

R_forecast

Jerry Feng

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R Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see <http://rmarkdown.rstudio.com>.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
library(tseries)
```

```
## Registered S3 method overwritten by 'quantmod':  
##   method           from  
##   as.zoo.data.frame zoo
```

```
library(forecast)  
library(vars)
```

```
## Loading required package: MASS
```

```
## Loading required package: strucchange
```

```
## Loading required package: zoo
```

```
##  
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':  
##  
##   as.Date, as.Date.numeric
```

```
## Loading required package: sandwich
```

```
## Loading required package: urca
```

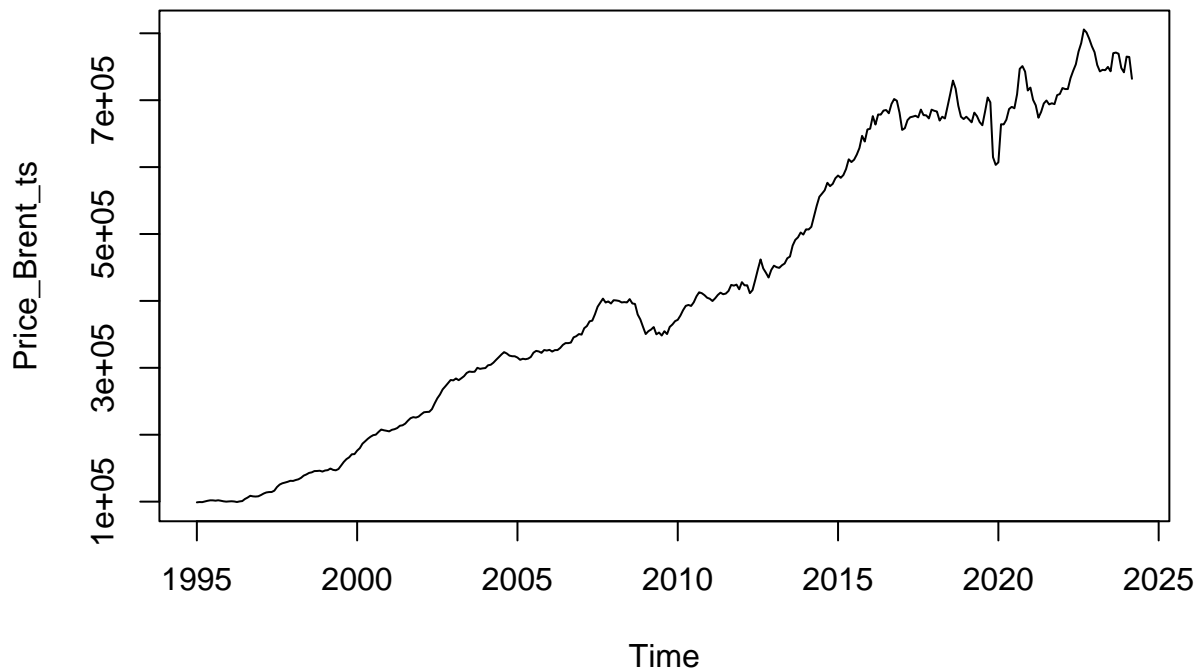
```
## Loading required package: lmtest
```

```
library(readr)
library(Metrics)
```

```
##
## Attaching package: 'Metrics'
```

```
## The following object is masked from 'package:forecast':
##
## accuracy
```

```
Brent_df <- read.csv("Updated_Brent.csv")
Brent_df$Date <- as.Date(Brent_df$Date, format = "%Y-%m-%d")
Price_Brent_ts <- ts(Brent_df$Average_Price, start = c(1995, 1), frequency = 12)
d_price <- ts(Brent_df$Detached_Average_Price, start = c(1995, 1), frequency = 12)
sd_price <- ts(Brent_df$Semi_Detached_Average_Price, start = c(1995, 1), frequency = 12)
t_price <- ts(Brent_df$Terraced_Average_Price, start = c(1995, 1), frequency = 12)
f_price <- ts(Brent_df$Flat_Average_Price, start = c(1995, 1), frequency = 12)
plot(Price_Brent_ts)
```

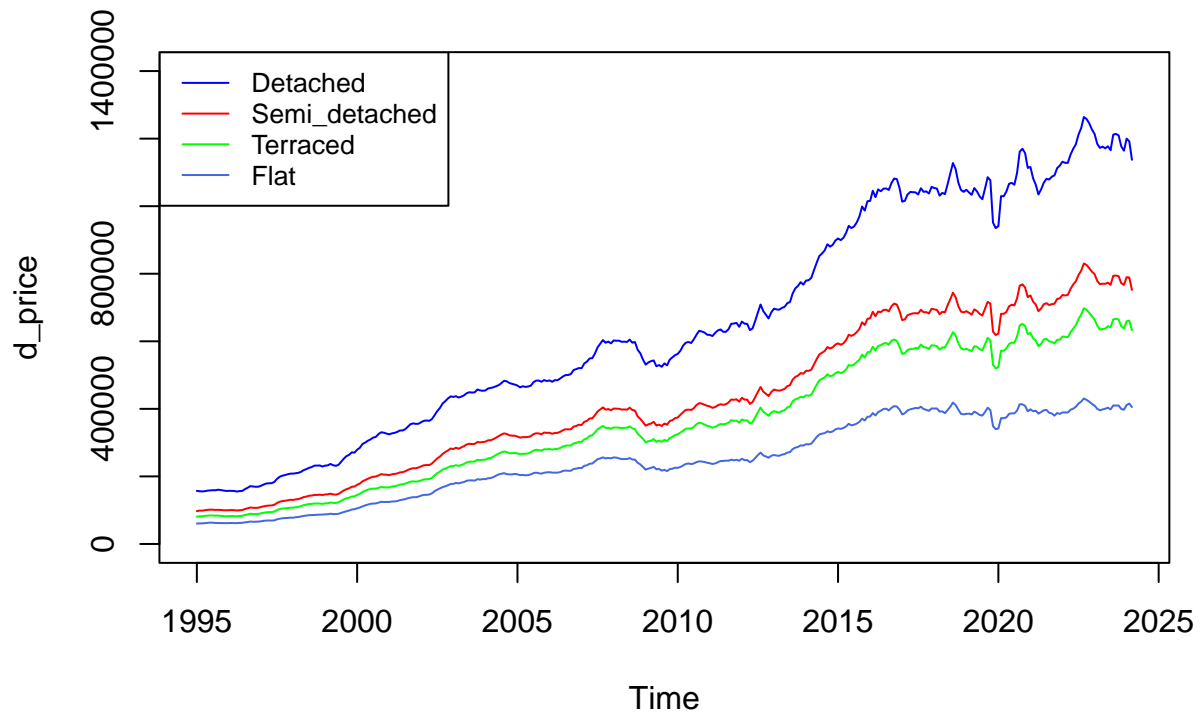


```
plot(d_price, col = "blue", ylim = c(0, 1400000))
lines(sd_price, col = "red")
lines(t_price, col = "green")
lines(f_price, col = "royalblue")
legend("topleft",
```

```

legend = c("Detached", "Semi_detached", "Terraced", "Flat"),
col = c("blue", "red", "green", "royalblue"),
lty = 1,
cex = 0.8)

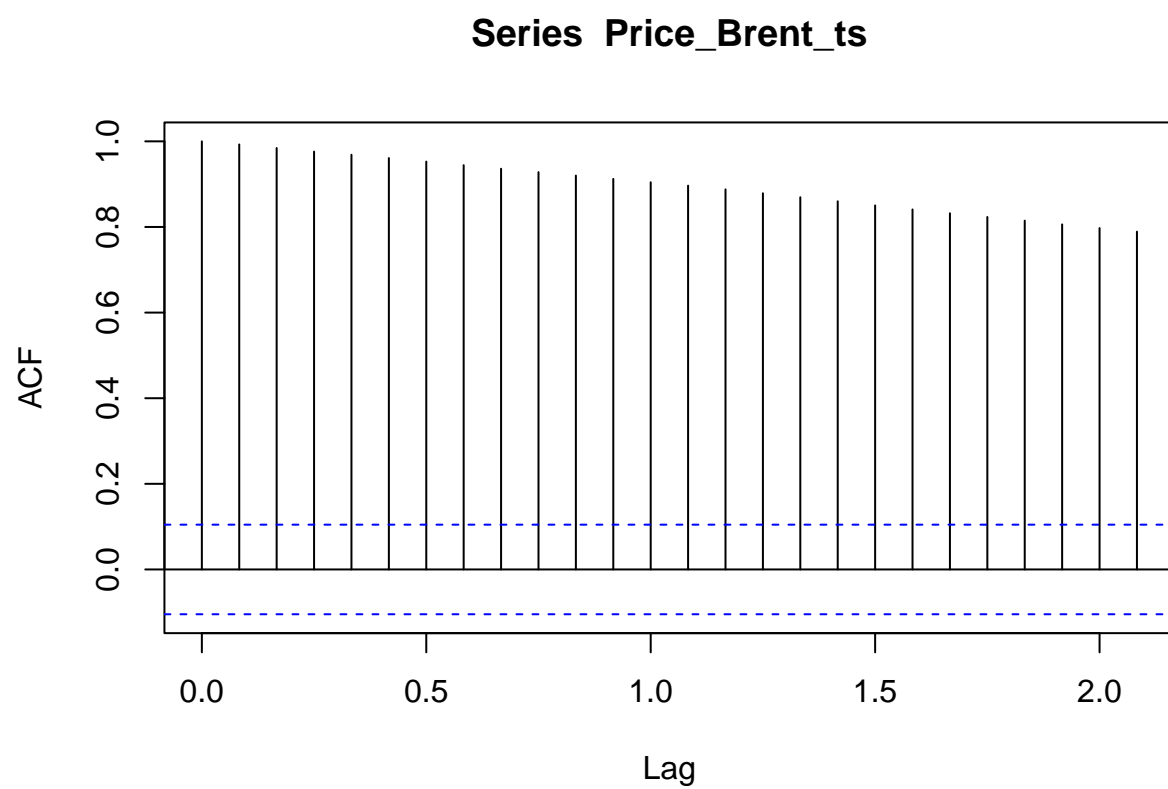
```



```

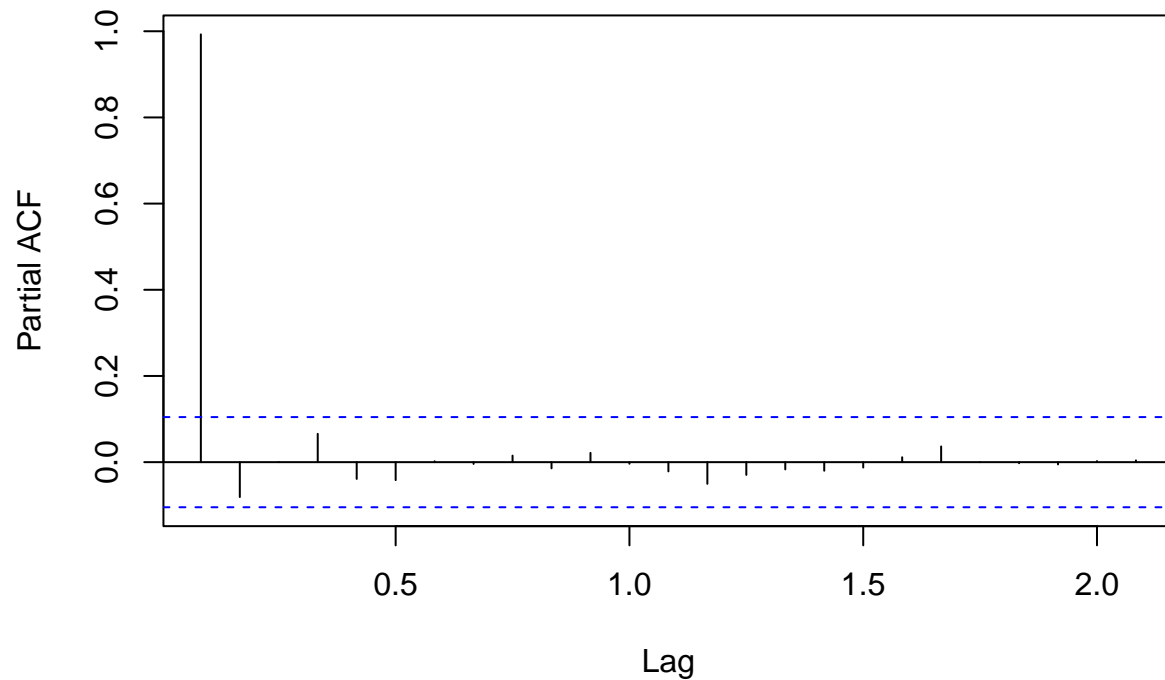
legacy_ts <- ts(Brent_df$Average_Price, start = c(1995, 1), end = c(2023, 6), frequency = 12)
Price_ts_2023_2024 <- window(Price_Brent_ts, start = c(2023, 6), end = c(2024, 3))
diff_legacy_ts <- diff(legacy_ts, differences=1)
acf(Price_Brent_ts)

```



```
pacf(Price_Brent_ts)
```

Series Price_Brent_ts



```
adf.test(Price_Brent_ts)
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: Price_Brent_ts  
## Dickey-Fuller = -2.3824, Lag order = 7, p-value = 0.4154  
## alternative hypothesis: stationary
```

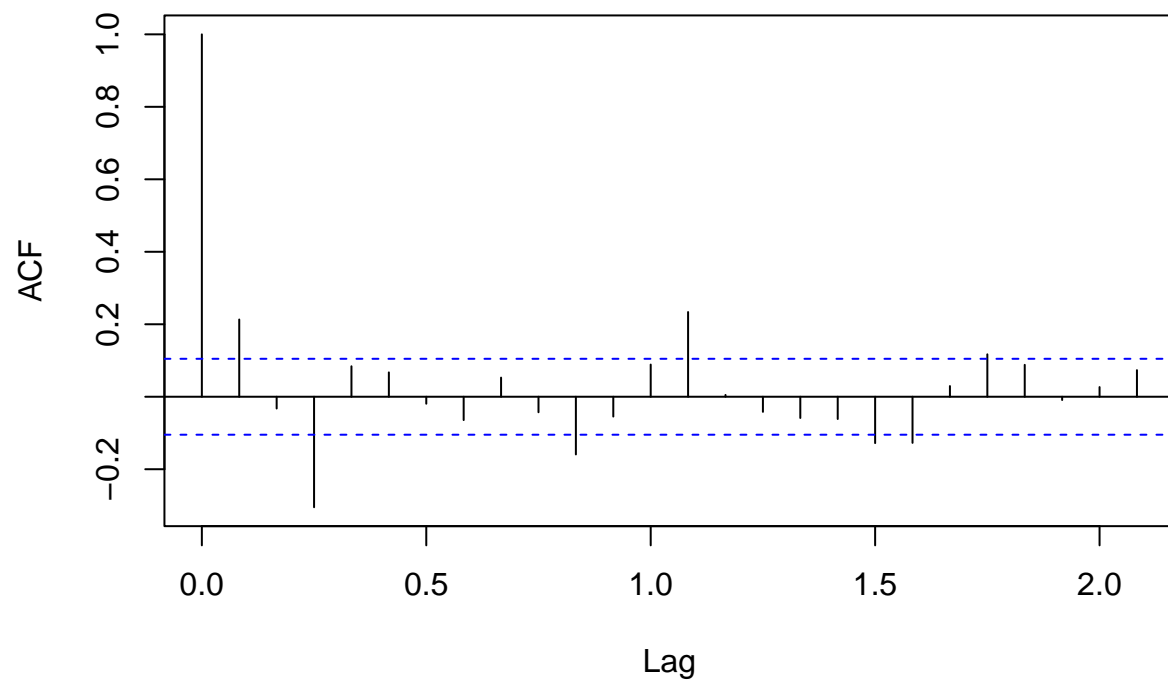
```
diff_Price_Brent_ts <- diff(Price_Brent_ts, differences=1)  
adf.test(diff_Price_Brent_ts)
```

```
## Warning in adf.test(diff_Price_Brent_ts): p-value smaller than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: diff_Price_Brent_ts  
## Dickey-Fuller = -5.7933, Lag order = 7, p-value = 0.01  
## alternative hypothesis: stationary
```

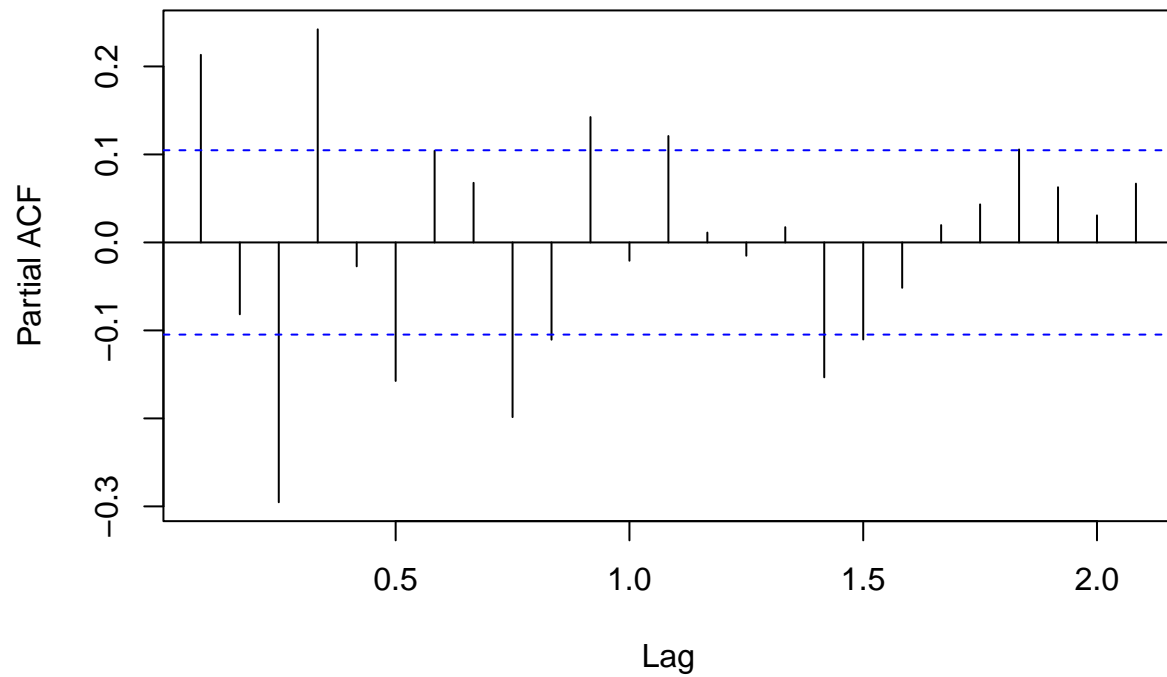
```
acf(diff_Price_Brent_ts)
```

Series diff_Price_Brent_ts



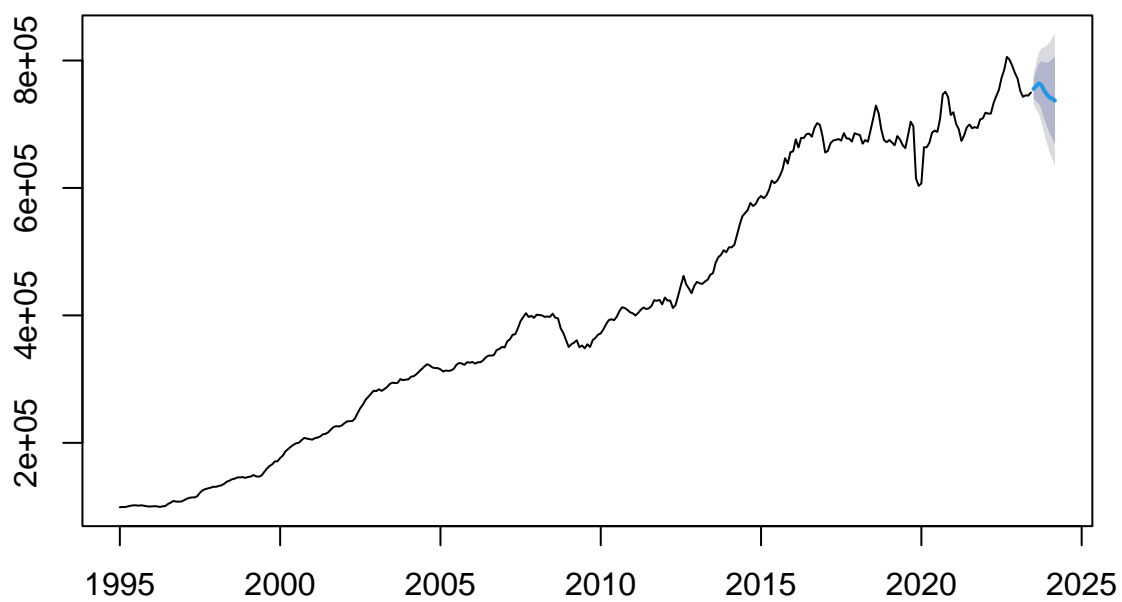
```
pacf(diff_Price_Brent_ts)
```

Series diff_Price_Brent_ts



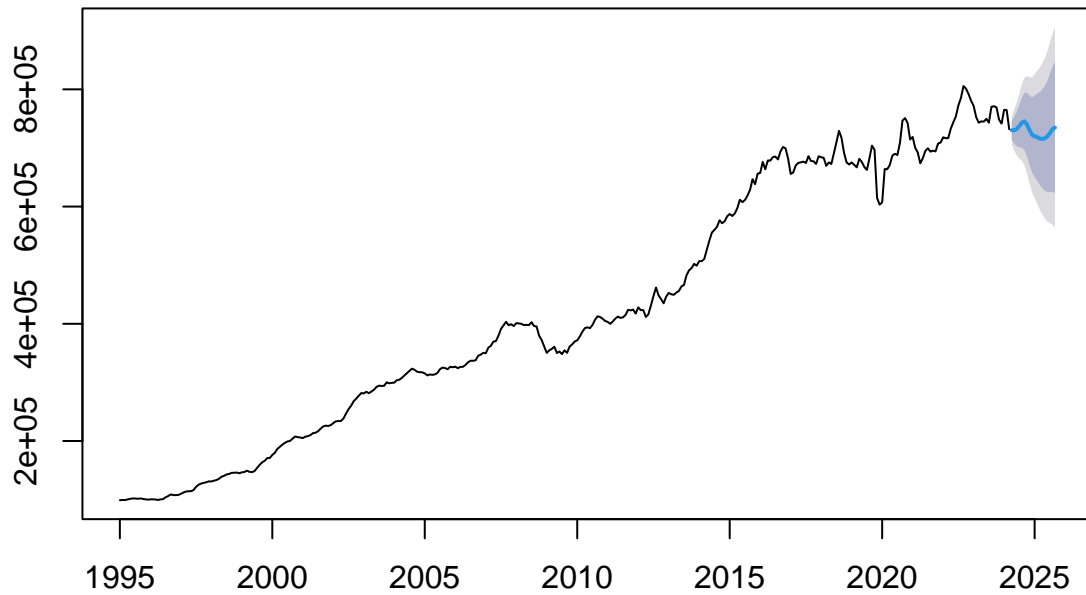
```
ets_Price_Brent_model <- ets(Price_Brent_ts, model = "ZZZ")
ets_Price_Brent_model_forecast <- forecast(ets_Price_Brent_model, h = 18)
ets_legacy <- ets(legacy_ts, model = "MAM")
ets_legacy_forecast <- forecast(ets_legacy, h=9)
ets_forecasted_values_legacy <- ets_legacy_forecast$mean
ets_forecasted_ts_legacy <- ts(ets_forecasted_values_legacy, start = c(2023, 6), frequency = 12)
plot(ets_legacy_forecast)
```

Forecasts from ETS(M,Ad,M)



```
plot(ets_Price_Brent_model_forecast)
```


Forecasts from ETS(M,Ad,M)



```
summary(ets_Price_Brent_model_forecast)
```

```
##
## Forecast method: ETS(M,Ad,M)
##
## Model Information:
## ETS(M,Ad,M)
##
## Call:
## ets(y = Price_Brent_ts, model = "ZZZ")
##
## Smoothing parameters:
##   alpha = 0.9998
##   beta  = 0.1056
##   gamma = 2e-04
##   phi   = 0.9284
##
## Initial states:
##   l = 98690.9278
##   b = 1236.2166
##   s = 0.9933 1.0031 1.0145 1.0202 1.0156 1.0055
##       0.9968 0.9912 0.9889 0.9886 0.9909 0.9915
##
## sigma: 0.0166
##
```

```

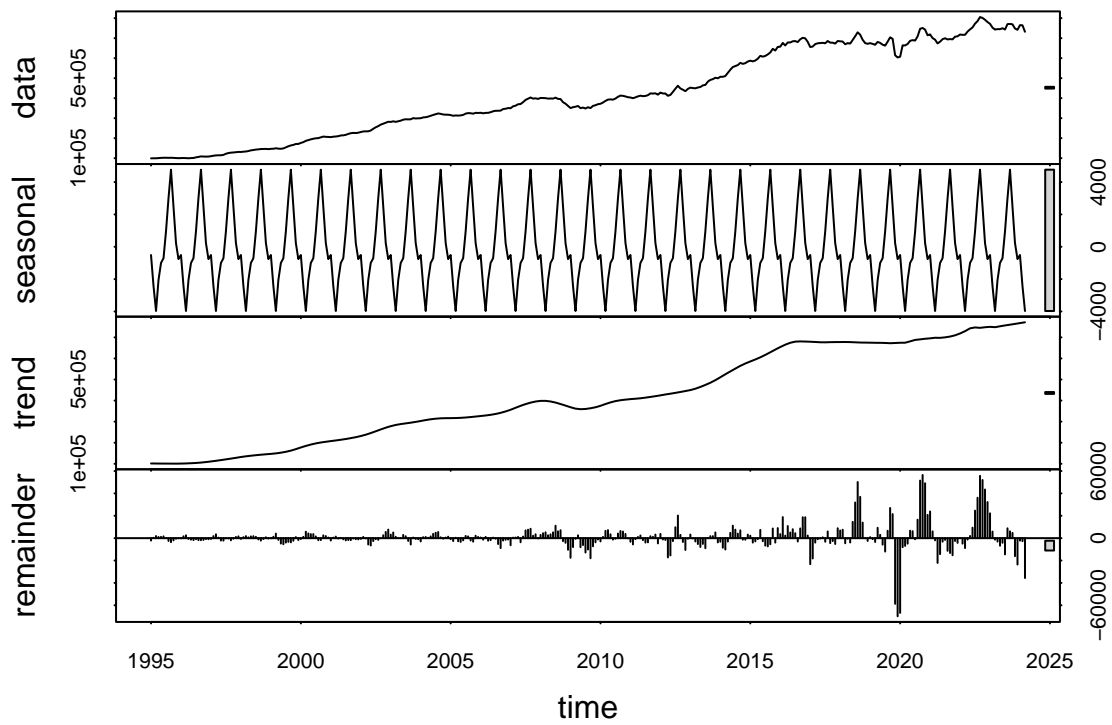
##      AIC      AICc      BIC
## 8174.991 8177.051 8244.485
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 722.7838 9067.059 5355.794 0.2295089 1.148674 0.170222 0.09078767
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Apr 2024      730253.7 714720.6 745786.8 706497.9 754009.5
## May 2024      730170.4 706986.3 753354.5 694713.4 765627.4
## Jun 2024      732599.7 702663.1 762536.2 686815.7 778383.7
## Jul 2024      737398.6 700985.6 773811.7 681709.7 793087.6
## Aug 2024      743295.8 700507.8 786083.8 677857.2 808734.4
## Sep 2024      745298.9 696457.1 794140.7 670601.8 819996.0
## Oct 2024      739867.9 685605.2 794130.7 656880.2 822855.7
## Nov 2024      730399.0 671222.7 789575.3 639896.6 820901.3
## Dec 2024      722194.1 658219.8 786168.4 624353.9 820034.4
## Jan 2025      719890.1 650750.3 789030.0 614149.8 825630.5
## Feb 2025      718506.2 644212.1 792800.3 604883.2 832129.2
## Mar 2025      715975.7 636745.0 795206.5 594802.7 837148.7
## Apr 2025      715421.7 631126.4 799717.0 586503.1 844340.2
## May 2025      716368.5 626899.1 805838.0 579536.8 853200.2
## Jun 2025      719714.3 624810.0 814618.7 574570.7 864858.0
## Jul 2025      725332.3 624700.6 825964.0 571429.4 879235.2
## Aug 2025      731981.8 625465.3 838498.3 569078.9 894884.7
## Sep 2025      734747.7 622917.8 846577.6 563718.6 905776.8

```

```

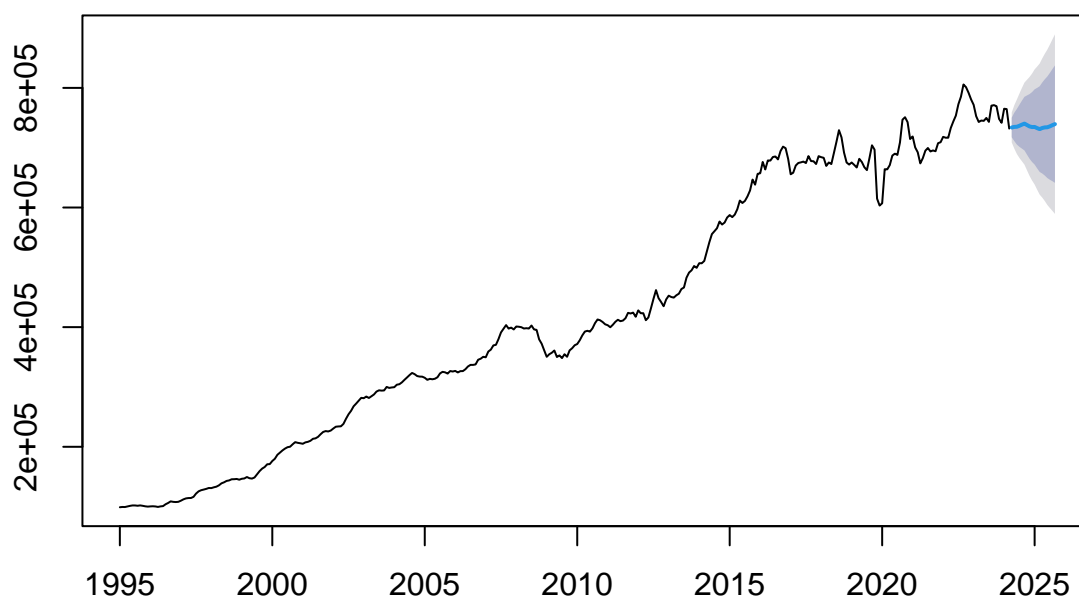
stl_Price_Brent_model <- stl(Price_Brent_ts, s.window="periodic", robust=TRUE)
plot(stl_Price_Brent_model)

```



```
stl_Price_Brent_model_forecast <- forecast(stl_Price_Brent_model, method="ets", h=18)
plot(stl_Price_Brent_model_forecast)
```

Forecasts from STL + ETS(M,A,N)



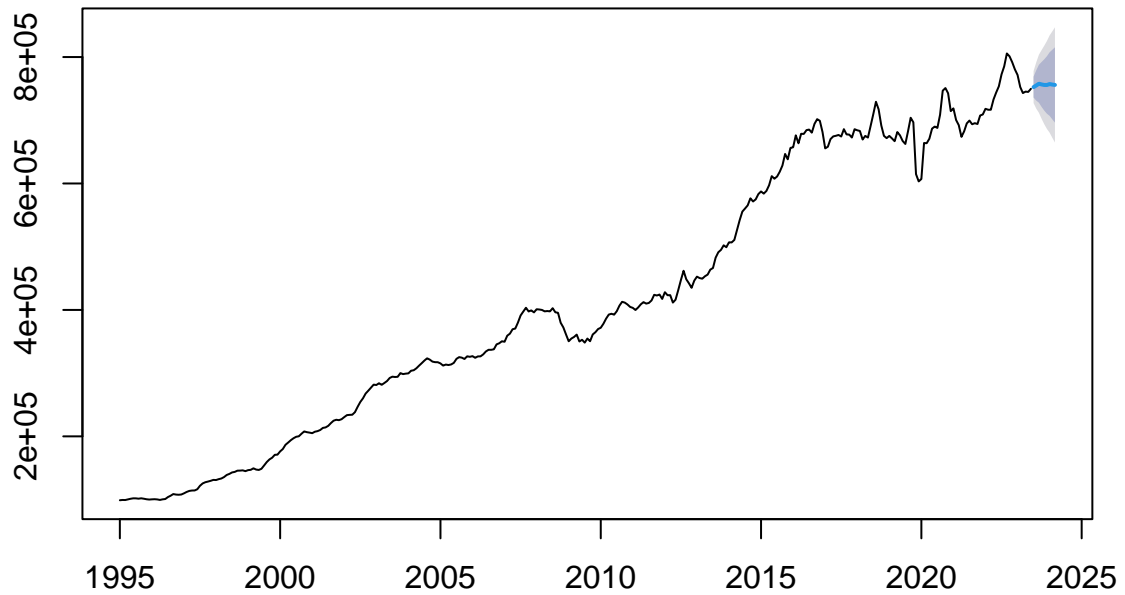
```
summary(stl_Price_Brent_model_forecast)
```

```
##
## Forecast method: STL + ETS(M,A,N)
##
## Model Information:
## ETS(M,A,N)
##
## Call:
## ets(y = na.interp(x), model = etsmodel, allow.multiplicative.trend = allow.multiplicative.trend)
##
## Smoothing parameters:
##   alpha = 0.9999
##   beta  = 0.046
##
## Initial states:
##   l = 102885.2623
##   b = 98.2728
##
## sigma: 0.0174
##
##      AIC      AICc      BIC
## 8195.481 8195.655 8214.785
##
## Error measures:
```

```
##
## Training set -10.54962 9420.835 5540.837 0.06758215 1.249905 0.1761031
## ACF1
## Training set 0.1655694
##
## Forecasts:
## Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## Apr 2024 733790.9 717412.4 750169.3 708742.2 758839.6
## May 2024 734775.8 711075.2 758476.4 698528.9 771022.8
## Jun 2024 734996.8 705305.2 764688.5 689587.3 780406.3
## Jul 2024 736585.7 701528.2 771643.2 682969.9 790201.6
## Aug 2024 738559.3 698494.7 778623.8 677285.8 799832.7
## Sep 2024 740254.6 695408.6 785100.6 671668.6 808840.7
## Oct 2024 737898.8 688419.9 787377.7 662227.3 813570.2
## Nov 2024 735572.9 681560.7 789585.1 652968.3 818177.4
## Dec 2024 734511.1 676032.2 792990.1 645075.3 823947.0
## Jan 2025 734690.4 671787.9 797592.9 638489.3 830891.4
## Feb 2025 732702.2 665402.3 800002.1 629775.9 835628.6
## Mar 2025 731085.9 659401.8 802770.1 621454.4 840717.5
## Apr 2025 732927.3 656862.2 808992.5 616595.7 849258.9
## May 2025 733912.3 653461.7 814362.9 610873.7 856950.9
## Jun 2025 734133.3 649286.6 818980.0 604371.4 863895.1
## Jul 2025 735722.2 646463.7 824980.6 599213.2 872231.2
## Aug 2025 737695.7 644005.9 831385.5 594409.5 880981.9
## Sep 2025 739391.1 641246.9 837535.2 589292.6 889489.6
```

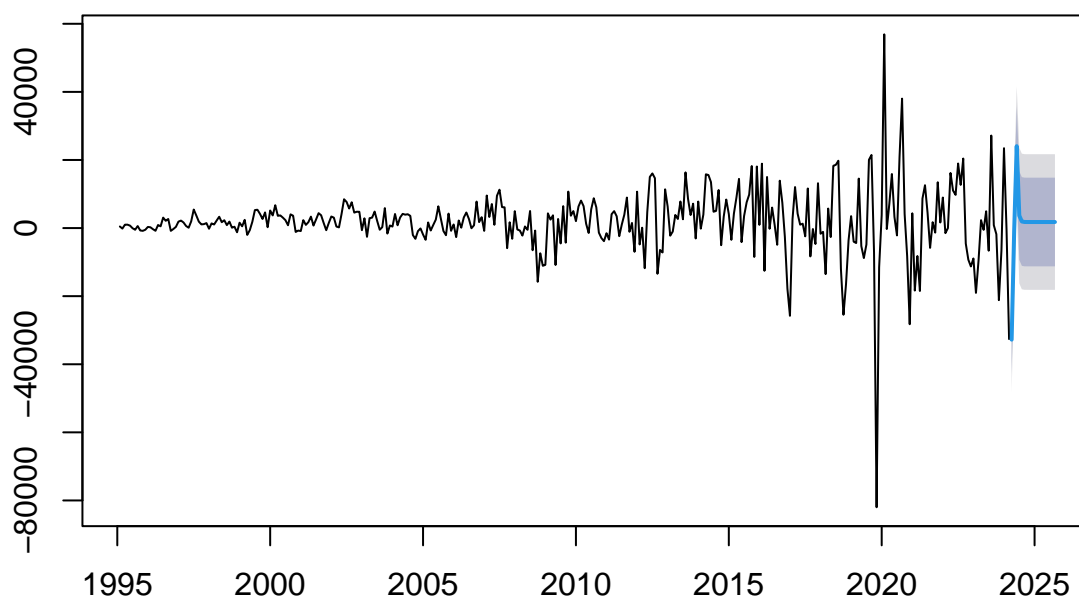
```
stl_legacy <- stl(legacy_ts, s.window="periodic", robust=TRUE)
stl_legacy_forecast <- forecast(stl_legacy, h=9)
stl_forecasted_values_legacy <- stl_legacy_forecast$mean
stl_forecasted_ts_legacy <- ts(stl_forecasted_values_legacy, start = c(2023, 6), frequency = 12)
plot(stl_legacy_forecast)
```

Forecasts from STL + ETS(M,A,N)



```
avg_Price_Brent_model <- auto.arima(diff_Price_Brent_ts, seasonal=FALSE)
avg_Price_Brent_model_forecast <- forecast(avg_Price_Brent_model, h=18)
plot(avg_Price_Brent_model_forecast)
```

Forecasts from ARIMA(1,0,3) with non-zero mean



```
summary(avg_Price_Brent_model_forecast)
```

```
##
## Forecast method: ARIMA(1,0,3) with non-zero mean
##
## Model Information:
## Series: diff_Price_Brent_ts
## ARIMA(1,0,3) with non-zero mean
##
## Coefficients:
##      ar1      ma1      ma2      ma3      mean
##    0.0854  0.3337  0.3228 -0.6367 1777.5154
## s.e.  0.0926  0.0712  0.0609  0.0611  466.0876
##
## sigma^2 = 61668538: log likelihood = -3635.74
## AIC=7283.48  AICc=7283.73  BIC=7306.63
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -3.603367 7796.638 4719.731 318.7985 434.8402 0.5936389
##              ACF1
## Training set 0.007675574
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
```

```
## Apr 2024      -32770.5927 -42834.540 -22706.65 -48162.071 -17379.11
## May 2024       -541.9856 -11453.724  10369.75 -17230.049  16146.08
## Jun 2024      24056.9306  12564.036  35549.83   6480.065  41633.80
## Jul 2024      3679.3688  -9332.054  16690.79 -16219.885  23578.62
## Aug 2024     1939.8647 -11081.974  14961.70 -17975.319  21855.05
## Sep 2024     1791.3742 -11230.540  14813.29 -18123.925  21706.67
## Oct 2024     1778.6985 -11243.216  14800.61 -18136.602  21694.00
## Nov 2024     1777.6164 -11244.298  14799.53 -18137.684  21692.92
## Dec 2024     1777.5241 -11244.391  14799.44 -18137.776  21692.82
## Jan 2025     1777.5162 -11244.399  14799.43 -18137.784  21692.82
## Feb 2025     1777.5155 -11244.399  14799.43 -18137.785  21692.82
## Mar 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## Apr 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## May 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## Jun 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## Jul 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## Aug 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
## Sep 2025     1777.5154 -11244.399  14799.43 -18137.785  21692.82
```

```
last_value <- tail(Price_Brent_ts, n = 1)
forecasted_values <- c(last_value, avg_Price_Brent_model_forecast$mean)
forecasted_values_L80 <- c(last_value, avg_Price_Brent_model_forecast$lower[, "80%"])
print(avg_Price_Brent_model_forecast$lower[, "80%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun
## 2024                -42834.540 -11453.724  12564.036
## 2025 -11244.399 -11244.399 -11244.399 -11244.399 -11244.399 -11244.399
##           Jul           Aug           Sep           Oct           Nov           Dec
## 2024  -9332.054 -11081.974 -11230.540 -11243.216 -11244.298 -11244.391
## 2025 -11244.399 -11244.399 -11244.399
```

```
forecasted_values_L95 <- c(last_value, avg_Price_Brent_model_forecast$lower[, "95%"])
print(avg_Price_Brent_model_forecast$lower[, "95%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun
## 2024                -48162.071 -17230.049   6480.065
## 2025 -18137.784 -18137.785 -18137.785 -18137.785 -18137.785 -18137.785
##           Jul           Aug           Sep           Oct           Nov           Dec
## 2024 -16219.885 -17975.319 -18123.925 -18136.602 -18137.684 -18137.776
## 2025 -18137.785 -18137.785 -18137.785
```

```
forecasted_values_U80 <- c(last_value, avg_Price_Brent_model_forecast$upper[, "80%"])
print(avg_Price_Brent_model_forecast$upper[, "80%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun           Jul
## 2024                -22706.65  10369.75  35549.83  16690.79
## 2025  14799.43  14799.43  14799.43  14799.43  14799.43  14799.43  14799.43
##           Aug           Sep           Oct           Nov           Dec
## 2024  14961.70  14813.29  14800.61  14799.53  14799.44
## 2025  14799.43  14799.43
```



```

forecasted_values_U95 <- c(last_value, avg_Price_Brent_model_forecast$upper[, "95%"])
print(avg_Price_Brent_model_forecast$upper[, "95%"])

```

```

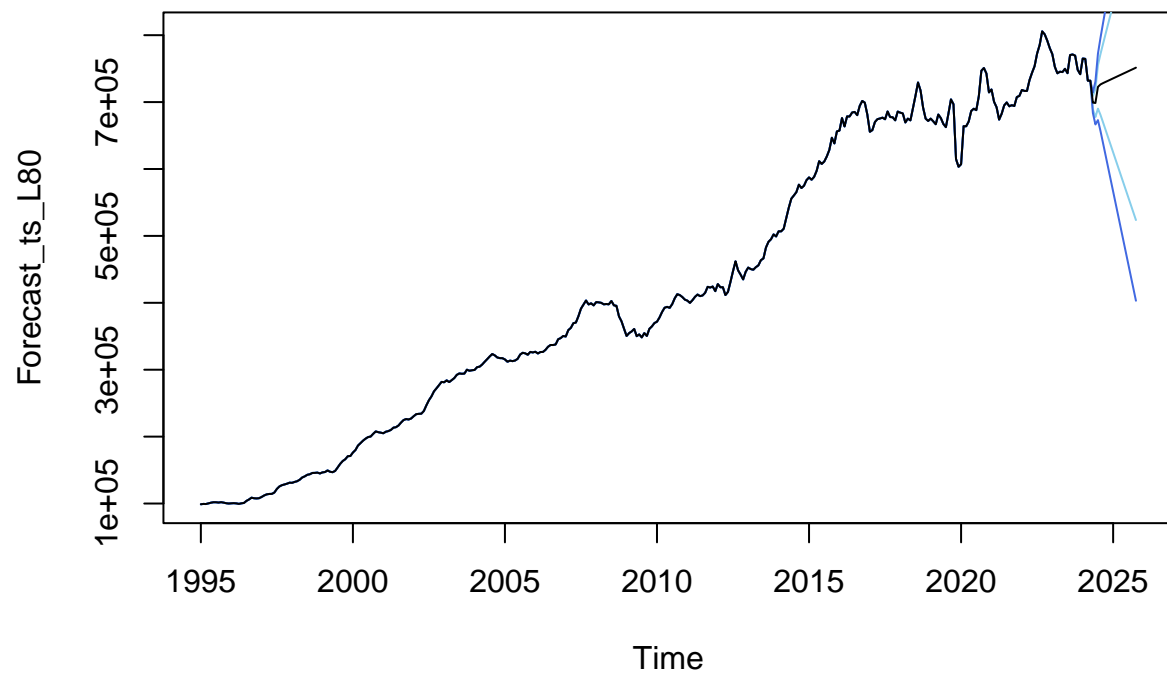
##           Jan           Feb           Mar           Apr           May           Jun           Jul
## 2024                -17379.11  16146.08  41633.80  23578.62
## 2025  21692.82  21692.82  21692.82  21692.82  21692.82  21692.82  21692.82
##           Aug           Sep           Oct           Nov           Dec
## 2024  21855.05  21706.67  21694.00  21692.92  21692.82
## 2025  21692.82  21692.82

```

```

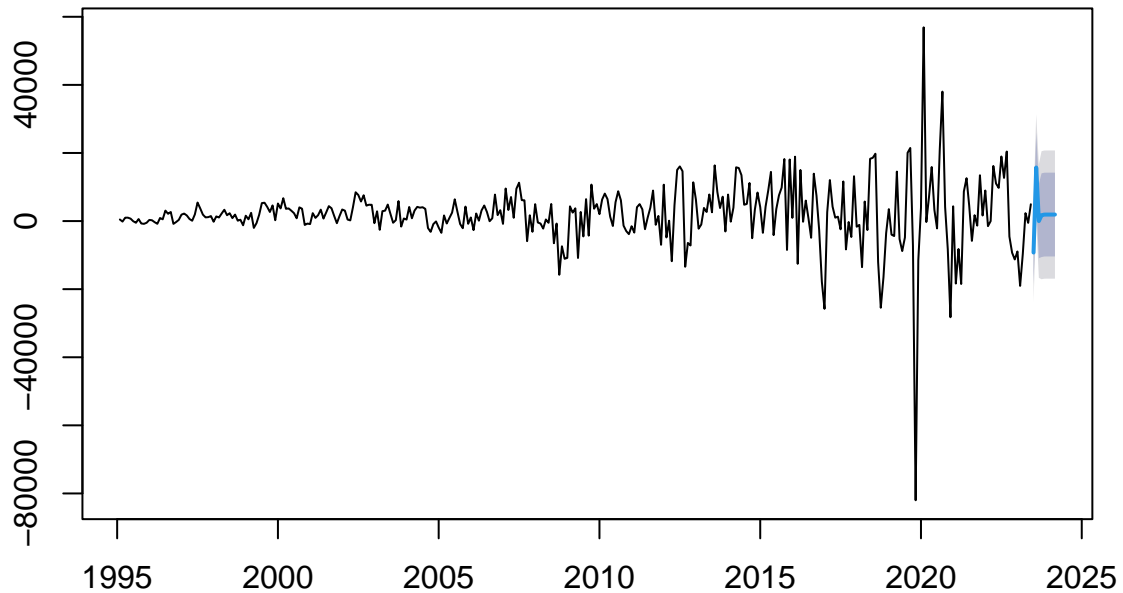
cumulative_forecasted_values_L80 <- cumsum(forecasted_values_L80)
cumulative_forecasted_values_L95 <- cumsum(forecasted_values_L95)
cumulative_forecasted_values_U80 <- cumsum(forecasted_values_U80)
cumulative_forecasted_values_U95 <- cumsum(forecasted_values_U95)
cumulative_forecasted_values <- cumsum(forecasted_values)
cumulative_forecasted_ts <- ts(cumulative_forecasted_values, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U80 <- ts(cumulative_forecasted_values_U80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U95 <- ts(cumulative_forecasted_values_U95, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L80 <- ts(cumulative_forecasted_values_L80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L95 <- ts(cumulative_forecasted_values_L95, start = c(2024, 2), frequency = 12)
combined <- c(Price_Brent_ts, cumulative_forecasted_ts)
combined_L80 <- c(Price_Brent_ts, cumulative_forecasted_ts_L80)
combined_L95 <- c(Price_Brent_ts, cumulative_forecasted_ts_L95)
combined_U80 <- c(Price_Brent_ts, cumulative_forecasted_ts_U80)
combined_U95 <- c(Price_Brent_ts, cumulative_forecasted_ts_U95)
Forecast_ts <- ts(combined, start = c(1995, 1), frequency = 12)
Forecast_ts_L80 <- ts(combined_L80, start = c(1995, 1), frequency = 12)
Forecast_ts_L95 <- ts(combined_L95, start = c(1995, 1), frequency = 12)
Forecast_ts_U80 <- ts(combined_U80, start = c(1995, 1), frequency = 12)
Forecast_ts_U95 <- ts(combined_U95, start = c(1995, 1), frequency = 12)
plot(Forecast_ts_L80, col = "skyblue")
lines(Forecast_ts_U80, col = "skyblue")
lines(Forecast_ts_L95, col = "royalblue")
lines(Forecast_ts_U95, col = "royalblue")
lines(Forecast_ts)

```



```
avg_legacy <- arima(diff_legacy_ts, order = c(1, 0, 3))  
avg_legacy_forecast <- forecast(avg_legacy, h=9)  
plot(avg_legacy_forecast)
```

Forecasts from ARIMA(1,0,3) with non-zero mean

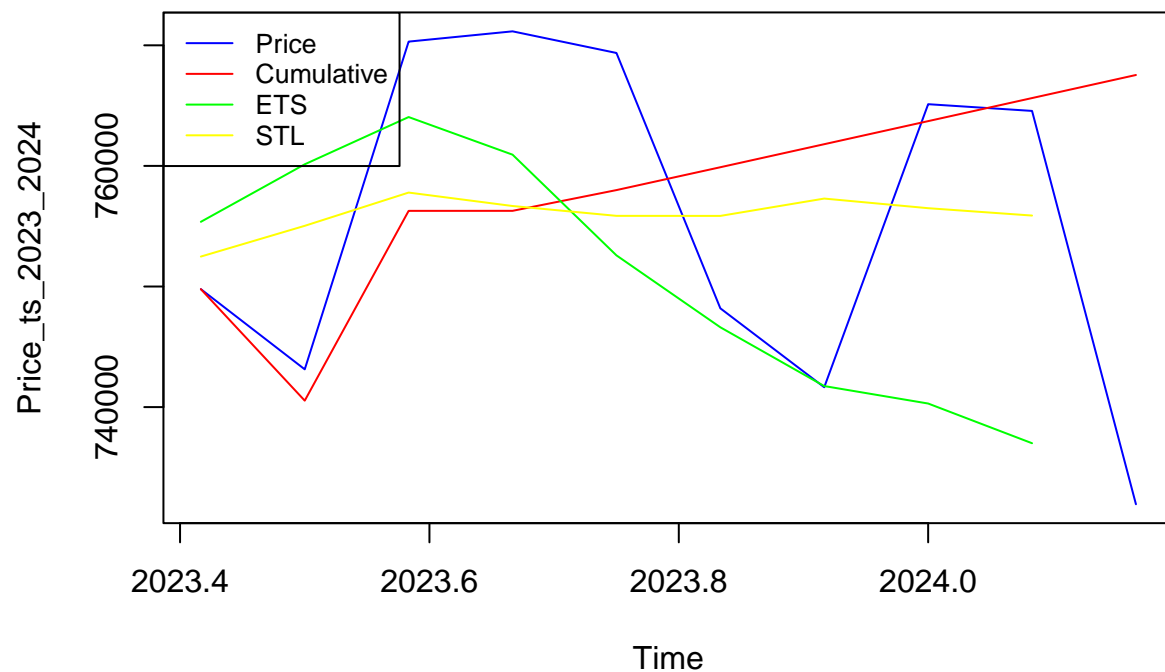


```
last_value_legacy <- tail(legacy_ts, n = 1)
forecasted_values_legacy <- c(last_value_legacy, avg_legacy_forecast$mean)
cumulative_forecasted_values_legacy <- cumsum(forecasted_values_legacy)
print(cumulative_forecasted_values_legacy)
```

```
## [1] 749779.5 740536.0 756272.5 756274.9 757995.6 759888.9 761799.6 763712.1
## [9] 765624.7 767537.4
```

```
cumulative_forecasted_ts_legacy <- ts(cumulative_forecasted_values_legacy, start = c(2023, 6), frequency = 4)

plot(Price_ts_2023_2024, type = "l", col = "blue")
lines(cumulative_forecasted_ts_legacy, col = "red")
lines(ets_forecasted_ts_legacy, col = "green")
lines(stl_forecasted_ts_legacy, col = "yellow")
legend("topleft",
      legend = c("Price", "Cumulative", "ETS", "STL"),
      col = c("blue", "red", "green", "yellow"),
      lty = 1,
      cex = 0.8)
```



```
mse_avg <- mean((Price_ts_2023_2024 - cumulative_forecasted_ts_legacy)^2)
print(mse_avg)
```

```
## [1] 236722721
```

```
mse_ets <- mean((Price_ts_2023_2024 - ets_forecasted_ts_legacy)^2)
print(mse_ets)
```

```
## [1] 235929800
```

```
mse_stl <- mean((Price_ts_2023_2024 - stl_forecasted_ts_legacy)^2)
print(mse_stl)
```

```
## [1] 127873405
```

```
mae_avg <- mae(Price_ts_2023_2024, cumulative_forecasted_ts_legacy)
print(mae_avg)
```

```
## [1] 11279.4
```

```
mae_ets <- mae(Price_ts_2023_2024, ets_forecasted_ts_legacy)
print(mae_ets)
```

```
## [1] 12210.04
```

```
mae_stl <- mae(Price_ts_2023_2024, stl_forecasted_ts_legacy)
print(mae_stl)
```

```
## [1] 10635.15
```

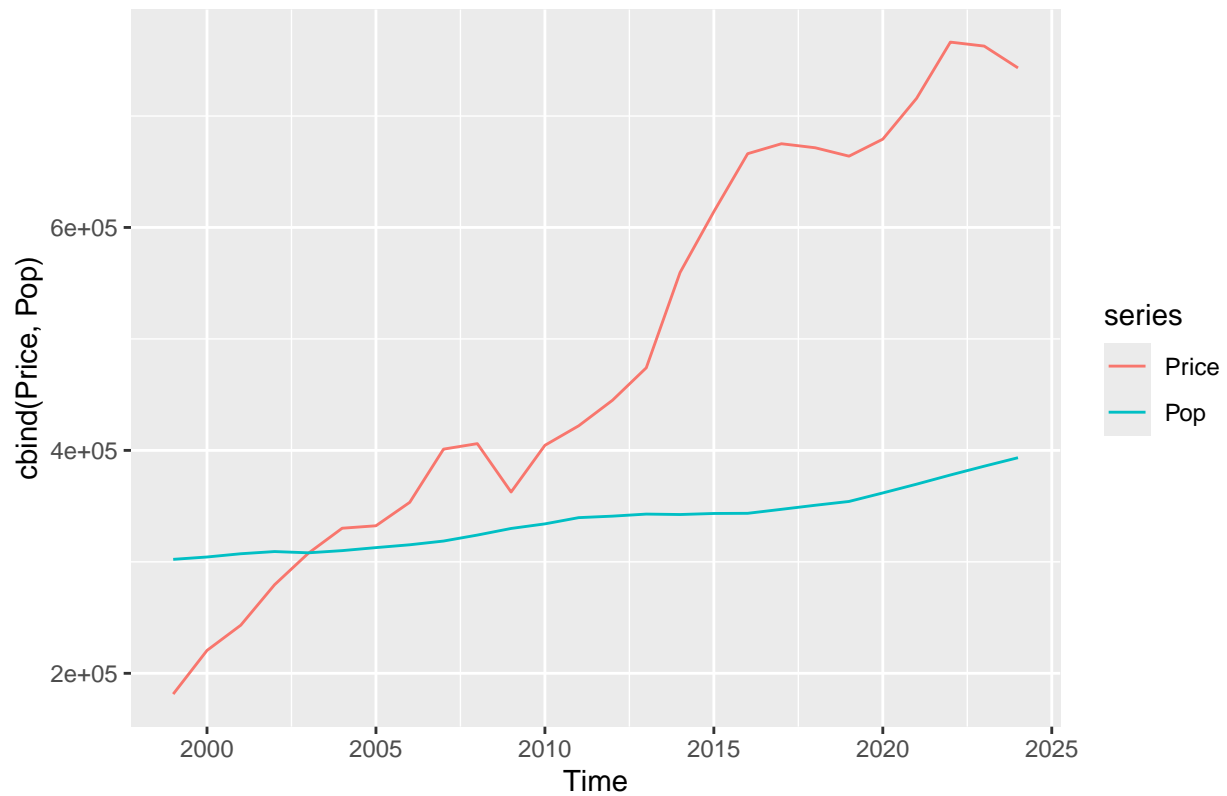
```
Brent_df <- read.csv("Merged_Brent_Data.csv")

Brent_df$Date <- as.Date(Brent_df$Date, format = "%Y")

Price <- ts(Brent_df$Yearly_Price, start = c(1999), frequency = 1)

Pop <- ts(Brent_df$Population, start = c(1999), frequency = 1)

autoplot(cbind(Price, Pop))
```



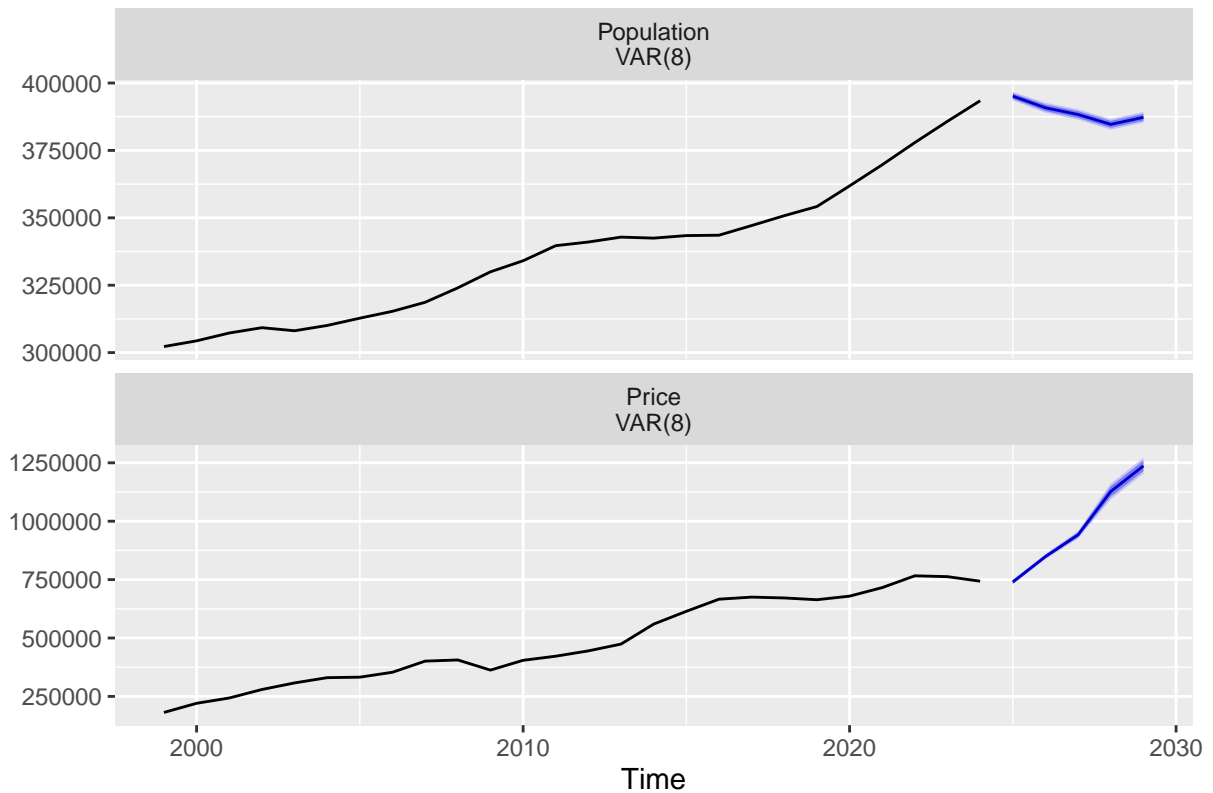
```
Brent_df.bv <- cbind(Price, Pop)
colnames(Brent_df.bv) <- cbind("Price", "Population")

lagselect <- VARselect(Brent_df.bv, lag.max = 12, type = "const")
lagselect$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      7      7      7      7
```

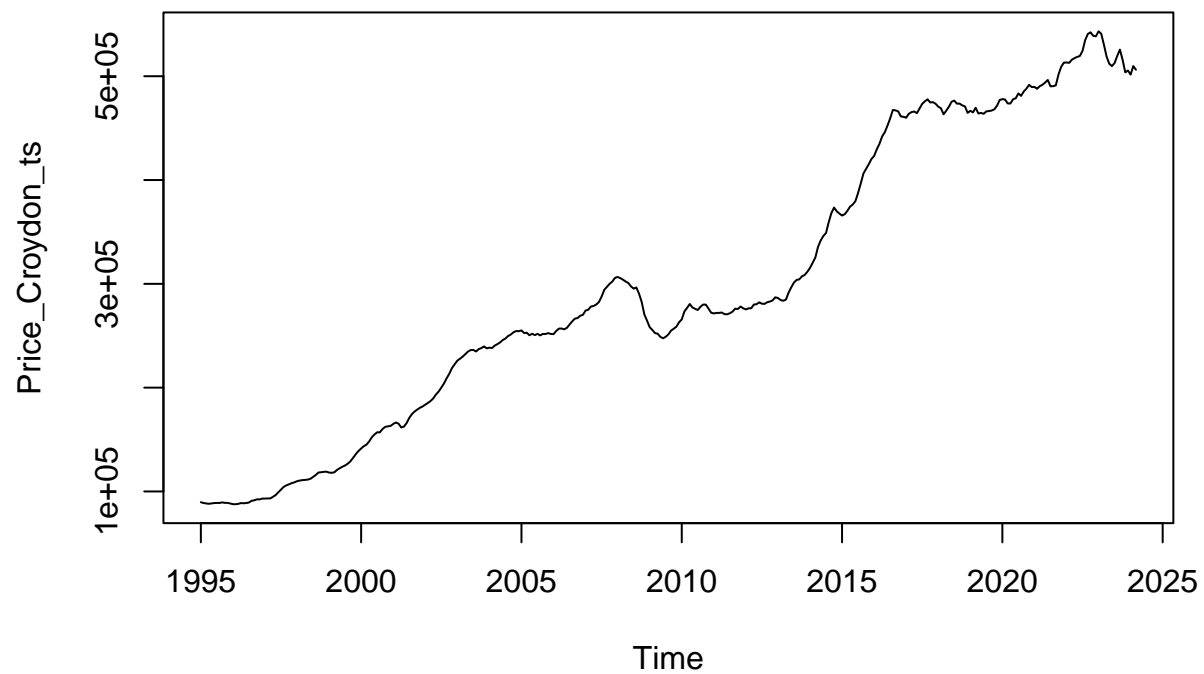
```
var_model <- VAR(Brent_df.bv, p = 8, type = "const")

forecast_values <- forecast(var_model, h = 5)
autoplot(forecast_values)
```

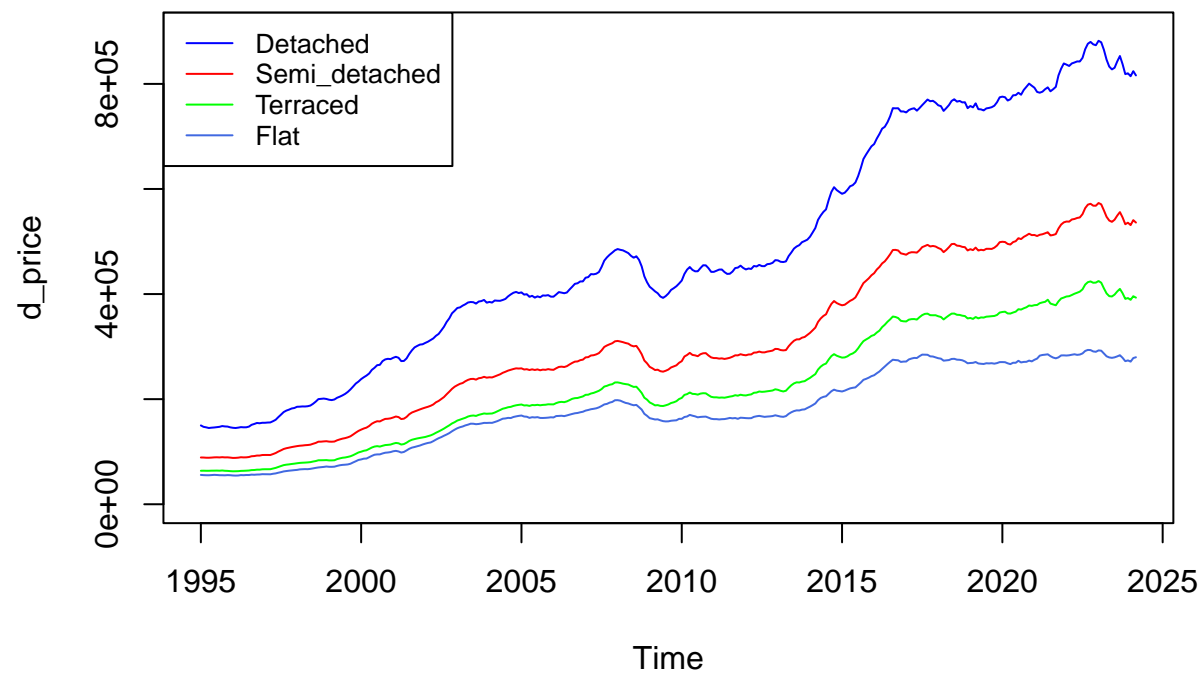


```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)

Croydon_df <- read.csv("Updated_Croydon.csv")
Croydon_df$Date <- as.Date(Croydon_df$Date, format = "%Y-%m-%d")
Price_Croydon_ts <- ts(Croydon_df$Average_Price, start = c(1995, 1), frequency = 12)
Price_ts_2023_2024 <- window(Price_Croydon_ts, start = c(2023, 6), end = c(2024, 3))
d_price <- ts(Croydon_df$Detached_Average_Price, start = c(1995, 1), frequency = 12)
sd_price <- ts(Croydon_df$Semi_Detached_Average_Price, start = c(1995, 1), frequency = 12)
t_price <- ts(Croydon_df$Terraced_Average_Price, start = c(1995, 1), frequency = 12)
f_price <- ts(Croydon_df$Flat_Average_Price, start = c(1995, 1), frequency = 12)
legacy_ts <- ts(Croydon_df$Average_Price, start = c(1995, 1), end = c(2023, 6), frequency = 12)
diff_legacy_ts <- diff(legacy_ts, differences=1)
plot(Price_Croydon_ts)
```

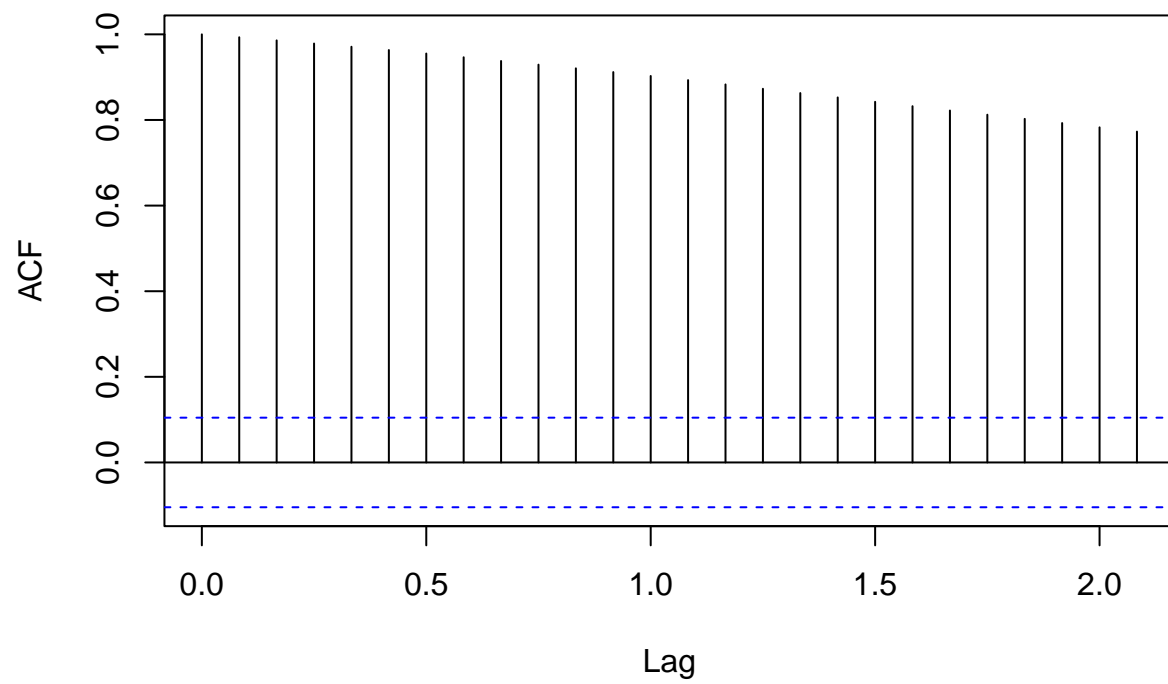


```
plot(d_price, col = "blue", ylim = c(0, 900000))
lines(sd_price, col = "red")
lines(t_price, col = "green")
lines(f_price, col = "royalblue")
legend("topleft",
      legend = c("Detached", "Semi_detached", "Terraced", "Flat"),
      col = c("blue", "red", "green", "royalblue"),
      lty = 1,
      cex = 0.8)
```



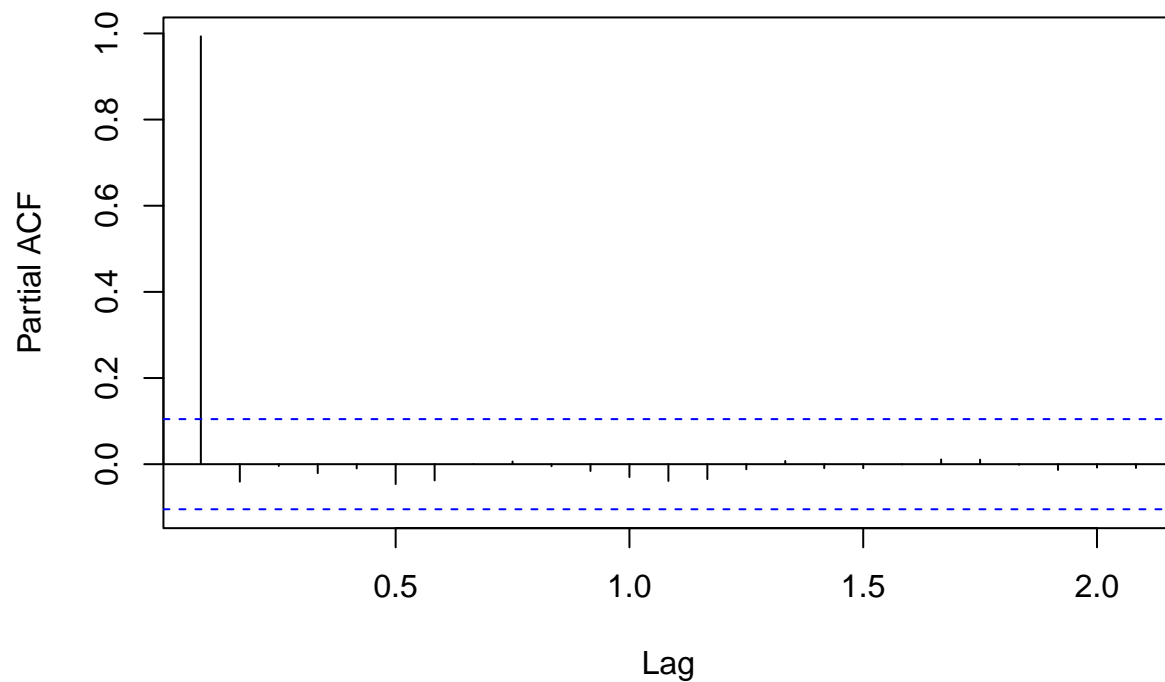
```
acf(Price_Croydon_ts)
```


Series Price_Croydon_ts



```
pacf(Price_Croydon_ts)
```

Series Price_Croydon_ts



```
adf.test(Price_Croydon_ts)
```

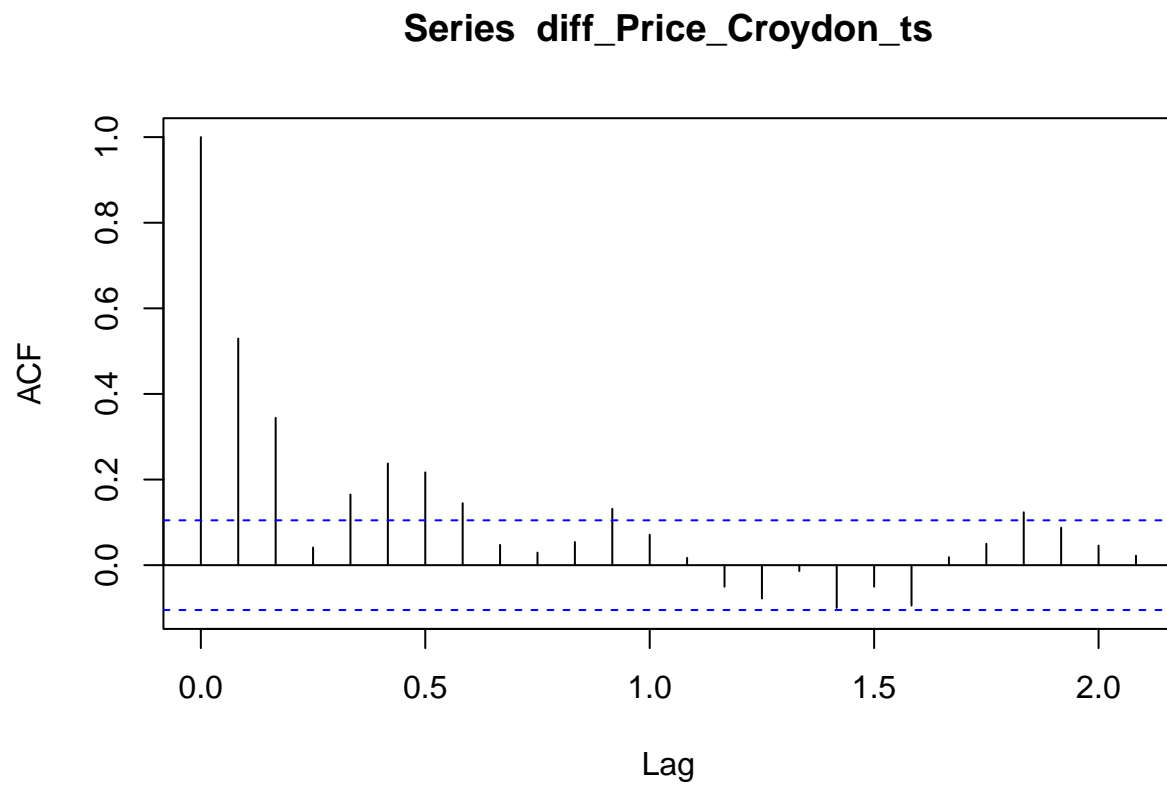
```
##  
## Augmented Dickey-Fuller Test  
##  
## data: Price_Croydon_ts  
## Dickey-Fuller = -2.3457, Lag order = 7, p-value = 0.4309  
## alternative hypothesis: stationary
```

```
diff_Price_Croydon_ts <- diff(Price_Croydon_ts, differences=1)  
adf.test(diff_Price_Croydon_ts)
```

```
## Warning in adf.test(diff_Price_Croydon_ts): p-value smaller than printed  
## p-value
```

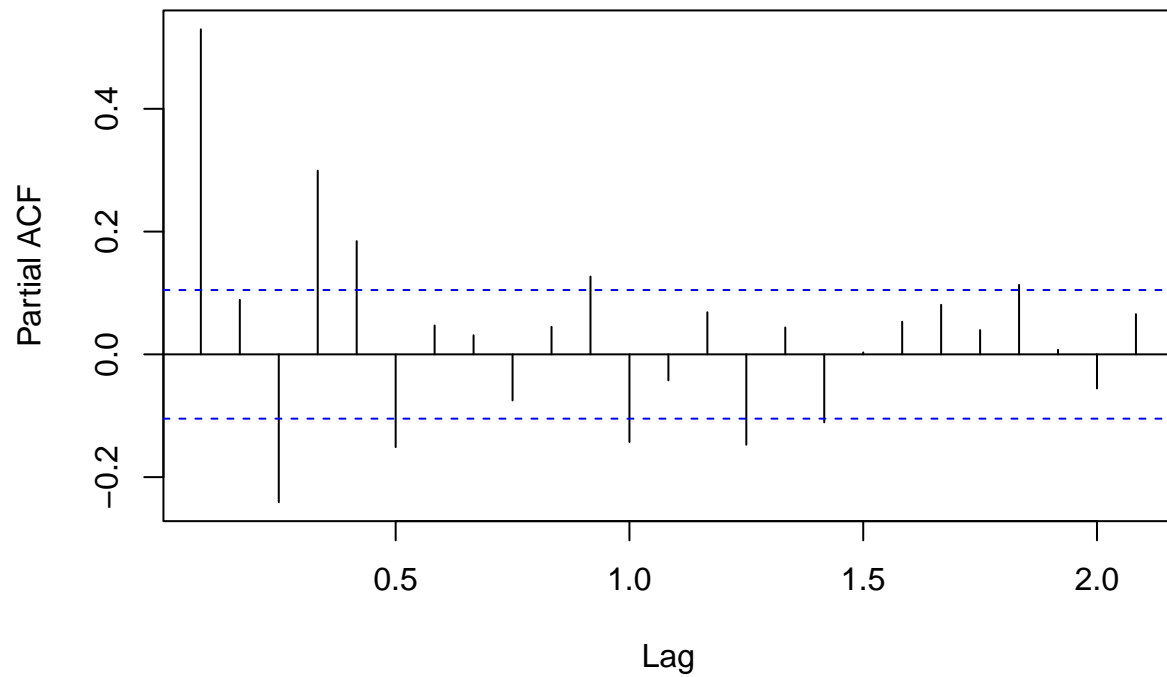
```
##  
## Augmented Dickey-Fuller Test  
##  
## data: diff_Price_Croydon_ts  
## Dickey-Fuller = -4.6989, Lag order = 7, p-value = 0.01  
## alternative hypothesis: stationary
```

```
acf(diff_Price_Croydon_ts)
```



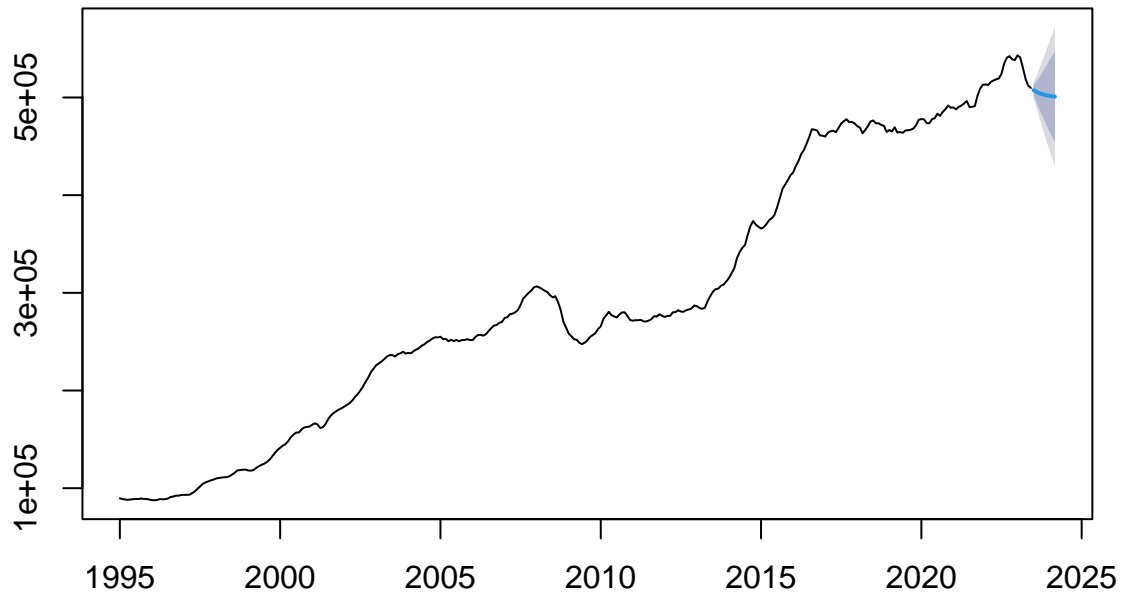
```
pacf(diff_Price_Croydon_ts)
```

Series diff_Price_Croydon_ts



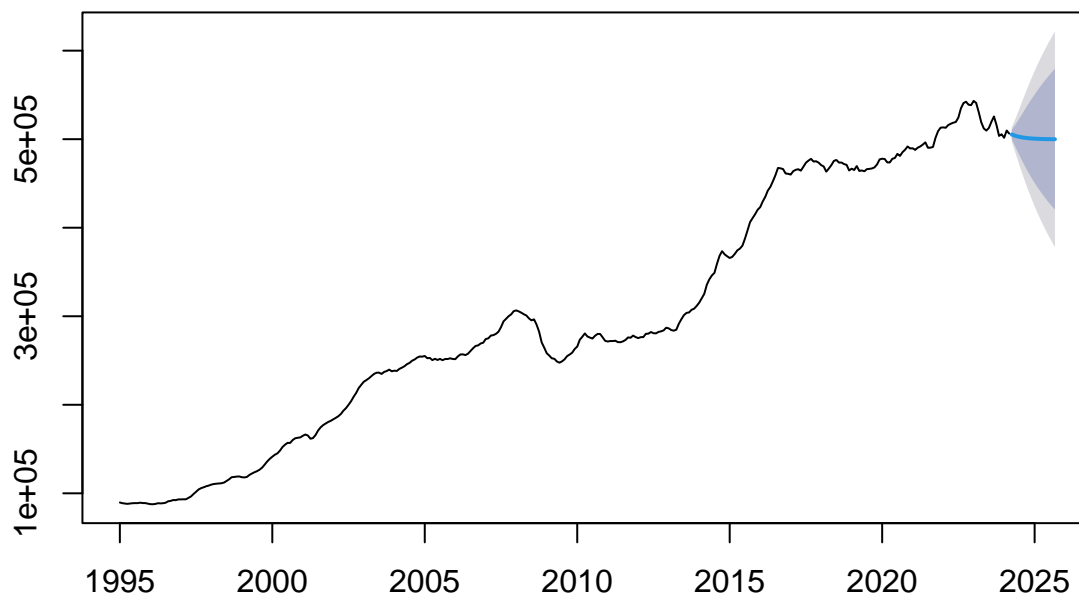
```
ets_Price_Croydon_model <- ets(Price_Croydon_ts, model = "ZZZ")
ets_Price_Croydon_model_forecast <- forecast(ets_Price_Croydon_model, h=18)
ets_legacy <- ets(legacy_ts, model = "MAN")
ets_legacy_forecast <- forecast(ets_legacy, h = 9)
ets_forecasted_values_legacy <- ets_legacy_forecast$mean
ets_forecasted_ts_legacy <- ts(ets_forecasted_values_legacy, start = c(2023, 6), frequency = 12)
plot(ets_legacy_forecast)
```

Forecasts from ETS(M,Ad,N)



```
plot(ets_Price_Croydon_model_forecast)
```

Forecasts from ETS(M,Ad,N)

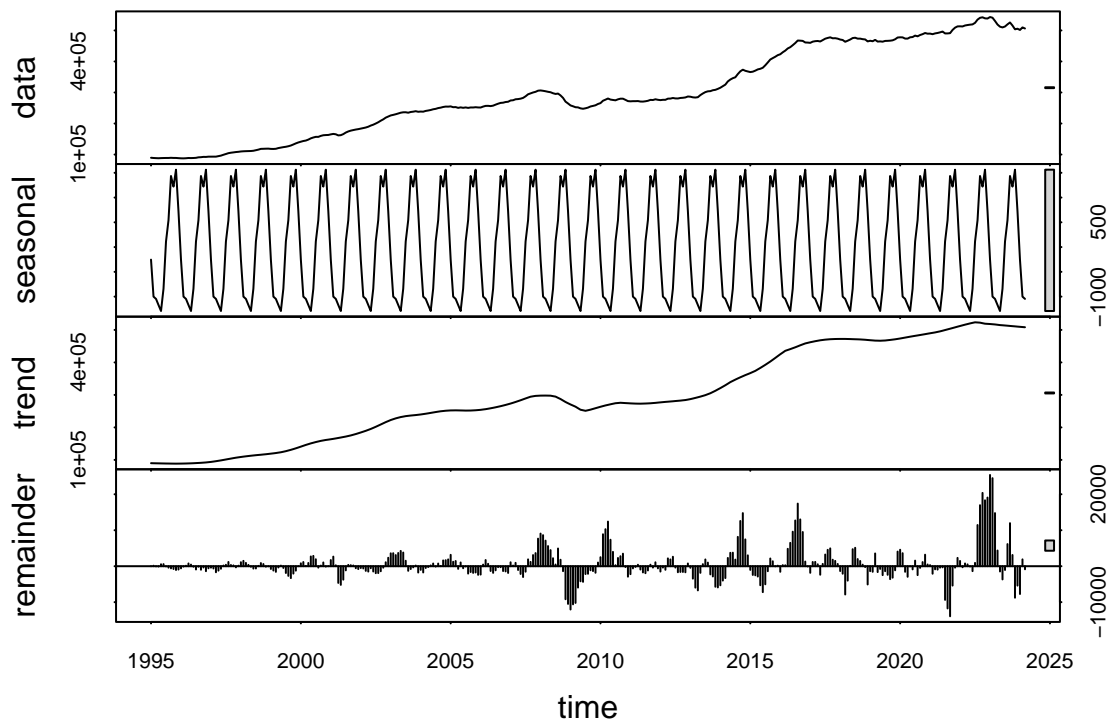


```
summary(ets_Price_Croydon_model_forecast)
```

```
##
## Forecast method: ETS(M,Ad,N)
##
## Model Information:
## ETS(M,Ad,N)
##
## Call:
## ets(y = Price_Croydon_ts, model = "ZZZ")
##
## Smoothing parameters:
##   alpha = 0.9554
##   beta  = 0.8375
##   phi   = 0.8
##
## Initial states:
##   l = 88745.0343
##   b = 19.8803
##
## sigma: 0.0083
##
##      AIC      AICc      BIC
## 7457.877 7458.121 7481.042
##
```

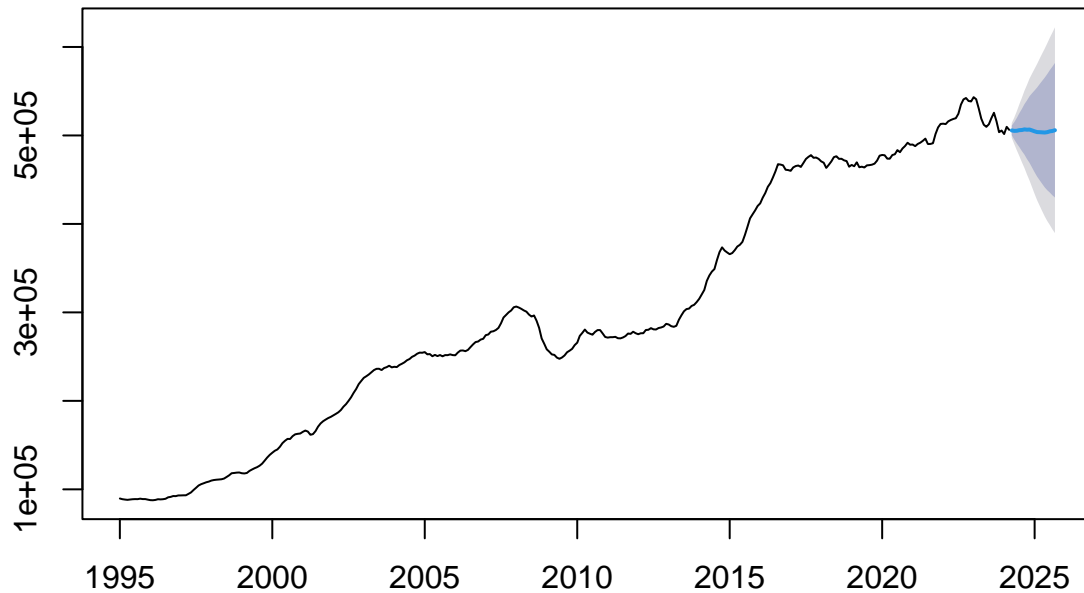
```
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 271.9737 2838.049 1947.398 0.1207829 0.6315575 0.09461202
##           ACF1
## Training set -0.06770104
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Apr 2024           505282.3 499924.8 510639.8 497088.7 513475.9
## May 2024           504191.2 493972.7 514409.6 488563.4 519818.9
## Jun 2024           503318.3 487887.7 518748.9 479719.2 526917.4
## Jul 2024           502620.0 481887.9 523352.1 470913.0 534326.9
## Aug 2024           502061.3 476074.1 528048.6 462317.2 541805.4
## Sep 2024           501614.4 470492.4 532736.5 454017.4 549211.5
## Oct 2024           501256.9 465160.2 537353.6 446051.8 556462.0
## Nov 2024           500970.9 460078.9 541862.9 438432.0 563509.8
## Dec 2024           500742.1 455240.6 546243.5 431153.5 570330.6
## Jan 2025           500559.0 450632.8 550485.2 424203.4 576914.6
## Feb 2025           500412.6 446240.6 554584.5 417563.7 583261.4
## Mar 2025           500295.4 442048.5 558542.3 411214.5 589376.3
## Apr 2025           500201.7 438040.9 562362.4 405135.0 595268.3
## May 2025           500126.7 434202.9 566050.4 399305.0 600948.3
## Jun 2025           500066.7 430520.7 569612.8 393705.2 606428.2
## Jul 2025           500018.7 426981.1 573056.3 388317.3 611720.1
## Aug 2025           499980.3 423572.5 576388.2 383124.6 616836.1
## Sep 2025           499949.6 420283.9 579615.3 378111.5 621787.7
```

```
stl_Price_Croydon_model <- stl(Price_Croydon_ts, s.window="periodic", robust=TRUE)
plot(stl_Price_Croydon_model)
```



```
stl_Price_Croydon_model_forecast <- forecast(stl_Price_Croydon_model, method="ets", h=18)
plot(stl_Price_Croydon_model_forecast)
```


Forecasts from STL + ETS(M,Ad,N)



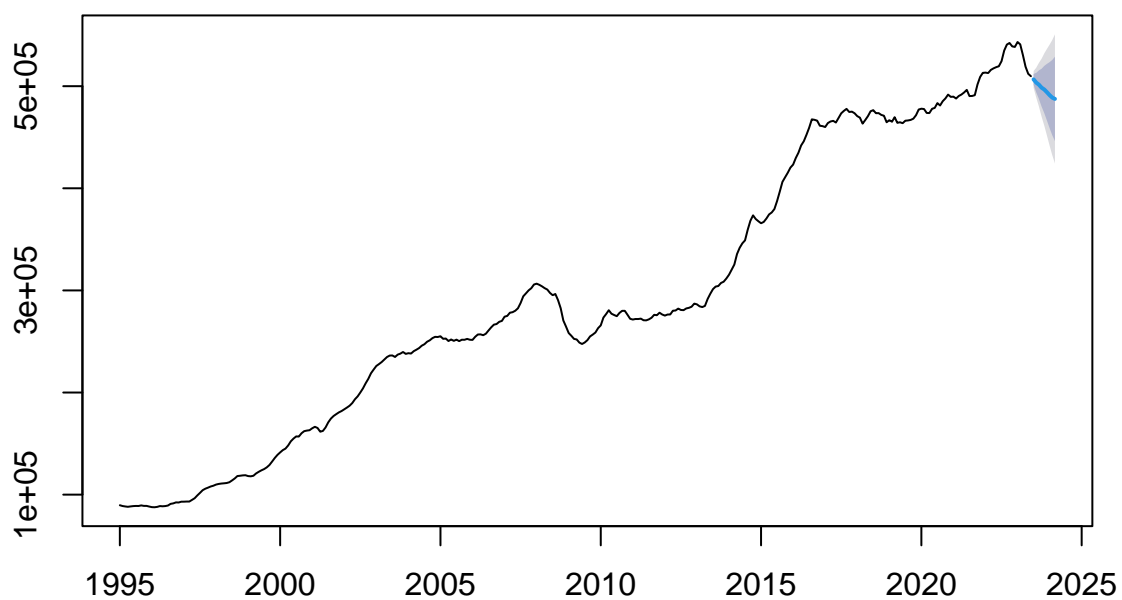
```
summary(stl_Price_Croydon_model_forecast)
```

```
##
## Forecast method: STL + ETS(M,Ad,N)
##
## Model Information:
## ETS(M,Ad,N)
##
## Call:
## ets(y = na.interp(x), model = etsmodel, allow.multiplicative.trend = allow.multiplicative.trend)
##
## Smoothing parameters:
##   alpha = 0.9999
##   beta  = 0.6123
##   phi   = 0.8427
##
## Initial states:
##   l = 90392.3146
##   b = -123.3315
##
## sigma: 0.0084
##
##      AIC      AICc      BIC
## 7464.994 7465.238 7488.159
##
```

```
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 275.9154 2840.452 1932.484 0.1223963 0.6366755 0.09388743
##           ACF1
## Training set -0.008402947
##
## Forecasts:
##           Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Apr 2024      505691.3 500262.8 511119.9 497389.1 513993.6
## May 2024      505174.6 495318.2 515031.0 490100.6 520248.6
## Jun 2024      505292.3 490829.7 519755.0 483173.6 527411.1
## Jul 2024      505961.5 486800.1 525122.9 476656.7 535266.3
## Aug 2024      506156.5 482282.1 530030.9 469643.7 542669.2
## Sep 2024      506848.7 478301.8 535395.7 463189.9 550507.6
## Oct 2024      506465.5 473322.9 539608.2 455778.2 557152.9
## Nov 2024      506666.0 469027.8 544304.1 449103.4 564228.5
## Dec 2024      505707.9 463688.7 547727.2 441445.0 569970.8
## Jan 2025      504629.5 458351.2 550907.8 433852.9 575406.0
## Feb 2025      503797.2 453385.2 554209.3 426698.7 580895.8
## Mar 2025      503679.7 449259.3 558100.0 420450.9 586908.4
## Apr 2025      503495.9 445190.7 561801.2 414325.8 592666.1
## May 2025      503324.4 441254.4 565394.5 408396.4 598252.5
## Jun 2025      503733.1 438013.8 569452.5 403224.1 604242.1
## Jul 2025      504647.5 435389.8 573905.3 398726.9 610568.1
## Aug 2025      505049.1 432358.5 577739.7 393878.4 616219.8
## Sep 2025      505915.5 429892.4 581938.7 389648.2 622182.9
```

```
stl_legacy <- stl(legacy_ts, s.window="periodic", robust=TRUE)
stl_legacy_forecast <- forecast(stl_legacy, h=9)
plot(stl_legacy_forecast)
```

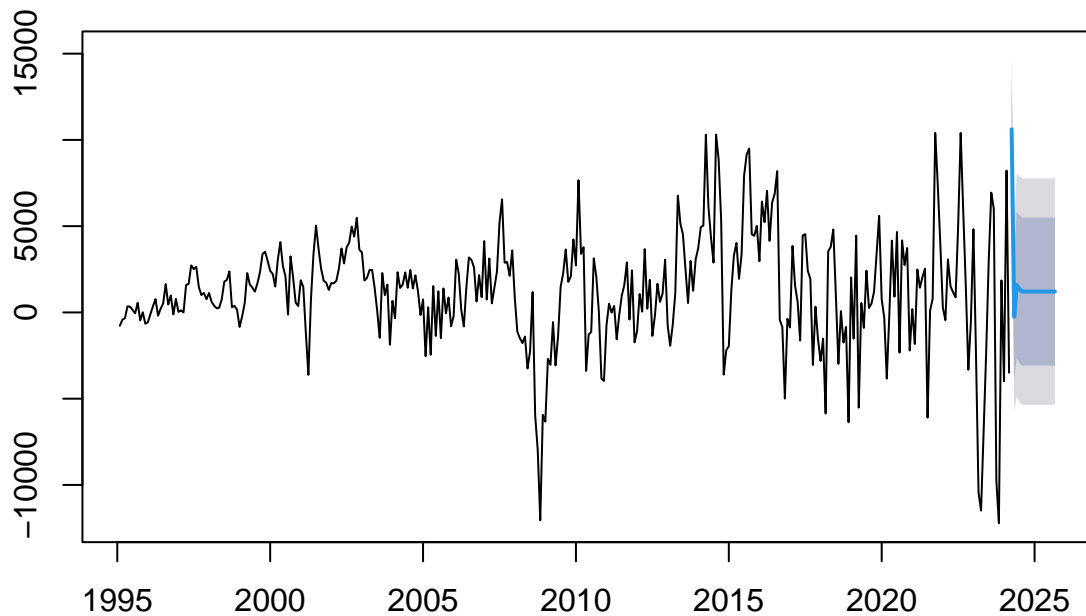
Forecasts from STL + ETS(M,Ad,N)



```
stl_forecasted_values_legacy <- stl_legacy_forecast$mean
stl_forecasted_ts_legacy <- ts(stl_forecasted_values_legacy, start = c(2023, 6), frequency = 12)

avg_Price_Croydon_model <- auto.arima(diff_Price_Croydon_ts, seasonal=FALSE)
avg_Price_Croydon_model_forecast <- forecast(avg_Price_Croydon_model, h=18)
plot(avg_Price_Croydon_model_forecast)
```

Forecasts from ARIMA(0,0,4) with non-zero mean



```
summary(avg_Price_Croydon_model_forecast)
```

```
##
## Forecast method: ARIMA(0,0,4) with non-zero mean
##
## Model Information:
## Series: diff_Price_Croydon_ts
## ARIMA(0,0,4) with non-zero mean
##
## Coefficients:
##          ma1      ma2      ma3      ma4      mean
##          0.6538  0.7542 -0.2192  0.1055 1210.2435
## s.e.    0.0545  0.0583   0.0578  0.0539  283.6067
##
## sigma^2 = 5451689: log likelihood = -3211.54
## AIC=6435.09  AICc=6435.33  BIC=6458.23
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 2.466439 2318.148 1599.495 1.608155 250.4054 0.5145618 0.008205948
##
## Forecasts:
##          Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Apr 2024    10615.4111  7623.121 13607.701  6039.099 15191.724
## May 2024     -251.7973 -3826.785  3323.191 -5719.270  5215.675
```

```
## Jun 2024      1590.3910 -2637.293  5818.075 -4875.294  8056.076
## Jul 2024      1368.0256 -2910.251  5646.302 -5175.033  7911.084
## Aug 2024      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Sep 2024      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Oct 2024      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Nov 2024      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Dec 2024      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Jan 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Feb 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Mar 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Apr 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## May 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Jun 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Jul 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Aug 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
## Sep 2025      1210.2435 -3079.669  5500.156 -5350.611  7771.098
```

```
last_value <- tail(Price_Croydon_ts, n = 1)
forecasted_values <- c(last_value, avg_Price_Croydon_model_forecast$mean)
forecasted_values_L80 <- c(last_value, avg_Price_Croydon_model_forecast$lower[, "80%"])
print(avg_Price_Croydon_model_forecast$lower[, "80%"])
```

```
##           Jan          Feb          Mar          Apr          May          Jun          Jul
## 2024                                7623.121 -3826.785 -2637.293 -2910.251
## 2025 -3079.669 -3079.669 -3079.669 -3079.669 -3079.669 -3079.669 -3079.669
##           Aug          Sep          Oct          Nov          Dec
## 2024 -3079.669 -3079.669 -3079.669 -3079.669 -3079.669
## 2025 -3079.669 -3079.669
```

```
forecasted_values_L95 <- c(last_value, avg_Price_Croydon_model_forecast$lower[, "95%"])
print(avg_Price_Croydon_model_forecast$lower[, "95%"])
```

```
##           Jan          Feb          Mar          Apr          May          Jun          Jul
## 2024                                6039.099 -5719.270 -4875.294 -5175.033
## 2025 -5350.611 -5350.611 -5350.611 -5350.611 -5350.611 -5350.611 -5350.611
##           Aug          Sep          Oct          Nov          Dec
## 2024 -5350.611 -5350.611 -5350.611 -5350.611 -5350.611
## 2025 -5350.611 -5350.611
```

```
forecasted_values_U80 <- c(last_value, avg_Price_Croydon_model_forecast$upper[, "80%"])
print(avg_Price_Croydon_model_forecast$upper[, "80%"])
```

```
##           Jan          Feb          Mar          Apr          May          Jun          Jul
## 2024                                13607.701 3323.191 5818.075 5646.302
## 2025 5500.156 5500.156 5500.156 5500.156 5500.156 5500.156 5500.156
##           Aug          Sep          Oct          Nov          Dec
## 2024 5500.156 5500.156 5500.156 5500.156 5500.156
## 2025 5500.156 5500.156
```

```
forecasted_values_U95 <- c(last_value, avg_Price_Croydon_model_forecast$upper[, "95%"])
print(avg_Price_Croydon_model_forecast$upper[, "95%"])
```

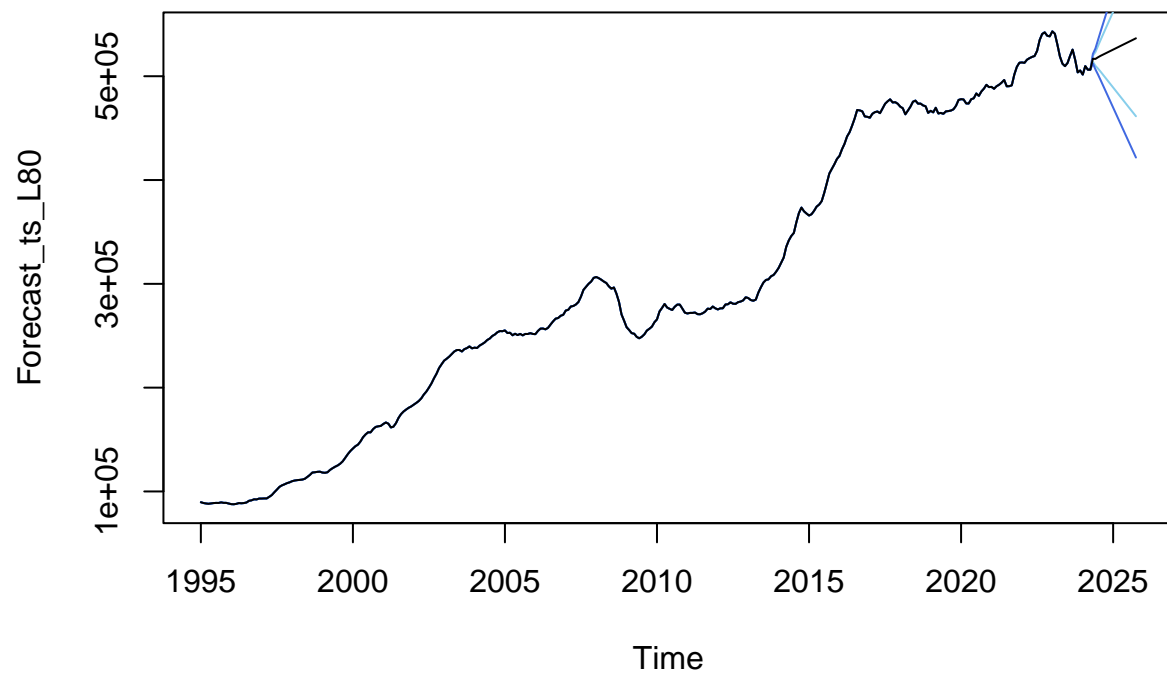
##	Jan	Feb	Mar	Apr	May	Jun	Jul
## 2024				15191.724	5215.675	8056.076	7911.084
## 2025	7771.098	7771.098	7771.098	7771.098	7771.098	7771.098	7771.098

##	Aug	Sep	Oct	Nov	Dec
## 2024	7771.098	7771.098	7771.098	7771.098	7771.098
## 2025	7771.098	7771.098			

```

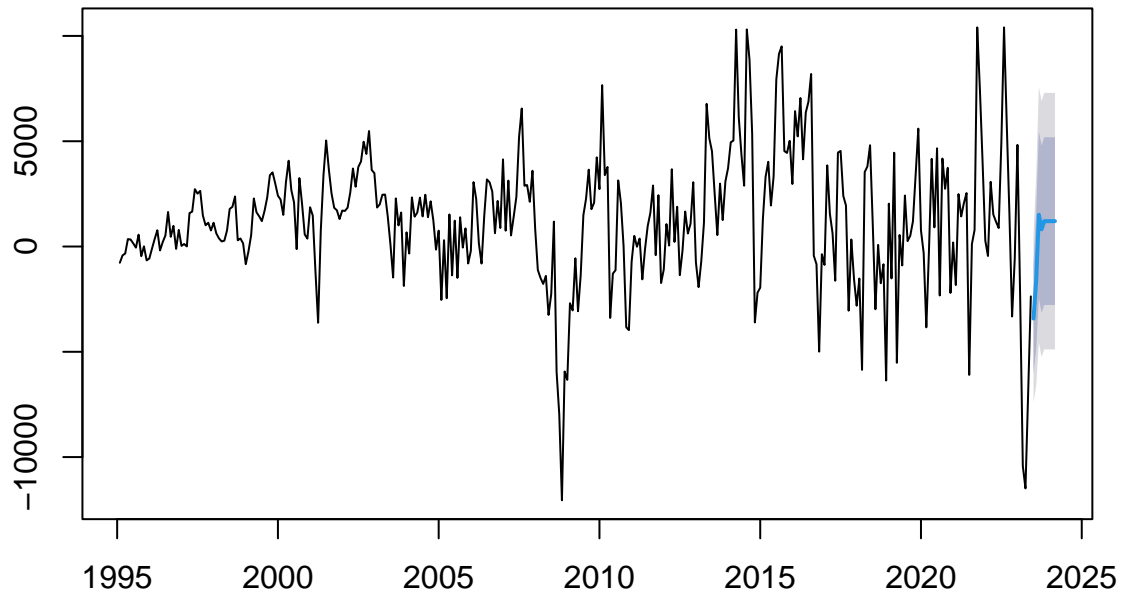
cumulative_forecasted_values_L80 <- cumsum(forecasted_values_L80)
cumulative_forecasted_values_L95 <- cumsum(forecasted_values_L95)
cumulative_forecasted_values_U80 <- cumsum(forecasted_values_U80)
cumulative_forecasted_values_U95 <- cumsum(forecasted_values_U95)
cumulative_forecasted_values <- cumsum(forecasted_values)
cumulative_forecasted_ts <- ts(cumulative_forecasted_values, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U80 <- ts(cumulative_forecasted_values_U80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U95 <- ts(cumulative_forecasted_values_U95, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L80 <- ts(cumulative_forecasted_values_L80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L95 <- ts(cumulative_forecasted_values_L95, start = c(2024, 2), frequency = 12)
combined <- c(Price_Croydon_ts, cumulative_forecasted_ts)
combined_L80 <- c(Price_Croydon_ts, cumulative_forecasted_ts_L80)
combined_L95 <- c(Price_Croydon_ts, cumulative_forecasted_ts_L95)
combined_U80 <- c(Price_Croydon_ts, cumulative_forecasted_ts_U80)
combined_U95 <- c(Price_Croydon_ts, cumulative_forecasted_ts_U95)
Forecast_ts <- ts(combined, start = c(1995, 1), frequency = 12)
Forecast_ts_L80 <- ts(combined_L80, start = c(1995, 1), frequency = 12)
Forecast_ts_L95 <- ts(combined_L95, start = c(1995, 1), frequency = 12)
Forecast_ts_U80 <- ts(combined_U80, start = c(1995, 1), frequency = 12)
Forecast_ts_U95 <- ts(combined_U95, start = c(1995, 1), frequency = 12)
plot(Forecast_ts_L80, col = "skyblue")
lines(Forecast_ts_U80, col = "skyblue")
lines(Forecast_ts_L95, col = "royalblue")
lines(Forecast_ts_U95, col = "royalblue")
lines(Forecast_ts)

```



```
avg_legacy <- arima(diff_legacy_ts, order = c(0, 0, 4))  
avg_legacy_forecast <- forecast(avg_legacy, h=9)  
plot(avg_legacy_forecast)
```

Forecasts from ARIMA(0,0,4) with non-zero mean

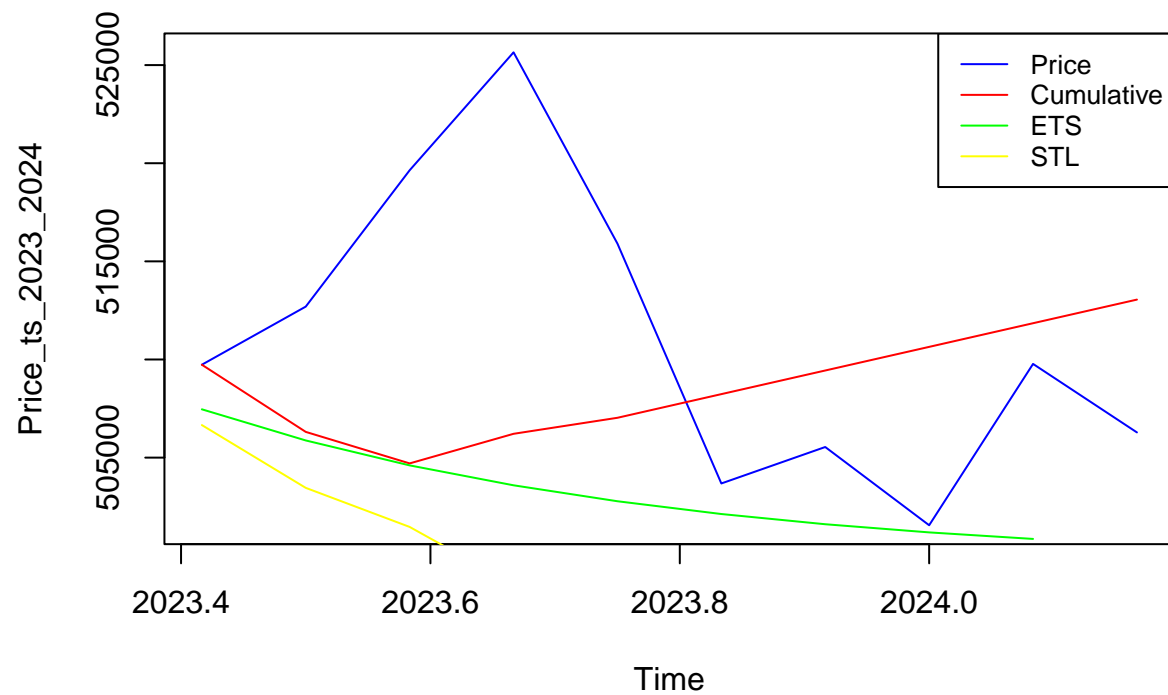


```
last_value_legacy <- tail(legacy_ts, n = 1)
forecasted_values_legacy <- c(last_value_legacy, avg_legacy_forecast$mean)
cumulative_forecasted_values_legacy <- cumsum(forecasted_values_legacy)
print(cumulative_forecasted_values_legacy)
```

```
## [1] 509733.8 506311.5 504704.5 506213.6 507029.8 508234.2 509438.6 510643.1
## [9] 511847.5 513051.9
```

```
cumulative_forecasted_ts_legacy <- ts(cumulative_forecasted_values_legacy, start = c(2023, 6), frequency = 12)

plot(Price_ts_2023_2024, type = "l", col = "blue")
lines(cumulative_forecasted_ts_legacy, col = "red")
lines(ets_forecasted_ts_legacy, col = "green")
lines(stl_forecasted_ts_legacy, col = "yellow")
legend("topright",
      legend = c("Price", "Cumulative", "ETS", "STL"),
      col = c("blue", "red", "green", "yellow"),
      lty = 1,
      cex = 0.8)
```

```
mse_avg <- mean((Price_ts_2023_2024 - cumulative_forecasted_ts_legacy)^2)
print(mse_avg)
```

```
## [1] 88885170
```

```
mse_ets <- mean((Price_ts_2023_2024 - ets_forecasted_ts_legacy)^2)
print(mse_ets)
```

```
## [1] 114910111
```

```
mse_stl <- mean((Price_ts_2023_2024 - stl_forecasted_ts_legacy)^2)
print(mse_stl)
```

```
## [1] 275808912
```

```
mae_avg <- mae(Price_ts_2023_2024, cumulative_forecasted_ts_legacy)
print(mae_avg)
```

```
## [1] 7600.35
```

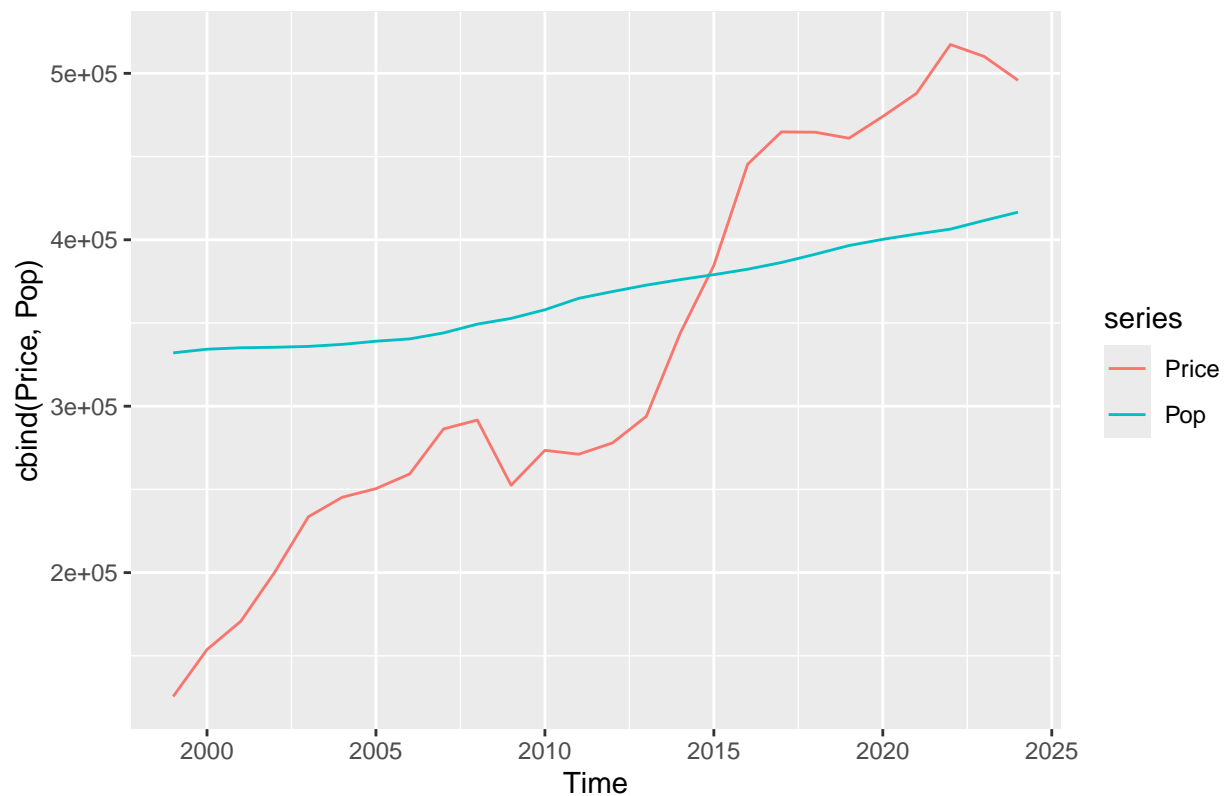
```
mae_ets <- mae(Price_ts_2023_2024, ets_forecasted_ts_legacy)
print(mae_ets)
```

```
## [1] 8231.699
```

```
mae_stl <- mae(Price_ts_2023_2024, stl_forecasted_ts_legacy)
print(mae_stl)
```

```
## [1] 15075.61
```

```
Croydon_df <- read.csv("Merged_Croydon_Data.csv")
Croydon_df$Date <- as.Date(Croydon_df$Date, format = "%Y")
Price <- ts(Croydon_df$Yearly_Price, start = c(1999), frequency = 1)
Pop <- ts(Croydon_df$Population, start = c(1999), frequency = 1)
autoplot(cbind(Price, Pop))
```



```
Croydon_df.bv <- cbind(Price, Pop)
colnames(Croydon_df.bv) <- cbind("Price", "Population")
lagselect <- VARselect(Croydon_df.bv, lag.max = 12, type = "const")
```

```
## Warning in log(sigma.det): NaNs produced
```

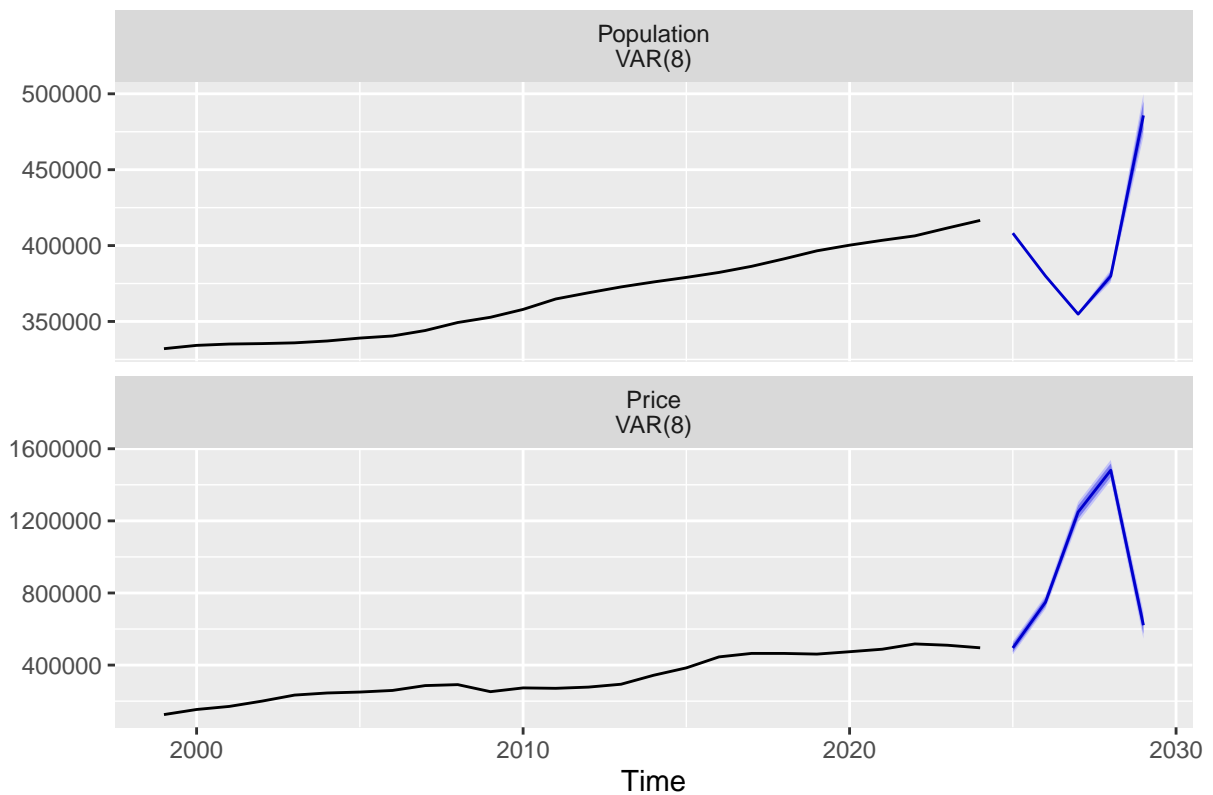
```
## Warning in log(sigma.det): NaNs produced
## Warning in log(sigma.det): NaNs produced
```

```
lagselect$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      7      7      7      6
```

```
var_model <- VAR(Croydon_df.bv, p = 8, type = "const")
```

```
forecast_values <- forecast(var_model, h = 5)
autoplot(forecast_values)
```



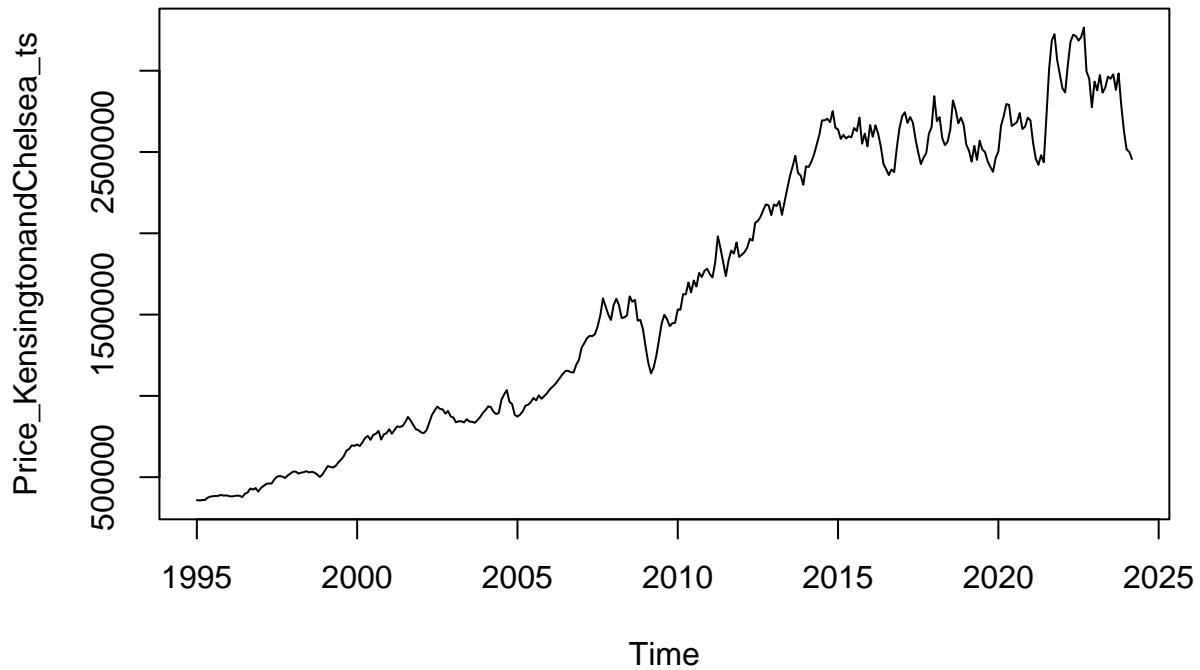
```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
```

```
KensingtonandChelsea_df <- read.csv("Updated_KensingtonandChelsea.csv")
KensingtonandChelsea_df$Date <- as.Date(KensingtonandChelsea_df$Date, format = "%Y-%m-%d")
Price_KensingtonandChelsea_ts <- ts(KensingtonandChelsea_df$Average_Price, start = c(1995, 1), frequency = 12)
d_price <- ts(KensingtonandChelsea_df$Detached_Average_Price, start = c(1995, 1), frequency = 12)
sd_price <- ts(KensingtonandChelsea_df$Semi_Detached_Average_Price, start = c(1995, 1), frequency = 12)
```

```

t_price <- ts(KensingtonandChelsea_df$Terraced_Average_Price, start = c(1995, 1), frequency = 12)
f_price <- ts(KensingtonandChelsea_df$Flat_Average_Price, start = c(1995, 1), frequency = 12)
legacy_ts <- ts(KensingtonandChelsea_df$Average_Price, start = c(1995, 1), end = c(2023, 6), frequency = 12)
Price_ts_2023_2024 <- window(Price_KensingtonandChelsea_ts, start = c(2023, 6), end = c(2024, 3))
diff_legacy_ts <- diff(legacy_ts, differences=1)
plot(Price_KensingtonandChelsea_ts)

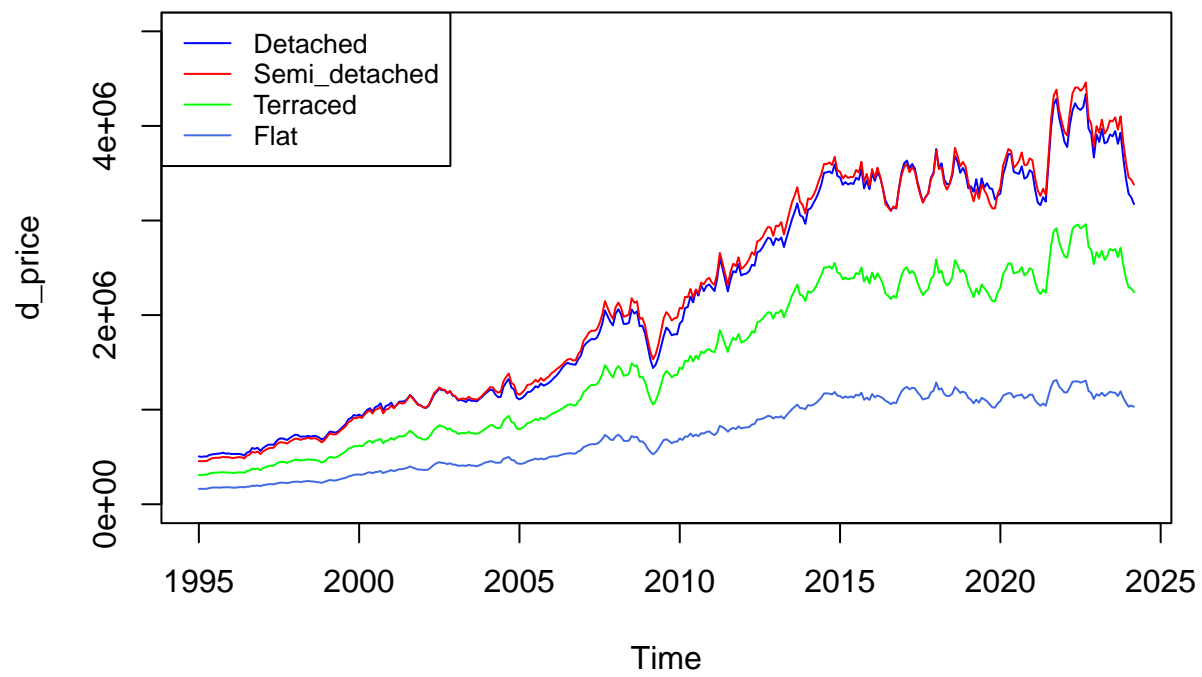
```



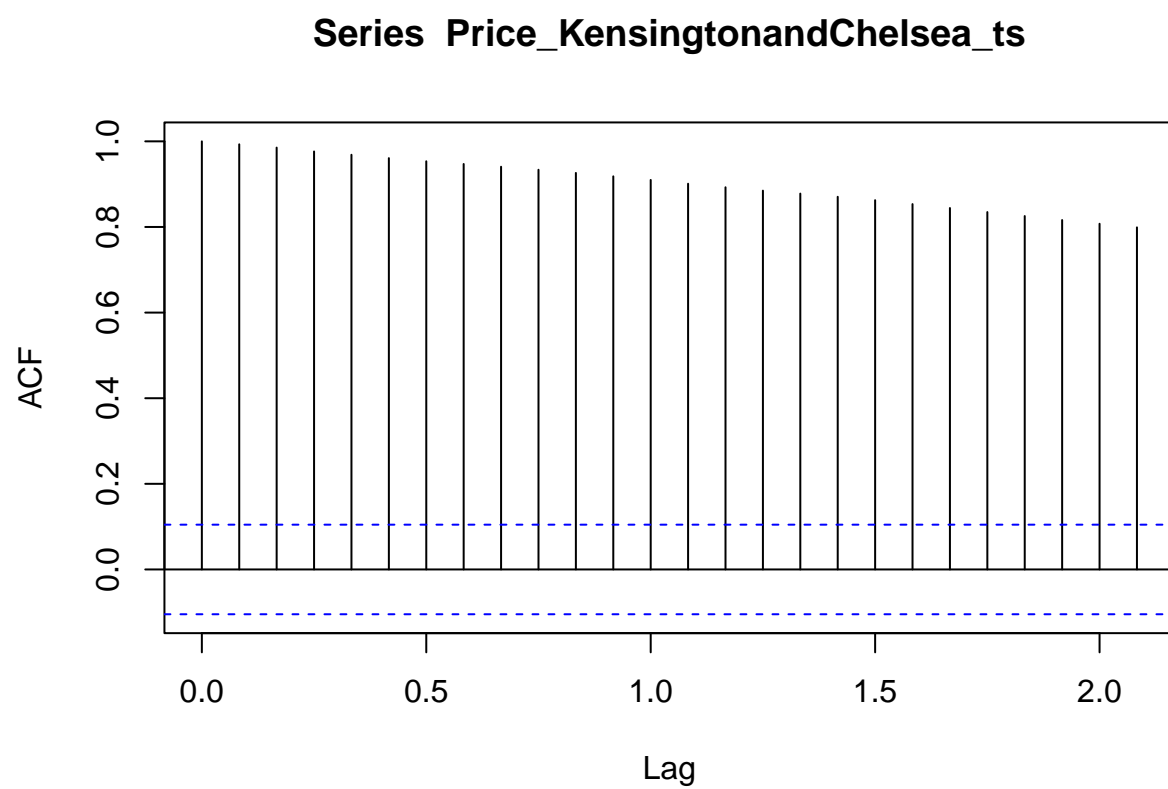
```

plot(d_price, col = "blue", ylim = c(0, 5000000))
lines(sd_price, col = "red")
lines(t_price, col = "green")
lines(f_price, col = "royalblue")
legend("topleft",
      legend = c("Detached", "Semi_detached", "Terraced", "Flat"),
      col = c("blue", "red", "green", "royalblue"),
      lty = 1,
      cex = 0.8)

```

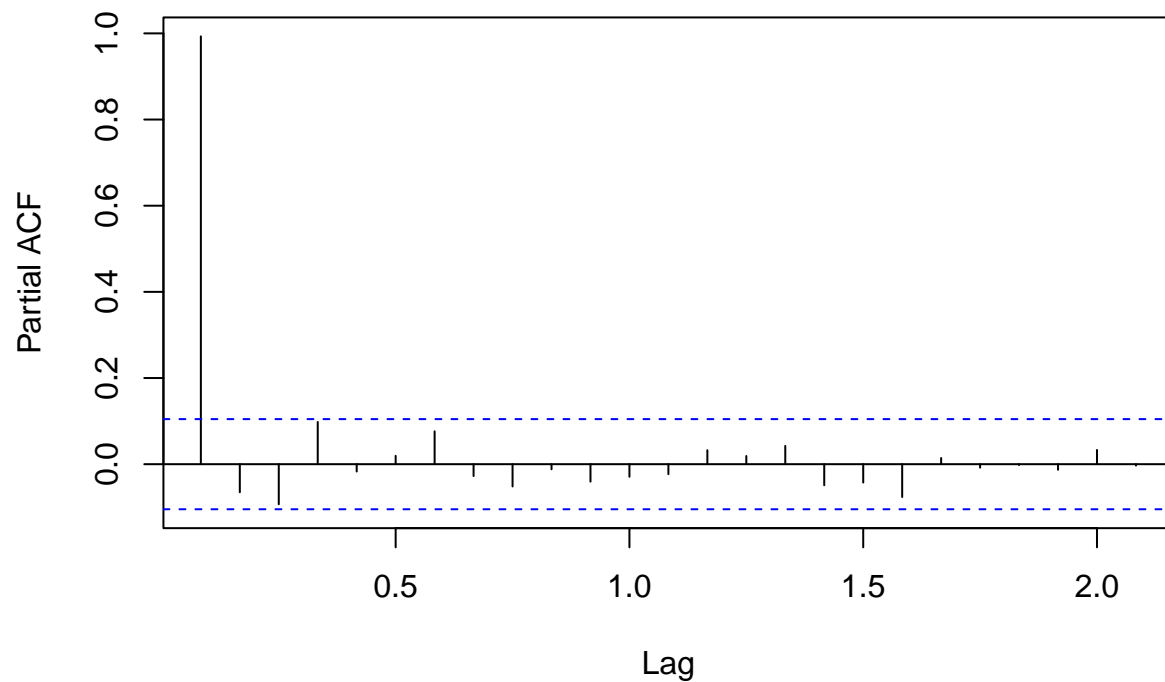


```
acf(Price_KensingtonandChelsea_ts)
```



```
pacf(Price_KensingtonandChelsea_ts)
```

Series Price_KensingtonandChelsea_ts



```
adf.test(Price_KensingtonandChelsea_ts)
```

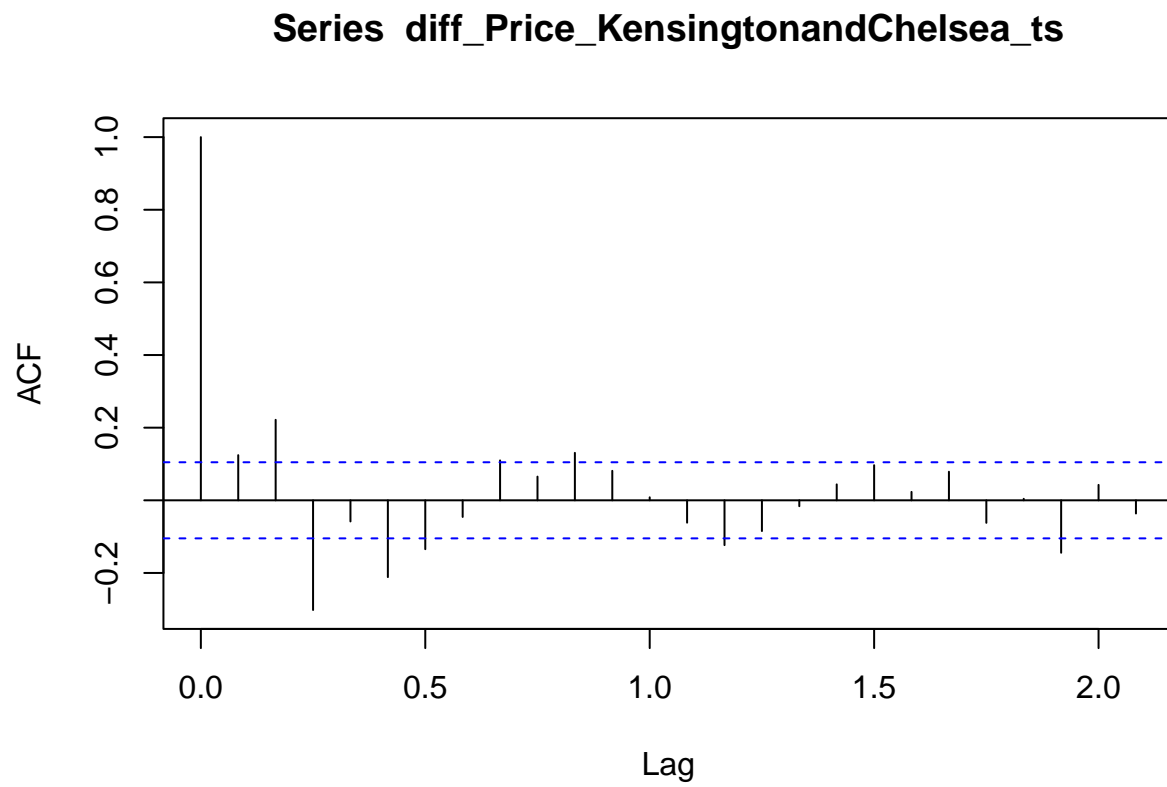
```
##
## Augmented Dickey-Fuller Test
##
## data: Price_KensingtonandChelsea_ts
## Dickey-Fuller = -1.4402, Lag order = 7, p-value = 0.813
## alternative hypothesis: stationary
```

```
diff_Price_KensingtonandChelsea_ts <- diff(Price_KensingtonandChelsea_ts, differences=1)
adf.test(diff_Price_KensingtonandChelsea_ts)
```

```
## Warning in adf.test(diff_Price_KensingtonandChelsea_ts): p-value smaller than
## printed p-value
```

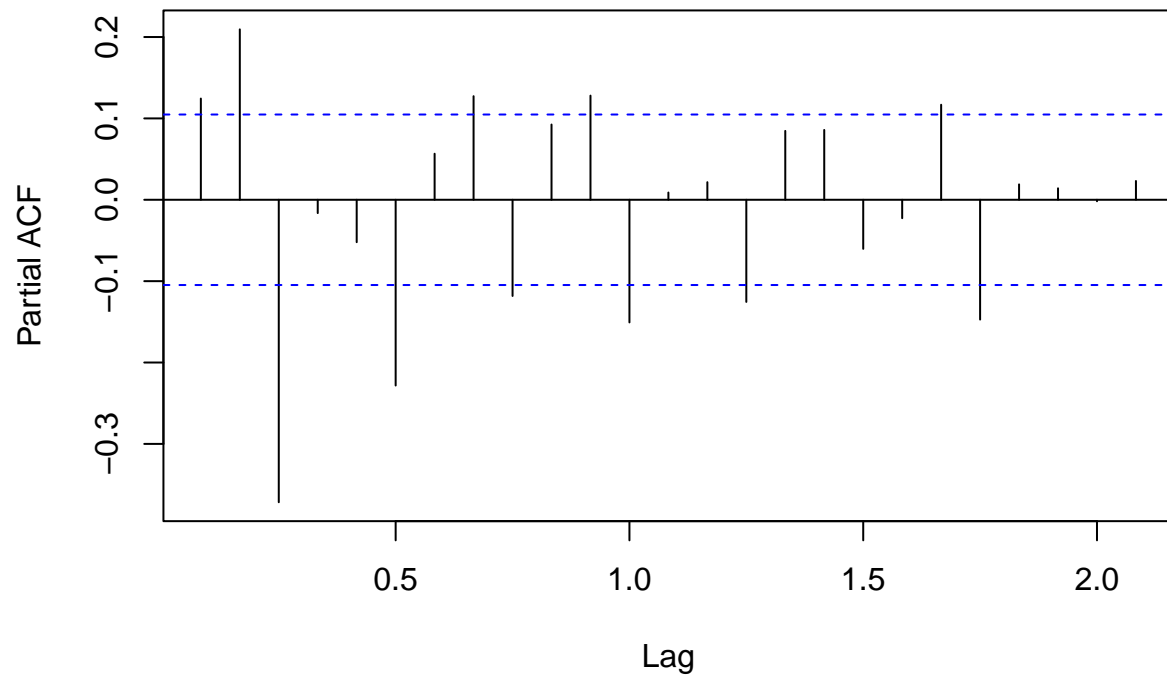
```
##
## Augmented Dickey-Fuller Test
##
## data: diff_Price_KensingtonandChelsea_ts
## Dickey-Fuller = -6.6572, Lag order = 7, p-value = 0.01
## alternative hypothesis: stationary
```

```
acf(diff_Price_KensingtonandChelsea_ts)
```



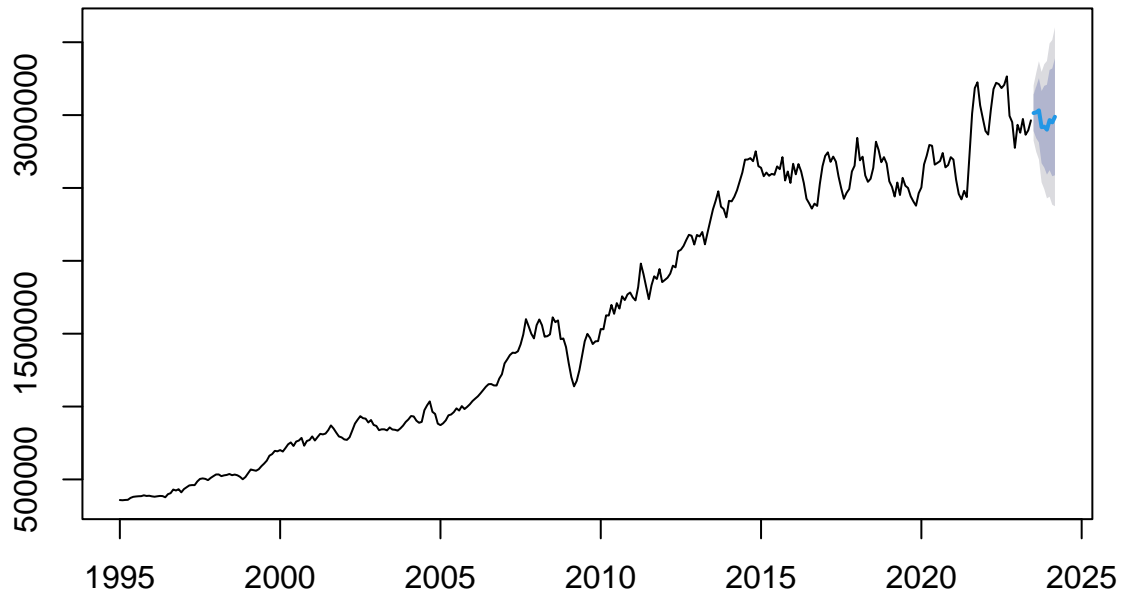
```
pacf(diff_Price_KensingtonandChelsea_ts)
```


Series diff_Price_KensingtonandChelsea_ts



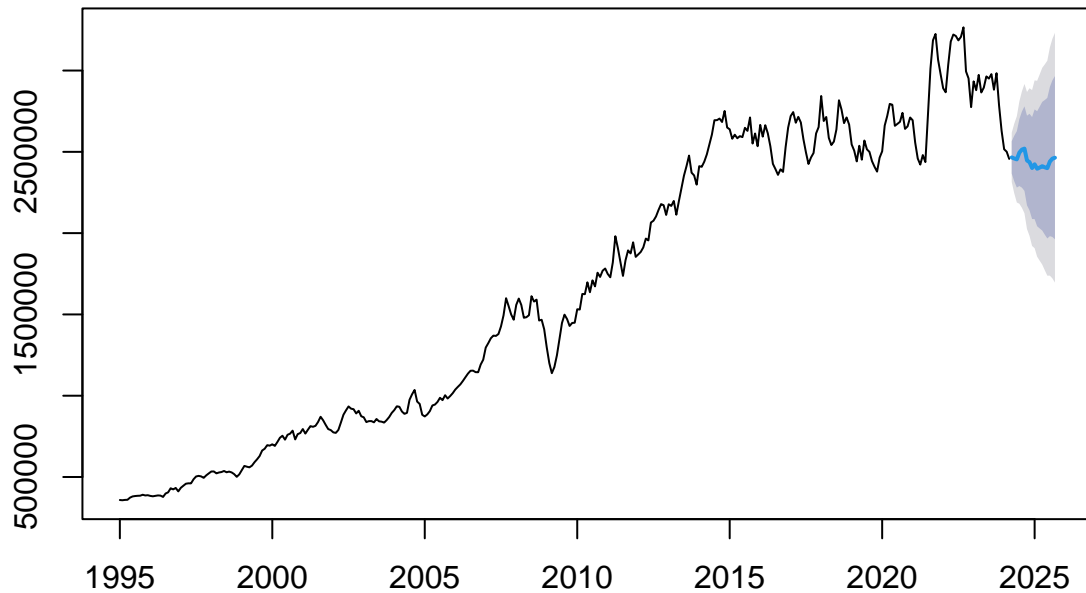
```
ets_Price_KensingtonandChelsea_model <- ets(Price_KensingtonandChelsea_ts, model = "ZZZ")
ets_Price_KensingtonandChelsea_model_forecast <- forecast(ets_Price_KensingtonandChelsea_model, h = 18)
ets_legacy <- ets(legacy_ts, model = "MAM")
ets_legacy_forecast <- forecast(ets_legacy, h=9)
ets_forecasted_values_legacy <- ets_legacy_forecast$mean
ets_forecasted_ts_legacy <- ts(ets_forecasted_values_legacy, start = c(2023, 6), frequency = 12)
plot(ets_legacy_forecast)
```

Forecasts from ETS(M,Ad,M)



```
plot(ets_Price_KensingtonandChelsea_model_forecast)
```

Forecasts from ETS(M,A,M)

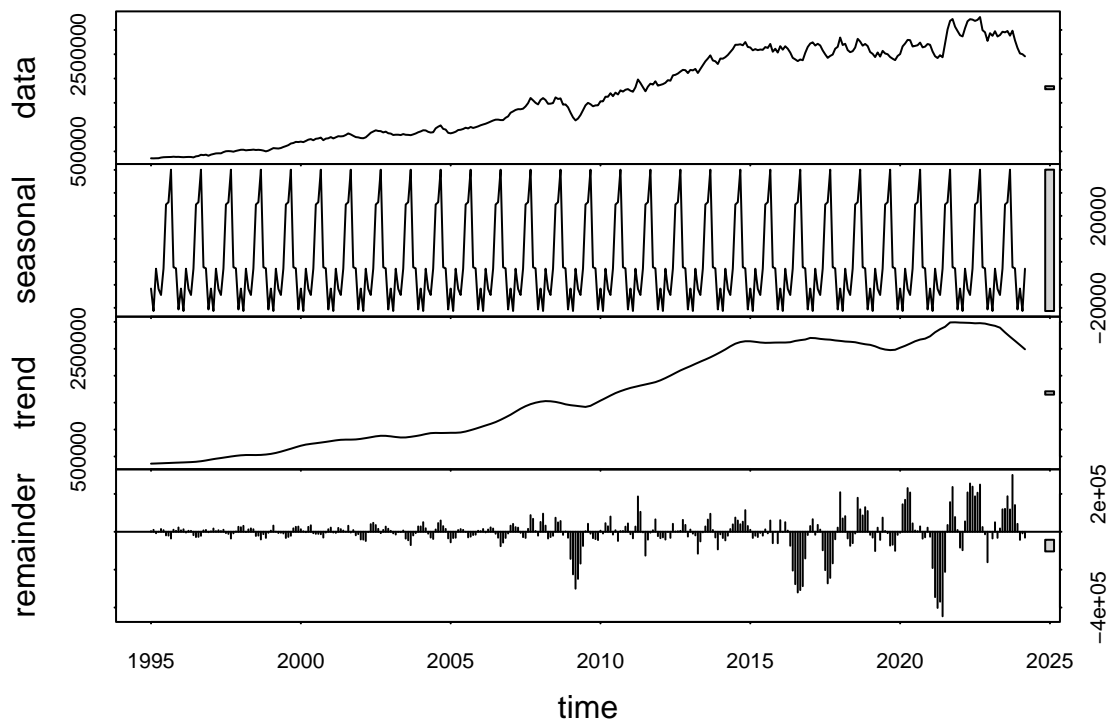


```
summary(ets_Price_KensingtonandChelsea_model_forecast)
```

```
##
## Forecast method: ETS(M,A,M)
##
## Model Information:
## ETS(M,A,M)
##
## Call:
## ets(y = Price_KensingtonandChelsea_ts, model = "ZZZ")
##
## Smoothing parameters:
##   alpha = 0.9835
##   beta  = 0.0207
##   gamma = 2e-04
##
## Initial states:
##   l = 357363.6086
##   b = 4923.0118
##   s = 0.9839 0.997 0.9991 1.027 1.0228 1.0134
##         0.9946 0.9949 0.9959 0.9906 0.9857 0.9952
##
## sigma: 0.0315
##
##      AIC      AICc      BIC
```

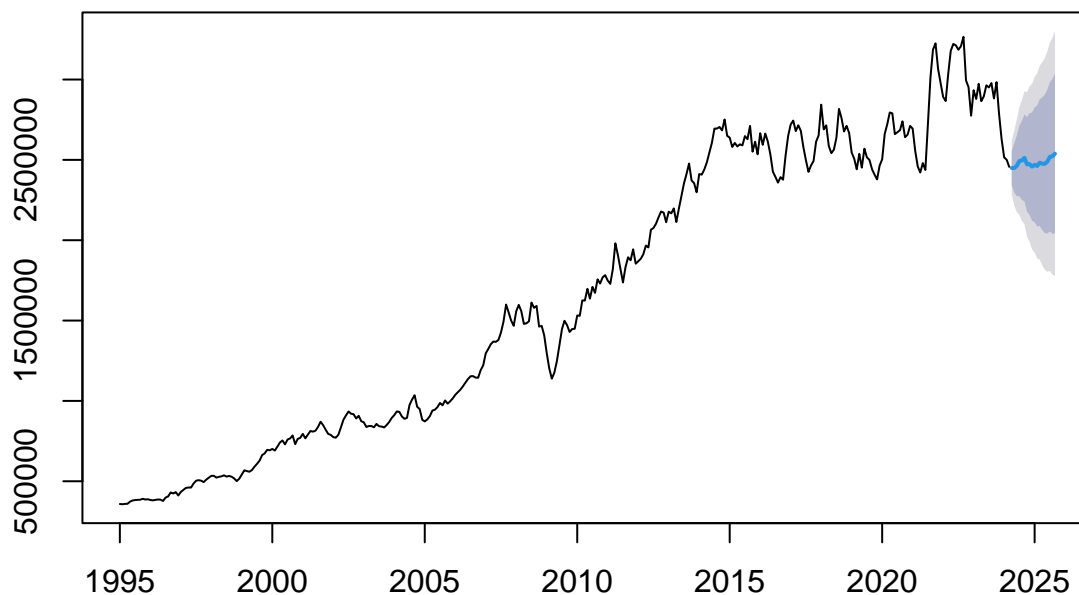
```
## 9567.111 9568.948 9632.744
##
## Error measures:
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -1270.778 62269.17 42966.05 -0.05526985 2.447566 0.2654621
##           ACF1
## Training set 0.1768669
##
## Forecasts:
##           Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Apr 2024           2465910 2366483 2565338 2313849 2617971
## May 2024           2458940 2318271 2599610 2243805 2674076
## Jun 2024           2453727 2280289 2627164 2188477 2718977
## Jul 2024           2495408 2289658 2701158 2180740 2810075
## Aug 2024           2513979 2279745 2748212 2155749 2872208
## Sep 2024           2519842 2259835 2779850 2122195 2917490
## Oct 2024           2446708 2171000 2722416 2025049 2868366
## Nov 2024           2437049 2140206 2733893 1983066 2891033
## Dec 2024           2400487 2086910 2714064 1920912 2880062
## Jan 2025           2423489 2086072 2760906 1907454 2939524
## Feb 2025           2396005 2042250 2749760 1854984 2937026
## Mar 2025           2403447 2028713 2778180 1830341 2976552
## Apr 2025           2411693 2015998 2807388 1806530 3016856
## May 2025           2404777 1990824 2818730 1771690 3037863
## Jun 2025           2399579 1967343 2831814 1738532 3060625
## Jul 2025           2440238 1981316 2899161 1738377 3142100
## Aug 2025           2458296 1976577 2940015 1721570 3195022
## Sep 2025           2463927 1961739 2966115 1695896 3231957
```

```
stl_Price_KensingtonandChelsea_model <- stl(Price_KensingtonandChelsea_ts, s.window="periodic", robust=
plot(stl_Price_KensingtonandChelsea_model)
```



```
stl_Price_KensingtonandChelsea_model_forecast <- forecast(stl_Price_KensingtonandChelsea_model, method=
plot(stl_Price_KensingtonandChelsea_model_forecast)
```

Forecasts from STL + ETS(M,A,N)



```
summary(stl_Price_KensingtonandChelsea_model_forecast)
```

```
##
## Forecast method: STL + ETS(M,A,N)
##
## Model Information:
## ETS(M,A,N)
##
## Call:
## ets(y = na.interp(x), model = etsmodel, allow.multiplicative.trend = allow.multiplicative.trend)
##
## Smoothing parameters:
##   alpha = 0.9999
##   beta  = 0.0087
##
## Initial states:
##   l = 373783.4794
##   b = 1795.9157
##
## sigma: 0.0342
##
##      AIC      AICc      BIC
## 9612.608 9612.782 9631.912
##
## Error measures:
```

```
##
```

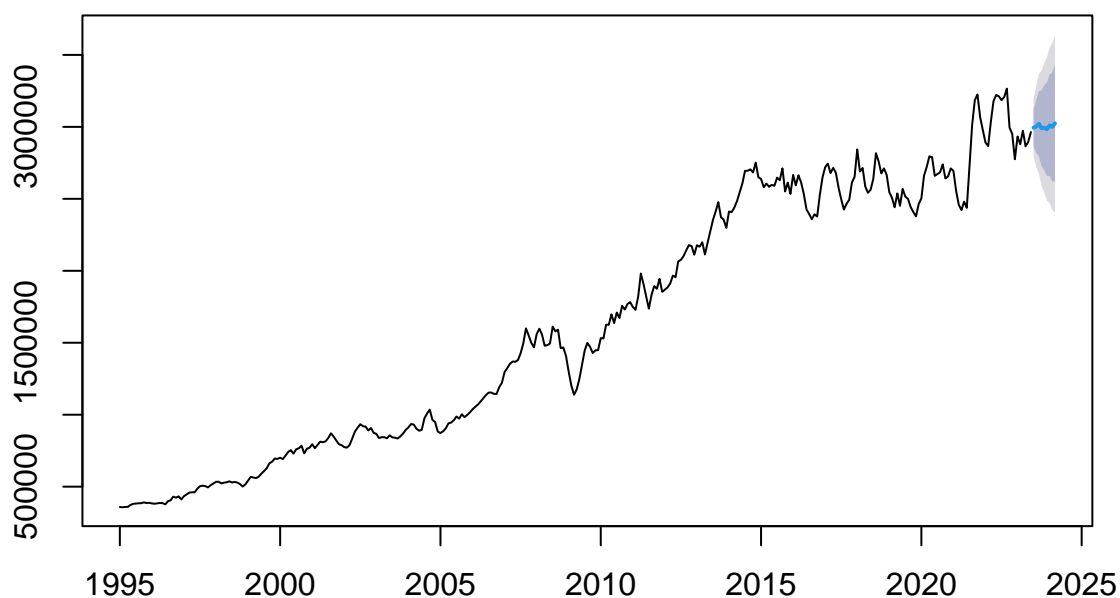
	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
## Training set	120.6386	63049.81	43931.16	0.105282	2.66542	0.271425	0.1503917

```
##
## Forecasts:
##
```

	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Apr 2024	2449907	2342078	2557735	2284998	2614815
## May 2024	2449415	2296155	2602675	2215024	2683806
## Jun 2024	2463101	2274447	2651754	2174580	2751622
## Jul 2024	2493103	2274164	2712042	2158264	2827941
## Aug 2024	2496276	2250260	2742291	2120028	2872523
## Sep 2024	2512585	2241733	2783436	2098353	2926816
## Oct 2024	2472288	2178268	2766309	2022623	2921954
## Nov 2024	2473987	2158093	2789881	1990869	2957105
## Dec 2024	2458271	2121543	2794999	1943289	2973252
## Jan 2025	2469516	2112806	2826225	1923976	3015056
## Feb 2025	2461925	2085947	2837902	1886917	3036932
## Mar 2025	2482481	2087842	2877121	1878932	3086030
## Apr 2025	2475873	2063091	2888654	1844577	3107168
## May 2025	2475381	2044907	2905854	1817029	3133733
## Jun 2025	2489067	2041296	2936837	1804261	3173873
## Jul 2025	2519069	2054348	2983789	1808340	3229798
## Aug 2025	2522242	2040878	3003605	1786060	3258423
## Sep 2025	2538551	2040819	3036282	1777336	3299766

```
stl_legacy <- stl(legacy_ts, s.window="periodic", robust=TRUE)
stl_legacy_forecast <- forecast(stl_legacy, h=9)
plot(stl_legacy_forecast)
```

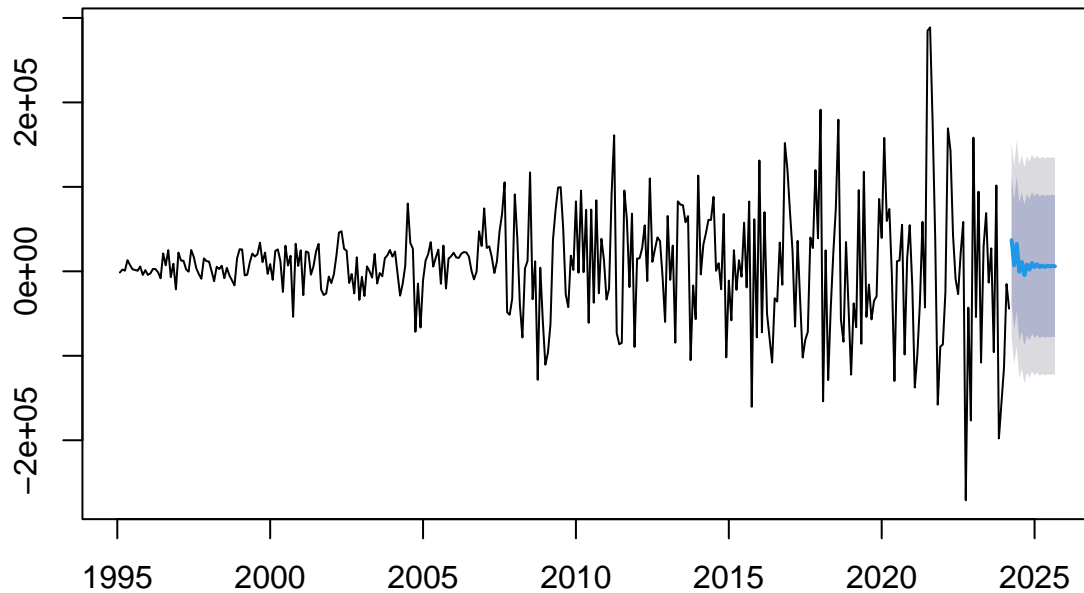
Forecasts from STL + ETS(M,A,N)



```
stl_forecasted_values_legacy <- stl_legacy_forecast$mean
stl_forecasted_ts_legacy <- ts(stl_forecasted_values_legacy, start = c(2023, 6), frequency = 12)

avg_Price_KensingtonandChelsea_model <- auto.arima(diff_Price_KensingtonandChelsea_ts, seasonal=FALSE)
avg_Price_KensingtonandChelsea_model_forecast <- forecast(avg_Price_KensingtonandChelsea_model, h=18)
plot(avg_Price_KensingtonandChelsea_model_forecast)
```


Forecasts from ARIMA(3,0,0) with non-zero mean



```
summary(avg_Price_KensingtonandChelsea_model_forecast)
```

```
##
## Forecast method: ARIMA(3,0,0) with non-zero mean
##
## Model Information:
## Series: diff_Price_KensingtonandChelsea_ts
## ARIMA(3,0,0) with non-zero mean
##
## Coefficients:
##          ar1      ar2      ar3      mean
##      0.1751  0.2448  -0.3715  6145.866
## s.e.  0.0495  0.0486   0.0496  3304.052
##
## sigma^2 = 3.491e+09: log likelihood = -4340.24
## AIC=8690.47  AICc=8690.65  BIC=8709.76
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set -14.79879 58744.3 38890.9 -31.24324 244.826 0.6247128 -0.006792641
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## Apr 2024      36876.1559 -38841.62 112593.93 -78924.18 152676.5
## May 2024       7091.4596 -69778.20  83961.12 -110470.54 124653.5
```

```
## Jun 2024      32539.2827 -47109.10 112187.67 -89272.41 154351.0
## Jul 2024      -417.6972 -82847.59 82012.20 -126483.35 125648.0
## Aug 2024     11105.6685 -71400.13 93611.47 -115076.06 137287.4
## Sep 2024     -4397.4277 -88010.78 79215.93 -132273.02 123478.2
## Oct 2024      7952.1907 -75790.19 91694.57 -120120.73 136025.1
## Nov 2024     2038.8895 -81711.98 85789.76 -126047.01 130124.8
## Dec 2024     9785.7329 -74177.49 93748.95 -118624.93 138196.4
## Jan 2025     5106.8637 -78861.99 89075.72 -123312.42 133526.2
## Feb 2025     8380.6166 -75606.13 92367.36 -120066.02 136827.3
## Mar 2025     4930.6263 -79083.68 88944.93 -123558.16 133419.4
## Apr 2025     6866.0760 -77149.22 90881.37 -121624.24 135356.4
## May 2025     5144.3049 -78878.18 89166.79 -123357.00 133645.6
## Jun 2025     6598.2474 -77427.21 90623.71 -121907.61 135104.1
## Jul 2025     5712.3640 -78313.62 89738.35 -122794.29 134219.0
## Aug 2025     6552.7722 -77474.88 90580.43 -121956.43 135062.0
## Sep 2025     5942.9438 -78085.06 89970.95 -122566.80 134452.7
```

```
last_value <- tail(Price_KensingtonandChelsea_ts, n = 1)
forecasted_values <- c(last_value, avg_Price_KensingtonandChelsea_model_forecast$mean)
forecasted_values_L80 <- c(last_value, avg_Price_KensingtonandChelsea_model_forecast$lower[, "80%"])
print(avg_Price_Brent_model_forecast$lower[, "80%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun
## 2024                -42834.540 -11453.724 12564.036
## 2025 -11244.399 -11244.399 -11244.399 -11244.399 -11244.399 -11244.399
##           Jul           Aug           Sep           Oct           Nov           Dec
## 2024 -9332.054 -11081.974 -11230.540 -11243.216 -11244.298 -11244.391
## 2025 -11244.399 -11244.399 -11244.399
```

```
forecasted_values_L95 <- c(last_value, avg_Price_KensingtonandChelsea_model_forecast$lower[, "95%"])
print(avg_Price_Brent_model_forecast$lower[, "95%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun
## 2024                -48162.071 -17230.049 6480.065
## 2025 -18137.784 -18137.785 -18137.785 -18137.785 -18137.785 -18137.785
##           Jul           Aug           Sep           Oct           Nov           Dec
## 2024 -16219.885 -17975.319 -18123.925 -18136.602 -18137.684 -18137.776
## 2025 -18137.785 -18137.785 -18137.785
```

```
forecasted_values_U80 <- c(last_value, avg_Price_KensingtonandChelsea_model_forecast$upper[, "80%"])
print(avg_Price_Brent_model_forecast$upper[, "80%"])
```

```
##           Jan           Feb           Mar           Apr           May           Jun           Jul
## 2024                -22706.65 10369.75 35549.83 16690.79
## 2025 14799.43 14799.43 14799.43 14799.43 14799.43 14799.43 14799.43
##           Aug           Sep           Oct           Nov           Dec
## 2024 14961.70 14813.29 14800.61 14799.53 14799.44
## 2025 14799.43 14799.43
```

```
forecasted_values_U95 <- c(last_value, avg_Price_KensingtonandChelsea_model_forecast$upper[, "95%"])
print(avg_Price_Brent_model_forecast$upper[, "95%"])
```

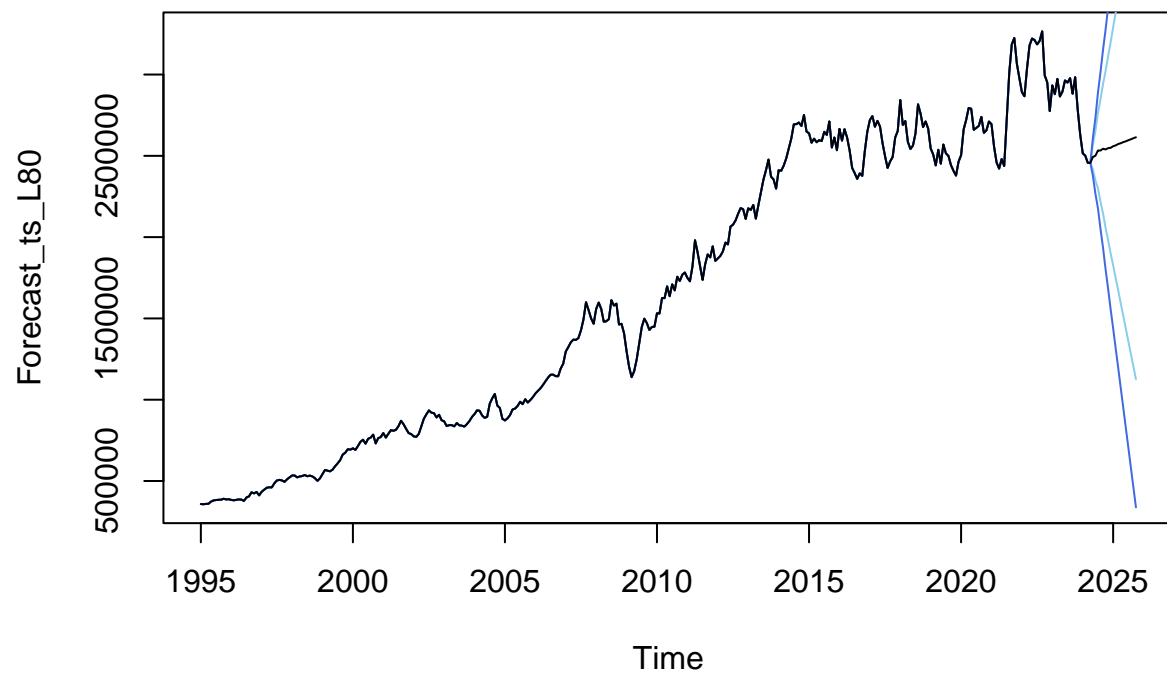
##	Jan	Feb	Mar	Apr	May	Jun	Jul
## 2024				-17379.11	16146.08	41633.80	23578.62
## 2025	21692.82	21692.82	21692.82	21692.82	21692.82	21692.82	21692.82

##	Aug	Sep	Oct	Nov	Dec
## 2024	21855.05	21706.67	21694.00	21692.92	21692.82
## 2025	21692.82	21692.82			

```

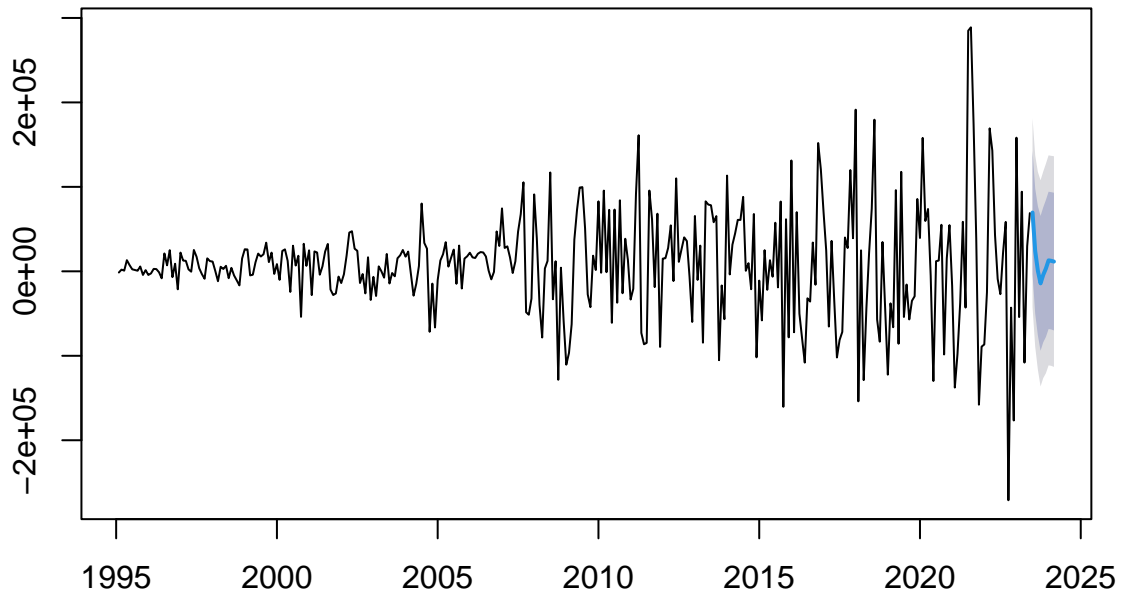
cumulative_forecasted_values_L80 <- cumsum(forecasted_values_L80)
cumulative_forecasted_values_L95 <- cumsum(forecasted_values_L95)
cumulative_forecasted_values_U80 <- cumsum(forecasted_values_U80)
cumulative_forecasted_values_U95 <- cumsum(forecasted_values_U95)
cumulative_forecasted_values <- cumsum(forecasted_values)
cumulative_forecasted_ts <- ts(cumulative_forecasted_values, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U80 <- ts(cumulative_forecasted_values_U80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_U95 <- ts(cumulative_forecasted_values_U95, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L80 <- ts(cumulative_forecasted_values_L80, start = c(2024, 2), frequency = 12)
cumulative_forecasted_ts_L95 <- ts(cumulative_forecasted_values_L95, start = c(2024, 2), frequency = 12)
combined <- c(Price_KensingtonandChelsea_ts, cumulative_forecasted_ts)
combined_L80 <- c(Price_KensingtonandChelsea_ts, cumulative_forecasted_ts_L80)
combined_L95 <- c(Price_KensingtonandChelsea_ts, cumulative_forecasted_ts_L95)
combined_U80 <- c(Price_KensingtonandChelsea_ts, cumulative_forecasted_ts_U80)
combined_U95 <- c(Price_KensingtonandChelsea_ts, cumulative_forecasted_ts_U95)
Forecast_ts <- ts(combined, start = c(1995, 1), frequency = 12)
Forecast_ts_L80 <- ts(combined_L80, start = c(1995, 1), frequency = 12)
Forecast_ts_L95 <- ts(combined_L95, start = c(1995, 1), frequency = 12)
Forecast_ts_U80 <- ts(combined_U80, start = c(1995, 1), frequency = 12)
Forecast_ts_U95 <- ts(combined_U95, start = c(1995, 1), frequency = 12)
plot(Forecast_ts_L80, col = "skyblue")
lines(Forecast_ts_U80, col = "skyblue")
lines(Forecast_ts_L95, col = "royalblue")
lines(Forecast_ts_U95, col = "royalblue")
lines(Forecast_ts)

```



```
avg_legacy <- arima(diff_legacy_ts, order = c(3, 0, 0))  
avg_legacy_forecast <- forecast(avg_legacy, h=9)  
plot(avg_legacy_forecast)
```

Forecasts from ARIMA(3,0,0) with non-zero mean

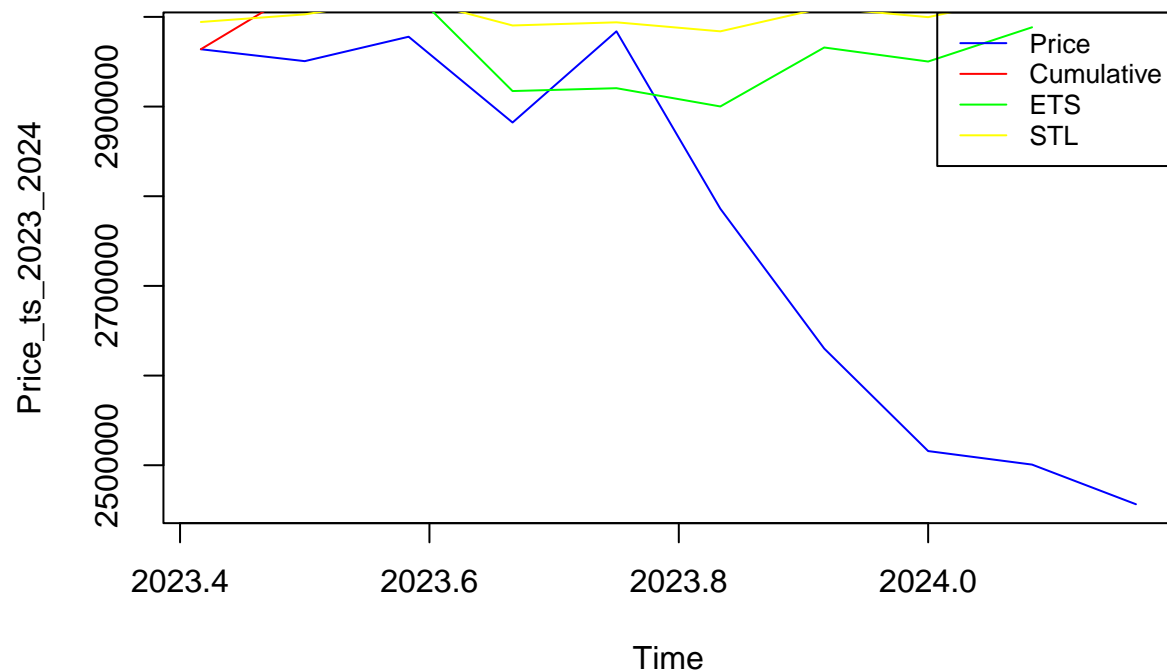


```
last_value_legacy <- tail(legacy_ts, n = 1)
forecasted_values_legacy <- c(last_value_legacy, avg_legacy_forecast$mean)
cumulative_forecasted_values_legacy <- cumsum(forecasted_values_legacy)
print(cumulative_forecasted_values_legacy)
```

```
## [1] 2963934 3033531 3057584 3058269 3044023 3039845 3043239 3056230 3068652
## [10] 3080196
```

```
cumulative_forecasted_ts_legacy <- ts(cumulative_forecasted_values_legacy, start = c(2023, 6), frequency = 12)

plot(Price_ts_2023_2024, type = "l", col = "blue")
lines(cumulative_forecasted_ts_legacy, col = "red")
lines(ets_forecasted_ts_legacy, col = "green")
lines(stl_forecasted_ts_legacy, col = "yellow")
legend("topright",
      legend = c("Price", "Cumulative", "ETS", "STL"),
      col = c("blue", "red", "green", "yellow"),
      lty = 1,
      cex = 0.8)
```



```
mse_avg <- mean((Price_ts_2023_2024 - cumulative_forecasted_ts_legacy)^2)
print(mse_avg)
```

```
## [1] 128652451532
```

```
mse_ets <- mean((Price_ts_2023_2024 - ets_forecasted_ts_legacy)^2)
print(mse_ets)
```

```
## [1] 63074514469
```

```
mse_stl <- mean((Price_ts_2023_2024 - stl_forecasted_ts_legacy)^2)
print(mse_stl)
```

```
## [1] 78850774087
```

```
mae_avg <- mae(Price_ts_2023_2024, cumulative_forecasted_ts_legacy)
print(mae_avg)
```

```
## [1] 279779.1
```

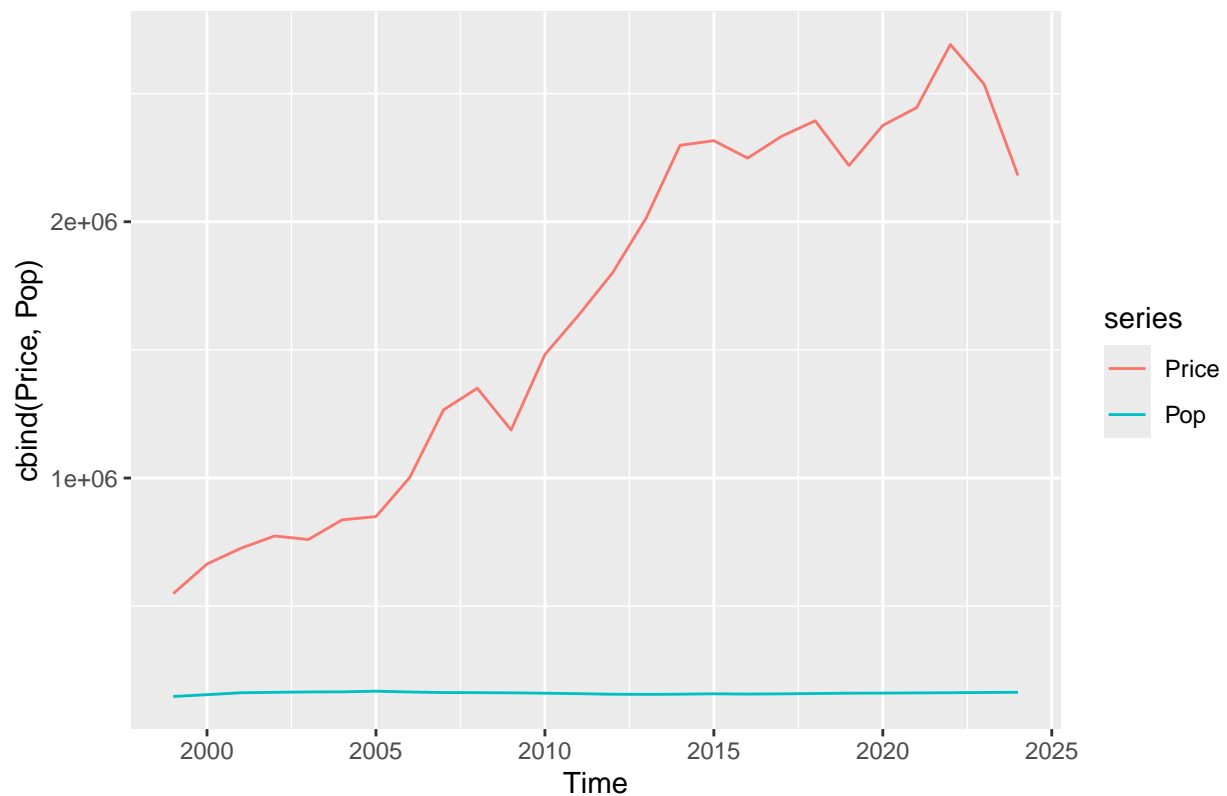
```
mae_ets <- mae(Price_ts_2023_2024, ets_forecasted_ts_legacy)
print(mae_ets)
```

```
## [1] 182562.7
```

```
mae_stl <- mae(Price_ts_2023_2024, stl_forecasted_ts_legacy)
print(mae_stl)
```

```
## [1] 203302.3
```

```
KensingtonandChelsea_df <- read.csv("Merged_KensingtonandChelsea_Data.csv")
KensingtonandChelsea_df$Date <- as.Date(KensingtonandChelsea_df$Date, format = "%Y")
Price <- ts(KensingtonandChelsea_df$Yearly_Price, start = c(1999), frequency = 1)
Pop <- ts(KensingtonandChelsea_df$Population, start = c(1999), frequency = 1)
autoplot(cbind(Price, Pop))
```



```
KensingtonandChelsea_df.bv <- cbind(Price, Pop)
colnames(KensingtonandChelsea_df.bv) <- cbind("Price", "Population")

lagselect <- VARselect(KensingtonandChelsea_df.bv, lag.max = 10, type = "const")
```

```
## Warning in log(sigma.det): NaNs produced
```

```
## Warning in log(sigma.det): NaNs produced
## Warning in log(sigma.det): NaNs produced
```

```
lagselect$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      8      8      8      7
```

```
var_model <- VAR(KensingtonandChelsea_df.bv, p = 12, type = "const")
```

```
forecast_values <- forecast(var_model, h = 5)
```

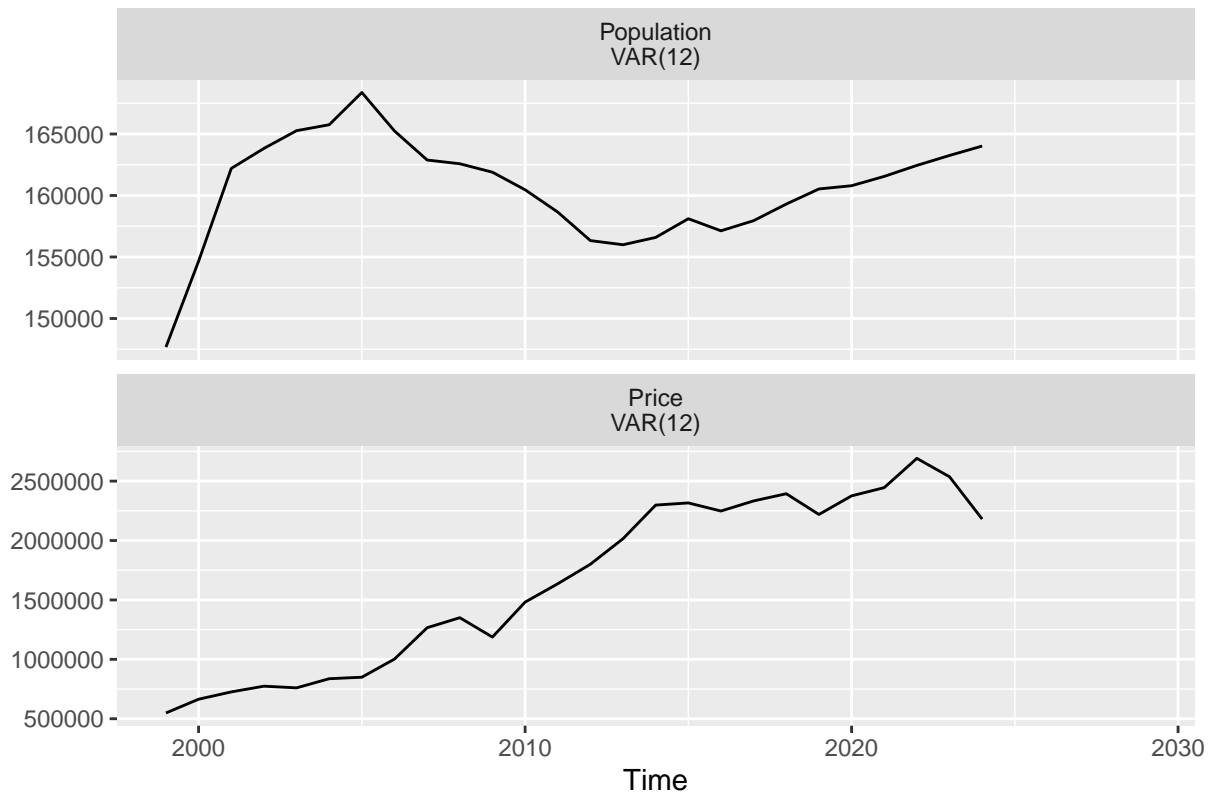
```
autoplot(forecast_values)
```

```
## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
## -Inf
```

```
## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
## -Inf
```

```
## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
## -Inf
```

```
## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
## -Inf
```




```

library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
df<-read.csv("Updated_Brent.csv")
d<-df$Detached_Average_Price
sd<-df$Semi_Detached_Average_Price
t<-df$Terraced_Average_Price
f<-df$Flat_Average_Price
price_data<-data.frame(d,sd,t, f)
cor_matrix<-cor(price_data)
print(cor_matrix)

```

```

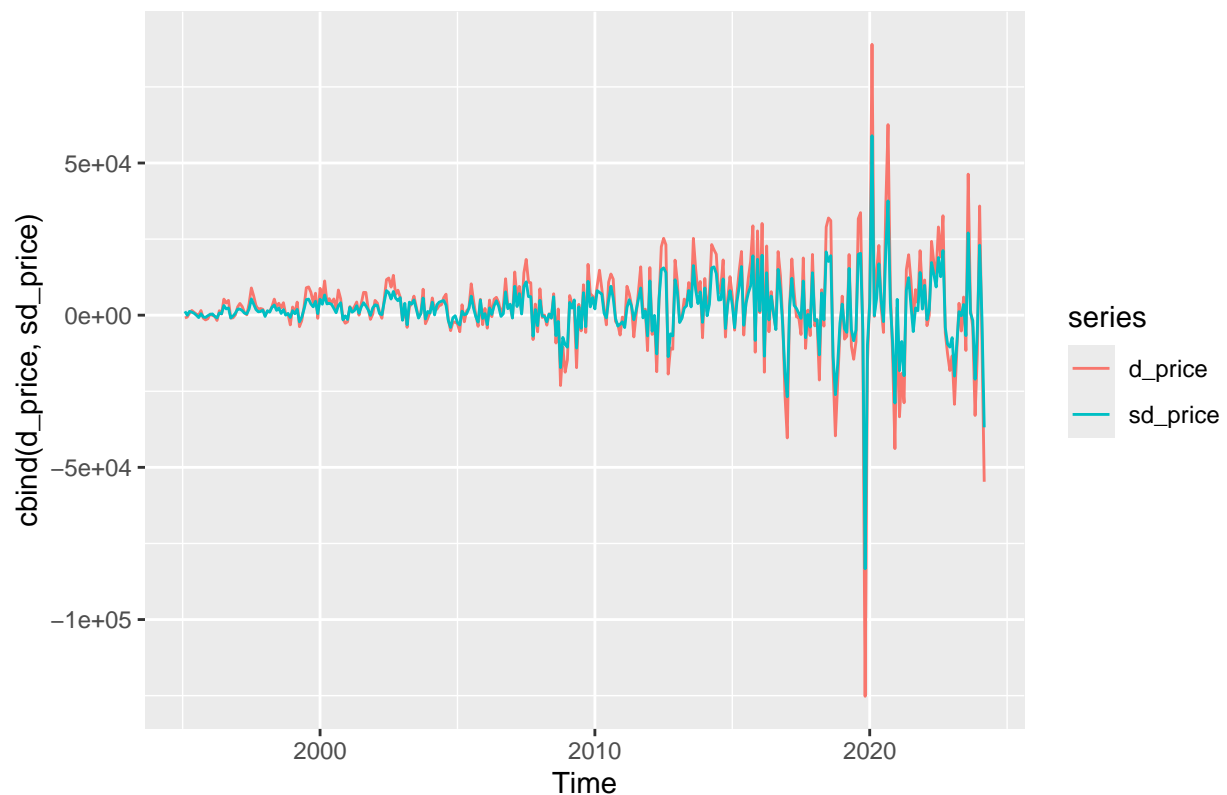
##           d           sd           t           f
## d  1.0000000 0.9997165 0.9990409 0.9917651
## sd 0.9997165 1.0000000 0.9995807 0.9936648
## t  0.9990409 0.9995807 1.0000000 0.9952224
## f  0.9917651 0.9936648 0.9952224 1.0000000

```

```

df$Date<-as.Date(df$Date,format="%Y-%m-%d")
d_price<-diff(ts(df$Detached_Average_Price,start=c(1995,1),frequency=12), d = 1)
sd_price<-diff(ts(df$Semi_Detached_Average_Price,start=c(1995,1),frequency=12), d= 1)
t_price<-diff(ts(df$Terraced_Average_Price,start=c(1995,1),frequency=12), d = 1)
autoplot(cbind(d_price,sd_price))

```



```
df.bv<-cbind(d_price,sd_price)
df.bv2<-cbind(sd_price,t_price)
colnames(df.bv)<-cbind("d_price","sd_price")
colnames(df.bv2)<-cbind("sd_price","t_price")
lagselect<-VARselect(df.bv,lag.max=12,type="const")
lagselect$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      11     10      6     11
```

```
var_model<-VAR(df.bv,p=12,type ="const")
summary(var_model)
```

```
##
## VAR Estimation Results:
## =====
## Endogenous variables: d_price, sd_price
## Deterministic variables: const
## Sample size: 338
## Log Likelihood: -6463.858
## Roots of the characteristic polynomial:
## 0.9435 0.9435 0.9268 0.9221 0.9221 0.9107 0.9107 0.9093 0.9093 0.8882 0.8882 0.8828 0.8828 0.8774 0.8774
## Call:
## VAR(y = df.bv, p = 12, type = "const")
##
##
## Estimation results for equation d_price:
## =====
## d_price = d_price.l1 + sd_price.l1 + d_price.l2 + sd_price.l2 + d_price.l3 + sd_price.l3 + d_price.l4 + sd_price.l4 + d_price.l5 + sd_price.l5 + d_price.l6 + sd_price.l6 + d_price.l7 + sd_price.l7 + d_price.l8 + sd_price.l8 + d_price.l9 + sd_price.l9 + d_price.l10 + sd_price.l10 + d_price.l11 + sd_price.l11
##
##
```

	Estimate	Std. Error	t value	Pr(> t)
d_price.l1	1.9408	0.4278	4.536	8.16e-06 ***
sd_price.l1	-2.4112	0.6565	-3.673	0.000282 ***
d_price.l2	-1.8850	0.4565	-4.129	4.68e-05 ***
sd_price.l2	3.1330	0.6934	4.518	8.84e-06 ***
d_price.l3	-1.6634	0.4859	-3.424	0.000700 ***
sd_price.l3	1.5364	0.7390	2.079	0.038422 *
d_price.l4	2.6464	0.5487	4.823	2.21e-06 ***
sd_price.l4	-3.4693	0.8228	-4.216	3.26e-05 ***
d_price.l5	-1.0106	0.5656	-1.787	0.074964 .
sd_price.l5	1.9760	0.8383	2.357	0.019039 *
d_price.l6	-1.3790	0.5741	-2.402	0.016886 *
sd_price.l6	1.3942	0.8579	1.625	0.105139
d_price.l7	2.1455	0.5750	3.731	0.000226 ***
sd_price.l7	-3.1506	0.8532	-3.693	0.000262 ***
d_price.l8	-0.5178	0.5871	-0.882	0.378512
sd_price.l8	1.1875	0.8651	1.373	0.170818
d_price.l9	-0.3773	0.5679	-0.664	0.506870
sd_price.l9	0.1737	0.8427	0.206	0.836791
d_price.l10	1.3991	0.4928	2.839	0.004821 **
sd_price.l10	-2.3499	0.7371	-3.188	0.001576 **
d_price.l11	-0.5627	0.4922	-1.143	0.253745

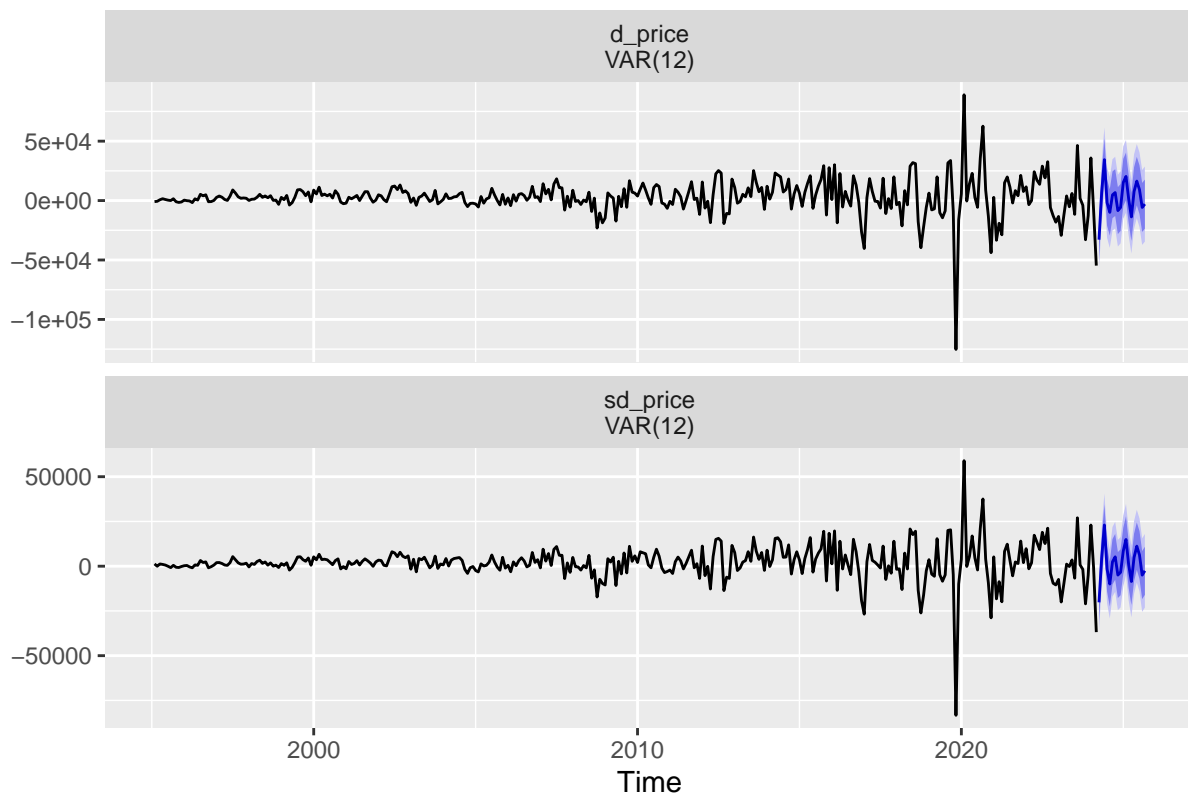
```

## sd_price.l11      1.0979      0.7364      1.491 0.136994
## d_price.l12      -0.2678      0.4615     -0.580 0.562220
## sd_price.l12       0.3311      0.6987      0.474 0.635896
## const           2563.3490     827.5569      3.097 0.002129 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 12190 on 313 degrees of freedom
## Multiple R-Squared:  0.4129, Adjusted R-squared:  0.3679
## F-statistic: 9.173 on 24 and 313 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation sd_price:
## =====
## sd_price = d_price.l1 + sd_price.l1 + d_price.l2 + sd_price.l2 + d_price.l3 + sd_price.l3 + d_price.l3
##
##               Estimate Std. Error t value Pr(>|t|)
## d_price.l1      1.0913      0.2785   3.919 0.000109 ***
## sd_price.l1     -1.3026      0.4273  -3.048 0.002498 **
## d_price.l2     -1.4201      0.2972  -4.779 2.71e-06 ***
## sd_price.l2      2.3153      0.4513   5.130 5.09e-07 ***
## d_price.l3     -0.6673      0.3162  -2.110 0.035647 *
## sd_price.l3      0.3703      0.4810   0.770 0.441975
## d_price.l4      1.5939      0.3571   4.463 1.13e-05 ***
## sd_price.l4     -2.0444      0.5356  -3.817 0.000163 ***
## d_price.l5     -0.8082      0.3682  -2.195 0.028876 *
## sd_price.l5      1.5196      0.5457   2.785 0.005679 **
## d_price.l6     -0.5837      0.3737  -1.562 0.119290
## sd_price.l6      0.4286      0.5584   0.768 0.443290
## d_price.l7      1.3483      0.3742   3.603 0.000366 ***
## sd_price.l7     -1.9941      0.5553  -3.591 0.000382 ***
## d_price.l8     -0.4317      0.3821  -1.130 0.259418
## sd_price.l8      0.9345      0.5631   1.660 0.097990 .
## d_price.l9     -0.0401      0.3696  -0.108 0.913683
## sd_price.l9     -0.1968      0.5485  -0.359 0.719988
## d_price.l10      0.8403      0.3208   2.620 0.009228 **
## sd_price.l10    -1.4281      0.4797  -2.977 0.003140 **
## d_price.l11     -0.4037      0.3203  -1.260 0.208497
## sd_price.l11      0.7818      0.4793   1.631 0.103889
## d_price.l12     -0.2035      0.3004  -0.677 0.498628
## sd_price.l12      0.2557      0.4548   0.562 0.574279
## const           1679.0340     538.6393   3.117 0.001995 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 7933 on 313 degrees of freedom
## Multiple R-Squared:  0.4134, Adjusted R-squared:  0.3684
## F-statistic: 9.19 on 24 and 313 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:

```

```
##          d_price sd_price
## d_price 148552062 95842074
## sd_price 95842074 62933089
##
## Correlation matrix of residuals:
##          d_price sd_price
## d_price  1.0000  0.9912
## sd_price  0.9912  1.0000
```

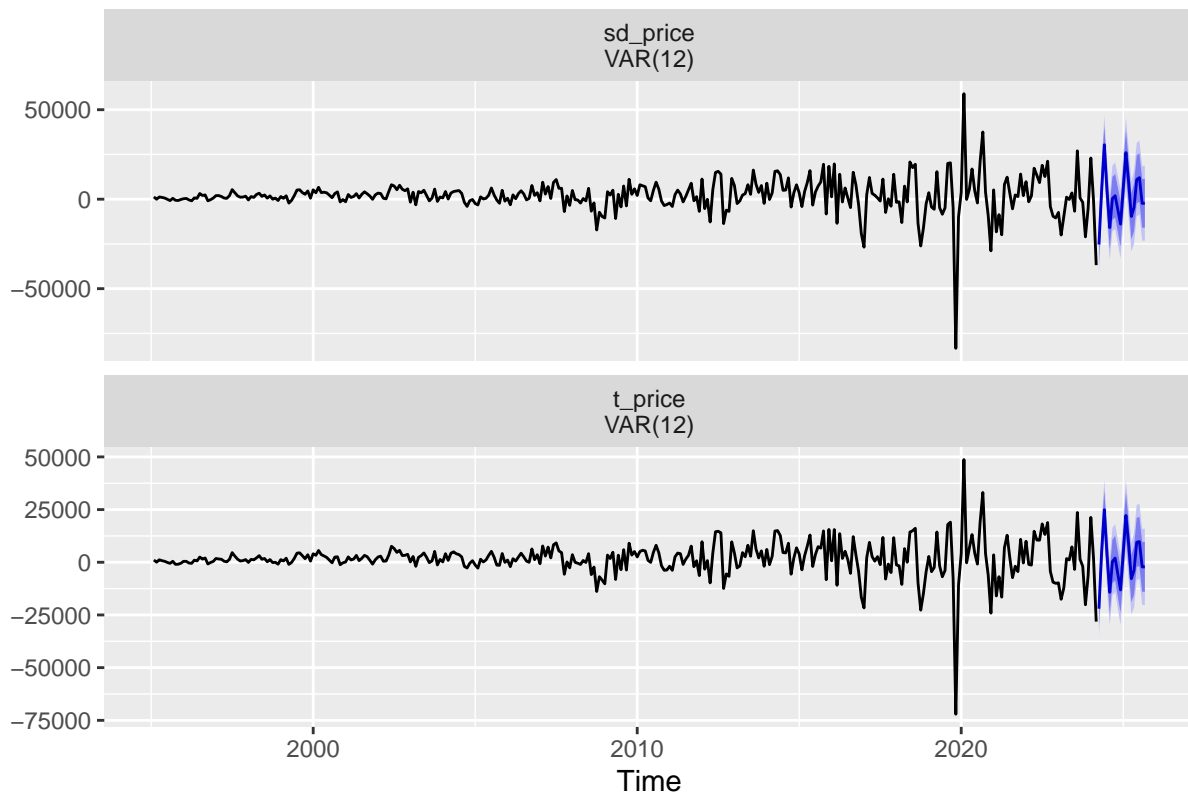
```
forecast_values<-forecast(var_model,h=18)
autoplot(forecast_values)
```



```
lagselect2<-VARselect(df.bv2,lag.max=12,type="const")
lagselect2$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##    12     9     9     12
```

```
var_model2<-VAR(df.bv2,p=12,type="const")
forecast_values2<-forecast(var_model2,h=18)
autoplot(forecast_values2)
```



```
summary(var_model2)
```

```
##
## VAR Estimation Results:
## =====
## Endogenous variables: sd_price, t_price
## Deterministic variables: const
## Sample size: 338
## Log Likelihood: -6262.744
## Roots of the characteristic polynomial:
## 0.9553 0.9553 0.9184 0.9184 0.9139 0.9139 0.9037 0.9037 0.8999 0.8999 0.8901 0.8901 0.8874 0.8874 0.
## Call:
## VAR(y = df.bv2, p = 12, type = "const")
##
##
## Estimation results for equation sd_price:
## =====
## sd_price = sd_price.l1 + t_price.l1 + sd_price.l2 + t_price.l2 + sd_price.l3 + t_price.l3 + sd_price
##
##           Estimate Std. Error t value Pr(>|t|)
## sd_price.l1 -0.75070    0.41142  -1.825  0.06900 .
## t_price.l1   1.21061    0.47900   2.527  0.01198 *
## sd_price.l2  0.90377    0.43590   2.073  0.03896 *
## t_price.l2  -0.92611    0.51116  -1.812  0.07098 .
## sd_price.l3  0.29593    0.45511   0.650  0.51602
```

```

## t_price.l3      -1.05600      0.53388     -1.978     0.04881 *
## sd_price.l4     -0.91701      0.48753     -1.881     0.06091 .
## t_price.l4       1.45356      0.57726      2.518     0.01230 *
## sd_price.l5       1.03628      0.48724      2.127     0.03421 *
## t_price.l5      -0.84391      0.57956     -1.456     0.14636
## sd_price.l6       1.22005      0.49458      2.467     0.01417 *
## t_price.l6      -1.87937      0.58752     -3.199     0.00152 **
## sd_price.l7      -0.05396      0.50852     -0.106     0.91556
## t_price.l7       0.11495      0.60417      0.190     0.84923
## sd_price.l8       0.52609      0.50727      1.037     0.30049
## t_price.l8      -0.21339      0.60272     -0.354     0.72355
## sd_price.l9       1.17709      0.51240      2.297     0.02227 *
## t_price.l9      -1.70688      0.60919     -2.802     0.00540 **
## sd_price.l10      0.44850      0.48409      0.926     0.35491
## t_price.l10     -0.73199      0.57155     -1.281     0.20124
## sd_price.l11     -0.97805      0.46142     -2.120     0.03482 *
## t_price.l11      1.38445      0.54586      2.536     0.01169 *
## sd_price.l12     -0.49637      0.45582     -1.089     0.27701
## t_price.l12       0.45931      0.53551      0.858     0.39172
## const           1683.43780    526.45599      3.198     0.00153 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 7734 on 313 degrees of freedom
## Multiple R-Squared:  0.4425, Adjusted R-squared:  0.3997
## F-statistic: 10.35 on 24 and 313 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation t_price:
## =====
## t_price = sd_price.l1 + t_price.l1 + sd_price.l2 + t_price.l2 + sd_price.l3 + t_price.l3 + sd_price.l4 +
##
##
##          Estimate Std. Error t value Pr(>|t|)
## sd_price.l1    -0.93968    0.35250   -2.666 0.008079 **
## t_price.l1      1.39435    0.41040    3.398 0.000768 ***
## sd_price.l2      0.52641    0.37348    1.409 0.159684
## t_price.l2     -0.50791    0.43796   -1.160 0.247044
## sd_price.l3      0.74357    0.38994    1.907 0.057447 .
## t_price.l3     -1.48284    0.45742   -3.242 0.001316 **
## sd_price.l4     -0.91095    0.41771   -2.181 0.029942 *
## t_price.l4      1.38132    0.49459    2.793 0.005546 **
## sd_price.l5      0.76956    0.41746    1.843 0.066210 .
## t_price.l5     -0.58730    0.49656   -1.183 0.237812
## sd_price.l6      1.41713    0.42375    3.344 0.000925 ***
## t_price.l6     -2.05899    0.50338   -4.090 5.48e-05 ***
## sd_price.l7     -0.18005    0.43569   -0.413 0.679711
## t_price.l7      0.26482    0.51765    0.512 0.609303
## sd_price.l8      0.27812    0.43462    0.640 0.522692
## t_price.l8      0.01791    0.51640    0.035 0.972357
## sd_price.l9      1.35494    0.43902    3.086 0.002208 **
## t_price.l9     -1.85641    0.52195   -3.557 0.000434 ***
## sd_price.l10     0.36866    0.41476    0.889 0.374770
## t_price.l10     -0.60322    0.48969   -1.232 0.218939

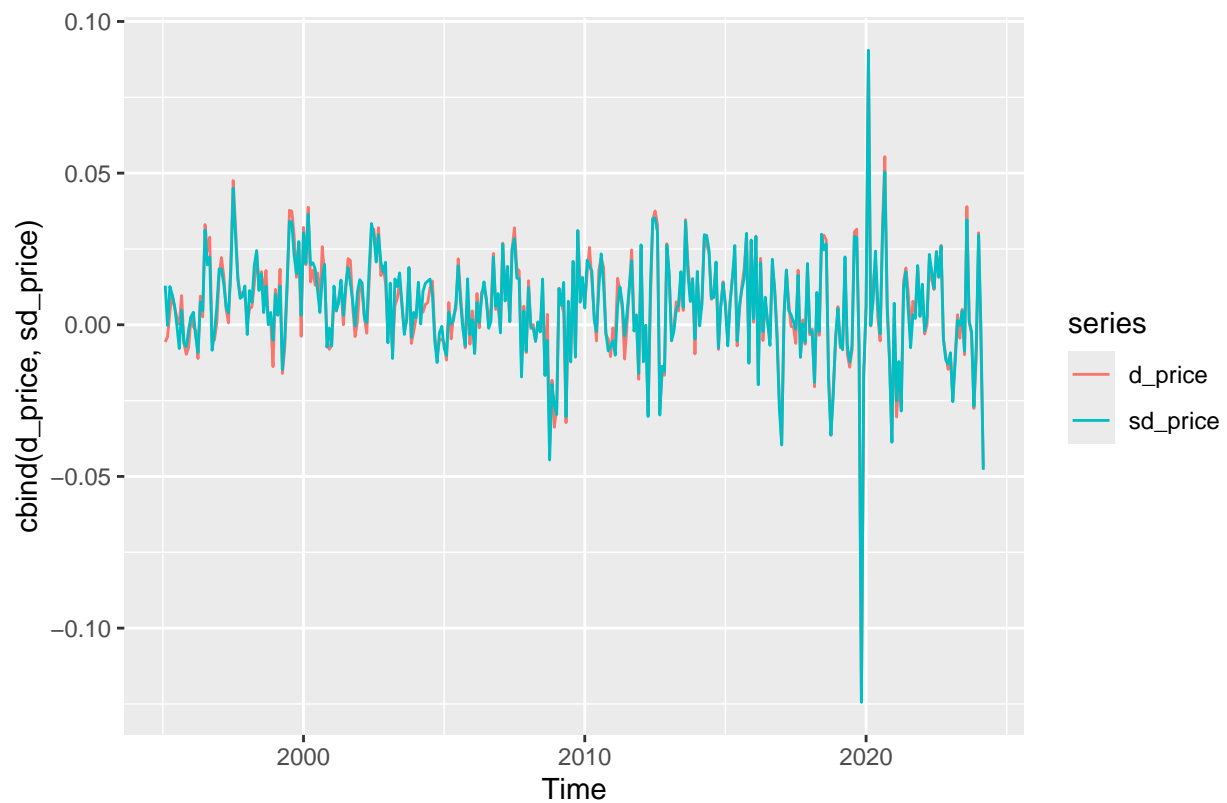
```

```
## sd_price.l11    -0.96447    0.39534   -2.440 0.015259 *
## t_price.l11     1.33052    0.46769    2.845 0.004736 **
## sd_price.l12    -0.29101    0.39054   -0.745 0.456744
## t_price.l12     0.24025    0.45882    0.524 0.600912
## const          1407.75388  451.06076    3.121 0.001971 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 6626 on 313 degrees of freedom
## Multiple R-Squared:  0.4542, Adjusted R-squared:  0.4123
## F-statistic: 10.85 on 24 and 313 DF,  p-value: < 2.2e-16
##
##
## Covariance matrix of residuals:
##          sd_price  t_price
## sd_price 59815031 50762251
## t_price  50762251 43909277
##
## Correlation matrix of residuals:
##          sd_price t_price
## sd_price  1.0000  0.9905
## t_price   0.9905  1.0000
```

```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
df<-read.csv("Updated_Brent.csv")
d<-df$Detached_Average_Price
sd<-df$Semi_Detached_Average_Price
t<-df$Terraced_Average_Price
f<-df$Flat_Average_Price
price_data<-data.frame(d,sd,t, f)
cor_matrix<-cor(price_data)
print(cor_matrix)
```

```
##          d          sd          t          f
## d  1.0000000 0.9997165 0.9990409 0.9917651
## sd 0.9997165 1.0000000 0.9995807 0.9936648
## t  0.9990409 0.9995807 1.0000000 0.9952224
## f  0.9917651 0.9936648 0.9952224 1.0000000
```

```
df$Date<-as.Date(df$Date,format="%Y-%m-%d")
d_price<-diff(ts(log(df$Detached_Average_Price),start=c(1995,1),frequency=12), d = 1)
sd_price<-diff(ts(log(df$Semi_Detached_Average_Price),start=c(1995,1),frequency=12), d= 1)
t_price<-diff(ts(log(df$Terraced_Average_Price),start=c(1995,1),frequency=12), d = 1)
autoplot(cbind(d_price,sd_price))
```



```
df.bv<-cbind(d_price,sd_price)
df.bv2<-cbind(sd_price,t_price)
colnames(df.bv)<-cbind("d_price","sd_price")
colnames(df.bv2)<-cbind("sd_price","t_price")
lagselect<-VARselect(df.bv,lag.max=12,type="const")
lagselect$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      11     11     10     11
```

```
var_model<-VAR(df.bv,p=12,type ="const")
summary(var_model)
```

```
##
## VAR Estimation Results:
## =====
## Endogenous variables: d_price, sd_price
## Deterministic variables: const
## Sample size: 338
## Log Likelihood: 2551.078
## Roots of the characteristic polynomial:
## 0.9618 0.9418 0.9418 0.9353 0.9353 0.9302 0.9302 0.9186 0.9186 0.8831 0.8759 0.8759 0.8755 0.8755 0.8755 0.8755 0.8755 0.8755 0.8755 0.8755
## Call:
## VAR(y = df.bv, p = 12, type = "const")
```



```
##  
##  
## Estimation results for equation d_price:  
## =====  
## d_price = d_price.l1 + sd_price.l1 + d_price.l2 + sd_price.l2 + d_price.l3 + sd_price.l3 + d_price.l  
##  
##           Estimate Std. Error t value Pr(>|t|)  
## d_price.l1    1.423826   0.343561   4.144 4.39e-05 ***  
## sd_price.l1   -1.021440   0.345448  -2.957 0.003344 **  
## d_price.l2    -1.448578   0.367600  -3.941 0.000100 ***  
## sd_price.l2    1.663545   0.364853   4.559 7.37e-06 ***  
## d_price.l3    -1.337687   0.386929  -3.457 0.000621 ***  
## sd_price.l3    0.742891   0.386561   1.922 0.055539 .  
## d_price.l4     1.958330   0.456963   4.286 2.43e-05 ***  
## sd_price.l4   -1.566270   0.451681  -3.468 0.000599 ***  
## d_price.l5    -0.797023   0.470087  -1.695 0.090979 .  
## sd_price.l5    1.063175   0.459199   2.315 0.021244 *  
## d_price.l6    -0.975961   0.484572  -2.014 0.044858 *  
## sd_price.l6    0.586395   0.477021   1.229 0.219888  
## d_price.l7     1.155106   0.475433   2.430 0.015678 *  
## sd_price.l7   -1.027147   0.467833  -2.196 0.028859 *  
## d_price.l8    -0.387239   0.468073  -0.827 0.408694  
## sd_price.l8    0.633174   0.456408   1.387 0.166338  
## d_price.l9    -0.220084   0.457972  -0.481 0.631164  
## sd_price.l9   -0.015708   0.451201  -0.035 0.972251  
## d_price.l10    0.940744   0.378470   2.486 0.013453 *  
## sd_price.l10  -1.007394   0.376938  -2.673 0.007922 **  
## d_price.l11   -0.471428   0.369954  -1.274 0.203506  
## sd_price.l11   0.622357   0.366144   1.700 0.090170 .  
## d_price.l12    0.175273   0.334987   0.523 0.601189  
## sd_price.l12  -0.240072   0.336200  -0.714 0.475712  
## const         0.003105   0.001071   2.900 0.003995 **  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
##  
## Residual standard error: 0.01434 on 313 degrees of freedom  
## Multiple R-Squared: 0.4017, Adjusted R-squared: 0.3558  
## F-statistic: 8.757 on 24 and 313 DF, p-value: < 2.2e-16  
##  
##  
## Estimation results for equation sd_price:  
## =====  
## sd_price = d_price.l1 + sd_price.l1 + d_price.l2 + sd_price.l2 + d_price.l3 + sd_price.l3 + d_price.l  
##  
##           Estimate Std. Error t value Pr(>|t|)  
## d_price.l1    1.094772   0.341545   3.205 0.001488 **  
## sd_price.l1   -0.693292   0.343421  -2.019 0.044362 *  
## d_price.l2    -1.740608   0.365442  -4.763 2.92e-06 ***  
## sd_price.l2    1.936765   0.362712   5.340 1.79e-07 ***  
## d_price.l3    -0.570482   0.384659  -1.483 0.139058  
## sd_price.l3   -0.017579   0.384293  -0.046 0.963543  
## d_price.l4     1.641806   0.454282   3.614 0.000351 ***  
## sd_price.l4   -1.237055   0.449030  -2.755 0.006214 **
```

```

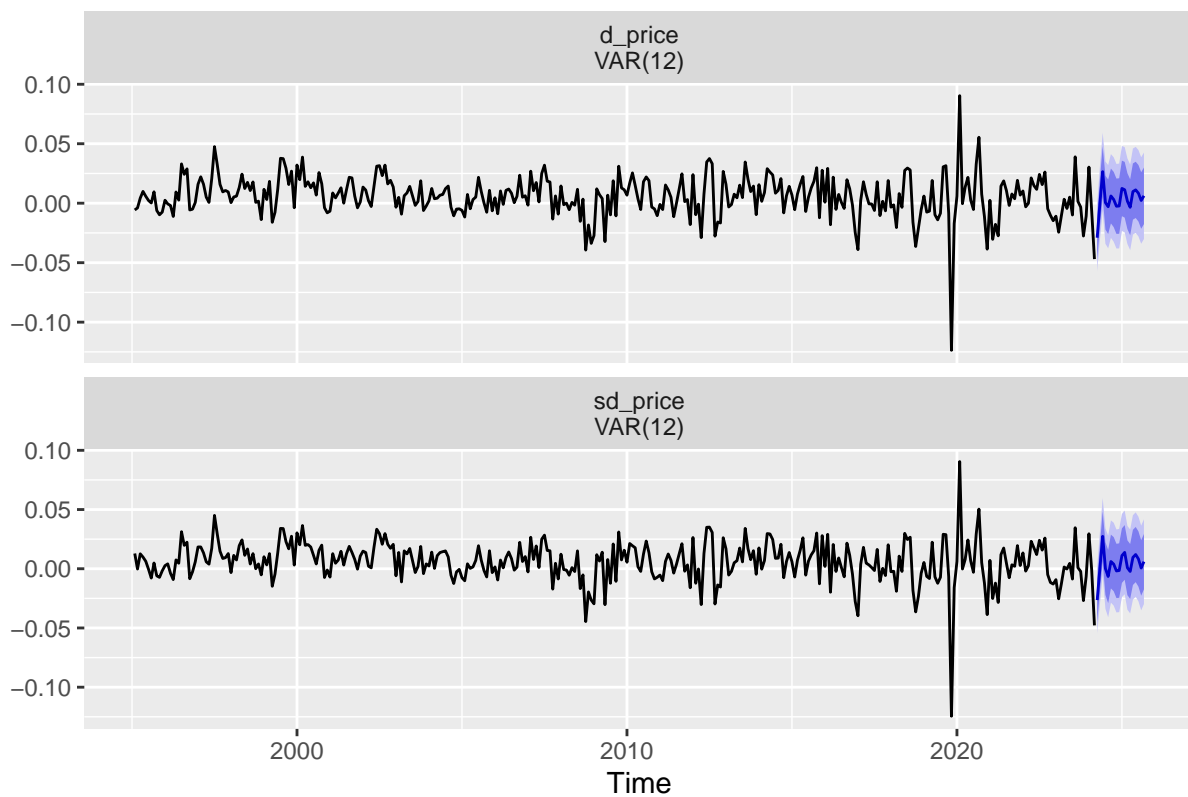
## d_price.l5    -1.136403    0.467328    -2.432 0.015589 *
## sd_price.l5   1.403283    0.456505     3.074 0.002298 **
## d_price.l6    -0.455736    0.481729    -0.946 0.344856
## sd_price.l6   0.058218    0.474222     0.123 0.902372
## d_price.l7     1.019076    0.472643     2.156 0.031836 *
## sd_price.l7   -0.892652    0.465088    -1.919 0.055853 .
## d_price.l8    -0.606030    0.465326    -1.302 0.193745
## sd_price.l8   0.870189    0.453730     1.918 0.056039 .
## d_price.l9     0.100622    0.455285     0.221 0.825229
## sd_price.l9   -0.342908    0.448554    -0.764 0.445160
## d_price.l10    0.802409    0.376249     2.133 0.033731 *
## sd_price.l10  -0.870653    0.374727    -2.323 0.020796 *
## d_price.l11   -0.551282    0.367783    -1.499 0.134899
## sd_price.l11   0.714111    0.363996     1.962 0.050664 .
## d_price.l12    0.047612    0.333021     0.143 0.886406
## sd_price.l12  -0.118837    0.334227    -0.356 0.722411
## const         0.003133    0.001064     2.943 0.003490 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.01426 on 313 degrees of freedom
## Multiple R-Squared:  0.3867, Adjusted R-squared:  0.3397
## F-statistic: 8.223 on 24 and 313 DF, p-value: < 2.2e-16
##
##
## Covariance matrix of residuals:
##           d_price sd_price
## d_price  0.0002056 0.0002017
## sd_price 0.0002017 0.0002032
##
## Correlation matrix of residuals:
##           d_price sd_price
## d_price   1.0000   0.9866
## sd_price  0.9866   1.0000

```

```

forecast_values<-forecast(var_model,h=18)
autoplot(forecast_values)

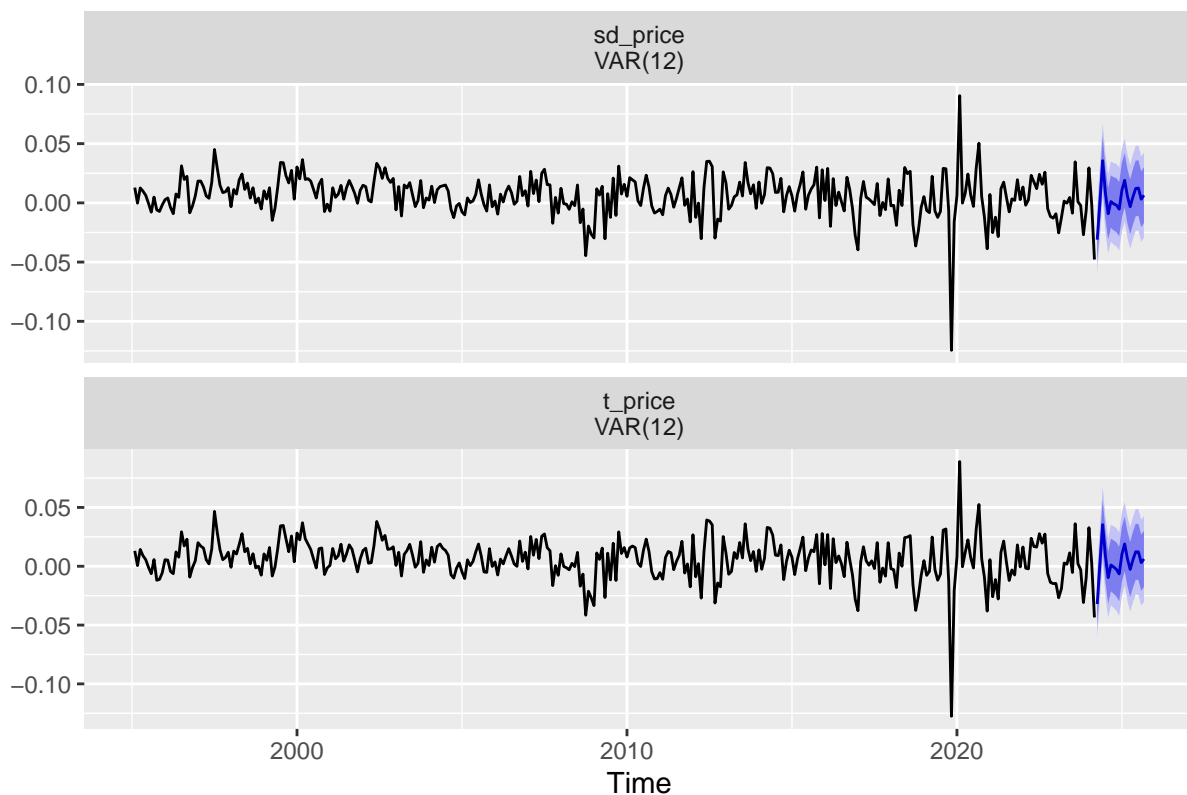
```



```
lagselect2<-VARselect(df.bv2,lag.max=12,type="const")
lagselect2$selection
```

```
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      9      9      6      9
```

```
var_model2<-VAR(df.bv2,p=12,type="const")
forecast_values2<-forecast(var_model2,h=18)
autoplot(forecast_values2)
```



```
summary(var_model2)
```

```
##
## VAR Estimation Results:
## =====
## Endogenous variables: sd_price, t_price
## Deterministic variables: const
## Sample size: 338
## Log Likelihood: 2577.798
## Roots of the characteristic polynomial:
## 0.9082 0.9082 0.8981 0.8981 0.893 0.893 0.8859 0.8859 0.8757 0.8757 0.8699 0.8699 0.8494 0.8494 0.8494
## Call:
## VAR(y = df.bv2, p = 12, type = "const")
##
##
## Estimation results for equation sd_price:
## =====
## sd_price = sd_price.l1 + t_price.l1 + sd_price.l2 + t_price.l2 + sd_price.l3 + t_price.l3 + sd_price
##
##
```

	Estimate	Std. Error	t value	Pr(> t)
sd_price.l1	-0.310446	0.384068	-0.808	0.41953
t_price.l1	0.670630	0.380158	1.764	0.07869 .
sd_price.l2	0.743585	0.404503	1.838	0.06697 .
t_price.l2	-0.571213	0.404373	-1.413	0.15877
sd_price.l3	-0.435950	0.421723	-1.034	0.30206

```

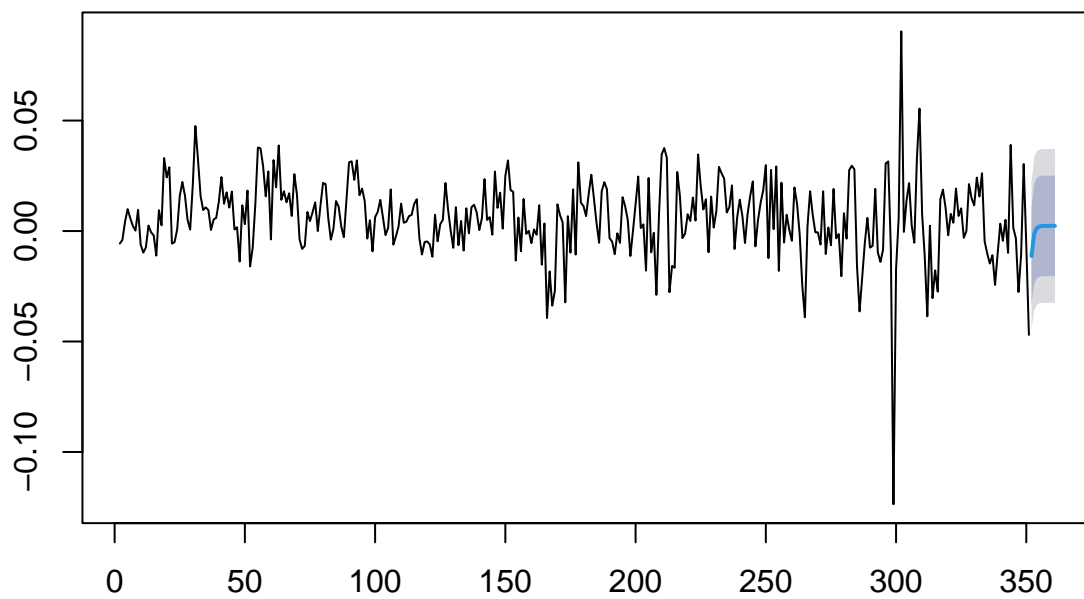
## t_price.l3    -0.107749    0.420163   -0.256    0.79778
## sd_price.l4   -0.759753    0.462507   -1.643    0.10145
## t_price.l4     1.139661    0.462112    2.466    0.01419 *
## sd_price.l5     0.964046    0.465415    2.071    0.03914 *
## t_price.l5    -0.680348    0.468353   -1.453    0.14733
## sd_price.l6     0.100143    0.470439    0.213    0.83157
## t_price.l6    -0.433543    0.471919   -0.919    0.35897
## sd_price.l7     0.284216    0.472514    0.601    0.54794
## t_price.l7    -0.160104    0.473709   -0.338    0.73561
## sd_price.l8     0.617291    0.468962    1.316    0.18904
## t_price.l8    -0.350620    0.471886   -0.743    0.45803
## sd_price.l9     0.079256    0.469821    0.169    0.86615
## t_price.l9    -0.346802    0.471229   -0.736    0.46231
## sd_price.l10    0.201184    0.425700    0.473    0.63683
## t_price.l10   -0.267137    0.426284   -0.627    0.53134
## sd_price.l11   -0.215515    0.407376   -0.529    0.59716
## t_price.l11     0.379612    0.409517    0.927    0.35465
## sd_price.l12   -0.612613    0.388796   -1.576    0.11611
## t_price.l12     0.509163    0.387750    1.313    0.19010
## const          0.003319    0.001078    3.078    0.00227 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.01441 on 313 degrees of freedom
## Multiple R-Squared:  0.3737, Adjusted R-squared:  0.3256
## F-statistic:  7.78 on 24 and 313 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation t_price:
## =====
## t_price = sd_price.l1 + t_price.l1 + sd_price.l2 + t_price.l2 + sd_price.l3 + t_price.l3 + sd_price.l4 + t_price.l4 + sd_price.l5 + t_price.l5 + sd_price.l6 + t_price.l6 + sd_price.l7 + t_price.l7 + sd_price.l8 + t_price.l8 + sd_price.l9 + t_price.l9 + sd_price.l10 + t_price.l10
##
##
##          Estimate Std. Error t value Pr(>|t|)
## sd_price.l1 -0.655224    0.387795  -1.690  0.09210 .
## t_price.l1   1.031096    0.383847   2.686  0.00761 **
## sd_price.l2  0.452458    0.408428   1.108  0.26880
## t_price.l2  -0.296814    0.408297  -0.727  0.46780
## sd_price.l3  0.159110    0.425815   0.374  0.70891
## t_price.l3  -0.706142    0.424241  -1.664  0.09702 .
## sd_price.l4 -0.961400    0.466995  -2.059  0.04035 *
## t_price.l4   1.336452    0.466596   2.864  0.00446 **
## sd_price.l5  0.820032    0.469931   1.745  0.08197 .
## t_price.l5  -0.552127    0.472897  -1.168  0.24388
## sd_price.l6  0.559493    0.475004   1.178  0.23974
## t_price.l6  -0.897823    0.476498  -1.884  0.06046 .
## sd_price.l7  0.144032    0.477099   0.302  0.76294
## t_price.l7  -0.010863    0.478306  -0.023  0.98190
## sd_price.l8  0.436981    0.473513   0.923  0.35680
## t_price.l8  -0.179106    0.476464  -0.376  0.70724
## sd_price.l9  0.389875    0.474380   0.822  0.41178
## t_price.l9  -0.647332    0.475802  -1.361  0.17465
## sd_price.l10 0.175447    0.429831   0.408  0.68342
## t_price.l10 -0.230800    0.430421  -0.536  0.59219

```

```
## sd_price.l11 -0.311868 0.411329 -0.758 0.44890
## t_price.l11 0.471218 0.413491 1.140 0.25532
## sd_price.l12 -0.540040 0.392569 -1.376 0.16991
## t_price.l12 0.437607 0.391513 1.118 0.26454
## const 0.003445 0.001089 3.164 0.00171 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.01455 on 313 degrees of freedom
## Multiple R-Squared: 0.3783, Adjusted R-squared: 0.3306
## F-statistic: 7.936 on 24 and 313 DF, p-value: < 2.2e-16
##
##
## Covariance matrix of residuals:
##      sd_price  t_price
## sd_price 0.0002076 0.0002073
## t_price 0.0002073 0.0002116
##
## Correlation matrix of residuals:
##      sd_price t_price
## sd_price 1.0000 0.9891
## t_price 0.9891 1.0000

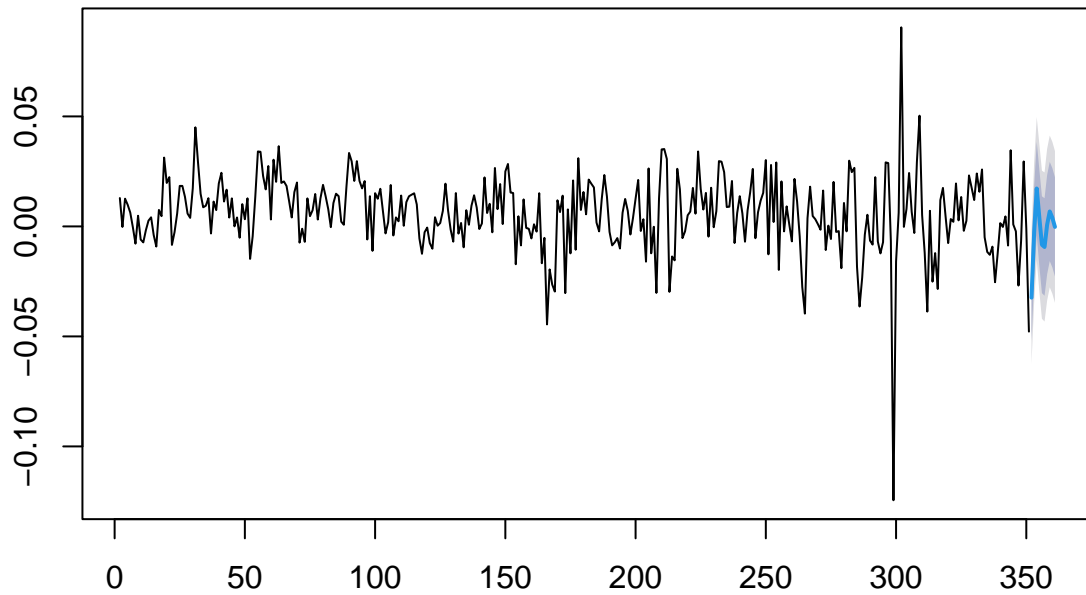
d_price <- diff(ts(log(df$Detached_Average_Price)), start = c(1995, 1), frequency = 12)
sd_price <- diff(ts(log(df$Semi_Detached_Average_Price)), start = c(1995, 1), frequency = 12)
d_arima <- auto.arima(d_price)
plot(forecast(d_arima))
```

Forecasts from ARIMA(1,1,1)

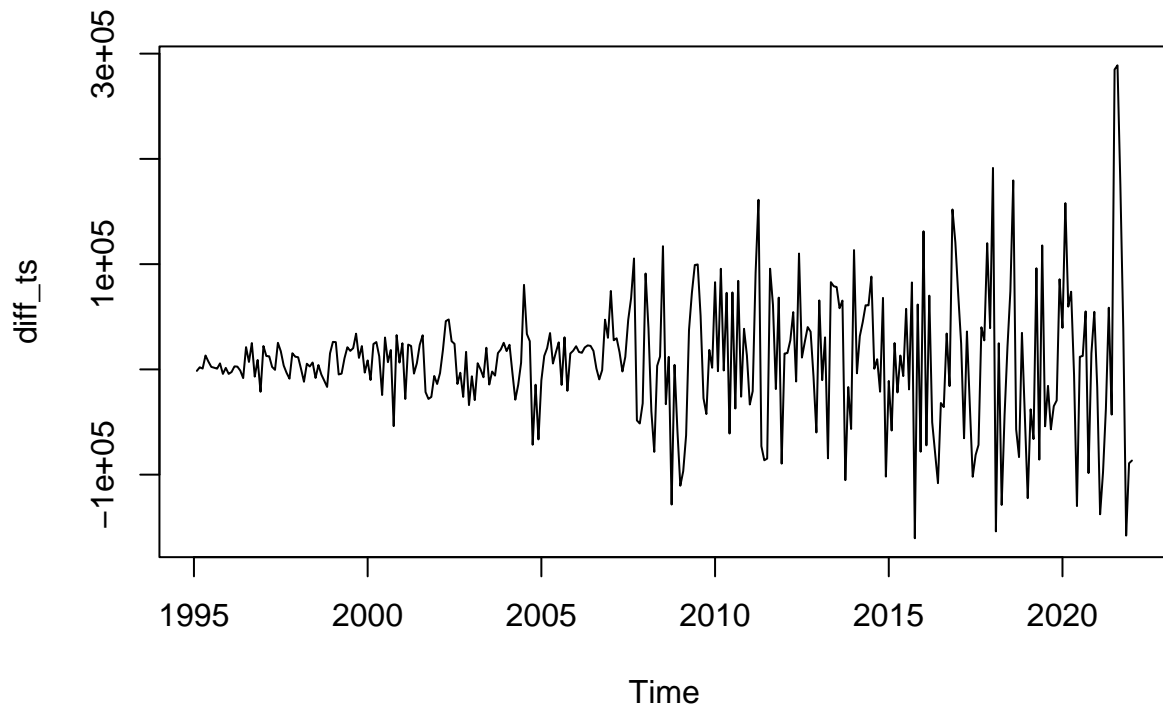


```
sd_arima <- auto.arima(sd_price)
plot(forecast(sd_arima))
```

Forecasts from ARIMA(5,1,2)



```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
df <- read.csv("Updated_KensingtonandChelsea.csv")
df$Date <- as.Date(df$Date, format = "%Y-%m-%d")
ts <- ts(df$Average_Price, start = c(1995, 1), end = c(2022, 1), frequency = 12)
diff_ts <- diff(ts, differences=1)
ts2022 <- ts(df$Average_Price, start = c(1995, 1), end = c(2022, 12), frequency = 12)
diff_ts2022 <- diff(ts2022, differences = 1)
plot(diff_ts)
```

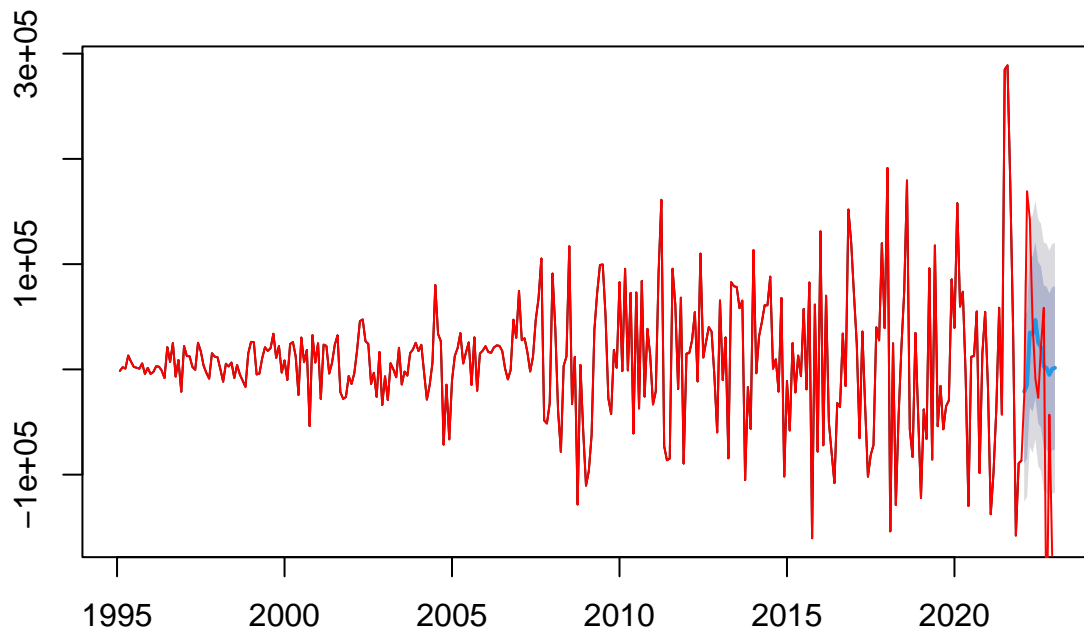



```
library(tseries)
library(forecast)
adf.test(ts)
```

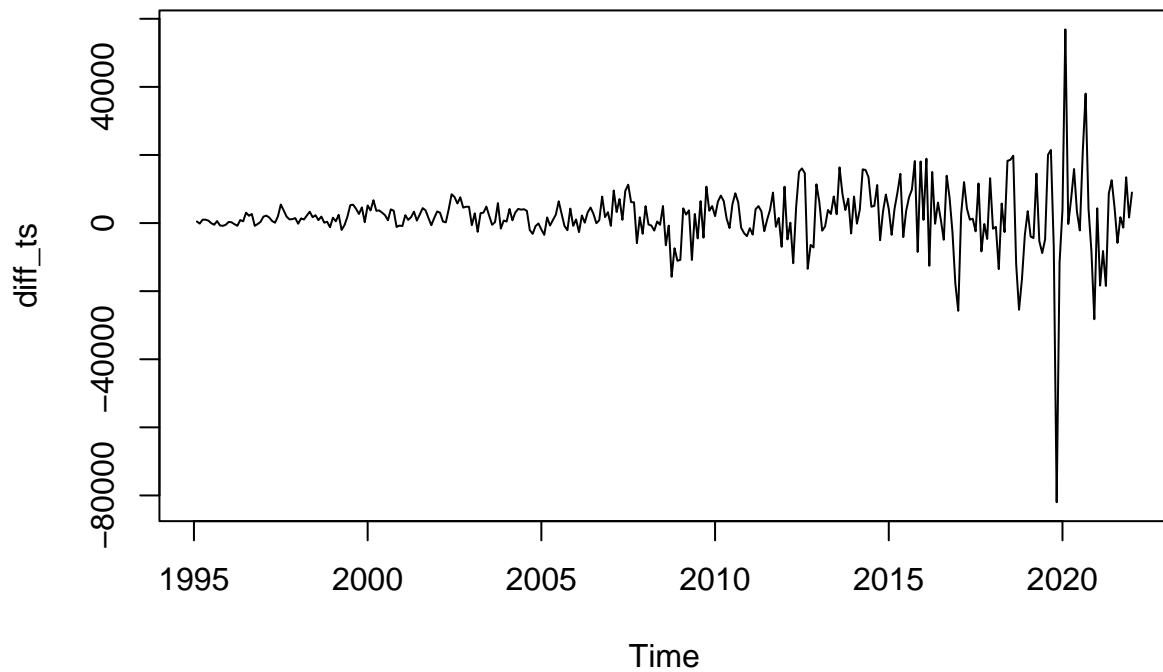
```
##
## Augmented Dickey-Fuller Test
##
## data: ts
## Dickey-Fuller = -2.1431, Lag order = 6, p-value = 0.5162
## alternative hypothesis: stationary
```

```
arima <- auto.arima(diff_ts)
arima_forecast <- forecast(arima, h = 12)
plot(arima_forecast)
lines(diff_ts2022, col = "red")
```

Forecasts from ARIMA(5,0,1) with non-zero mean



```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
df <- read.csv("Updated_Brent.csv")
df$Date <- as.Date(df$Date, format = "%Y-%m-%d")
ts <- ts(df$Average_Price, start = c(1995, 1), end = c(2022, 1), frequency = 12)
diff_ts <- diff(ts, differences=1)
ts2022 <- ts(df$Average_Price, start = c(1995, 1), end = c(2022, 12), frequency = 12)
diff_ts2022 <- diff(ts2022, differences = 1)
plot(diff_ts)
```

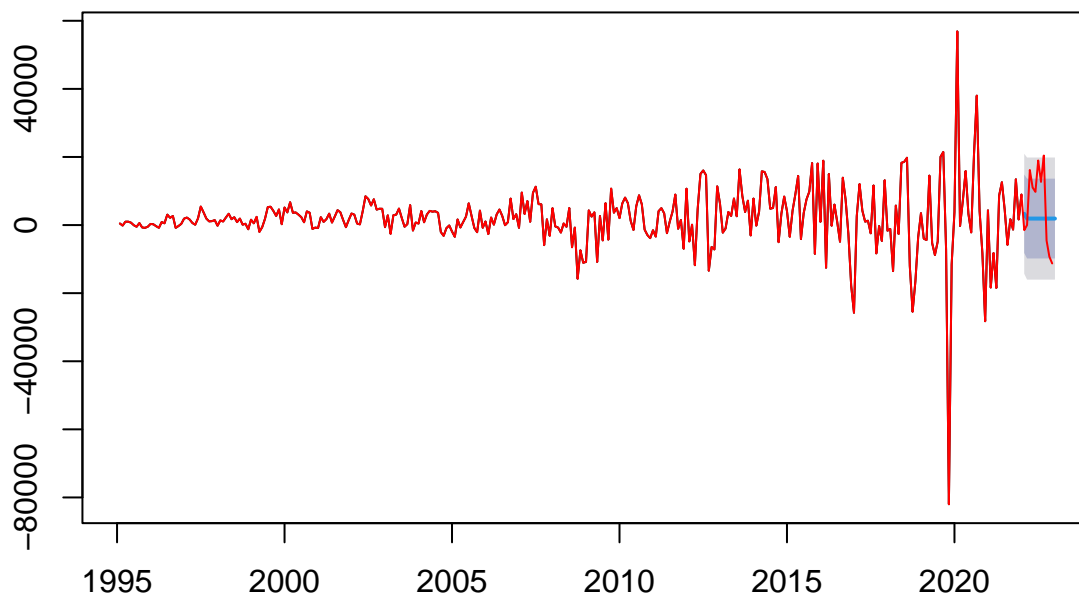


```
library(tseries)
library(forecast)
adf.test(ts)
```

```
##
## Augmented Dickey-Fuller Test
##
## data: ts
## Dickey-Fuller = -2.0401, Lag order = 6, p-value = 0.5596
## alternative hypothesis: stationary
```

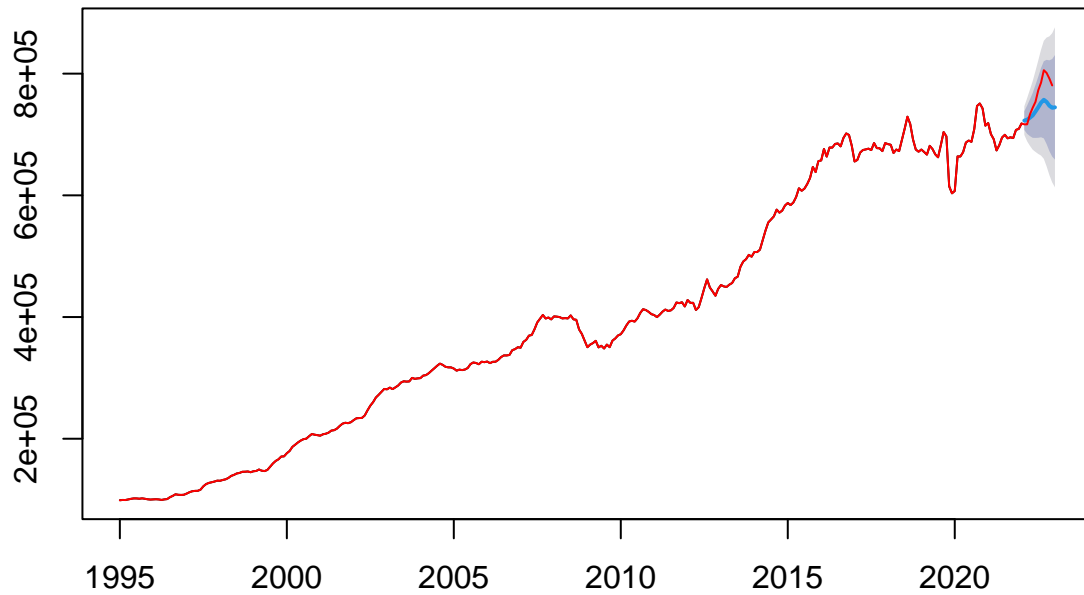
```
arima <- auto.arima(diff_ts)
plot(forecast(arima, h = 12))
lines(diff_ts2022, col = "red")
```

Forecasts from ARIMA(0,0,1) with non-zero mean

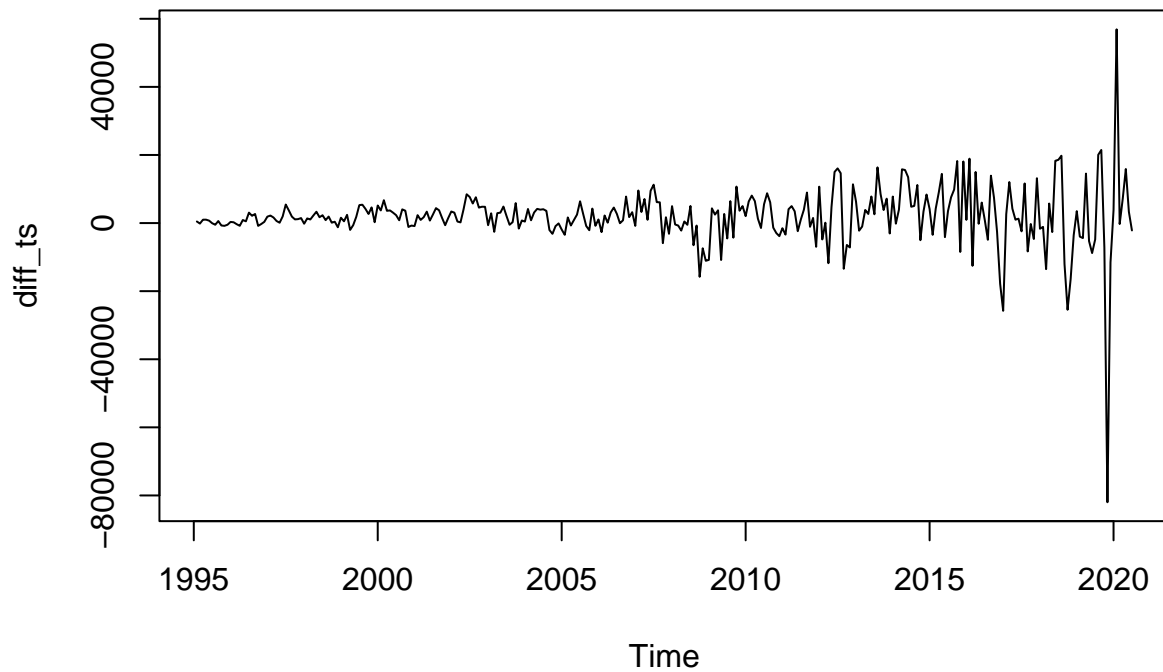


```
ets <- ets(ts)
ets_forecast <- forecast(ets, h = 12)
plot(ets_forecast)
lines(ts2022, col = "red")
```

Forecasts from ETS(M,Ad,M)



```
library(tseries)
library(forecast)
library(vars)
library(readr)
library(Metrics)
df <- read.csv("Updated_Brent.csv")
df$Date <- as.Date(df$Date, format = "%Y-%m-%d")
ts <- ts(df$Average_Price, start = c(1995, 1), end = c(2020, 7), frequency = 12)
diff_ts <- diff(ts, differences=1)
ts2020 <- ts(df$Average_Price, start = c(1995, 1), end = c(2020, 12), frequency = 12)
diff_ts2020 <- diff(ts2020, differences = 1)
plot(diff_ts)
```

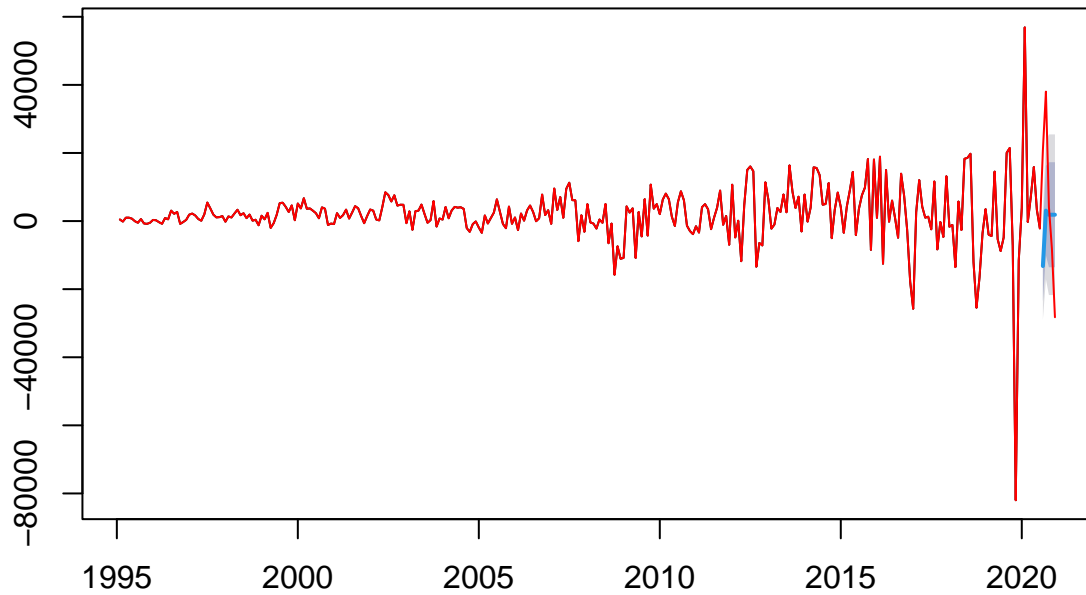


```
library(tseries)
library(forecast)
adf.test(ts)
```

```
##
## Augmented Dickey-Fuller Test
##
## data: ts
## Dickey-Fuller = -1.6042, Lag order = 6, p-value = 0.7432
## alternative hypothesis: stationary
```

```
arima <- auto.arima(diff_ts)
plot(forecast(arima, h = 5))
lines(diff_ts2020, col = "red")
```

Forecasts from ARIMA(0,0,2) with non-zero mean



```
ets <- ets(ts)
ets_forecast <- forecast(ets, h = 5)
plot(ets_forecast)
lines(ts2020, col = "red")
```

Forecasts from ETS(M,Ad,M)

