignored; all other interpretations are Strings matched by lexical functions with the predefined sort LAYOUT as result sort will be skipped. When a string is matched by both a LAYOUT function and (one or more) functions with passed to the syntax analysis phase (see Section 4.7)

```
-> LETTER
-> LAYOUT
-> LAYOUT
          syntax
lexical surf
               [a-z]
                           ..'u
```

Figure 4.4. Letters and spaces.

The lexical syntax in Figure 4.4 defines the sort Letter and defines three functions: one with output sort LETTER and two with the (predefined) sort LAYOUT. The derived regular grammar is:

"2" | ... | "E" = <LETTER-LEX> <LAYOUT-LEX> The input string x y z will, initially, be subdivided in the following five tokens:

(<LAYOUT-LEX>, ""), (<LETTER-LEX>, "y"), (<LETTER-LEX>, "x"), (<LETTER-LEX>, "z"). Since all layout tokens will be skipped, only the tokens of sort LETTER will remain. In other words, the result of lexical analysis will consist or the following three tokens:

9

(<LETTER-LEX>, "y"), (<LETTER-LEX>, "z").

4.5. Repetition: * and +

In many cases, lexical tokens can only be described by patterns that exhibit a certain repetition. Two postfix operators are available for this purpose. The operators * and + denote, respectively, zero or more and one or more repetitions of the sort, literal, or character class to which they are attached.

In the derived regular grammar, repetitions are mapped on the corresponding repetition operators in the regular grammar. See rule R4 in Chapter 8.

```
-> LETTER-OR-DIGIT
-> ID
                    -> LETTER
                                              -> LAYOUT
sorts LETTER LETTER-OR-DIGIT ID
                                    LETTER LETTER-OR-DIGIT*
         lexical syntax
                             [a-z0-9]
                     [2-g]
  4.2.6.4.2.6
```

Figure 4.5. Identifiers.

Figure 4.5. illustrates the definition of identifiers by means of the *-operator. The derived regular grammar for this example is:

```
<LETTER-LEX>
<LETTER-OR-DIGIT-LEX> = "a" | ... | "2" | "0" | ... | "9"
<ID-LEX> 
                                                                          <LAYOUT-LEX>
```

The input string "r2d2 2de", will be subdivided in the following three lexical tokens (after elimination of the single layout token occurring in it):

```
(<LETTER-OR-DIGIT-LEX>, "2"),
(<ID-LEX>, "r2d2"),
```

(<ID-LEX>, "de"),

This subdivision may seem arbitrary, but is justified in the discussion of lexical ambiguities in the next section.

A more concise definition of identifiers is given in Figure 4.6. Here, the *-operator is applied directly to a character class. Note that, due to the elimination of the sort LETTER-OR-DIGIT, the above input string "r2d2 2de" is now erroneous.

```
ID
LAYOUT
     ^ ^
  [a-z] [a-z0-9]*
lexical syntax
```

Figure 4.6. More concise definition of identifiers

pear in the context-free syntax are added to the derived regular grammar. We reserve the symbol <LITERAL-LEX> for this purpose in the derived regular grammar. It will contain all literal symbols In Chapter 5 we will see that all literal symbols such as keywords and operator symbols that apin the context-free grammar as alternatives. See rule R5 in Chapter 8.

A context-free syntax containing the literals "if", "then", "(", ")" and ", " will, for instance, lead to the following definition of <LITERAL-LEX>:

```
ITERAL-LEX> = "if" | "then" | "(" | ")" | ","
```

4.7. Disambiguation of lexical syntax

We first illustrate ambiguities at the lexical level by means of Figure 4.5. Consider all ten possible interpretations of the input string xy:

```
(<LETTER-LEX>, "x"), (<LETTER-DEX>, "y")
(<LETTER-LEX>, "x"), (<LETTER-DGIT-LEX>, "y")
(<LETTER-LEX>, "x"), (<ID-LEX>, "y")
(<LETTER-DR-DIGIT-LEX>, "x"), (<ID-TER-DGIT-LEX>, "y")
(<LETTER-OR-DIGIT-LEX>, "x"), (<ID-LEX>, "y")
(<LETTER-OR-DIGIT-LEX>, "x"), (<ID-LEX>, "y")
(<ID-LEX>, "x"), (<ID-LEX>, "y")
```

Ambiguities are taken as seriously as possible in SDF, but it is clear that some automatic disambiguation method is needed to reduce the vast amount of lexical ambiguities. Three disambiguation rules are used:

- Prefer Longest Match,
- Prefer non-Layout, and
 - Drefer I iterals

The Prefer Longest Match rule rejects all interpretations of the input string that are included in a longer interpretation. In other words, the longest possible match is preferred. In Figure 4.5, only the interpretation (<ID-LEX>, "xy") remains after application of this rule. Note that this is the only possible interpretation in Figure 4.6.

After application of the Prefer Longest Match Rule, there may still be more than one interpretation of the lexical token left. The rules Prefer non-Layout and Prefer Literals serve the purpose of reducing the number of possibilities still further.

The Prefer non-Layout rule eliminates all interpretations of the lexical token as layout symbol. When, after applying this rule, no interpretation remains, the next lexical token is taken from the

The Prefer Literals rule applies to literals such as keywords and operator symbols that are introduced in the context-free syntax. Ambiguities may arise because some literal strings may be equal to lexemes defined in the lexical syntax or variables defined in the variables section (see Section 7.2). The Prefer Literals rule gives precedence to interpretations of the input string as literals. This applies, for instance, to identifiers defined in the lexical syntax that are also keywords defined in the context-free syntax. The Prefer Literals rule thus favours a so-called reserved word strategy for keywords. (In Section 11.3 it will be shown how this restriction can be circum-

After applying the above disambiguation rules, all remaining interpretations of the input string are passed to the syntactic analysis phase.

1.8. Rationale for the definition of legical syntax

There are three major reasons for making a distinction between lexical syntax and context-free syntax. First, the handling of ambiguities is different. At the lexical level myriads of (uninteresting or unintended) ambiguities exist. One needs fixed disambiguation rules to eliminate them (see Section 4.7). All possible interpretations that remain after application of these rules are returned by the lexical scanner. We even allow lexical ambiguities within the same sort. However, since lexemes are represented as linear strings of characters, the distinction between these

2

ambiguities will be lost. At the context-free level, the resolution of ambiguities has to be defined in the specification. For instance, by giving the priority and associativity of operators in the context-free syntax (see Chapter 6). In general, all disambiguation rules have disadvantages if one considers the problem of combining several modules containing SDF definitions (see Chapter 9).

Second, the value constructed after recognition is different. At the lexical level, tokens are constructed consisting of a name and a string. At the context-free syntax level, abstract syntax trees are constructed. This difference has consequences for the association of semantics with SDF definitions (see Chapter 9).

Finally, implementation techniques (and associated implementation trade-offs) are different for texical syntax and for context-free syntax (see Chapter 10).

The limitations of our current disambiguation rules are discussed in Section 11.3.

5. CONTEXT-FREE SYNTAX

5.1. Introduction

Context-free syntax describes the concrete and abstract syntactic structure of sentences in a language. The definition of context-free syntax in an SDF definition consists of declarations of context.

In Section 5.2, the simplest form of context-free functions is described. In Section 5.3 syntactic repetition is discussed. Chain and bracket functions are described in Section 5.4. Both lead to the elimination of certain nodes from abstract syntax trees. A rationale for the definition of context-free syntax concludes this chapter.

Note that context-free functions may be followed by a list of attributes. In this chapter we will only describe the bracket attribute (Section 5.4). All other attributes have to do with priorities and are described in Chapter 6.

5.2. Context-free functions

In their simplest form, context-free functions are declared by giving their syntax (a list consisting of zero or more literal symbols and/or names of sorts) and their result sort.

We define the meaning of context-free functions by specifying their contribution to the derived regular grammar, derived BNF grammar, derived signature, and the mapping from parse trees to abstract syntax trees.

The contributions to the derived regular grammar, derived BNF grammar and derived signature are now described in more detail:

- For each literal symbol "lit" appearing in a function definition in the context-free syntax do the following:

 (a) add "lit" as alternative of the predefined lexical non-terminal <LITERAL-LEX> in the
 - derived regular grammar,
 - (b) add "lit" as terminal to the derived BNF grammar.
- The lexical token LETAL LE
- For each function declaration in the context-free syntax do the following:
 (a) add the grammar rules obtained by exchanging the left-hand and right-hand side of the function declarations to the derived BNF grammar;
- (b) add function declarations to the derived signature!: for each function some new name (see below) is generated and the sorts of its arguments and of its result are obtained from the sort names appearing in the original function definition.

See rules RS, G2, G5 and S6 in Chapter 8.

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Except chain and bracket functions as we will see in Section 5.4.

function always gets the same abstract name and no two different context-free functions obtain the same abstract name. SDF does not prescribe any particular naming scheme in this case. In this The new names mentioned in (b) may be chosen arbitrarily as long as the same context-free manual we generate abstract function names by concatenating (some of) the literals in the original

SDF function definition according to the following rules:

- (1) consecutive literals in the new name are separated by hyphens;
- (2) if there occur no literals in the function declaration, the name empty is used,
- (3) if the name generated by rules (1)-(2) contains characters that are not alpha-numeries or hyphens, it is surrounded by double quotes;
- (4) all names should be unique: a name generated by rules (1)-(3) can be postfixed with a hyphen and an arbitrary numeric string to make it unique.

Finally, we define the contribution of the context-free syntax to the mapping from parse trees to tions in the context-free syntax and both rules in the derived BNF grammar and function definitions in the derived signature. This makes it straightforward to define the mapping from parse trees over the derived BNF grammar to abstract syntax trees over the derived signature. The mapping is recursively defined by giving the transformation for a parse tree P to an abstract synabstract syntax trees. In principle, there is a one-to-one correspondence between function defini-

with lexical non-terminal <L-Lex>, with L \neq LITERAL, the result of transforming P is an abstract syntax tree whose root is labeled with the lexical constructor function for sort L (see If the root of P is labeled with a non-terminal and has a single child C whose root is labeled

(a) Recursively transform all children of the root of P that are labeled with a non-terminal. Otherwise, the root of P is labeled with a non-terminal and P is transformed as follows: Section 4.2) and whose single child is the result of transforming C.

(b) The root of P corresponds to some rule R in the derived BNF grammar and some function definition F in the derived signature. P is now transformed into an abstract syntax tree consisting of the function defined in F with the elements of A as children. This gives a list A of abstract syntax trees².

See rules MI, M2 and M8 in Chapter 8.

tree with a string, one should be aware of the fact that more than one parse tree may exist for a given string, and that more than one abstract syntax tree may thus be associated with it. This When the mapping from parse tree to abstract syntax tree is used to associate an abstract syntax problem is discussed in Section 6.

```
PROGRAM
PROGRAM
                          -> LAYOUT
                                         -> COORD
-> CMND
                                                          -> CMND
-> PROGR
-> PROGR
                -> NAT
sorts NAT COORD CMND PROGRAM
                                  context-free syntax
"('NAT "," NAT ")"
"line" "to" COORD
"move" "to" COORD
           lexical syntax
                                                                     CMND PROGRAM
                   +[6-0]
                            ["]
                            55.
```

Figure 5.1. Simple drawing language.

Figure 5.1 describes a simple drawing language. A drawing program consists of a sequence of zero or more commands. There are two commands: one for moving the pen to a position in the plane, and one for drawing a line from the current position to a new position. A position is denoted by a pair of numbers. The derived regular grammar of this SDF definition is:

<NAT_LEX> = ("0" | ... | "9")+
<LAYOUT_LEX> = " | "\n"
<LITERAL_LEX> = " (" | "," | ")" | "line" | "to" | "move" [4] [6,7,8]

The derived BNF grammar is:

```
::= <NAT-LEX>
::= "(" <NAT> "," <NAT> ")
::= "line" "co" <COORD>
::= "line" "to" <COORD>
::= "move" "to" <COORD>
::= <CMND> <PROGRAM>
                                                          <PROGRAM>
                                              <PROGRAM>
             <COORD>
                                    <CMND>
    <NAT>
   [6]
```

The derived signature is:

```
-> CHAR
-> CHAR
CHAR NAT COORD CMND PROGRAM
                                                empty-1 : CMND # PROGRAM
                                "(-,-)" : NAT # NAT
                                                        empty-2:
      functions
                                             move
                                        line
                            [3]
[6]
[7]
[8]
[9]
 \Xi
```

generation rules given previously. Note that a certain freedom exists in the choice of names 'o be generated. For instance, the names move, move-to and to can be generated for the full lion corresponding to the move command. Lines 9 and 10 illustrate the use of the name empty for In this signature we have introduced new names for the functions in the signature using the name functions without syntax. Also note the use of numeric postfixes to make the name of each func-

fined above, the parse trees and corresponding abstract syntax trees for the drawing language programs line to (15, 2) and line to (15,2) move to (3,4) line to (5,6) are Using the derived BNF grammar and the mapping from parse trees to abstract syntax trees deshown in Figures 5.2 and 5.3.

In Figure 5.1 we have quoted all literals occurring in the definition of context-free functions. As an abbreviation, these quotes may be omitted when the literal begins with a lower case letter and consists only of letters and digits. To avoid confusion between unquoted literals and sorts, we require that sort names begin with an upper case letter. Line 7, for instance, can be abbreviated to:

-> COORD. line to COORD We will always use this convention in all examples (also see appendix A).

5.3. Repetition: * and +

fined sequence of commands. The resulting abstract syntax trees encode the list structure by The context-free syntax in Figure 5.1 explicitly defines a drawing program as a recursively demeans of a fixed-arity list constructor (empty-1 in the example). There are several problems with this approach

Exceptions to this general rule will be introduced in the description of lists (Section 5.3), and chain and bracket

²Note that all children that are labeled with a terminal are eliminated and do not appear in the abstract syntax tree. functions (Section 5.4).

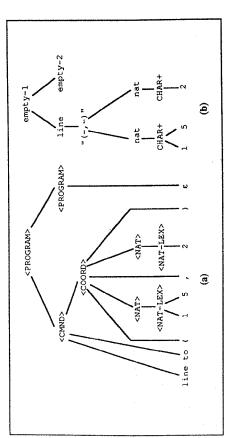


Figure 5.2. (a) Parse tree, and (b) corresponding abstract syntax tree.

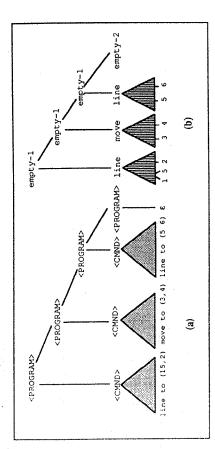


Figure 5.3. (a) Parse tree, and (b) corresponding abstract syntax tree.

- The SDF definition does not express the repetitive nature of the syntax in a clear way
- The resulting abstract syntax trees are deeply nested and have a bias towards the left or the right, depending on the form of the SDF definition.

When attempting to define lists with separators using this style, the poor readability of the resulting definition becomes even more apparent. Therefore, SDF supports list constructs separately They can have the following two forms:

- Lists without separators of the form SORT* or SORT+ indicating respectively zero or more and one or more repetitions of sort sorr.
- Lists with separators of the form (SORT sep) , where \in is either * or +, indicating respecified y zero or more or one or more repetitions of sort sort separated by the literal sep.

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Lists may only be used in the left-hand side of a function definition (and may thus not appear as

In this manual, we will frequently write (SORT sep) to denote all of the above list constructs, where ⊗ is either * or + and sep may be the empty string. The case of lists without separators

The effect of list constructs on the derived grammar and signature is as follows. For each list will be treated as the special case that sep is equal to the empty string.

construct of the form (sorr sep) & that appears in a function declaration, define a non-terminal with the name < SORT-in-sep-list> and add the rule

Each occurrence of a list construct in the SDF definition is translated into the corresponding list construct in the grammar, i.e., a list of the form (SORT sep)⊗ is translated to (<SORT-in-seplist> sep}⊗.

The definition of the derived signature is also affected. In all function definitions, occurrences of list constructs of the form (SORT sep) are translated to corresponding lists of the element sort in the signature, i.e. to {SORT sep}⊗.

The mapping from parse trees to abstract syntax trees is extended as follows. Let P be a parse ree whose root is labeled with (SORT Sep) . There are two cases:

- (a) sep is empty: let $C_1,...,C_k$ be the k children of the root of P; or (b) sep is not empty, the root of P has 2k-1 children and let $C_1,...,C_k$ be the odd-numbered
 - children (i.e., the children corresponding to list elements and not to separators).

The result of transforming P is an abstract syntax tree whose root is labeled with (SORT sep) \otimes beled with <sorr-in-sep-list> are removed and do not appear in the abstract syntax tree. The and with the transformed versions of C1,..., Ck as children. Nodes in the parse tree that are laeffects of list constructs are summarized in rules G4, G5, S6, M3, M7 in Chapter 8.

				-
	lexical syncax [0-9]+	Ŷ	-> NAT	
4	[a/]	î	-> SPACE	
5.	context-free syntax			
9	"(" NAT "," NAT ")"	٨	COORD	
7.	line to COORD	î	-> CWIND	
	move to COORD	Ŷ	CMND	
6	CMND*	Ŷ	PROGRAM	

Figure 5.4. Use of a list operation in definition of the drawing language.

The use of list constructs in the definition of the drawing language is shown in Figure ...4. Lines 9 and 10 of Figure 5.1 have been replaced by the single line 9. The derived regular grammar is not affected by this modification. The derived BNF grammar becomes:

EX>	::= "(" <nat> "," <nat> ";</nat></nat>	"to" <coord></coord>	"to" <coord></coord>
::# <nat-lex></nat-lex>	N> ::) :: :::	::= "line"	::= "move"
<nat></nat>	<c000rd></c000rd>	<cmnd></cmnd>	<cmnd></cmnd>
Ξ	[9]	[7]	[8]

One may wonder why we use this, seemingly too complex, translation scheme. A much simpler method would be to map list constructs directly on the corresponding construct in the grammar, i.e., {SORT sep}⊗ in a function definition is mapped on (SORT sep)⊗ in the derived grammar. However, in Chapter 7 we will see that this simple method cannot be extended to the case that the SDF definition contains definitions of variables.

```
a : -> CHAR
b : -> CHAR
...Declarations of constants for all characters in the alphabet...
                                                                                                                             -> NAT
-> COORD
-> CMND
-> CMND
-> CMND
-> CMND
<PROGRAM> ::= <CMND-in--list>*
<CMND-in--list> ::= <CMND>
                                                          sorts
CHAR NAT COORD CMND PROGRAM
                                                                                                                                      "(-,-)": NAT # NAT
line : COORD
move : COORD
empty : CMND*
                                   The derived signature becomes:
                                                                              functions
                                                                                                                               nat
   69
                                                                   \Xi
                                                                                                                                 93163
```

Figure 5.5 shows the parse tree and corresponding abstract syntax for the same sentence as used in Figure 5.3. Note, how the list construct is represented by a node with a variable number of children.

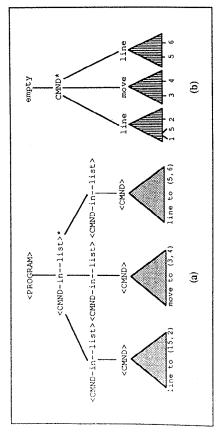


Figure 5.5. (a) Parse tree and (b) abstract syntax tree containing a * operator.

In Figure 5.6 the use of a list constructor with a separator is illustrated. The example shows a simple form of variable declarations in a Pascal-like language. A declaration consists of the keyword dec1, one or more identifiers separated by commas, followed by a colon and a type.

```
-> ID
-> LAYOUT
                                              -> DECL
-> TYPE
-> TYPE
                                      context-free syntax
docl { ID ","}+ ":" TYPE
sorts ID DECL TYPE
          syntax
                                                         integer
real
                   [a-z] +
          lexical
```

Figure 5.6. Declarations.

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The derived regular grammar is:

```
<ID-LEX> = ("a" | ... | "z") +
<LAYOUT-LEX> = " "
<LITERAL-LEX> = "decl" | "," | ";" | "integer" | "real"
+ ("a" | ... | "z") =
                                           [6,7,8]
```

The derived BNF grammar is:

```
<TYPE><TYPE>
[3]
[6]
[7]
[8]
```

The derived signature is:

```
-> ID
-> DECL
-> TYPE
-> TYPE
                        : (ID ",")+ # TYPE
sorts
CHAR ID DECL TYPE
                        decl :
          functions
    [1]
                    [8]
```

Figure 5.7 shows the parse tree and corresponding abstract syntax tree for the sentence decl ab, c, xyz : real.

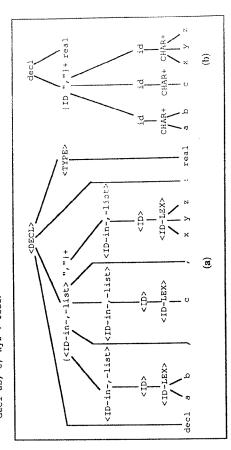


Figure 5.7. (a) Parse tree and (b) corresponding abstract syntax tree.

5.4. Chain and bracket functions

Abstract syntax trees form a concise way of representing the structure of sentences. Further abbreviations are possible, however, by eliminating certain classes of nodes from the tree. SDF defines abbreviations for chain and bracket functions.

A chain function has a definition of one of the following forms:

```
-> BIG
-> BIG
      {SMALL sep}⊗
 la.
        1b.
```

tablishes an inclusion relation between two sorts. The above function declarations will lead to the where SMALL and BIG are previously defined sorts and sep is a literal. A chain function only esrules

```
::= {<SMALL-in-sep-list> sep}
                            ::= <SMALL>
::= <SMALL>
                              <SMALL-in-sep-list>
                 <BIG>
   <BIG>
   [la]
                 [91]
```

in the derived BNF grammar and to the function declarations

```
empty : \{SMALL sep\} \otimes -> BIG
 -> BIG
empty : SMALL
  [14]
                  [1p]
```

in the derived signature. According to the rules of abstract syntax tree formation given earlier, a tree of sort (SMALL sep)⊗ cannot occur directly at a position where a tree of sort BIG is required, but will have to be embedded in an application of the function empty. Such nodes corresponding to chain functions are undesirable for two reasons:

- ited during a walk through the tree. However, since no syntax is associated with chain functions, no textual distinction can be made between a visit to the node itself or a visit to When the abstract syntax tree is used by a syntax-directed editor, these nodes may be viscither its parent or its child.
- When semantic rules are associated with abstract syntax trees, extra rules are needed for the processing of chain functions, but in general the concrete form of such rules will be am-

In SDF, the nodes corresponding to chain functions are therefore eliminated from abstract syntax trees in the following way:

- In the derived signature subsort declarations rather than ordinary function declarations are generated for each chain function.
 - In the mapping from parse tree to abstract syntax tree the result of transforming a parse tree P whose root node corresponds to a chain function is defined as the result of transforming the single child of the root of P. The resulting tree is correct due to the subsort declaration generated in the previous step.

This leads to rules S3, S6 and M4 in Chapter 8.

In the sequel, it will be convenient to have a parent-child relationship in parse trees that distregards nodes corresponding to chain rules. Therefore, we will use "child" (i.e., child between double quotes) to mean either an immediate child or a child that can be reached via one or more chain rules.

A bracket function has a definition of the following form:

```
s
^-
. "open" S "close"
```

where "open" and "close" are arbitrary, non-empty, literals acting as opening and closing sions and the delimiters "begin" and "end" in programs. Here again, application of the standard definitions leads to the appearance of additional nodes in the abstract syntax tree corresponding to (see Chapter 6), but have no further meaning. Therefore, SDF provides the facility for declaring that a certain function is used only for bracketing by attaching the attribute bracket to it. More bracket functions. In most cases, brackets are only introduced for grouping and disambiguation brackets for the sort s. Typical examples are the parentheses "(" and ")" in arithmetic expresprecisely, by declaring the above function as

```
[bracket]
  Ŷ
. "open" S "close"
```

the following effect is achieved:

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In the derived signature no function declaration is generated for functions with the attribute

P whose root corresponds to a bracket function is defined as the result of transforming the second child of the root of P, i.e., the only child labeled v ith a non-terminal. The resulting In the mapping from parse tree to abstract syntax tree the result of transforming a parse tree tree is correct since the argument and result sorts of a bracket function are equal.

Since brackets are necessary for overruling the priority and associativity of functions (see This leads to rules S6 and M5 in Chapter 8.

Chapter 6), we require that suitable bracket functions are declared for the argument and result sorts of

- all functions occurring in priority declarations or group associativity declarations, and
- all functions having one of the attributes left, right, assoc of non-assoc.

In this way we guarantee that every abstract tree t over the derived signature has a corresponding string representation s such that $abs(s) = \{t\}$ (cf. Figure 2.3).

gramming language is defined with identifiers and natural numbers as lexical sorts, and several language constructs which can be combined into programs. The function in line 8 defines beginend brackets for lists of statements. The function in line 9 is a chain function from (STRT ";"). Figure 5.8 illustrates the concepts of chain functions and bracket functions. A simple proto SERIES. The functions in lines 13 and 14 are chain functions that convert identifiers and numbers to expressions. The derived regular grammar for Figure 5.8 is:

```
"begin" | "end" | ";" | ":=" | "jf"
|se" | "fi" | "until" | "do" | "od"
                                                                                         "then" | "else" | "fi" |
= ("a" | ... | "z") +
= ("0" | ... | "9") +
= " " | "\tau | "\n"
                                                                            = "program" |
                                                                                <LITERAL-LEX>
                                           <LAYOUT-LEX>
                                            [5] <LAYOU1-L.
[7,8,9,10,11,12]
                          <NAT-LEX>
```

The derived BNF grammar is:

```
::= "begin" <SERIES> "end"
::= { <STAT-in-;-list> ";" }*
::= <ID-LEX>
::= <NAT-LEX>
::= "program" <SERIES>
                                                <STAT-in-;-list>::= <STAT>
                      <PROGRAM>
                                <SERIES>
                                         <SERIES>
                                                          <STAT>
                                                                     <STAT>
                                                                               <STAT>
                                                                                         <EXP>
                                                                                                  <EXP>
             <NAT>
   <11>
                                                             10]
```

The derived signature is:

```
characters in the alphabet...
                                                                           -> NAT
-> PROGRAM
                                                                   11
                                                 ...Declarations of constants for all id : CHAR+
                                                                                              Ŷ
                                                                                                       ^ ^
      CHAR ID NAT PROGRAM SERIES STAT EXP
                                                                                                       EXP # SERIES # SERIES
EXP # SERIES
                        STAT ";" > < SERIES
                                                                                                ID # EXP
                                                                                       SERIES
                                                                     : CHAR+
                                                                              : CHAR+
                                 ID < EXP
                                                                                         program
                                                    functions
                 subsorts
                                                                                                                    until
                                                                                 nat
sorts
                                                                                                 [10]
[11]
[12]
                                   [13]
[14]
          []
                           [6]
```

Figure 5.8. A simple programming language.

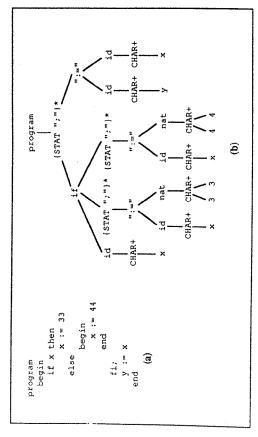


Figure 5.9. (a) Program and (b) corresponding abstract syntax tree.

```
1. sorts E

2. lexical syntax

3. {0-9}+ -> E

4. {0-9}+ -> E

5. context-free syntax

6. E "+" E -> E

7. E "+" E -> E

7. E "+" E -> E

8. "("E")" -> E (bracket)
```

Figure 6.1. Ambiguous definition of simple arithmetic expressions

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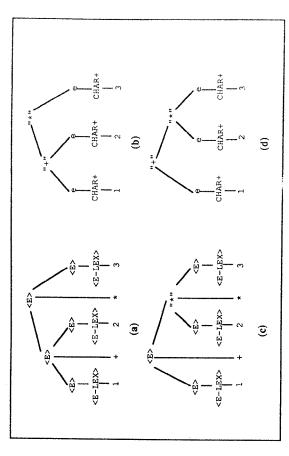


Figure 6.2 (a,c) Parse trees and (b,d) corresponding g abstract syntax trees for 1+2+3.

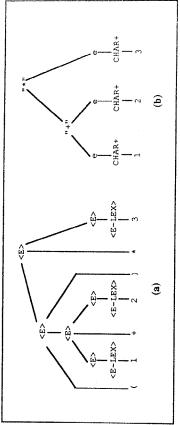


Figure 6.3. (a) Parse tree and (b) abstract syntax tree for (1+2) *3.

6. PRIORITIES

6.1. Motivation

The derived BNF grammar of an SDF definition may be ambiguous. As a consequence, there may be sentences in the language defined by the derived grammar which have more than one parse tree (and thus more than one abstract syntax tree). Consider the SDF definition of arithmetic expressions with addition and multiplication in Figure 6.1. An ambiguous sentence in this language is, for instance, 1+2*3, with parses (1+2) *3 and 1+(2*3). The associated trees are shown

for the sentence (1+2) *3 are shown. It is instructive to compare the (identical) abstract syntax trees in Figures 6.2(b) and in 6.3(b). The former has to be rejected because the corresponding parse tree contains a priority conflict between + and *, whereas the latter is acceptable. This in Figure 6.2. The ambiguity in this example is clearly caused by the lack of a definition of the priority (and, in other sentences, associativity) of the operators + and *. The parse tree in Figure 6.2(a) should be rejected when, as usual, * has a higher priority than +. In Figure 6.3 the trees shows that parse trees rather than abstract syntax trees should be used for disambiguation.

explicit definitions of priority and associativity to the grammar. This latter method is adopted in There are at least two general methods to remove ambiguities from a context-free grammar. The first method is to introduce new non-terminals encoding the priority and associativity of the operator symbols in the grammar. The new non-terminals prevent certain derivations that were possible in the original grammar and made it ambiguous. This method has the disadvantage that the definition of priorities and associativities is implicit and that additional measures are necessary to prevent the new non-terminals from affecting the abstract syntax. The second method is to add

6.2. Priority and associativity

SDF provides three mechanisms for the definition of priority and associativity of functions in the context-free syntax (and thus of rules in the derived BNF grammar):

- relative priorities of functions,
- associativity of functions, and
- associativity of groups of functions.

The relative priority of functions is established by declarations of the form

f > 8

where f and g are complete function declarations. Notice that we do not assign absolute priority levels to functions, but establish only their priority relative to other ones. By taking the transitive closure of the priority declarations given in the SDF definition, a strict, i.e., non-reflexive, partial order on the set of context-free functions should be obtainable.

Functions with a higher priority bind more strongly and the corresponding nodes in the parse lower priorities. Chain and bracket functions may not appear in priority declarations. Priorities are declared in a separate section in the context-free syntax. Lists of function declarations serve as tree should thus appear at lower levels in the tree than nodes corresponding to functions with abbreviation, i.e., $f > \{g, h\}$ is an abbreviation for f > g, f > h.

Associativity attributes can be attached to binary functions of the form s op s -> s, where op is a literal or empty. Without associativity attributes, nested occurrences of such functions immediately lead to ambiguities, as is shown by the sentence

S-string op S-string op S-string,

parse trees containing related occurrences of a single function. The following associativity atwhere s-string is a sentence of sort s. The particular associativity associated with op determines the intended parse of such sentences. When a node corresponding to a function f has a first or last "child" (i.e., disregarding any intermediate chain function nodes) corresponding to a function g, we call these occurrences of f and g related. Associativity attributes define how to accept or reject tributes can be attached to a function f.

related occurrences of fassociate from left to right; related occurrences of fassociate from right to left; related occurrences of fassociate from left to right; right a 8 8 0 C left

related occurrences of f are not allowed.

non-assoc

30

From a syntactic point of view there is no difference between left and assoc. However, the attribute assoc in the SDF definition is translated into an assoc attribute in the derived signature (see rule S6 in Chapter 8). Therefore, assoc also has semantic consequences.

rences of different functions with the same priority. Group associativity is defined by prefixing a Group associativity attributes define how to accept or reject parse trees containing related occurist of function declarations in a priority declaration with one of the following attributes:

```
related occurrences of f and g associate from left to right;
                                              related occurrences of f and g associate from right to left;
                                                                                         related occurrences of f and g are not allowed,
                                                                                             non-assoc
                                                     right
```

The simplest application of priority and associativity declarations is elimination of parse trees where f and g are different functions appearing in the list.

a parent has a first or last "child" that is in conflict with the associativity of parent and a parent has a "child" with a lower priority than the parent itself; that contain one of the following conflicts:

Three examples will illustrate this use of priority and associativity. One way of making the ex-

ample in Figure 6.1 unambiguous is shown in Figure 6.4. The choices made in this definition are: * has a higher priority than +. The only interpretation of 1+2*3 thus becomes 1+ (2*3).

- + is left-associative. The only interpretation of 1+2+3 is thus (1+2) +3.
 - is also left-associative.

```
{bracket}
                                                                  ы
                                                                  (left)
                                            (left)
                      -> LAYOUT
                              syntax
                                           ы ы
^ ^
               ы
^
        syntax
                                     î
                              context-frae
                                                  "("E")"
                                                          priorities
E "*" E ->
              +[6-0]
sorts E
lexical
                      [u]
```

Figure 6.4. Unambiguous version of example in Figure 6.1.

Ŷ

```
٨
                                                                          E
                                                                          Ŷ
                                                                          ம வ
                                                                         E 1/1
                                                                          Ε'.
                                                                          î
                                                                                (c)
                                                                         {non-assoc: E "*" E . (left: E "+" E -> E,
                                     {non-assoc}
                                                 (non-assoc)
                                                             (bracket)
                                                       (right)
                                          (left)
                              (left)
           -> E
-> LAYOUT
                        syntax
                                                       의 되
수 수
                                                                          ٨
                                     Ŷ
                                          î
                                                 Ŷ
      syntax
                                                                          ω
                        context-tree
                                                                   priorities
                                                                          ы
           +[6-0]
                                                      -
sorts E
      lexical
                                                            Ξ ..)
                 [ \n]
                                                                          ω
```

Figure 6.5. More elaborate arithmetic expressions.

A more elaborate version of arithmetic expressions is given in Figure 6.5. The operators in these expressions have the following properties:

- has the highest priority and associates from right to left.
- * and / are next in the priority ordering, * is left-associative, / is non-associative, and *
 - and / form a non-associative group.

+ and - have the lowest priority, + is left-associative, - is non-associative, and + and - form
a left-associative group.

a left-associative group. This leads to the following association of parses with sentences:

Parse	1^(2^3)	(1-2) *3	(1*2)*3	none	none	none	(1+2)+3	(1-2)+3	
Sentence	1^2^3	1^2*3	1*2*2	1/2/3	1*2/3	1-2-3	1+2+3	1-2+3	

The solution of the classical dangling else problem is shown in Figure 6.6. The priority declaration selects the parses in which else-parts are associated with the nearest possible preceding if-part. The sentence if x then if y then stat else stat will thus be parsed as if x then begin if y then stat else stat end.

Figure 6.6. Solution to the dangling else problem.

The examples in Figures 6.1, 6.4, 6.5 and 6.6 illustrate how the definition of priority and associativity can be used to reject certain parse trees of a sentence. There are, however, SDF definitions for which this form of disambiguation is not sufficient since they generate sentences that have more than one *conflict-free* parse tree. How can in such cases the set of remaining parse trees be reduced still further? Our solution is to extend the priority ordering > on functions to a priority ordering > on parse trees and to reject a parse tree if there is another parse tree with a higher priority. The relation $P_1 >> P_2$ holds between two parse trees P_1 and P_2 if

- P_1 is not equal to P_2 , and
- if, for any f, P_1 contains more nodes corresponding to f than P_2 , then P_2 contains more nodes corresponding to some function g with g < f than P_1 .

(This also covers the cases that there are no nodes corresponding to f in P_2 or no nodes corresponding to g in P_1).

The ordering >> is a variant of the so-called multiset ordering [DM79,JL82].

32

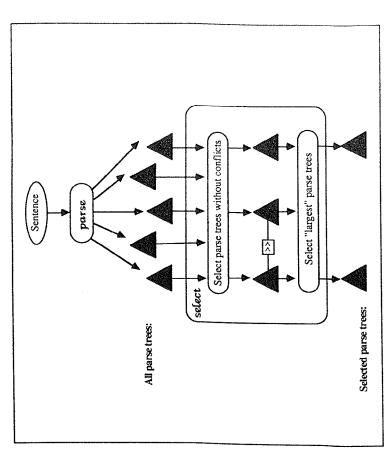


Figure 6.7. Selection of parse trees for a given sentence.

The parse trees for a given sentence are thus selected in two phases. First, the parse trees containing conflicts are removed. Next, all parse trees are removed that are smaller than another remaining parse tree. Note that whereas the first phase may invalidate a sentence by blocking all its parse trees, the second phase always selects at least one parse tree, so a sentence that passes the first selection phase also passes the second one. The total selection process is illustrated in Figure

We illustrate this approach with the example in Figure 6.8 in which arithmetic expressions with the operators + and * are defined over natural and real numbers. In this example, the sorts N and R stand for, respectively, the natural and real numbers. On both sorts, the operators + and * are defined. Finally, there is a chain function embedding N in R. Ambiguities may arise in this example since one can sometimes choose between using an operator defined on N together with a conversion from N to B, or using the operator defined on R directly. Therefore, priorities are defined such that

- * on N has a higher priority than * on R;
- + on n has a higher priority than + on R;
- * always has a higher priority than + irrespective of the sort involved (as usual).

33

```
N "+" N -> N > E "+" R -> E
                                                                         R "*" R -> R >
                                             (left)
                           LAYOUT
                                                                         ۸
2
                      Ŷ
                            ^
     syntax
                                                                          ^- Z = * :
z
z
                                                                   priorities
                                                        04 p4
                      Ω...
                                             N .. * :
           +[6-0]
sorts D
                            [u]
      lexical
                                                                          z
     3.5.
3.7.
3.7.
110.
120.
```

Figure 6.8. Arithmetic expressions for natural and real numbers.

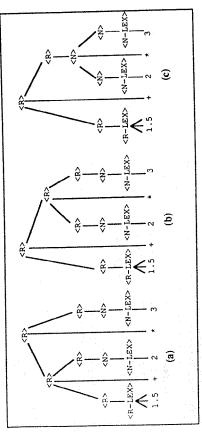


Figure 6.9. The three parse trees of 1.5 + 2 * 3.

free. Comparing these two trees, one sees that (c) >> (b) holds. The only function that occurs by the fact that * on R (which has a lower priority) appears once in (b) but not in (c). Hence, tree sponding to * on R has as chird a node corresponding to + on R. Trees (b) and (c) are conflictmore often in (c) than in (b) is * on N: it occurs once in (c) but not in (b). This is compensated for These priorities select parses with the ordinary priority of + and * and a preference for functions on N. Figure 6.9 shows the three possible parse trees for the sentence 1.5+2*3. The priorities from the example are now applied as follows. Tree (a) contains a conflict since a node corre-(c) is the (only) parse tree associated with the sentence 1.5+2*3.

script followed by a superscript in a special way. Therefore, the special case "E sub E sup E" is As a final example, we show in Figure 6.10 how the interaction between general context-free nates from [AJU75] and concerns expressions describing subscripts and superscripts in the typesetting language EQN. The crucial point is that, for typesetting reasons, we want to treat a subintroduced in line 5, which should have priority over a combination of the functions defining sub functions and special case functions can be described by means of priorities. The example origiand sup in lines 3 and 4.

*

ω -> E > {left: E sub E -> E, E sup E -> (bracket) Ŷ Ŷ **^ ^** ы ы sorts E context-free E sub E E sup E dns E dns E qns E priorities ans 3

Figure 6.10. Expressions for subscripts and superscripts.

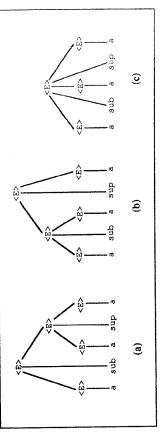


Figure 6.11. The three parse trees of a sub a sup

6.11(a) has to be rejected since it contains a conflict (caused by left group associativity). From the two remaining trees, the one in 6.11(c) is selected since it is larger (in the multiset ordering) than Figure 6.11 shows the three parse trees of the sentence a sub a sup a. The parse tree in the one in 6.11(b).

7. VARIABLES IN SDF DEFINITIONS

7.1. Motivation

The lexical and context-free syntax sections in an SDF definition completely define which input modify them. There are, however, cases in which the need arises for incomplete or parameterized sentences are legal and how they should be mapped onto (one or more) abstract syntax trees. These input sentences are constant and completely fixed; there is no systematic way to extend or input sentences. Two important cases are:

- If one associates semantic rules with SDF functions (see Chapter 9), it is necessary to use numbers, one needs rules of the form $x^*(y+1) = x^*y+x$, where x and y are variables over variables in these rules. For instance, when defining the rules for multiplication on natural the sort of natural numbers.
- complete. The text contains "holes" that still have to be filled in with strings of a certain During syntax-directed editing, the program text under construction is most likely to be intype. It is desirable to be able to determine the syntactic correctness of such incomplete pro-

To handle such cases, SDF allows the definition of variables.

7.2. Definition of variables

Variables are declared in the fifth (and last) section of an SDF definition. The variables section consists of a list of declarations of variables together with their sort. Each declaration defines a numing scheme for variables and may thus declare an unlimited number of variables. A naming scheme is an arbitrary regular expression like the ones allowed in a lexical function declaration, except that we do nor allow sorts in it. The sort of a variable is a basic sort that may be contained in a list construct with or without separators.

We first describe the overall effect of variables on the derived BNF grammar, derived signature, and mapping from parse trees to abstract syntax trees. Next, we discuss the treatment of variables of the predefined sort CHAR.

Variables lead to additional rules in the derived regular grammar and the derived BNF grammar. For each variable declaration of the form

```
naming-scheme -> SORT,
```

e rule

<SORT-VAR> = naming-scheme

is added to the derived regular grammar. Note that *sorr* may be either a basic sort or a list sort. Now there are two cases:

(a) If the declaration has the form naming-scheme -> SORT with SORT a basic sort, add the

```
<SORT> ::= <SORT-VAR>
```

to the derived BNF grammar;

(b) If the declaration has the form naming-scheme -> (SORT sep) &, the rule

<SORT-in-sep-list> ::= <{SORT sep}⊗-VAR>

is added to the derived BNF grammar. In principle, lists declared as {SORT sep}@ may contain variables of type SORT, {SORT sep}*, or {SORT sep}+ as elements. A subtle point arises when a list declared as {SORT sep}*, contains only variables of type {SORT sep}*. In that case, the list may become empty after substitution, and this is clearly incorrect in view of the type of the original list. Therefore, we impose the restriction that a variable of type {SORT sep}* may only occur in a list of type {SORT sep}* if that list contains at least one other element of type SORT or {SORT sep}*. This restriction is not encoded in the derived BNF grammar, but it forms an additional constraint on it.

```
1. sorts ID DECL TYPE
3. |a-z|+
3. |a-z|+
-> LAYOUT
5. context-free syntax
6. decl (ID ",")+ ":" TYPE -> DECL
integer -> TYPE
7. variables
7. variables
7. ids0 -> TYPE
7. ids0 -> TYPE
7. ids1 -> (ID ",")+
```

Figure 7.1. Declarations extended with variables.

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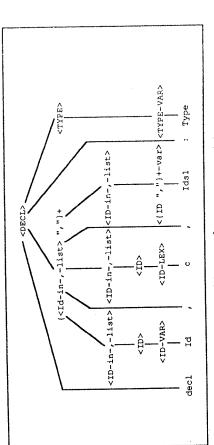


Figure 7.2. (a) Parse tree for decl Id, c, Ids1 : Type

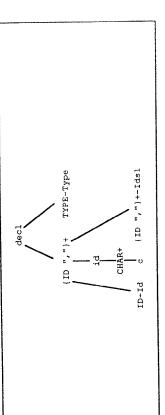


Figure 7.2. (b) Abstract syntax tree for decl Id, c, Ids1 : Type.

In the mapping from parse trees to abstract syntax trees, variables are mapped on corresponding variables in the derived signature. A variable declaration of the form

```
naming-scheme -> SORI,
```

will lead to variables named SORT-name1, SORT-name2, etc., where name1 and name2 are strings matched by the regular expression naming-scheme. This leads to rules R6, G6, and M6 in Chapter 8.

Recall that such variables are implicitly defined by a signature (see Section 2.3). Also recall from Section 4.7 that the Prefer Literals rule gives precedence to the literals of the context-free syntax over variables. In this sense, variables behave just like other lexical items.

syntax over variables, in this sense, variables to the declaration language introduced earlier in Figure 5.6. The derived regular grammar is:

```
[3] <ID-LEX> = ("a" | ... | "z") +
[4] <LAYOUT-LEX> = " "
[6,7,8] <LITERAL-LEX> = "decl" | "," | ":" | "integer" | "real"
[10] <ID-VAR> = "Id"
```

```
::* <ID-LEX> | <ID-VAR>
::= "decl" { <ID-in-,-list> "," }+ ":" <TYPE>
                                                                                                                                                                   <ID-in-,-list> ::= <ID> | <{ID ","}*-VAR> | <|ID ","}+-VAR>
<TYPE> ::= "integer" | "real" | <TYPE-VAR>
<TYPE-VAR> = "Type"
<{ID ","}*-VAR> = "Ids0"
<{ID ","}+-VAR> = "Ids1"
                                                                            The derived BNF grammar is:
                                                                                                                                   <DECL>
                                                                                                                                                                                            (7,8,11) <TYPE>
                                                                                                                <1D>
                                                                                                                                     [6] <
                                                                                                                (3,10]
```

The derived signature is:

```
-> ID
-> DECL
                              -> TYPE
-> TYPE
                   id : CHAR+
decl : {ID ","}+ # TYPE
CHAR ID DECL TYPE
                                integer:
        functions
 []
                   [6]
```

1d, c, 1ds1 : Type, which contains occurrences of the variables 1d, 1ds1 and Type. Note that variables, unlike lexical items, do not have any further structure in the abstract syntax tree. Figure 7.2 shows the parse tree and the corresponding abstract syntax tree for the sentence deca

```
-> ID
-> LAYOUT
                                               -> DECL
-> TYPE
-> TYPE
                                      context-free syntax
decl { ID ","}+ ":" TYPE
integer
                                                                                   -> ID
-> TYPE
-> (ID ",")*
-> (ID ",")+
sorts ID DECL TYPE
lexical syntax
{a-z}+
                                                                                                                                  -> CHAR+
                                                                                                                          CHAR
                                                                           variables
                                                                                                                                 Chairs
                                                                                             Type
Ids0
Ids1
```

Figure 7.3. Declarations further extended with variables of sort CHAR

Now we turn our attention to the special case of variables of the predefined sort CHAR. Apart from the standard treatment of variables given above, some additional steps are necessary:

- Add to the derived regular grammar the symbol <CHAR-LEX> and associate with it a regular expression that enumerates all characters in the alphabet. •
- Add to the derived BNF grammar the non-terminal <CHAR> as well as the rules

```
::= <CHAR-LEX>, and
                   <CHAR-in--list> :: = <CHAR>
```

which defines a concrete representation for the lexical constructor function associated with ::= "sort" "(" <CHAR-in--list>+ ")", For each lexical sort sort add a rule of the form

This leads to rules R2 and G7 in Chapter 8.

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The effect of adding variables over the predefined sort CHAR is shown in Figure 7.3. The only difference with the previous example is the addition of the variables Char and Chars.

The derived regular grammar now becomes:

```
= "decl" | "," | ";" | "integer" | "real" = "Id"
# ("a" | ... | "z") +
                                                         <TYPE-VAR> = "Type"
<(ID ",")*-VAR> = "Ids0"
<(ID ",")+-VAR> = "Ids1"
                                    <LITERAL-LEX>
<ID-VAR>
                         <LAYOUT-LEX>
                         [4]
[6,7,8]
```

= "a" | ... | "z" | "0" | ... | "9" | = "Char"

= "Chars"

<CHAR+-VAR> <CHAR-LEX>

[14, 15]

The derived BNF grammar is:

```
::= <ID-LEX> | <ID-VAR> |
"id" "(" <CHAR-in--list>+ ")"
::= "decl" { <ID-in-, -list> "," }+ ":" <TYPE>
                                                                                         ::= <ID> | <{ID ","}+~VAR> | <(ID ",")*-VAR>
                                                                                                                                                                                                         ::= <CHAR> | <CHAR+-VAR> | <CHAR*-VAR>
                                                                                                                            ::= "integer" | "real" | <TYPE-VAR>
                                                                                                                                                                   ::= <CHAR-LEX> | <CHAR-VAR>
                                                                                                                                                                                                            <CHAR-in--list>
                                                                                             <ID-in-,-list>
                                                        <DECL>
                                                                                                                                  <TYPE>
                                                                                                                                                                       <CHAR>
[3, 10, 14, 15]
                   <II>
                                                          [6] <D|
[6,12,13]
                                                                                                               [7,8,11]
                                                                                                                                                    [14,15]
                                                                                                                                                                                         [14,15]
```

The derived signature is:

```
...Declarations of constants for all characters in the alphabet... id : CHAR+
                             -> ID
-> TYPE
-> TYPE
                                       decl : {ID ","}+ # TYPE
CHAR ID DECL TYPE
                                                  integer:
real:
         functions
 []
                               [6]
```

Figure 7.4 shows the parse tree and corresponding abstract syntax tree for the sentence decl ab, id(Char y Chars) : Type.

7.3. Substitution of variables

Is it possible to define a notion of string substitution for ariables in concrete sentences that is g abstract syntax trees as defined in Section 2.3? Given a string s containing a marked occurrence of a variable x of sort A and a string s' of sort A' $\leq A$, we want to define s[x:=s] as the syntactically correct string in which the marked occurrence of x has been replaced by s' in such a way that directly related to variable substitution in the corresp-

abs(s[x:=s]) = abs(s)[A-x:=abs(s)]

where abs(s) is the set of abstract syntax trees of s (cf. Figure 2.3), A-x is the variable of sort A that corresponds to x in the derived signature, and the :=-operator in the right-hand side is the substitution operator on abstract syntax trees defined in Section 2.3. For the above requirement to be meaningful we assume that s, s' and s[x:=s] have only a single abstract syntax tree.

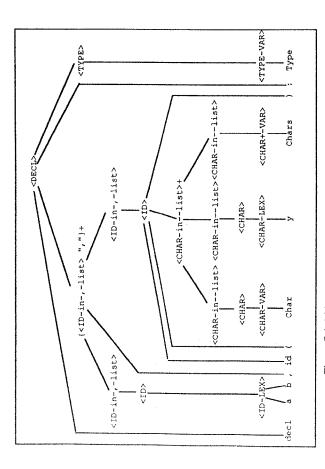
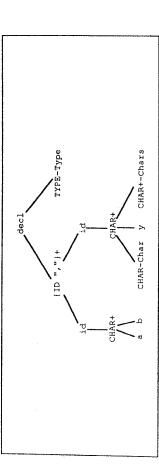


Figure 7.4. (a) Parse tree for decl ab, id (Char y Chars) : Type



id(Char y Chars) Figure 7.4. (b) Abstract syntax tree for decl ab,

Even if all three abstract syntax trees involved are unique, the :=-operator on strings cannot be as simple as that on abstract syntax trees for two reasons:

- To ensure that abs distributes over :=, as we require, it will sometimes be necessary to enclose s' in brackets before the actual string substitution is performed
- If x is a list variable occurring in a list with non-empty separators and s' is the empty string, substitution of s' for x may require removal of one of the list separators adjacent to x.

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It will sometimes be necessary to insert a layout symbol before and after the substituted string to avoid differences in the lexical interpretation of the string before and after

We now discuss the first two points in more detail and assume that the third point can always be resolved. We call a string substitution s[x:=s] improper if the abstract syntax tree obtained after tree substitution is not equal to the tree obtained after performing the string substitution and reparsing the resulting string, or, in other words, if

 $abs(s[x:=s]) \neq abs(s)[A-x:=abs(s')].$

We first define prot(s'), the protected version of s' in the substitution s[x:=s]. There are two

- If the substitution s[x:=s] is improper, define prov(s) as the string open s' close, where "open" A' "close" -> A' is an arbitrary bracket function for the sort A'. Such a sinction always exists (cf. Section 5.4).
- Otherwise, prot(s') = s'

Next, we define s[x:=s] as the string obtained by replacing a substring z of s by prot(s), where z is defined as follows:

- If x is a variable of sort (SORT sep)*, with sep not empty, that appears as element of a list, and t is the empty list distinguish three cases:

 (a) if x is the only element of the list, z is the marked occurrence of x;

 (b) otherwise, if x is the last element of the list, z is the marked occurrence of x together with the separator sep preceding it and the layout in between (if any);

 (c) otherwise, z is the marked occurrence of x together with the separator sep following it
- and the layout in between (if any).
- In all other cases, z is the marked occurrence of x.

We give some examples. Continuing the example giving in Figure 7.1, let

s = decl Ids1, c, Id : Type, with corresponding bystract syntax tree t, x = Ids1, and

s' = a, b, with corresponding tree t'.

The value of the string substitution s[Ids1:=s] is decl a, b, c, Id : Type with corresponding abstract syntax tree $t[\{ID ","\}+-Ids1;=t']$.

As a second example, let

s = decl Ids0, c, Id : Type, with corresponding tree t,

x = Ids0, and

 $s' = \varepsilon$, with corresponding tree t'.

The value of the string substitution s[Ids0:=s] is decl c, Id : Type with corresponding abstract syntax tree t[(ID ",")*-Ids0:=t]. Note the elimination of the separator "," following

Next, consider the arithmetic expressions defined in Figure 6.1. We add a declaration

```
Exp -> E
```

variables

for the variable Exp to it. First look at

s = Exp + 4, with corresponding tree t,

x = Exp, and

s' = 2 * 3, with corresponding tree t'.

The value of s[Exp:=s] is 2 * 3 + 4 with abstract syntax tree t[E-Exp:=t], Next, look at

s = Exp * 4, with corresponding tree t,

s' = 2 + 3, with corresponding tree t'.

in this case, brackets have to be inserted since the function at the root of s' (i.e. "+") has a lower becomes (2 + 3) * 4. Clearly, 2 + 3 * 4 would be an incorrect value for s[Exp:=s], since priority than the function at the parent node of Exp (i.e. "*"). Therefore, the value of s[Exp:=s] /[E-Exp:=t] is not an abstract syntax tree for it.

dering) of the selection of parse trees based on the priority declarations. Consider the example A final example will illustrate the effect of the second phase (i.e., application of the multiset orgiven in Figure 6.10, after adding the declaration

variables Exp -> E for the variable Exp to it. Now look at

s = a sub Exp, with corresponding tree t,

= Exp, and ×

= a sup a, with corresponding tree t'.

To block the higher priority but improper parse using the E sub E sup -> E function, brackets have to be inserted and the value of s[Exp:=s] becomes a sub (a sup a) with abstract syntax ree f(E-Exp)=f.

7.4. Discussion

First, ambiguities may occur between the regular expressions defining variables and other regular cally. Probably, some general disambiguation rule should be introduced (e.g. "Prefer non-Vari-Three problems have not yet been solved very satisfactorily in the above definition of variables. expressions defined in the lexical syntax. Currently, these ambiguities are not resolved automatiables"), but we need more experience with SDF before we can formulate it.

and efficiently, implement substitution. Such an implementation will, of course, not insert a tion to determine whether this substitution was proper or not. We expect that sufficient conditions Second, a naive implementation of substitution would have to reparse the string after substitucan be found to determine this and that an implementation based on these conditions can correctly, minimal number of brackets.

implementation (Generic Syntax-directed Editor, see Chapter 10), for each declared sort s, a without fixing a particular syntax for them. However, the implementation of a syntax-directed Therefore, we take the point of view that the syntax-directed editor may automatically extend a given SDF definition with standard declarations for variables for each sort. In our current variable declaration of the form "<s>" -> s is generated. These variables are only used by the Finally, some comments are in order regarding our uniform treatment of variables and "holes" (also known as "meta-variables"). Clearly, SDF variables allow a general description of holes, editor is considerably simplified when certain assumptions about the syntax of holes can be made. editor and may not be used otherwise.

8. SUMMARY OF SDF

8.1. Deriving grammars, signature and parse-tree-to-abstract-tree mapping

We can now give the final version of the definitions of derived regular grammar, derived BNF grammar, derived signature, and mapping from parse trees to abstract syntax trees.

8.1.1. Derived regular grammar

The derived regular grammar is obtained as follows:

RI For each sort L (including the predefined sort LAYOUT) that appears as the result sort of a sion with it consisting of the or of all left-hand sides (translated using rules R3, and R4) of lexical function, introduce the lexical non-terminal <1-1.Ex> and associate a regular expres-

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lexical function declarations for sort L. Replace sort names appearing in these left-hand sides by the corresponding lexical non-terminals defined before.

If the variables section contains declarations for variables of the predefined sort CHAR, introduce the (reserved) lexical non-terminal <CHAR-LEX> and associate a regular expression with it that enumerates all characters in the alphabet. 2

(Negated) character classes are replaced by an or of all characters in the class.

Repetitions are mapped onto the corresponding repetition operators in the regular grammar. 222

Each literal symbol occurring in a function definition in the context-free syntax is added as alternative to the (reserved) lexical non-terminal LITERAL-LEX>.

For each variable declaration of the form 88

naming-scheme -> SORT

where naming-scheme is a regular expression, and SORT may be either a simple sort or a list sort, add a regular expression of the form

<SORT-VAR> = naming-scheme

to the derived regular grammar.

8.1.2. Derived BNF grammar

rived grammar". In those cases we always mean that the non-terminal or rule is added unless it is In the following definition we will frequently say that a non-terminal or rule is "added to the dealready defined in the derived grammar. The derived BNF grammar is obtained as follows:

Introduce a non-terminal <s> for each sort s.

- The terminals are both the literal symbols appearing in context-free function declarations as well as the lexical non-terminals of the derived regular grammar, except <LAYOUT-LEX> and <LITERAL-LEX>. 55
 - For each sort L that appears as the result sort of a lexical function add a rule of the form: <L> ::= <L-LEX>, 3

where <L-Lex> is a lexical non-terminal introduced as terminal in G2.

For each list construct of the form (sorr sep) appearing in a context-free function declaration or a variable declaration, introduce a non-terminal < SORT-in-sep-list> and add a rule of the form: 25

<SORT-in-sep-list> ::= <SORT>.

For each context-free function declaration add rules obtained by exchanging the left-hand into the corresponding non-terminal as introduced in G1, and translate each occurrence of a side and the right-hand side of the function declaration. Translate each occurrence of a sort list construct in the function declaration into the corresponding list construct in the grammar, i.e., a list of the form (sorr sep)⊗ is translated to (<sorr-in-sep-list> sep)⊗, where < SORT-in-sep-list> is the non-terminal introduced in G4. SS

(a) If the declaration has the form naming-scheme -> SORI, with SORI a basic sort, add For each variable declaration distinguish two cases: 95

<SORT> :: = <SORT-VAR>,

where <sorr-var> is a lexical non-terminal of the derived regular grammar (R6).

(b) If the declaration has the form naming-scheme -> (sorr sep\⊗, add the rule: <SORT-in-sep-list> ::= <{SORT sep}⊗-VAR>

If the variables section contains declarations using the predefined sort CHAR do the followwhere <(sorr sep) ⊗-vAR> is a lexical non-terminal of the derived regular grammar (R6). 67

(a) Add the rules

::= <CHAR-LEX>, and

<CHAR-in--list> ::= <CHAR>,

where <CHAR-LEX> is a lexical non-terminal introduced as terminal symbol by G2.

(b) For each sort $sort \neq Layout$ that appears as the result sort of a lexical function, add a rule of the form

::= "sort" "(" <CHAR-in--list>+ < SORT>

This rule defines the concrete representation for the lexical constructor function associated with SORT (see S5 below).

8.1.3. Derived signature
The derived signature has the form:

- A declaration for the predefined sort CHAR.
- Declarations for all sorts declared in the SDF definition.
- Declarations of constants of sort CHAR for all characters in the alphabet. Subsort declarations for all chain functions in the context-free syntax.
- Declarations for lexical constructor functions of the form \$25 \$4 \$5 \$5

1 : CHAR+ ->

for each sort L that appears as result sort of a lexical function, where 1 is the name L written in lower case letters.

Function declarations for each function declared in the context-free syntax except chain new name is generated (in a manner not prescribed by SDF) and the types of its arguments and of its result are obtained from the sort names appearing in the original function definition. List constructs of the form (SORT Sep) are translated to corresponding lists in the functions and functions with the bracket attribute: for each such function some unique signature, i.e., to (SORT sep) . If the attribute assoc is attached to the original function declaration, it is inherited by the function declaration in the derived signature. 9S

Recall that variables are implicitly defined by a signature (Section 2.3), therefore there is no explicit translation from the variables section of an SDF definition to its derived signature (also see M6 in Section 8.1.4).

8.1.4. Mapping from parse trees to abstract syntax trees

- If the root of P is labeled with a non-terminal and has a single child C whose root is labeled with lexical non-terminal <1-LEX>, with $L \neq LITERAL$, the result of transforming P is an abstract syntax tree whose root is labeled with the lexical constructor function for sort L and The mapping from parse trees to abstract syntax trees is defined as follows. Let P be a parse tree: MI If the root of P is labeled with a non-terminal and has a single child C whose root is labeled whose single child is the result of transforming C (by using rule M2).
- If the root of P is labeled with lexical token $\langle L-LEX \rangle$, with $L \neq LITERAL$, its children form a list C of characters. Such a P is transformed into an abstract syntax tree whose root is labeled with CHAR+ and with the characters in the list C as children. 3
 - If the root of P is labeled with {SORT sep}⊗, there are two cases: N
- (a) sep is empty: let $C_1,...,C_k$ be the k children of the root of P; or
- (b) sep is not empty, the root of P has 2k-1 children and let $C_1,C_3,...,C_{2k-1}$ be the odd numbered children (i.e. the children corresponding to list elements and not to separators).
- Let A be the list of abstract syntax trees obtained by recursively transforming the trees Ci. The result of transforming P is a tree whose root is labeled with $\{sorr sep\} \otimes and that has$ the elements of A as children.
- If the root of P is labeled with a non-terminal and corresponds to a chain function, the result of transforming P is the transformation of the single child of its root. ユ

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- bracket attribute, the result of transforming P is the transformation of the second child of If the root of P is labeled with a non-terminal and corresponds to a function with the XS.
- its root, i.e., the only child labeled with a non-terminal. If the root of P is labeled with lexical token < L-VAR>, it must have a list consisting of charactersC₁,...,C_k as its single child. Such a P is transformed into the corresponding variable L-c1...ck in the derived signature. **№**
 - If the root of P is labeled with <sorr-in-sep-list>, the result of transforming P is the transformation of its single child. 2
 - (a) All children of the root of P that are labeled with a non-terminal are transformed recur-Otherwise, the root of P is labeled with a non-terminal and P is transformed as follows: sively. This gives a (possibly empty) list A of abstract syntax trees. <u>X</u>
- (b) The root of P together with its children correspond to the application of some rule R in the derived BNF grammar and some function F in the derived signature. P is now transformed into an abstract syntax tree whose root is labeled with F and with the elements of Aas children.

8.2. Static constraints on SDF definitions

All constraints on SDF definitions are now listed for ease of reference (some of them were already mentioned in the preceding Chapters 3, 4, 5 and 6).

Sorts

- Multiple declarations of sorts are forbidden.
- The names LAYOUT and CHAR are predefined and cannot be used in a sort declaration.
- The sort LAYOUT may only occur as result sort of a lexical function.
- The sort CHAR may only be used as result sort of variable declarations.
- All sort names used in lexical or context-free functions, or variable declarations should be declared
- Each sort should occur as result sort of at least one (lexical or context-free) function declaration.

Lexical syntax

- Multiple declarations of lexical functions are forbidden.
- All sorts used in lexical function declarations should be declared.

 Each sort occurring in the left-hand side of a lexical function declaration should occur as result sort in at least one other lexical function declaration.
 - No cyclic dependency may exist between lexical function declarations.
- Each result sort (except LAYOUT) should occur in the left-hand side of at least one (lexical or context-free) function declaration.
 - Character classes should satisfy the restrictions given in Section 4.3. .

Context-free syntax

- Multiple declarations of context-free functions are forbidden (even if they have different attributes).
- Each sort occurring in the left-hand side of a context-free function declaration should occur All sorts used in context-free function declarations should be declared.
 - as result sort in at least one other (lexical or context-free) function declaration.
 - No cyclic dependency may exist between chain functions
- The attribute bracket is only allowed for functions of the form "open" S "close" s (see Section 5.4).
 - The associativity attributes Left, right, assoc, and non-assoc are only allowed for binary functions of the form s "op" s -> s (see Section 6.2).

A suitable bracket function should be declared for the argument and result sorts of all context-free functions that either have an associativity attribute or occur in priority or group associativity declarations.

Priorities

All functions occurring in a priority declaration should be declared in the context-free syn-

The group associativity attributes left, right, and non-assoc are only allowed for

No cyclic dependency may exist between context-free functions due to priority declarations. binary functions of the form s "op" s -> s (see Section 6.2). Chain and bracket functions are not allowed in priority declarations.

Variables

All result sorts (except CHAR) occurring in variable declarations should occur as result sort All result sorts (except CHAR) occurring in variable declarations should be declared. in the context-free syntax.

tax-directed editor from a given SDF definition, and, as explained in the introduction, it can also Having completed the definition of SDF itself, we have now at our disposal a powerful method for transforming concrete strings into (sets of) abstract terms. This is sufficient to generate a synbe used to couple semantics to it by means of abstract syntax tree matching.1. 9 ATTACHING SEMANTICS TO SDF DEFINITIONS

In Section 9.1, we will show SDF can be combined with algebraic semantics. In Section 9.2. we introduce modularity constructs. In both cases, ASF [BHK89, Chapter 1] will be used as semantic specification formalism.

9.1. Attaching algebraic semantics to SDF

ture, declaring sorts and functions, and a set of conditional equations over this signature. The functions declared in such a module have a fixed syntax. We will now combine ASF with SDF In its simplest form, a module in the algebraic specification formalism ASF consists of a signa-(obtaining ASF+SDF) in the following manner:

- · Replace the signature in the ASF module by an SDF definition (this defines a derived signature as well as concrete notation for all functions in the signature);
- Replace equations written in abstract form by equations written in concrete form (see be-

The result is a formalism with completely user-definable syntax.

In its simplest form, an ASF equation is described by the grammar rule

<equation> ::= <tag> <term> "=" <term>

fix form). The two terms appearing in an equation should be of the same sort. An example of an where <tag> is a label identifying the equation and <term> defines all well-formed terms (in pre-ASF equation is:

[Bi] or(true, false) = true.

Now, the key idea is to replace the (abstract) terms in the above definition of equations by their concrete counterpart as defined by an SDF definition. For each specification SPEC, this can be achieved by using the following, parameterized, grammar rule <equation>[SPEC] for equations:

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SDF definition Semantic rules "-" BOOL -> BOOL > BOOL -> BOOL -> BOOL > BOOL -> BOOL BOOL (bracket) -> BOOL (assoc) BOOL (assoc) -- LAYOUT B2 v B1 false true false --> BOOL -> BOOL BOOL = false = false = true context-free syntax Ŷ Ŷ ٨ lexical syntax î BOOL "A" BOOL BOOL "V" BOOL false A false "-" BOOL ")" true A false false A true true A true priorities B v false B v true variables equations B [0-9]* B1 V B2 true false false <u>-</u> 18. 17.

Figure 9.1. Booleans: a specification of the Boolean data type.

∴	sorts ID PAIR TABLE lexical syntax [a-z]+	SDF definition -> ID -> LAYOUT	no
5	context-free syntax "("ID":"ID")" empty-table PAIR "0" TABLE lookup ID in TABLE variables Id ""*	-> PAIR -> TABLE -> ID -> ID	
13.	12. 1 13. equations 14. lookup Id in (Id : Id')	Semantic rules	les
15.	lookup Id 'in (Id' :]	Id ≠ Id' lookup Id in (Id' : Id'') ◊ T = lookup Id in T	

Figure 9.2. Tables: specification of a table data type.

where \$1,...,\$n are the sorts declared in the (SDF part of the) specification SPEC, and <s1>,...,<sn> are the non-terminals corresponding to these sorts in the derived BNF-grammar. Each concrete equation

^{*}Lists, subsorts and associative functions should be taken care of by the matching process.

(1) u = v

with u and v strings, can now be transformed into the abstract equation

```
[1'] abs(u) = abs(v)
```

provided that

- u and v are both syntactically correct strings;
- both u and v are unambiguous (alternatively, one could impose the weaker condition that the sets of abstract syntax trees for u and v both contain only a single tree of the same sort).

This same mapping can be carried out for conditional equations in the specification. The grammar to be used for parsing each equation of the specification SPEC thus consists of:

- an instance of the parameterized rule <equation>[SPEC] given above;
 - the derived grammar for the SDF part of SPEC.

The example in Figure 9.1 will illustrate this method. The derived regular grammar is:

The derived BNF grammar is:

The derived signature is:

		BOOL	BOOL		BOOL	TOOR VE
		î	î	î	î	1
				BOOL	BOOL	
				*# #	*10:	
ĭ				BOOL	BOOL	BOOT.
ĕ	n C	••	•••	••	••	•
sorts	functions	true:	false	: '<	:>:	֧֧֧֧֭֓֞֝֝֝֝ ֓
[]		[2]	(9)	[7]	[8]	(6)

Finally, the instantiation of <equation>[Booleans] for the example in Figure 9.1. is:

```
<equation>{Booleans} ::= <tag> <Bool> "=" <Bool>
```

Given these ingredients it should now be obvious how equations in concrete form are mapped to equations in abstract form. Equations 17 and 20, for instance, will be mapped to

```
[17] "^"(true, false) = false
[26] "\"(ROOL-B, true) = true
```

We conclude this section with three more examples. Figure 9.2 shows a definition of a table data type. It illustrates the use of a conditional equation in line 15. Figure 9.3 shows a definition of identifiers on which a length function is defined. Here we use character variables in combination with the (implicitly generated) lexical function id. Figure 9.4, shows a definition of natural numbers based on their decimal representation. It illustrates, among other things, the use of list variables.

Semantic rules SDF definition = succ(0)
= succ(length(id(Chars))) ID LAYOUT CHAR CHAR+ NAT NAT Ŷ **^ ^** Ŷ **^ ^** length(id(Char))
length(id(Chars Char)) context-free syntax length "(" ID ")" "(" NAT ")" lexical syntax
[a-z] [a-z0-9]* sorts ID NAT variables equations = 12. 1 2 6 4 3 2 1

Figure 9.3. Identifiers: specification of identifiers with a length function.

9.2. Binding SDF to a modular specification formalism

Once we have explained how ASF and SDF can be combined at the level of a single module, it is relatively straightforward to cover the modularization constructs of ASF as well. The operations to be considered are

- export/hiding of sorts and functions;
- import of a module in another module;
- renaming of sorts and functions of a module;
- actualization of parameterized modules

In ASF, the meaning of these operations is defined by means of a normalization procedure, i.e. a textual expansion procedure that eliminates all modular structure from a specification and yields a single, unstructured, specification consisting of a signature and equations. By and large, the same method can be applied to the combination of ASF and SDF. Examples of ASF+SDF specifications can be found in [Hen89, vdM88, HK89b].

10. NOTES ON THE IMPLEMENTATION OF SDF

A prototype implementation of SDF has been completed. It is written in LeLisp and uses ISG (Incremental Scanner Generator [HKR87b]) to generate lexical scanners from the lexical syntax of the SDF definition, and IPG (Incremental Parser Generator [HKR88]) to generate parsers from the context-free syntax of the SDF definition. Both generators are *lazy* as well as *incremental* (i.e., only those parts of the scanner and parser are generated that are actually needed, and modifications to the lexical and context-free syntax are propagated to the already generated scanner and parser, thus avoiding their complete regeneration). The underlying principles have been described in [HKR87a].

Another distinctive feature of ISG and IPG is that they allow ambiguities. ISG may produce more than one interpretation for a lexeme; IPG can handle arbitrary context-free grammars and may thus produce more than one abstract syntax tree for a given input string.

The current SDF implementation has been incorporated in a Generic Syntax-directed Editor (GSE) [Log88, DK89a,b]. A single SDF definition is thus all that is needed to generate a syntax-directed editor.

move digit(cl) in 0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18 = nats1 SDF definition Semantic rules = n, nats2 nats nats nats nats nats * nat(c) nat(c1) + nat(c2) = nat(x c)x1) + nat(0 x2) + nat(0 x) = nat(y)in n1,n2,n3,n4,n5,n6,n7,n8,nats in n1,n2,n3,n4,n5,n6,n7,n8,n9,nats + nat (y1) move digit (c2) in nats1 nat(c1) + nat(c2) "+" NAT -> NAT *("," TAN) * nat(y2) = nat(y)NAT-LIST NAT-LIST + nat (x2 c2) = nat (y nl, n2, n3, n4, n5, n6, n7, nats DIGIT CHAR* CHAR NAT NAT in nl,n2,n3,n4,n5,n6,nats in nl,n2,n3,n4,n5,n6,n7,n NAT = nat (y 0) n2,n3,n4,n5,nats Ŷ Ŷ Á Ŷ Ŷ Ŷ **^^^** , n3, n4, nats priorities NAT "*" NAT -> NAT > NAT , n2, n3, nats sorts DIGIT NAT NAT-LIST move DIGIT in NAT-LIST Û , n2, nats syntax = nat(y) * nat (y2 nl, nats n2 syntax nat(x1 c1) context-free NAT "+" NAT nats [0-9]* *("," TAN) variables *[6-0] *[6-0] u * [6-0] nat(0 y) equations nat (0 DIGIT+ lexical move move move move move move 30. 925. ERE BOSE

Figure 9.4. Naturals: specification of decimal natural numbers.

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As far as the implementation of ASF+SDF is concerned, we are currently in the research phase. Some major problems have to be addressed:

- How should the composition of grammars (resulting from the composition of ASF+SDF modules) be implemented? [Kli89] and [Rek89] describe our first results in this area.
- A similar composition problem exists at the semantic level: how are compiled versions of the equations in different modules to be combined?

11. DISCUSSION

11.1. Basic assumptions

We briefly recall some of the main assumptions and choices underlying the design of SDF:

- The implementation of SDF does not impose restrictions on the class of acceptable grammars. This has several major advantages: it is never necessary to rewrite a given grammar to fit a particular subclass of the context-free grammars and the composition of grammars is always possible. It also means that context-free and abstract syntax bear a close resemblance to each other. As a consequence, there is little need for explicit abstract syntax tree construction rules (see next point). The other side of the picture is that grammars may become ambiguous.
- There is a fixed mapping between parse trees and abstract syntax trees. The advantages of
 this choice are twofold: the writer of the specification does not have to give a separate definition of the tree construction process and the user of the specification sees trees that correspond to grammar rules in a completely predictable way. Clearly, a degree of freedom has
 been lost here. Associating "non-standard" trees with a grammar rule can only be achieved,
 in our case, by computing them by means of semantic rules.
- Lexical entities are represented as strings of characters and not as trees. While the latter representation is attractive from a theoretical point of view, we opted for the former for reasons of efficiency in the SDF implementation.

11.2, Omissions

Some of the features not included in SDF are:

- There is no way of expressing prettyprinting formats for functions. The main reason for this omission is that adding this information would make SDF function definitions harder to read. The editors generated from SDF-definitions by the GSE editor generator mentioned in the previous Chapter do not use prettyprinting but maintain both the original text representation as well as the corresponding abstract syntax tree.
 - There is no notion of optional constructs in context-free functions.
 - There is no alternative operator.
- Repetitions (in lexical syntax as well as in the context-free syntax) cannot be restricted to a fixed number of repetitions. This has to be expressed by means of semantic rules.

11.3. Limitations of lexical syntax

As explained in Section 4.7, SDF uses the Prefer Longest Match rule for eliminating ambiguities in the lexical syntax and the Prefer Literals rule for eliminating ambiguities between lexical and context-free syntax. Both rules impose some limitations on the expressive power of the lexical syntax.

The Prefer Longest Match rule rejects all lexemes that are included in a longer one. After applying it there may still be more than one lexical token, but all of them will correspond to the same (maximal) lexeme. Unfortunately, this may lead to rejection of the intended lexical interpretation of a sentence. Some examples of this phenomenon are:

• A Pascal range expression like "3..5" will be split in the lexemes "3." (a real constant with empty fraction part) and ".5", whereas the intended interpretation is "3", "..." (the range

- operator), and "5". A similar problem exists for the lexical analysis of the Fortran expres-
- In some languages, such as Fortran and Algol68, layout is completely ignored and keywords may even occur as prefix of, for instance, identifiers. In such cases, only the com plete identifier (and not the embedded keyword) will be recognized.

One way of solving these problems is to add new operators (such as the look ahead operator of proach is to generalize our current model for lexical analysis even further and to allow ambiguous LEX) that allow an explicit treatment of such exceptional cases. A potentially more interesting aplexical interpretations corresponding to overlapping lexemes of different length. The (general context-free) parser can then select the correct sequence of lexical tokens.

as a legal statement in the example in Figure 11.1, since the tokens if, while, and then are only recognized as literals, and not also as identifiers. One, not very satisfactory, way to circumvent this limitation is shown in Figure 11.2: all keywords have been added explicitly as alternatives of The Prefer Literals rule (Section 5.2) gives precedence to literals in the context-free syntax over other fexical tokens. As a consequence, the sentence if .= while + then will not be accepted sort ID to the context-free syntax. This definition has the disadvantage that identifiers (defined by a function in the lexical syntax) and keywords (defined by constants in the context-free syntax) are represented differently in the abstract syntax. This difference will manifest itself when string matching is attempted on an identifier that happens to be equal to a literal. Altematives for solving this problem are:

- Forbid constants in the context-free syntax.
- Add exceptions to the definition of the derived signature and of the mapping from parse trees to abstract syntax trees in such a way that constants defined in the context-free syntax and lexical functions are represented in a uniform way.
 - Add a mechanism to (de)activate the Prefer Literals rule.

Further research is needed to determine the best approach to this problem.

Another, general, limitation of the definition of lexical syntax in SDF, is that no "actions" (i.e., updating of counters, consulting symbol tables, etc.) can be performed when a token is being recognized. As a result, several aspects of lexical syntax are difficult to express in SDF:

- Nesting of comments (as, for instance, in C);
- The use of indentation for indicating block structure (as, for instance, in ABC and OC-CAMO

Apart from a default solution in the form of attaching extra semantic rules to the SDF definition, we do not yet see a really elegant solution to this class of problems.

```
-> ID
-> LAYOUT
                                               STAT
STAT
EXP
EXP
                                         -> STAT
                                                ^ ^ ^ ^
                               context-free syntax
                                               while EXP do STAT
ID ":=" EXP
                                       if EXP then STAT
sorts ID EXP STAT
         syntax
                                                               EXP "+" EXP
              [a-z]+
        lexical
                       [u]
                                                                       9
```

Figure 11.1. A simple language.

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ID LAYOUT ID ID ID ID STAT STAT EXP **^ ^** Ŷ ٨ Ŷ Ŷ **^ ^** Ŷ syntax do STAT if EXP then STAT EXP STAT syntax ID ":=" EXP EXP "+" EXP context-free while EXP +[2-e] lexical while 2 10.

Figure 11.2. Language from Figure 11.1 with ever' pping keywords and identifiers.

cessor of Smalltalk-80 --- did support syntactic extensibility: each class had to parse the messages These ideas have led to user-definable syntax for operators in Algoló8, Prolog, Snobol4 and other programming languages, and to various styles of macro-definitions (PL/I, Lisp). Around 1970, there was much interest in so-called extensible languages [Iro70, Sta75, Weg70]. The aim tion formalism. New language constructs could then be added to the base language by defining however, the overall goal of full syntactic and semantic language extensibility has never been completely achieved. Although it does not have a syntactic extension mechanism, Smalltalk-80 send to it explicitly. This feature has been replaced by a more limited scheme of keyword paramof this line of research was to define a small base language in combination with a syntax definitheir syntax and by describing their semantics in terms of the base language. For various reasons, may be viewed as the most successful extensible language in existence. (Smalltalk-72 — a prodeeters in Smalitalk-80. This new scheme result in more readable programs and allows a more effi-There have been many attempts to introduce user-definable syntax in programming languages cient implementation.)

rected translations [Iro61, ASU85]. Lex/Yacc and Metal (to be discussed below) fall into this caregory. The Lithe system [San82] combines syntax-directed translations with classes. Apart from tional specifications [Odo85] constitute an alternative to syntax-directed translations. Most closely A successful method for defining the syntax of language constructs is by means of syntax-dithe fact that its lexical syntax is fixed, Lithe has user-definable LR(1)-syntax. O'Donnell's notarelated to our work are the user-definable distfix operators in OBJ [FGJM85] and Asspegique/Cigale [Voi86].

The following features can be used to characterize syntax definition formalisms:

- (a) The class of acceptable grammars.
- (b) The integration between the description of lexical and of context-free syntax.
 - (c) The class of context-free syntax/abstract syntax pairs that can be described.
- (d) The integration between the description of context-free syntax and of abstract syntax.
 - (e) The treatment of variables.

Metal (the specification language of the Mentor system [KLMM83]), SSL (the specification language of the Synthesizer Generator [Rep84, RT89]), and the specification language of the PSG We will restrict ourselves to some representative examples, namely Lex [LS79], Yacc [Joh79], system [BS86]. In [HK89a] we have already compared SDF with Lex, Yacc and Metal by studying several examples in each of these formalisms.

The syntax definitions for Lex/Yacc, Metal, and SSL are restricted to LALR(1) grammars, those for PSG to LL(1) grammars, while SDF definitions allow arbitrary context-free grammars.

In Lex/Yacc explicit token names are used for the communication between lexical and contextree syntax. A similar method is used in Metal, SSL and PSG. In SDF, there is a better integration between lexical and context-free syntax. Token names are, for instance, generated automati-

Léx/Yacc allow the greatest freedom in the creation of abstract syntax trees (i.e., arbitrary C data structures). In Metal, abstract syntax is described by means of a signature-like notation. With each rule in the context-free grammar, a tree construction rule is associated which defines the abstract syntax tree to be constructed for strings accepted by this grammar rule. This allows the construction of arbitrary trees provided that they conform to the given signature. In SSL, the construction of abstract syntax trees is described by a separate attribute grammar. In this respect, SSL has the same expressive power as Metal. In PSG, abstract syntax is defined by a collection of class and constructor rules resembling signatures, while concrete syntax is defined by a collection of class and constructor and a constructor of the abstract syntax is associated with each context-free grammar rule (this limits the set of trees that can be constructed for each grammar rule). In SDF, there is a fixed correspondence between rules in the context-free syntax and rules in the abstract syntax. It is therefore impossible to associate an arbitrary tree with strings accepted by a given syntax rule.

Metal, SSL and PSG have built-in notations for variables (also called meta-variables, placeholders, or holes). SDF has no such standard convention but allows the definition of naming schemes for variables.

11.5. Future developments

The following problems remain to be solved:

- The treatment of ambiguities needs further research: (a) it is desirable to have a sufficient but not overly restrictive condition on SDF definitions that guarantees that they define a non-ambiguous language; (b) the use of type information to resolve ambiguities should be
- Generalization of the model for lexical analysis as discussed in Section 11.3.
 - Implementation techniques will have to be developed for ASF+SDF.
- The combination of SDF with other formalisms such as TYPOL [Des84, Kah87], Prolog, and first-order logic should be studied. Some of the problems involved are: (a) signature and term translations (necessary to map the derived signature of SDF definitions and terms over it on signatures and terms as they exist in the target specification formalism); (b) modelling of relations (SDF only provides definitions of functions).

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LITERATURE

- [AJU75] A.V. Aho, S.C. Johnson & J.D. Ullman, "Deterministic parsing of ambiguous grammars", Communications of the ACM, Vol. 18, No.8, 1975, pp.441-452.
 - [ASU85] A.V. Aho, R. Sethi & J.D. Ullman, Compilers: Principles, Techniques and Tools, Addison-Wesley, 1985.

- [BHK89] J.A. Bergstra, J. Heering & P. Klint (eds.), Algebraic Specification, ACM Press in co-operation with Addison-Wesley, 1989.
- [BS86] R. Bahike & G. Snelting, "The PSG system: from formal language definitions to interactive programming environments", *Transactions on Programming Languages and Systems*, Vol. 8, Number 4, 1986, pp. 547-576.
- [DK89a] M.H.H. van Dijk & J.W.C. Koorn, "Implementation of a generic syntax-directed editor", Fourth Annual Report ESPRIT Project GIPE, 1989.
 - [DK89b] M.H.H. van Dijk & J.W.C. Koorn, "GSE User's manual", User's Manual of the
- Centaur System, Version 0.9, 1989.

 N. Dershowitz & Z. Manna, "Proving termination with multiset orderings", Communications of the ACM, Vol. 22, Number 8, 1979, pp. 465-476.
- [Des84] T. Despeyroux, "Executable specification of semantics", in Semantics of Data Types, G. Kahn, D.B. MacQueen & G. Plotkin (eds.), Lecture Notes in Computer
- Science, Vol. 173, Springer-Verlag, 1984, pp. 215-233.

 K. Futatsugi, J. A. Goguen, J.-P. Jouannaud, and J. Meseguer, "Principles of OBJ2", in Conference Record of the Twelfth Annual ACM Symposium on Principles.
 - ples of Programming Languages, ACM, 1985, pp. 52-66.

 [HK89a] J.Heering & P. Klint, "The syntax definition formalism SDF", in [BHK89, Chapter 6]. Also in ESPRIT '86: Results and Achievements, North-Holland,
- 1987, pp. 619-630.
 [HK89b] J. Heering & P. Klint, "PICO revisited", in [BHK89, Chapter 9]. Also in ESPRIT '88: Putting the Technology to Use, North-Holland, 1988, pp. 365-379.
- [HKKL85] J. Heering, G. Kahn, P. Klint & B. Lang, "Generation of interactive programming environments", in ESPRIT '85: Status Report of Continuing Work, Part I, North-Holland, 1986, pp. 467-477.
- [HKR87a] J. Heering, P. Klint & J. Rekers, "Principles of lazy and incremental program generation", Report CS-R8749, Centre for Mathematics and Computer Science,
- Amsterdam, 1987. [HKR87b] J. Heering, P. Klint & J. Rekers, "Incremental generation of lexical scanners", Report CS-R8761, Centre for Mathematics and Computer Science, Amsterdam,
- [HKR88] J. Heering, P. Klint & J. Rekers, "Incremental generation of parsers", CS-R8822, Centre for Mathematics and Computer Science, Amsterdam, 1988.
 - [Hen89] P.R.H. Hendriks, "Type-checking Mini-ML", in [BHK89, Chapter 7]. Abbreviated version in Proceedings of CSN87: Computing Science in the Netherlands, SION, 1987, pp. 21-38.
- [Iro61] E.T. Irons, "A syntax-directed compiler for Algol 60", Communications of the ACM, Vol. 4, No. 1, 1961, pp. 51-55.
- [Iro70] E.T. Irons, "Experience with an extensible language", Communications of the ACM, Vol. 13, No. 1, 1970, pp. 31-40.
- [JGHMK86] W.N. Joy, S.L. Graham, Ch.B. Haley, M.K. McKusick & P.B. Kessler, "Berkeley Pascal User's Manual—Version 3.1, April 1986", 4.3 Berkeley Software Distribution, Computer Systems Research Group, University of California, Berkeley, 1986.
 - [JL82] J.-P. Jouannaud & P. Lescanne, "On multiset orderings", Information Processing Fenters Vol 15 No. 2, 1982, pp. 57-63.
 - Letters, Vol. 15, No. 2, 1982, pp. 57-63.
 [Joh79] S.C. Johnson, "YACC— yet another compiler-compiler", in UNIX Programmer's Manual, Vol. 2B, Bell Laboratories, 1979.

	101111111111111 , science of Computer 1 regramming, 101: 3, 1363, pp. 131-166.	
[Kah87]	G. Kahn, "Natural semantics", in Fourth Annual Symposium on Theoretical As-	
	pects of Computer Science, ed. F.J. Brandenburg, G. Vidal-Naquet, and M.	
	Wirsing, Lecture Notes in Computer Science, Vol. 247, Springer-Verlag, 1987,	
	pp. 22-39.	

[Kli89]	P. Klint, "Scanner generation for modular regular grammars", in Liber Amicorum,
	J.W. de Bakker, 25 jaar Semantiek, Centre for Mathematics and Computer Sci-
	ence, Amsterdam, 1989, pp. 291-305.

[88go7]	M. Logger, "An integrated text and syntax-directed editor", Report CS-R8820,
	Centre for Mathematics and Computer Science, Amsterdam, 1988.

E.A. van der Meulen, "Algebraic specification of a compiler for a language with pointers", Report CS-R8848, Centre for Mathematics and Computer Science, Amsterdam, 1988. [vdM88]

M. J. O'Donnell, Equational Logic as a Programming Language, MIT Press, [ODo85]

T. Reps & T. Teitelbaum, The Synthesizer Generator: a System for Constructing [RT89]

Language-based Editors, Springer-Verlag, 1989.

J. Rekers, "Modular parser generation", Report, Centre for Mathematics and Computer Science, Amsterdam, to appear, 1989. [Rek89]

T. Reps, Generating Language-Based Environments, MIT Press, Cambridge, [Rep84]

D. Sandberg, "Lithe: A language combining a flexible syntax and classes", in Conference Record of the Ninth Annual ACM Symposium on Principles of Pro-Mass., 1984. [San82]

gramming Languages, ACM, 1982, pp. 142-145.

T. A. Standish, "Extensibility in programming language design", SIGPLAN No-tices, Vol. 10, No. 7, 1975, pp. 18-21.

F. Voisin, "Cigale: a tool for interactive grammar construction and expression [Sta75]

[Voi86]

parsing", Science of Computer Programming, Vol 7., 1986, pp. 61-86.

B. Wegbreit, Studies in Extensible Programming Languages, Dissertation, Harvard, 1970, Reprinted by Garland Publishing, 1980. [Weg70]

APPENDIX 1: SDF IN SDF

Lit iorF		-> CharRange -> CharClass -> L-Char -> L-Char -> Literal -> Literal	-> LAYOUT -> LAYOUT -> LAYOUT -> SPEDEfinition -> Module		-> Section -> CfBlem -> CfBlem -> CfBlem -> CfBlem -> CfBlem -> CfBlem -> Attributes -> Attribute
Id Iterator Id Iterator Esochar C-char CharRange Charclass L-char Spredefination Module Section LexicalFunction BasicLexelem LexElem CFFunction CfElem Attributes Attribute PriorChain FunctionList GroupAttribute Pr. Variable VarSort A-Zi A-	[A-Za [] [] [0-1] [0-1] [C-char "-" C-char "[" charRange* "]" ~ [\000-\037"\\] Escchar "\" L-char* "\"" [a-z] [a-z] [A-Za-z0-9\]* [A-Za-z0-9]	<pre>[\t\n\r] "\$" ~ (\n] * "\n" "\$" ~ (\n\$] + "\$" context-free syntax Section* "module" Id SDFDefinition</pre>	Id+	"context-free" "syntax" CfFunction+ [CfElem* "->" Id Attributes Id Literal Id Iterator "[" Id Literal"]" Iterator % empty % Attribute "[" [Attribute","]+ "]" "pracket" "ssoc" "non-assoc" "left"

-> Section -> PriorChain -> PriorChain -> FunctionList -> FunctionList -> PriorFun -> PriorFun -> GroupAttribute -> GroupAttribute

"priorities" Priorchain

(FunctionList ">")+

(FunctionList "<")+

PriorFun
"(" (PriorFun ",")+ ")"

"(" GroupAttibute ":" (PriorFun ",")+ ")"

Cfelam "->" Id
"left"

-> Attribute

"right"

-> Section
-> Variable
-> VarSort
-> VarSort
-> VarSort
-> VarSort
-> VarSort
-> VarSort

"variables" Variable+
LexElem+ "->" VarSort
Id
Id Iterator
"(" Id Literator
"(" HRN" Iterator
"CHAR".

"non-assoc"

"right"

	Decl FuncDecl LabelList LeType rt Variant	-> LAYOUT -> LAYOUT -> StarcomChar -> StarcomChar -> LAYOUT -> LAYOUT	-> Id -> Base -> Base	-> StringElem -> StringElem -> CharString -> CharString	-> OctalConst -> UnsignedInt -> SignedInt -> SignedInt	-> UnsignedReal -> UnsignedReal -> UnsignedReal	-> Number -> Number -> Number	-> Program -> Program -> Progleading -> Block	-> Decl -> Decl -> ConstDecl -> Const -> Const -> Const
sorts StarComChar Id StringElem CharString Base UnsignedInt SignedInt UnsignedReal Number OctalConst	Program ProgHeading Block Decl LabelDecl ConstDecl TypeDecl VarDecl ProcDecl FuncDer ProcHeading FuncHeading Pars Par Const Type SimpleType FileType NonfileType StructType Field FieldList VariantPart Var Var QualifiedVar Statement Assignment CaseListElem Expr SetElem ActualPar	<pre>lexical syntax [\t\n\r] "(" ~[)] * ")" * [*] "*" ~ [)] "(*" StarComChar "*)" "#inolude" ~[\n] * "\n"</pre>	[a-zA-Z] [a-zA-Z0-9]* "oct" "hex"	<pre>~ ['\n] "'" StringElem+ "'" "*" StringElem+ "'"</pre>	[0-7]+ [bB] [0-9]+ UnsignedInt [+\-] UnsignedInt	UnsignedInt "." UnsignedInt UnsignedInt "." UnsignedInt [eE] SignedInt UnsignedInt [eE] SignedInt	UnsignedInt UnsignedReal OctalConst	<pre>context-free syntax ProgHeading Decl* Block "." Decl* program Id "(" [Id ",")+ ")" "," begin (Statement ",")+ end</pre>	<pre>label (UnsignedInt ",")+ const {ConstDecl ",", "," Id "=" Const CharString Id Number "+" Number</pre>

> QualifiedVar	-> Assignment -> Statement	<pre>~> CaseListElem -> CaseListElem</pre>	-> Expr ->	
OualifiedVar "^"	Var ":=" Expr Assignment begin (Statement ";")+ end if Expr then Statement if Expr then Statement if Expr then Statement repeat (Statement ";")+ until Expr for Assignment too Expr do Statement for Assignment downto Expr do Statement asse Expr of (CaseListElem ";")+ end with (Var ",")+ do Statement Id "(" (ActualPar ",")+ ")" UnsignedInt Statement goto UnsignedInt \$ empty \$	<pre>{Const ","}+ ":" Statement</pre>	Number nil Charstring Var Id "(" {ActualPar ","}+ ")" not Expr "-" Expr "+" Expr Expr "-" Expr	

-> SimpleType -> SimpleType -> SimpleType -> FileType -> NonfileType -> NonfileType -> NonfileType -> NonfileType

Id "(" [Id ",")+ ")" Const ".." Const file of NonfileType SimpleType

packed StructType

StructType

StructType packed StructType

-> Decl -> TypeDecl -> Type -> Type -> Type -> Type

-> Const

type {TypeDecl ";"}+ ";"
Id "=" Type

"-" Number

SimpleType

FileType

-> StructType -> StructType -> StructType -> FieldList -> Field -> VariantPart -> VariantPart -> VariantPart -> VariantPart -> VariantPart -> VariantPart -> VariantPart

array "[" (SimpleType ",")+ "]" of Type set of SimpleType record FieldList end Field.",")+ VariantPart [Id ",")+ ":" Type

% empty %
{Const ","}+ ":" (" FieldList ")"

% empty %

var (VarDec1 ";")+ ";"
{Id ",")+ ":" Type

ProcDecl

% empty %
case Id of {Variant ";"}+
case Id ":" Id of {Variant ";"}+

-> Decl
-> ProcHeading
-> ProcDecl
-> ProcDecl
-> ProcDecl
-> ProcDecl
-> ProcDecl

procedure Id Pars ";"
ProcHeading Dec1* Block ";"
ProcHeading forward ";"
ProcHeading external ";"
ProcHeading external ";"

-> Decl -> VarDecl -> Decl -> FuncHeading -> FuncDecl -> FuncDecl -> FuncDecl -> FuncDecl

function Id Pars ":" Type ";"
Funcheading Decl* Block ";"
Funcheading forward ";"
Funcheading external I;"
Funcheading external I";"

FuncDecl

--> Pars --> Pars --> Par --> Par --> Par

% empty % [Id "."] + "]" [Id "."] + ":" Id procedure [Id Pars function Id Pars ":" Id

--> Var --> Var --> QualifiedVar --> QualifiedVar --> QualifiedVar --> QualifiedVar --> QualifiedVar

QualifiedVar "," + "]"

GualifiedVar "[" {Expr "," } + "]"

QualifiedVar "[" {Expr "," } + "]"

Id "." Id

Id "." Id

9

```
75
```

```
/ non-assoc:

{ non-assoc:
    Expr ">" Expr ">" Expr ">" Expr "<" Expr ">" Expr ">"
                                                                                                                                                                                                                                                                                                                                                { left:
   Expr "*" Expr -> Expr, Expr "6" Expr -> Expr, Expr "/" Expr -> Expr,
   Expr div Expr -> Expr, Expr mod Expr -> Expr,
   Expr and Expr -> Expr )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  / left:
Expr "+" Expr -> Expr, Expr "-" Expr -> Expr, Expr "|" Expr -> Expr,
Expr or Expr -> Expr )
priorities

{ not Expr -> Expr, "~" Expr -> Expr,
 "+" Expr -> Expr, "-" Expr -> Expr }
```

Notes:

- This definition of Pascal conforms to [JGHMK86].
 The lexical definition of the range operator ".." is incorrect (see Section 11.3).