Job Leon Feldbrugge

Univeristy of Edinburgh Higgs Centre for Theoretical Physics James Clerk Maxwell Building Peter Guthrie Tait Road Edinburgh, EH9 3FD, Scotland Job.Feldbrugge@ed.ac.uk jfeldbrugge.github.io

Referees

Prof. Neil Turok, University of Edinburgh, Edinburgh, Scotland and Perimeter Institute for Theoretical Physics, Waterloo, Canada (neil.turok@ed.ac.uk)

Prof. Ue-Li Pen, Academia Sinica, Taipei, Taiwan and Canadian Institute for Theoretical Astrophysics, Toronto, Canada (pen@cita.utoronto.ca)

Prof. Rien van de Weygaert, University of Groningen, Groningen, The Netherlands (weygaert@astro.rug.nl)

Academic positions

HIGGS FELLOW at the Higgs Centre for Theoretical Physics at the University of Edinburgh (Scotland)
POSTDOC at the Perimeter Institute (Canada) and the Department of Physics, Carnegie Mellon University
(United States)

Education

July 2015

July 2010

August 2011

	Education
2015 - 2019	РнD Physics, Perimeter Institute, University of Waterloo
	Advisor: Neil Turok
	Thesis: Path integrals in the sky: Classical and quantum problems with minimal assumptions
	Defence date: October 17, 2019
2014 - 2015	MASTER Part III Mathematics (with distinction), University of Cambridge
	Committee: Paul Shellard and Tommaso Giannantonio
	Thesis: Primordial non-Gaussianity and large-scale structure
2012 - 2014	MASTER Physics (cum laude), van Swinderen Institute, University of Groningen
2012 - 2014	MASTER Astronomy (cum laude), Kapteyn Institute, University of Groningen
2012 - 2014	MASTER Mathematics (cum laude), Bernoulli Institute, University of Groningen
	Committee: Rien van de Weygaert (cosmology and large-scale structure formation)
	Diederik Roest (string cosmology)
	Aernout van Enter (statistical mechanics)
	Thesis: Statistics of caustics in large-scale structure formation
2009 - 2012	BACHELOR Physics (cum laude), van Swinderen Institute, University of Groningen
2009 - 2012	BACHELOR Astronomy (cum laude), Kapteyn Institute, University of Groningen
2009 - 2012	BACHELOR Mathematics (cum laude), Bernoulli Institute, University of Groningen
	Committee: Rien van de Weygaert (cosmology and large-scale structure formation)
	Elisabetta Pallante (quantum field theory)
	Gert Vegter (computational geometry)
	Thesis: Analysis of Betti numbers and persistence diagrams of 2D Gaussian random fields
July 2016	SUMMER SCHOOL It from qubit summer school, Perimeter Institute, Canada (two weeks)
July 2015	SUMMER SCHOOL Prospects in theoretical physics: new insights into quantum matter, Institute for Ad-
	vanced Studies, Princeton (one week)

SUMMER SCHOOL Princeton summer school on condensed matter physics (one week)

SUMMER SCHOOL Dealing with environmental heritage, Bath, United Kingdom (two weeks)

SUMMER SCHOOL University of Cambridge international summer school in science (two weeks)

Awards

April 2020 Canadian Association of Physicists' Division of Theoretical Physics (DTP) and Winnipeg Institute for

Theoretical Physics (WITP) P.R. Wallace PhD Thesis Prize

Best PhD thesis in Theoretical Physics from a Canadian university (2020).

November 2014 De Zeeuw-Van Dishoeck award 2014

Best master thesis in Astronomy from a Dutch university (2014).

July 2014 GUF-100 prize 2014

Best student in the Faculty of Mathematics and Natural Sciences at the University of Groningen (2014).

November 2011 Silver medal in the university physics competition 2011

A university competition in which groups of three physics students all over the world solve a problem

and write an article in 48 hours.

September 2010 Young Talent encouragement prize 2010 in Physics

Prize awarded by the Koninklijke Hollandse Maatschappij der Wetenschappen (Royal Holland Society of Sciences and Humanities) for the best freshman Physics student at the University of Groningen in

2009-2010.

November 2007 Third place in the CanSat competition

The CanSat project is an annual competition organized by the Delft University of Technology. Teams of

secondary school students design and build a satellite in a Coca-Cola can.

Scholarships

University of Waterloo scholarship, for PhD at the Perimeter Institute

July 2014

Hendrik Muller fund 2014: Scholarship for excelling Dutch students

VSB fund 2014: Scholarship for Dutch students studying in abroad

Research Visits

May 2023 Research visit to Beatrice Bonga, Radboud University, Nijmegen, The Netherlands

March 2023 Research visit to Ue-Li Pen, Academia Sinica Institute of Astronomy and Astrophysics, Taipei, Taiwan

March 2023 Research visit to Beatrice Bonga, Radboud University, Nijmegen, The Netherlands

January 2023 Research visit to Beatrice Bonga, Radboud University, Nijmegen, The Netherlands

June 2022 Research visit to Rien van de Weygaert, Kapteyn Institute, Groningen, The Netherlands

Research visit to Beatrice Bonga, Radboud University, Nijmegen, The Netherlands

June 2019 Research visit to Rien van de Weygaert, Kapteyn Institute, Groningen, The Netherlands

October 2018 Research visit to Rien van de Weygaert, Kapteyn Institute, Groningen, The Netherlands

May 2018 Research visit to Jean-Luc Lehners, Albert Einstein Institute, Potsdam, Germany

Feb - Apr 2017 Research visit to DAMTP, University of Cambridge, United Kingdom

March 2017 Research visit to Jean-Luc Lehners, Albert Einstein Institute, Potsdam, Germany

Publications & talks

JOURNAL ARTICLES

2023

2023

2023

2023

J. Feldbrugge, D. L. Jow, U.-L. Pen, "Crossing singularities in the saddle point approximation", *Physical Review Letters* (2023, submitted). arXiv:2309.12427 [quant-ph]

J. Feldbrugge, D. L. Jow, U.-L. Pen, "Complex classical paths in quantum reflections and tunneling", *Physical Review D* (2023, R&R). arXiv:2309.12420 [quant-ph]

J. Feldbrugge, N.M.D. Niezink, "Orthogonality relations for conical functions of imaginary order", *Integral Transforms and Special Functions* (2023, submitted). arXiv:2309.05616 [math]

J. Feldbrugge, "Complex evaluation of angular power spectra: Going beyond the Limber approximation", *Physical Review D* (2023) nr. 108, 103007. arXiv:2304.13064 [astro-ph.C0]

J. Feldbrugge, Y. Yan, and R. van de Weygaert, "Statistics of tidal and deformation eigenvalue fields in the primordial Gaussian matter distribution: the two-dimensional case", *Monthly Notices of the Royal Astronomical Society* (2023). arXiv:2301.07200 [astro-ph.CO]

J. Feldbrugge, and R. van de Weygaert, "Cosmic web & caustic skeleton: non-linear constrained realizations - 2D case studies", *Journal of Cosmology and Astroparticle Physics* (2013) no.2, 58. arXiv:2212.07840 [astro-ph.CO]

- J. Feldbrugge, U.-L. Pen, and N. Turok, "Oscillatory path integrals for radio astronomy," *Annals of Physics* (2023) no.451, 169255. arXiv:1909.04632 [astro-ph.HE]
- J. Feldbrugge, "Multi-plane lensing in wave optics," Monthly Notices of the Royal Astronomical Society (2023) nr.250, 2995-3006. arXiv:2010.03089 [astro-ph.CO]
- J. Feldbrugge, and N. Turok, "Existence of real time quantum path integrals", *Annals of Physics* (2023) arXiv:2207.12798 [hep-th]
 - D. Jow, U.-L. Pen, and **J. Feldbrugge**, "Regimes in astrophysical lensing: refractive optics, diffractive optics, and the Fresnel scale", *Monthly Notices of the Royal Astronomical Society* (2022). arXiv:2204.12004 [astro-ph.CO]
 - G. Wilding, K. Nevenzeel, R. van de Weygaert, G. Vegter, P. Pranav, B.J.T. Jones, K. Efstathiou, and **J. Feldbrugge**, "Persistent homology of the cosmic web. I: Hierarchical topology in ΛCDM cosmologies" *Monthly Notices of the Royal Astronomical Society* (2020) nr.507, 2968-2990. arXiv:2011.12851 [astro-ph.C0]
 - J. Feldbrugge, and N. Turok, "Gravitational lensing of binary systems in wave optics," *Physical Review Letters* (2020, R&R). arXiv:2008.01154 [gr-qc]
 - **J. Feldbrugge**, M. van Engelen, R. van de Weygaert, P. Pranav, and G. Vegter, "Stochastic homology of Gaussian vs. non-Gaussian random fields: Graphs towards Betti numbers and persistence diagrams, *Journal of Cosmology and Astroparticle Physics* (2019) no.9, 52–100. arXiv:1908.01619 [astro-ph.CO]
 - A. Di Tucci, **J. Feldbrugge**, J.-L. Lehners, N. Turok, "Quantum incompleteness of inflation," *Physical Review D*, 100 (2019) no.6, 63517. arXiv:1906.09007 [hep-th]
 - P. Pranav, R. van de Weygaert, G. Vegter, B.J.T. Jones, R.J. Adler, **J. Feldbrugge**, C. Park, T. Buchert, and M. Kerber, "Topology and geometry of Gaussian random fields I: on Betti numbers, Euler characteristic, and Minkowski functionals" *Monthly Notices of the Royal Astronomical Society*, *485* (2019) no.3, 4167–4208. arXiv:1812.07310 [astro-ph.C0]
 - **J. Feldbrugge**, J.-L. Lehners, and N. Turok, "Inconsistencies of the new no-boundary proposal," *Universe*, 4 (2018), no.10, 100–115. arXiv:1805.01609 [hep-th]
 - **J. Feldbrugge**, R. van de Weygaert, J. Hidding, and J. Feldbrugge, "Caustic skeleton & cosmic web," *Journal of Cosmology and Astroparticle Physics* (2018) no.05, 27–81. arXiv:1703.09598 [astro-ph.CO]
 - **J. Feldbrugge**, J. Lehners, and N. Turok, "No rescue for the no boundary proposal: Pointers to the future of quantum cosmology," *Physical Review D*, 97 (2018), no.2, 23509 arXiv:1708.05104 [hep-th]
 - **J. Feldbrugge**, J.-L. Lehners, and N. Turok, "No smooth beginning for spacetime," *Physical Review Letters*, 119 (2017), no.17, 171301. arXiv:1705.00192 [hep-th]
 - **J. Feldbrugge**, J.L. Lehners, and N. Turok, "Lorentzian quantum cosmology," *Physical Review D*, 95 (2017), no.10, 103508. arXiv:1703.02076 [hep-th]
 - **J. Feldbrugge**, J. Hidding, and R. van de Weygaert "Statistics of caustics in large-scale structure formation," *The Zeldovich Universe: Genesis and Growth of the Cosmic Web, Proceedings of the International Astronomical Union, IAU Symposium*, 308 (2016), 107–114. arXiv:1412.5121 [astro-ph.C0]
 - R. van de Weygaert, G. Vegter, H. Edelsbrunner, B.J.T. Jones, P. Pranav, C. Park, W. Hellwing, B. Eldering, N. Kruithof, E.G.P. Bos, J. Hidding, **J. Feldbrugge**, E. ten Have, M. van Engelen, M. Caroli, and M. Teillaud, "Alpha, Betti and the megaparsec universe: On the topology of the cosmic web," *Transactions on Computational Science XIV: Special Issue on Voronoi Diagrams and Delaunay Triangulation. Lecture Notes in Computer Science, Vol. 6970. Springer Berlin Heidelberg* (2013). arXiv:1306.3640 [astro-ph.CO]

THESES

2022

2021

2019

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2019

2015

2014

2012

- **J. Feldbrugge**, "Path integrals in the sky: classical and quantum problems with minimal assumptions," PhD thesis, Perimeter Institute, University of Waterloo, supervised by N. Turok. Available online.
 - **J. Feldbrugge**, "Primordial non-Gaussianity and large-scale structure," Part III Essay, University of Cambridge, supervised by P. Shellard and T. Giannantonio. Available online.
 - **J. Feldbrugge**, "Statistics of caustics in large-scale structure formation," Master thesis, University of Groningen, supervised by R. van de Weygaert, D. Roest, A.E. van Enter. Available online.
 - **J. Feldbrugge** and M. van Engelen, "Analysis of Betti numbers and persistence diagrams of two-dimensional Gaussian random fields," Bachelor thesis, University of Groningen, supervised by R. van de Weygaert, E. Pallante, G. Vegter. Available online.

INVITED TALKS

December 2023 Gauge-Gravity by the ghats' seminar, Center for High Energy Physics (CHEP), Indian Institute of Science, India.

Presentation: Complex classical paths in quantum reflections and tunnelling

December 2023 Large-scale parity violation, Academia Sinica, Institute of Astronomy and Astrophysics, Taipei, Taiwan,

Presentation: Dissecting the cosmic web with caustics

October 2023 International Loop Quantum Gravity Seminar

Presentation: Complex saddle points in gravitational path integrals

September 2023 Complexity and Cosmos, Gran Sasso Science Institute, L'Aquila, Italy

Presentation: On the existence of real-time path integrals

July 2023 Quantum Gravity 2023, Radboud University, Nijmegen, The Netherlands

Presentation: On the existence of real-time path integrals

July 2023 Theoretical physics group, University of New Brunswick, New Brunswick, Canada

Presentation: On the existence of real-time path integrals

March 2023 Optimal Transport Theory and Applications to Physics, Ecole Physique, Les Houches, France

Presentation: Dissecting the cosmic web with caustics

September 2022 2nd Roman Juskiewicz Symposium, Nicolaus Copernicus Astronomical Center, Warsaw, Poland

Presentation: Dissecting the cosmic web with caustics

June 2022 Information Universe 4, University of Groningen, Groningen, The Netherlands

Presentation: Dissecting the cosmic web with caustics Cosmology seminar, Oxford University, Oxford, England

Presentation: Dissecting the cosmic web with caustics

May 2022 UK Cosmo Meeting 2022, Newcastle University, Newcastle, England

Presentation (keynote): Dissecting the cosmic web with caustics

October 2021 Higgs hour, University of Edinburgh, Edinburgh, Scotland

Presentation: Interference, caustics and oscillatory integrals

May 2021 Seminar Universidad Nacional Autonoma de Mexico, Mexico city

Presentation: Interference phenomena in lensing and quantum physics

May 2021 Sirius A symposium 2021: To infinity and beyond

Presentation: The caustic skeleton of the cosmic web

October 2020 Quantum & Gravity Seminar, Radboud Universiteit, Nijmegen, The Netherlands

 $Presentation: Lorentzian \ quantum \ cosmology$

October 2020 Pusar group meeting, CITA, Toronto, Canada

Presentation: Multi-plane lensing and gravitational binary lensing in wave optics

November 2019 Scintillometry 2019, Max Planck Institute for Radio Astronomy, Bonn, Germany

Presentation: Oscillatory path integrals for radio astronomy

June 2018 Rotman summer institute in philosophy of cosmology, Godrich, Canada

Presentation: Lorentzian quantum cosmology (two lectures)

September 2016 CITA-PI day: Gravitational non-linear instability, CITA, Toronto, Canada

Presentation: Shocks in the early universe and gravitational waves

CONTRIBUTED TALKS

February 2023 The Co-evolution of the Cosmic Web and Galaxies across Cosmic Time, Kavli Institute for Theoretical

Physics, UC Santa Barbara, California, United States Presentation: Dissecting the cosmic web with caustics

July 2022 Cosmology from Home

Presentation: Dissecting the cosmic web with caustics

March 2022 Cosmic Cartography 2022: Exploring the Cosmic Web and Large-Scale Structure, Kavli IPMU, Kashiwa,

Japan

May 2022

Presentation: The caustic web and non-linear constrained Gaussian random fields

October 2021 Tuorla-Tartu meeting 2021, University of Turku, Turku, Finland

Presentation: Caustic skeleton of the cosmic web

September 2020 Cosmology from home 2020, virtual conference on all aspects of cosmology.

Presentation: The caustic skeleton of the cosmic web

March 2020 Topological statistics group meeting. Department of statistics at Carnegie Mellon University, Pittsburgh,

United States

Two presentations: Cosmology and topology I, and Cosmology and topology II

February 2020 The centre for the universe Waterloo Centre for Astrophysics day, Waterloo, Canada

Presentation: Path integrals for radioastronomy and gravitational lensing II

February 2020 Cosmology group meeting, Perimeter Institute, Waterloo, Canada

Presentation: The caustic skeleton of the cosmic web

January 2019 The cosmic web in the local universe, Lorentz center, Leiden, The Netherlands

Presentation: The caustics skeleton of the cosmic web

October 2019 The Future of Astronomy, Waterloo Centre for Astrophysics, Waterloo, Canada

Poster: Oscillatory path integrals for radio astronomy

September 2019 Theory group meeting, Carnegie Mellon University, Pittsburgh, United States

Presentation: Interference and Picard-Lefschetz theory

September 2019 Simplicity III, Perimeter Institute, Waterloo, Canada

Presentation: Fun with path integrals II

August 2019 Graduate student meeting, Perimeter Institute, Waterloo, Canada

Presentation: Oscillatory integrals in the complex plane

June 2019 Probabilities in cosmology, University of Groningen, The Netherlands

Presentation: Lorentzian beginnings of the universe

June 2019 The cosmic web: from galaxies to cosmology, Edinburgh, United Kingdom

Presentation: Caustic skeleton of the cosmic web

May 2019 Cosmology group meeting Perimeter Institute, Waterloo, Canada

Presentation: lenses and oscillatory integrals

May 2018 Albert Einstein Institute group meeting, Potsdam, Germany

Presentation: Classical and weak trajectories

November 2017 Path integral of gravity, Perimeter Institute, Waterloo, Canada

Presentation: Quantum incompleteness of inflation II

September 2017 Cosmology group meeting CITA, Canada

Presentation: The instability of the no-boundary proposal

July 2017 Cosmic web day, University of Toronto, Toronto, Canada

Presentation: The caustic skeleton of the cosmic web

May 2017 PI-day, Perimeter Institute, Waterloo, Canada

Presentation: Lorentzian quantum cosmology

May 2017 Theory Canada 12, York University, Toronto, Canada

Presentation: Lorentzian quantum cosmology

May 2017 Cosmology group meeting Perimeter Institute, Waterloo, Canada

Presentation: Caustics in large-scale structure

May 2017 String cosmology group meeting Van Swinderen Institute, Groningen, Netherlands

Presentation: Lorentzian quantum cosmology

April 2017 New Thoughts 3: About the universe and more, Ely, United Kingdom

Presentation: Lorentzian quantum cosmology

April 2017 British gravity meeting 2017, University of Oxford, Oxford, United Kingdom

Presentation: Lorentzian quantum cosmology

June 2016 Cosmology group meeting CITA, Canada

Presentation: Statistics of caustics in large-scale structure

May 2016 Cosmology group meeting Perimeter Institute, Canada

Presentation: Statistics of caustics in large-scale structure

March 2016 Statistics of extrema of large-scale structure, Lorentz center, Leiden, The Netherlands

Presentation: Statistics of caustics in large-scale structure

June 2014 IAUS 308: The Zel'dovich universe, Tallinn, Estonia

Presentation: Statistics of caustics in large-scale structure formation

October 2012 Structure of the cosmic web, Leibniz institute astrophysics, Potsdam, Germany

Presentation: Analysis of Betti numbers and persistence diagrams in 2D GRFs

CONFERENCES AND WORKSHOPS (ATTENDED ONLY)

January 2023 New Directions in Theoretical Physics 4, University of Edinburgh, Edinburgh, Scotland

June 2022 Analogue Models of Gravity and Fluctuation-Induced phenomena, University of Edinburgh, Edinburgh,

Scotland

June 2022 Online Workshop "Physics of the Early Universe"

January 2021 Cosmology 2021: the rise of field theory, University of Cambridge, Cambridge, The United Kingdom

October 2020 The information universe: What is the role of information in our Universe? University of Groningen,

Groningen, The Netherlands

January 2020 First Dutch Mathematical Relativity Day, Radboud University Nijmegen, Nijmegen, The Netherlands

September 2019 Cosmological frontiers in fundamental physics 2019, Perimeter Institute, Waterloo, Canada

November 2018 Quantum universe, in celebration of Neil Turok's 60th birthday, Centro de Estudio Cientificos (CECs),

Valdivia, Chile

August 2018 Cosmology and gravitational physics with lambda, Nordita, Stockholm, Sweden

June 2018	Scanning new horizons: Emergent space-time, black holes and quantum information, Van Swinderen
	Institute, Groningen, The Netherlands
January 2018	Gravity in the early universe, Princeton University, Princeton, United States
June 2017	Bounce scenarios in cosmology, Perimeter Institute, Waterloo, Canada
January 2017	Fundamentals of the universe, Van Swinderen Institute, Groningen, The Netherlands
January 2017	New directions in theoretical physics II, Higgs center for theoretical physics, Edinburgh, United Kingdom
October 2016	Midwest relativity meeting, Perimeter Institute, Waterloo, Canada
June 2016	Time in cosmology, Perimeter Institute, Canada
June 2016	Concepts and paradoxes in a quantum universe, Perimeter Institute, Canada
June 2016	Cosmological frontiers in fundamental physics 2016, Perimeter Institute, Canada
June 2015	Convergence, Perimeter Institute, Canada
	Quantum universe 4, University of Groningen, The Netherlands
April 2014	Quantum universe 4, University of Groningen, The Netherlands Quantum universe 3, University of Groningen, The Netherlands
March 2013	Qualitum universe 3, Oniversity of Gronnigen, the Netherlands
	Advising
2023 - present	Advisor PhD project, Benjamin Hertzsch, University of Edinburgh, Edinburgh, United Kingdom: Prob -
	ing cosmological redshift surveys with the caustic skeleton
2023	Advisor master project, Vera Li, University of Edinburgh, Edinburgh, United Kingdom: The caustic
,	skeleton and redshift space distortions
2023 - present	Co-advisor PhD project, Ariadna Metidieri, Radboud University, Nijmegen, The Netherlands: Lensing of
2025 present	rotating stars and photons in wave optics
2022 - present	Advisor master project, Joshua Jones, University of Cambridge, United Kingdom: Monte Carlo integra
2022 - present	tion of oscillatory integrals
	Co-advisor bachelor project, Yonatan Sklansky, University of Pennsylvania, United States: Topology of
2022 - 2023	multi-stream regions in N -body simulations
2022 - 2023	Advisor master project, Yihan Yan, University of Waterloo, Canada: Statistics of critical points in
	eigenvalue fields
2020 - 2022	Co-advisor PhD project, Georg Wilding, University of Groningen, The Netherlands: Topology of the
	two-dimensional cosmic web
2021 - 2022	Advisor bachelor project, Yihan Yan, Waterloo University, Canada: Homology of two- and three-
	dimensional Gaussian random fields
2020 - 2021	Co-advisor PhD project, Varun Rustagi, University of Groningen, The Netherlands: The caustic skele-
	ton of the local universe
2018 - 2022	Co-supervisor master project Kevin Bixerman, University of Groningen, The Netherlands: The caustic
	skeleton of the local universe
	Teaching
	School on Fundamentale of the Universe Lements Contan Leiden The Niele of the Universe Lements
June 2023	School on Fundamentals of the Universe, Lorentz Center, Leiden, The Netherlands
June 2018	2018 Rotman summer institute in philosophy of cosmology, Godrich, Canada
	Two lectures on Lorentzian quantum cosmology
January 2018	PSI winter school, co-supervisor project 'Pair creation in de Sitter spacetime', Huntsville, Canada
2010 - 2015	Physics lecturer, exam training for secondary school students, UOCG Market BV
2013 - 2014	Developer of teaching material for exam training in physics, UOCG Market BV
2008 - 2014	Tutoring in mathematics and physics for secondary school students
	Service
2022	Co-organizer of the conference New Directions in Theoretical Physics 4 at the University of Edinburgh
2018 - present	Reviewer for Physical Review Letters (PRL), Physical Review D (PRD), the Journal of Cosmology and
F	Astroparticle Physics (JCAP), the Journal of High Energy Physics (JHEP), and Universe.
2012 - 2014	Chairman of the professor Hendrik de Waard foundation
2013 - 2014	Treasurer of the professor Hendrik de Waard foundation
2012 - 2013	Member of the education committee mathematics, chairman of the student council
2011 - 2012	Guide at the Gratama telescope of the Blaauw observatory, Groningen, at stargazing events
2010 - 2014	outue at the oratalia telescope of the blaatiw observatory, oronnigen, at stargazing events

Languages

DutchMother tongueEnglishFluentGermanElementaryFrenchElementary

Latin Elementary

Programming experience

MathematicaFluent C++ Fluent Python Moderate Matlab ModerateSwift Moderate Julia Elementary Fortran Elementary R Elementary