

Eg 4

Verlet:

$$x(t+\Delta t) = x(t) + v(t)\Delta t + \frac{1}{2}a(t)\Delta t^2$$

$$v(t+\Delta t) = v(t) + \frac{1}{2}(a(t) + a(t+\Delta t))\Delta t$$

0

$$x_{n+1} = x_n + v_n h + \frac{1}{2} a_n(t) h^2$$

$$v_{n+1} = v_n + \frac{1}{2}(a_n + a_{n+1})h$$

$$J = \frac{\partial x_{n+1}}{\partial x_n} \frac{\partial v_{n+1}}{\partial v_n} - \frac{\partial x_{n+1}}{\partial v_n} \frac{\partial v_{n+1}}{\partial x_n} = 1$$

$$J = (1)(1) - (h)(0) = 1 \quad \checkmark$$