

Big-O Notation Practice

This is an ungraded class activity and you may not have time to answer all of the questions. You have until approximately 2:35-2:40 to work on this.

Review of limits - evaluate the following:

$$\lim_{n \rightarrow \infty} \frac{n^{10} - 1000n^4 + 12}{3n^{10} - n^9}$$

$$\lim_{n \rightarrow \infty} \frac{1}{e^n}$$

$$\lim_{n \rightarrow \infty} \frac{n!}{n^n}$$

$$\lim_{n \rightarrow \infty} \frac{n^4 + n^3 - 36}{n + 8}$$

Instructions: Answer the remainder of the questions on this worksheet **twice** - once using the limit definition of big-O notation, and once using the inequality definition.

An algorithm takes $f(n) = n^7 + 12$ operations to execute. How should you describe this run-time using big-O notation? Prove that your answer is correct using each definition.

Prove that the function from the last question is $O(8n^{11})$. Even though this fits the definition of big-O, what is wrong with using $8n^{11}$ to describe the run-time of your algorithm?

Prove that the function f is not $O(n + \sqrt{n})$.