

Methods for modeling variability among-animals in habitat-selection studies

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BIOLOGGING

Journal of Animal Ecology



Accounting for individual-specific variation in habitat-selection studies: Efficient estimation of mixed-effects models using Bayesian or frequentist computation

Stefanie Muff^{1,2} | Johannes Signer³ | John Fieberg⁴

Outline

- ▶ Motivation for studying variability among-animals
- ▶ Methods for modeling variability among-animals
 - ▶ 2-step methods
 - ▶ Mixed-effects models



Causes and consequences of among-animal variability

Methods for modeling among-animal variability

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015

Sex-specific adjustments in habitat selection contribute to buffer mouflon against summer conditions FREE

Pascal Marchand, Mathieu Garel, Gilles Bourgoïn, Dominique Dubray, Daniel Maillard, Anne Loison [Author Notes](#)

Behavioral Ecology, Volume 26, Issue 2, 1 March 2015, Pages 472–482,
<https://doi.org/10.1093/beheco/aru212>

Causes of Individual Variability



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Received: 22 August 2016 | Revised: 12 December 2016 | Accepted: 22 December 2016
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ORIGINAL RESEARCH

WILEY *Ecology and Evolution*

Complex variation in habitat selection strategies among individuals driven by extrinsic factors

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Funding information

Division of Environmental Biology; National
Science Foundation (NSF); Grant/Award
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Abstract

Understanding behavioral strategies employed by animals to maximize fitness in the face of environmental heterogeneity, variability, and uncertainty is a central aim of animal ecology. Flexibility in behavior may be key to how animals respond to climate and environmental change. Using a mechanistic modeling framework for simultaneously quantifying the effects of habitat preference and intrinsic movement on space use at the landscape scale, we investigate how movement and habitat selection vary among individuals and years in response to forage quality–quantity tradeoffs, environmental conditions, and variable annual climate. We evaluated the association of dynamic, biotic forage resources and static, abiotic landscape features with large grazer movement decisions in an experimental landscape, where forage resources vary in response to prescribed burning, grazing by a native herbivore, the plains bison (*Bison bison*), and a continental climate. Our goal was to determine how biotic and abiotic factors mediate bison movement decisions in a nutritionally heterogeneous grassland. We integrated spatially explicit relocations of GPS-collared bison and extensive vegetation surveys to relate movement paths to grassland attributes over a time pe-

Causes of Individual Variability



Volume 26, Issue 2
March-April 2015



[Evolutionary Ecology](#)

March 1989, Volume 3, [Issue 1](#), pp 80–94 | [Cite as](#)

Density-dependent habitat selection: Testing the theory with fitness data

Authors

Authors and affiliations

Douglas W. Morris

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Complex variation in habitat selection strategies among individuals driven by extrinsic factors

| John M. Briggs¹ | Anthony Joern¹



OIKOS 92: 542–554. Copenhagen 2001

Habitat selection by predators and prey in communities with asymmetrical intraguild predation

Michael R. Heithaus

Heithaus, M. R. 2001. Habitat selection by predators and prey in communities with asymmetrical intraguild predation. – *Oikos* 92: 542–554.

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WILEY *Ecology and Evolution*

Vol. 137, Supplement

The American Naturalist

June 1991



OIKOS 92: 542–554. Copenhagen 2001

Habitat selection by predators asymmetrical intraguild predation

Michael R. Heithaus

Heithaus, M. R.
asymmetrical ir

GENETIC VARIATION FOR HABITAT PREFERENCE: EVIDENCE AND EXPLANATIONS

JOHN JAENIKE AND ROBERT D. HOLT

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Museum of Natural History and Department of Systematics and Ecology,
University of Kansas, Lawrence, Kansas 66045

Abstract.—Because adaptive shifts may often be initiated by evolutionary changes in behavior, it is of interest to determine the extent to which natural populations harbor genetic variation for ecologically important behaviors. Habitat preference is an especially significant behavior, because it determines the regime of natural selection acting on loci that affect adaptation to the environment. A survey of the literature reveals that genetic variation for habitat selection is common, especially in arthropods and mollusks, the groups that have been studied most frequently. Possible adaptive mechanisms by which this variation could be maintained within populations include a genetic correlation between density-independent fitness in a habitat and a preference for it; and soft selection, whereby density-dependent population regulation occurs independently in separate habitats. Several studies have documented a phenotypic correlation between habitat preference and fitness, but few studies have documented a genetic correlation between these two traits.

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Why do we care about individual variability?

Both Environment and Genetic Makeup Influence Behavior

By: Michael D. Breed (Department of Ecology & Evolutionary Biology, University of Colorado at Boulder) & Leticia Sanchez (Department of Ecology & Evolutionary Biology, University of Colorado at Boulder) © 2010 Nature Education

Citation: Breed, M. & Sanchez, L. (2010) Both Environment and Genetic Makeup Influence Behavior. *Nature Education Knowledge* 3(10):68



How do genes and the environment come together to shape animal behavior? Both play important roles. Genes capture the evolutionary responses of prior populations to selection on behavior. Environmental flexibility gives animals the opportunity to adjust to changes during their own lifetime.

- A -

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Journal of Applied Ecology



Journal of Applied Ecology 2015, 52, 496–504

doi: 10.1111/1365-2664.12400

Adjustments in habitat selection to changing availability induce fitness costs for a threatened ungulate

Chrystel L. Losier^{1,2}, Serge Couturier¹, Martin-Hugues St-Laurent^{2,3,4}, Pierre Drapeau^{2,5}, Claude Dussault⁶, Tyler Rudolph^{2,5}, Vincent Brodeur⁷, Jerod A. Merkle^{1,2} and Daniel Fortin^{1,2*}

¹Chaire de recherche industrielle CRSNG – Université Laval en sylviculture et faune, Département de biologie, Université Laval, Québec, QC G1V 0A6, Canada; ²Centre d'étude de la forêt, 2405 rue de la Terrasse, Québec, QC G1V 0A6, Canada; ³Département de Biologie, Chimie et Géographie, Université du Québec à Rimouski, Rimouski, QC G5L 3A1, Canada; ⁴Centre d'études nordiques, 2405 rue de la Terrasse, Québec, QC G1V 0A6, Canada; ⁵Chaire de recherche industrielle CRSNG – Université du Québec en Abitibi-Témiscamingue et Université du Québec à Montréal en aménagement forestier durable, Département des sciences biologiques, Université du Québec à Montréal, Montréal, QC H3C 3P8, Canada; ⁶Ministère du Développement durable, de l'Environnement et de la Faune et des Parcs, Directeur régional par intérim du Saguenay – La-Pointe-Saint-Jean, 3950 boul. Harvey, Jonquière, QC G7X 8L6, Canada; and ⁷Ministère du Développement durable, de l'Environnement et de la Faune et des Parcs, Direction des opérations régionales du Nord-du-Québec, 951 boul. Hamel, Chibougamau, QC G8P 2Z3, Canada

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ECOLOGY LETTERS

Ecology Letters (2018) 21: 665–673

doi: 10.1111/ele.12933

LETTER

Intragroup competition predicts individual foraging specialisation in a group-living mammal

Catherine E. Sheppard,¹
Richard Inger,² Robbie A.
McDonald,³ Sam Barker,³
Andrew L. Jackson,⁴ Rye J.
Thompson,⁵ Emma I. K.
Vikari,⁶ Michael A. Cant^{1*}
and Harry H. Marshall^{1,6*}

Abstract

Individual foraging specialisation has important ecological implications, but its causes in group-living species are unclear. One of the major consequences of group living is increased intragroup competition for resources. Foraging theory predicts that with increased competition, individuals should add new prey items to their diet, widening their foraging niche (optimal foraging hypothesis). However, classic competition theory suggests the opposite: that increased competition leads to niche partitioning and greater individual foraging specialisation (niche partitioning hypothesis). We tested these opposing predictions in wild, group-living banded mongooses (*Mungos mungos*) using stable isotope analysis of banded mongoose whiskers to quantify individual and group foraging niche. Individual foraging niche size declined with increasing group size, despite all groups having a similar overall niche size. Our findings support the prediction that competition promotes niche partitioning within social groups and suggest that individual foraging specialisation may play an important role in the formation of stable social groupings.

Keywords

banded mongoose, competition, foraging behaviour, foraging niche, group-living, *Mungos mungos*, social group, specialisation, stable isotope.

Ecology Letters (2018) 21: 665–673



Journal of Applied Ecology

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Chrystel L. Losier^{1,2}, Serge Couturier¹, Martin-Hugues St-Laurent^{2,3,4}, Pierre Drapeau^{2,5}, Claude Dussault⁶, Tyler Rudolph^{2,5}, Vincent Brodeur⁷, Jerod A. Merkle^{1,2} and Daniel Fortin^{1,2*}

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Food limitation leads to behavioral diversification and dietary specialization in sea otters

M. Tim Tinker¹, Gena Bental¹, and James A. Estes¹

¹Department of Ecology and Evolutionary Biology, University of California, Center for Ocean Health, 100 Shaffer Road, Santa Cruz, CA 95060; ²Sea Otter Research and Conservation, Monterey Bay Aquarium, 886 Cannery Row, Monterey, CA 93940; and ³U.S. Geological Survey, Western Ecological Research Center, Long Marine Laboratory, 100 Shaffer Road, Santa Cruz, CA 95060

Edited by Robert I. Paine, University of Washington, Seattle, WA, and approved November 28, 2007 (received for review September 28, 2007)

Dietary diversity often varies inversely with prey resource abundance. This pattern, although typically measured at the population level, is usually assumed to also characterize the behavior of individual animals within the population. However, the pattern might also be produced by changes in the degree of variation among individuals. Here we report on dietary and associated behavioral changes that occurred with the experimental translo-

cation of sea otters from a high prey environment to a low prey environment. We have obtained longitudinal records of sea otter diet and foraging behavior from tagged individuals that span multiple years (8). Moreover, the experimental translocation of sea otters from central California (henceforth CC) to San Nicolas Island (henceforth SN) in the southern California Bight in 1987–1990 established a second population in a comparatively food-rich environment where the diversity of potential inverte-

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Oecologia (2017) 185:415–425
DOI 10.1007/s00442-017-3939-8

BEHAVIORAL ECOLOGY –ORIGINAL RESEARCH

Not accounting for interindividual variability can mask habitat selection patterns: a case study on black bears

Rémi Lesmerises¹ · Martin-Hugues St-Laurent²

Catherine E. Sheppard,¹
Richard Innes,² Robbie A.
McDonald,² Sam Barker,²
Andrew L. Jackson,¹ Rye J.
Thompson,¹ Emma L. K.
Vikari,¹ Michael A. Cant^{1*}
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Abstract

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Keywords

Banded mongoose, competition, foraging behaviour, foraging niche, group-living, *Mungos mungos*, social group, specialisation, stable isotope.

Ecology Letters (2018) 21: 665–673

50 YEARS OF
IMPACT

Journal of Applied Ecology 2015, 52, 496–504

Journal of Applied Ecology

doi: 10.1111/1365-2666.13400

Adjustments in habitat selection to changing availability induce fitness costs for a threatened ungulate

Chrystel L. Losier^{1,2}, Séverine Couturier¹, Martin-Hugues St-Laurent^{2,3,4}, Pierre Drapeau^{2,5}, and Niel Fortin^{1,2*}



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M. Tim Tinker¹, Gena Bental¹, and James A. Estes⁵

¹Department of Ecology and Evolutionary Biology, University of California, Center for Ocean Health, 100 Shaffer Road, Santa Cruz, CA 95060; ²Sea Otter Research and Conservation, Monterey Bay Aquarium, 886 Cannery Row, Monterey, CA 93940; and ³U.S. Geological Survey, Western Ecological Research Center, Long Marine Laboratory, 100 Shaffer Road, Santa Cruz, CA 95060

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Understanding Functional Responses

Habitat selection parameters, β , are informed by habitat use relative to habitat availability.

- ▶ when $f^u(x) > f^a(x) \Rightarrow$ “preference” for habitat x .

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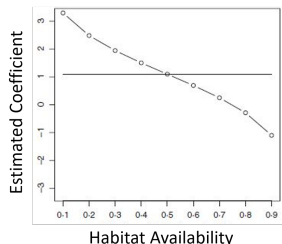
Some resources, like water, may be needed in small and relatively constant amounts

Understanding Functional Responses

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Aarts, G., Fieberg, J., Brasseur, S., & Matthiopoulos, J. (2013). Quantifying the effect of habitat availability on species distributions. *Journal of animal ecology*, 82(6), 1135-1145.

FUNCTIONAL RESPONSES IN HABITAT USE: AVAILABILITY INFLUENCES RELATIVE USE IN TRADE-OFF SITUATIONS

ATLE MYSTERUD AND ROLF ANKER IMS

Department of Biology, Division of Biology, P.O. Box 1050 Blindern, University of Oslo, N-0316 Oslo, Norway

Habitat-use patterns depend on:

- ▶ habitat availability and. . .
- ▶ interactions between different resources risks, and conditions

Individuals may spend more time feeding if resource rich patches are near areas with good escape cover.



Mysterud and Ims (1998)

- Developed an approach to modeling functional responses
- Limited to considering two discrete habitat types

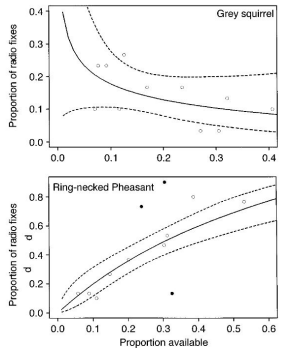


FIG. 1. Logistic regression of proportional use against proportion of that habitat available within an individual's home range for gray squirrel and Ring-necked Pheasants, with 95% confidence envelopes. Note that the regression for the Ring-necked Pheasant includes three misfitting observations (solid circles); thus the confidence envelopes may be underestimated.

Generalized Functional Responses

Ecology, 92(3), 2011, pp. 583–589
© 2011 by the Ecological Society of America

Generalized functional responses for species distributions

JASON MATTHIOPOULOS,^{1,2,7} MARK HERBLEWHITE,³ GEERT AARTS,^{4,5} AND JOHN FIEBERG⁶

¹*Scottish Oceans Institute, School of Biology, University of St. Andrews, East Sands, St. Andrews,
Fife KY16 8LB Scotland, United Kingdom*

²*Centre for Research into Environmental and Ecological Modeling, University of St Andrews, The Observatory, Buchanan Gardens,
St Andrews, Fife KY16 9LZ Scotland, United Kingdom*

³*Wildlife Biology Program, Department of Ecosystem and Conservation Sciences, College of Forestry and Conservation,
University of Montana, Missoula, Montana 59812 USA*

⁴*Royal Netherlands Institute for Sea Research (NIOZ), P.O. Box 59, 1790 AB Den Burg, The Netherlands*

⁵*IMARES Wageningen UR, Institute for Marine Resources and Ecosystem Studies, P.O. Box 167,
1790 AD Den Burg, The Netherlands*

⁶*Biometrics Unit, Minnesota Department of Natural Resources (Minnesota DNR), 5463-C West Broadway,
Forest Lake, Minnesota 55025 USA*

Capture variability in habitat-selection parameters (in RSFs) across multiple sampling instances using:

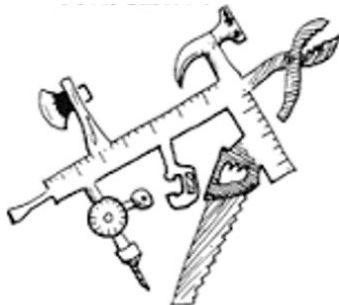
- ▶ moments of availability (mean, variance)
- ▶ interactions between these moments
- ▶ random coefficients

Causes and consequences of among-animal variability

Methods for modeling among-animal variability

Methods for modeling among-animal variability

1. Fit models to individual animals (or sampling instances) and treat the estimates as data (two-step approach)
2. Mixed models, hierarchical models, random-effect models: allow parameters to vary by animal



Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(\mathbf{s}) \propto \exp(x_1(\mathbf{s})\beta_{1i} + x_2(\mathbf{s})\beta_{2i} + \dots x_p(\mathbf{s})\beta_{pi})$$

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(\mathbf{s}) \propto \exp(x_1(\mathbf{s})\beta_{1i} + x_2(\mathbf{s})\beta_{2i} + \dots x_p(\mathbf{s})\beta_{pi})$$

Step 2: Do statistics on $(\hat{\beta}_{1i}, \dots, \hat{\beta}_{pi})$

Two-Step Approach

Step 1: fit models to individuals

$$f_i^u(s) \propto \exp(x_1(s)\beta_{1i} + x_2(s)\beta_{2i} + \dots x_p(s)\beta_{pi})$$

Step 2: Do statistics on $(\hat{\beta}_{1i}, \dots, \hat{\beta}_{pi})$



Covariates:

- ▶ elevation
- ▶ population density
- ▶ forest (yes/no)

Fieberg J, Bohrer G, Davidson SC, Kays R (2018) Short course on analyzing animal tracking data. Presented at the North Carolina Museum of Natural Sciences, Raleigh, NC, USA. May 21-23, 2018.
<https://movebankworkshopraleighnc.netlify.com/>

LaPoint, S., Gallery, P., Wikelski, M., and Kays, R. 2013. Animal behavior, cost-based corridor models, and real corridors. *Landscape Ecology*, 28, 1615-1630.

amt: Individual-Specific Coefficients

Quick and easy using the `amt` package in conjunction with `tidyverse` in R

Fit models to individuals:

```
rsffits <- dat_rsf %>% nest(data=!c(id, sex)) %>%  
  mutate(mod = map(data, function(x)  
    glm(case_ ~ elevation + popden + forest,  
        data = x, weight=w, family = binomial)))
```

Pull off coefficients:

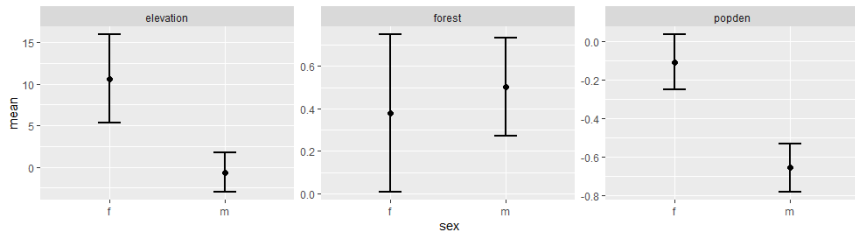
```
rsffits2 <- rsffits %>%  
  dplyr::mutate(tidy = purrr::map(mod, broom::tidy),  
               n = purrr::map(data, nrow) %>% simplify()) %>%  
  unnest(tidy) %>% select(-c(data, mod))
```


Data Frame: Individual-Specific Coefficients

```
> rsffits2
# A tibble: 24 x 8
   id sex term estimate std.error statistic p.value n
  <dbl> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <int>
1 2 f (Intercept) -8.36 0.489 -17.1 1.33e-65 14828
2 2 f forest 1.02 0.0602 16.9 2.04e-64 14828
3 2 f elevation 1.64 0.524 3.13 1.75e- 3 14828
4 2 f popden 0.142 0.0777 1.83 6.73e- 2 14828
5 4 f (Intercept) 1.79 0.950 1.88 5.95e- 2 11132
6 4 f forest 0.160 0.0667 2.39 1.67e- 2 11132
7 4 f elevation 13.0 1.12 11.7 2.25e-31 11132
8 4 f popden -0.260 0.0723 -3.60 3.22e- 4 11132
9 5 f (Intercept) 6.69 2.85 2.35 1.90e- 2 5599
10 5 f forest -0.0470 0.114 -0.412 6.80e- 1 5599
# ... with 14 more rows
> |
```

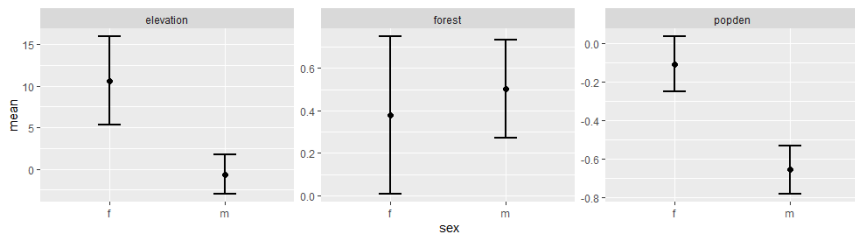
Signer, J., J. Fieberg, and T. Avgar (2019). Animal movement tools (amt): R package for managing tracking data and conducting habitat selection analyses. *Ecology and Evolution* 9:880-890.

Step 2: Statistics on Statistics



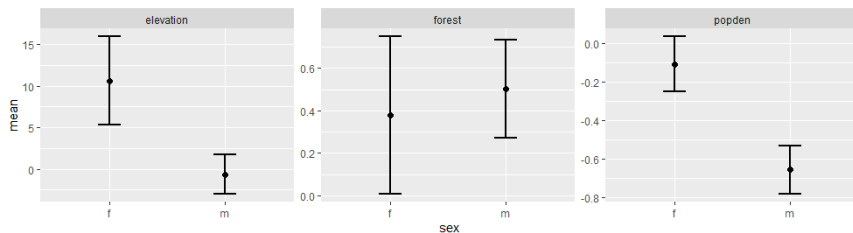
- relate coefficients to animal-specific characteristics (e.g., age, sex) using say `lm`

Step 2: Statistics on Statistics



- ▶ relate coefficients to animal-specific characteristics (e.g., age, sex) using say `lm`
- ▶ calculate variance/covariance (biased high due to sampling variability)

Step 2: Statistics on Statistics



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In the context of step-selection functions:

- ▶ Craiu, R. V., T. Duchesne, D. Fortin, and S. Baillargeon (2011). Conditional logistic regression with longitudinal follow-up and individual-level random coefficients: A stable and efficient two-step estimation method. *Journal of Computational and Graphical Statistics* 20, 767-784.
- ▶ Craiu, R. V., T. Duchesne, D. Fortin, and S. Baillargeon (2016). TwoStepCLogit: Conditional Logistic Regression: A Two-Step Estimation Method. R package version 1.2.5.

Mixed-Effect Models

Contain fixed and random effects. What is the difference?

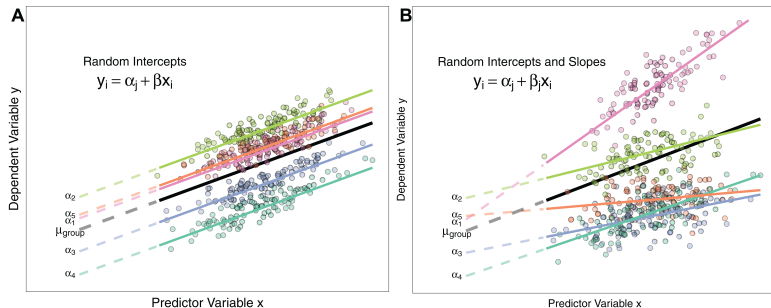
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Random intercepts and random slopes:



Mixed models

$$f_i^u(\mathbf{s}) \propto \exp(x_1(\mathbf{s})\beta_{1i} + x_2(\mathbf{s})\beta_{2i} + \dots x_p(\mathbf{s})\beta_{pi})$$

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Further assume:

$$(\beta_{1i}, \dots, \beta_{2i}) \sim N(\mu, \psi)$$

Similar 2-step approach, but assume the regression parameters come from a common normal distribution.

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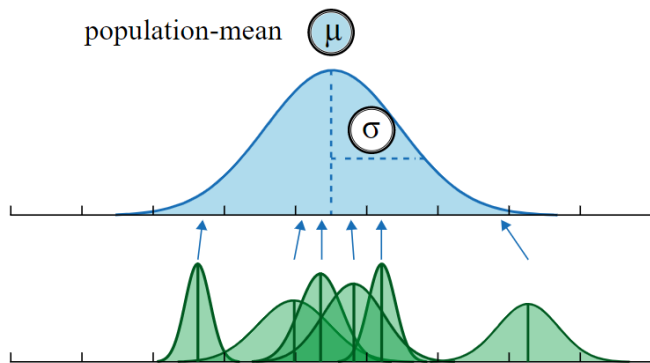
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- ▶ can estimate μ, ψ while accounting for sampling variability

Individual Estimates Borrow Strength (Exhibit Shrinkage)



Downside of Random Effects

- ▶ More assumptions (parameters are normally distributed)
- ▶ Added complexity (requires numerical integration to calculate the likelihood), computationally challenging to fit
- ▶ Potentially more difficult for practitioners to understand, correctly specify, and communicate

Random Effects and Habitat-selection Models

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Step-selection functions:

- ▶ conditional logistic regression, few good options
- ▶ `coxme` for small numbers of strata (SLOW!)
- ▶ `TwoStepCLogit::Ts.estim()`, a formal two-step approach (will fail if some individuals do not experience all levels of a categorical variable)


Accounting for individual-specific variation in habitat-selection studies: Efficient estimation of mixed-effects models using Bayesian or frequentist computation

Stefanie Muff^{1,2}  | Johannes Signer³  | John Fieberg⁴ 



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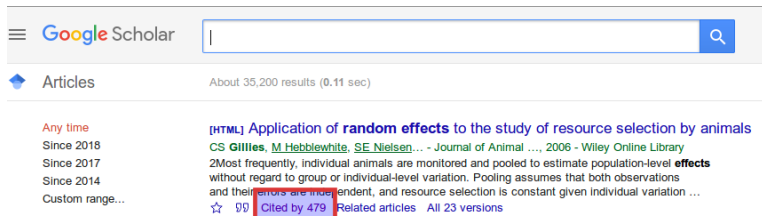


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- ▶ How are random effects used in applications of RSFs?
- ▶ Develop computationally efficient method of fitting SSFs with random effects

One Step: Random Effects

- Random effects were proposed for RSFs over 10 years ago¹



The screenshot shows a Google Scholar search interface. The search bar is empty. Below the search bar, the text 'Articles' is displayed with a blue diamond icon. To the right, it says 'About 35,200 results (0.11 sec)'. On the left side, there are filters for 'Any time', 'Since 2018', 'Since 2017', 'Since 2014', and 'Custom range...'. The main search result is for the article 'Application of random effects to the study of resource selection by animals' by Gillies, M. Hebblewhite, and S.E. Nielsen, published in the Journal of Animal Ecology in 2006. The article is highlighted in green. Below the title, there is a red box around the text 'Cited by 479'. To the right of the red box, there are links for 'Related articles' and 'All 23 versions'.

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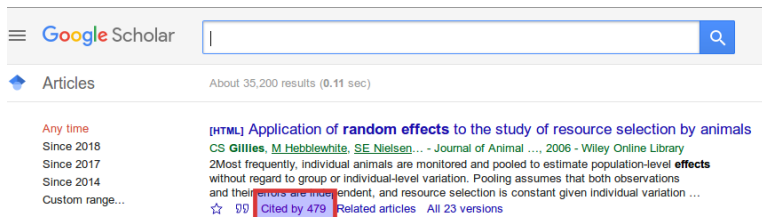
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- ▶ Majority of studies (80 % since 2016) only include random intercept and no random slope(s).

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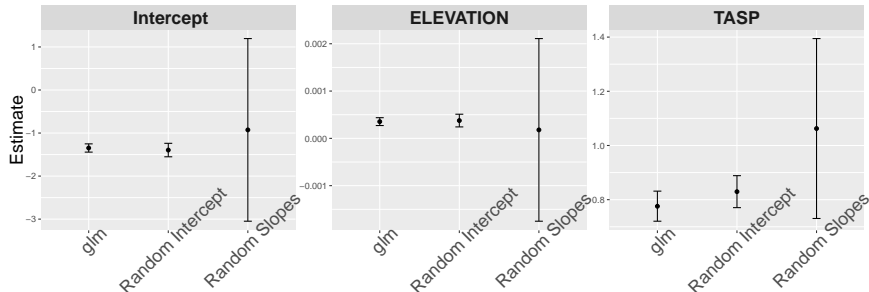
RSFs: Random Intercept-Only Models

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3. SEs will be too small, particularly with lots of observations for each animal

Schielzeth, H. and W. Forstmeier (2009). Conclusions beyond support: Overconfident estimates in mixed models. *Behavioral Ecology* 20, 416-420.

Example: Goat RSFs

```
glm <- glm(STATUS ~ TASP + ELEVATION, family=binomial(),  
           data = goats)  
glmer_int <- glmmTMB(STATUS ~ TASP + ELEVATION + (1|ID),  
                    family=binomial(), data = goats)  
glmer_randcoef <- glmmTMB(STATUS ~ TASP + ELEVATION +  
                          (1+TASP+ELEVATION|ID),  
                          family=binomial(), data = goats)
```



Computationally Efficient Step-Selection Functions

How can we fit SSFs with random effects?

Computationally Efficient Step-Selection Functions

How can we fit SSFs with random effects?

Reformulate SSFs as a Poisson model with stratum-specific intercepts α_{nt} (Armstrong et al. 2014):

- ▶ Same likelihood kernel as condition logistic regression likelihood, same $\hat{\beta}$, same $SE(\hat{\beta})$
- ▶ Treat intercepts as random with large fixed variance:
 $\alpha_{nt} \sim N(0, 10^6)$ (avoids shrinkage)
- ▶ Options: `glmmTMB` or `INLA` (Bayesian)

Armstrong et al. 2014. Conditional Poisson models: a flexible alternative to conditional logistic case cross-over analysis. *BMC medical research methodology* 14:122.

Statistical Properties

Simulation study (SSFs):

- ▶ verify that the Poisson trick works, but only when fixing the variance of the random intercepts!
- ▶ compare models assuming independence, mixed-effect Poisson glmm, formal two-step approach

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Applied example (RSFs and SSFs):

- ▶ compare two-step and mixed-effect approaches

▶ Applied Example

SSF: Simulation Study

Simulate movements of 20 animals according to a biased random walk

Candidate locations:

- ▶ Step-lengths: $\sim \text{exponential}(\lambda = 1)$
- ▶ Turn angles: $\text{uniform}(-\pi, \pi)$

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Select among candidate locations with probability:

$$w(x) \propto \exp(x_1\beta_1 + x_2\beta_2 + x_1b_{1i} + x_2b_{2i})$$

- ▶ x_1 and x_2 measure habitat quality and elevation
- ▶ β_1 and β_2 are fixed effects
- ▶ b_{1i} and b_{2i} are random effects: $(b_{1i}, b_{2i}) \sim N(0, \psi)$

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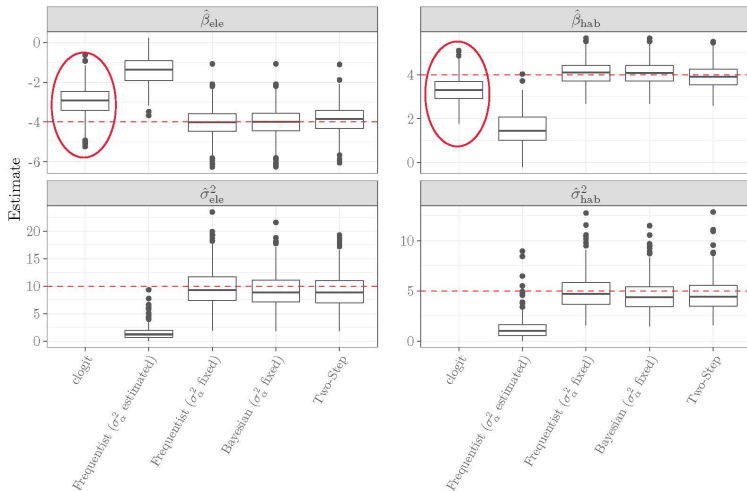
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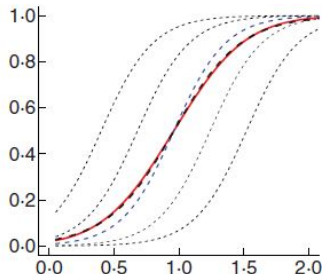
Fixed Effects Only (Attenuation Bias)



Population Averaged vs. Subject Specific

- ▶ clogit (pooled data): estimates a response curve for the population
- ▶ mixed model (setting all random effects = 0): estimates a response pattern for a 'typical individual'

These are not the same!

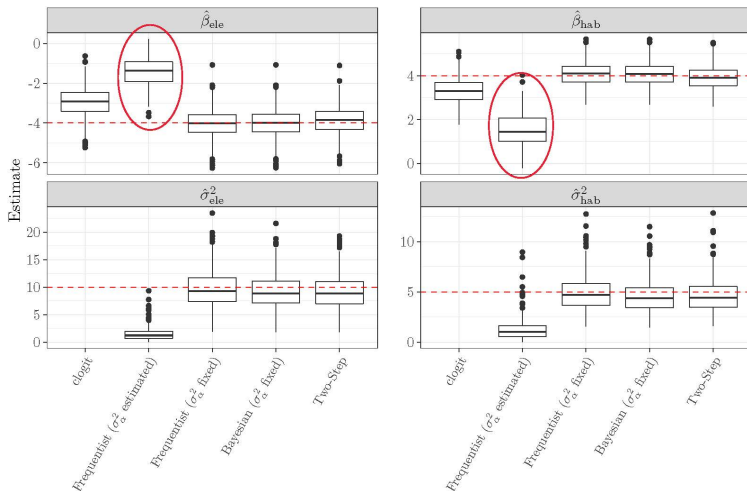


Muff, S., Held, L., & Keller, L. F. (2016). Marginal or conditional regression models for correlated non-normal data?. *Methods in Ecology and Evolution*, 7(12), 1514-1524.

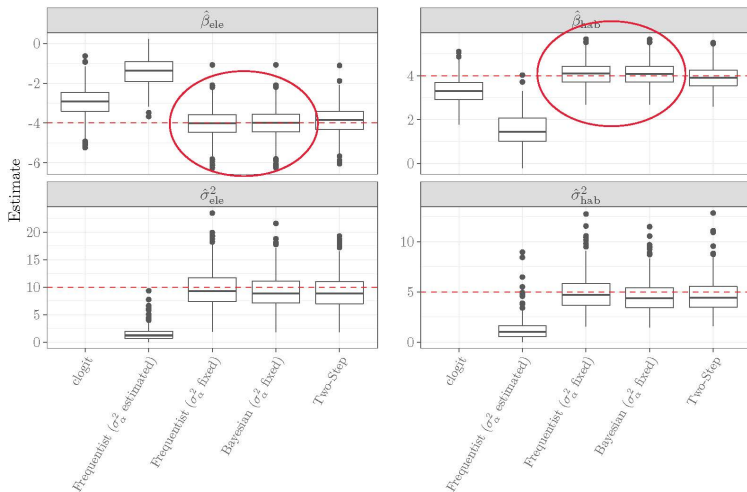
Fieberg, J., Rieger, R.H., Zicus, M. C., Schildcrout, J. S. 2009. Regression modelling of correlated data in ecology: subject specific and population averaged response patterns. *Journal of Applied Ecology* 46:1018-1025.

Fieberg, J., J. Matthiopoulos, M. Hebblewhite, M.S. Boyce, J. L. Frair. 2010. Correlation and studies of habitat selection: problem, red herring, or opportunity? *Philosophical Transactions of the Royal Society, Series B* 365:2233-2244.

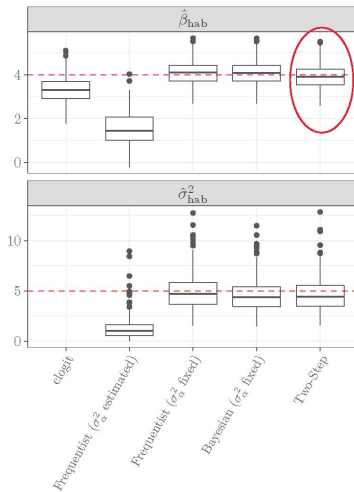
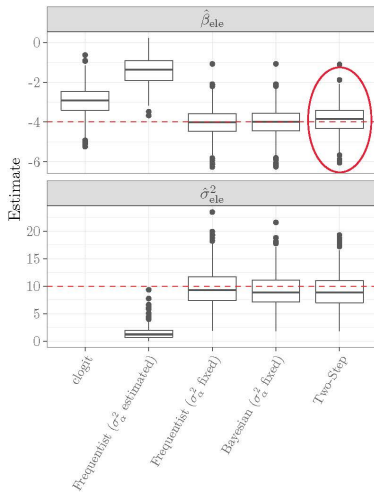
Random Effects with Estimated Intercept Variance



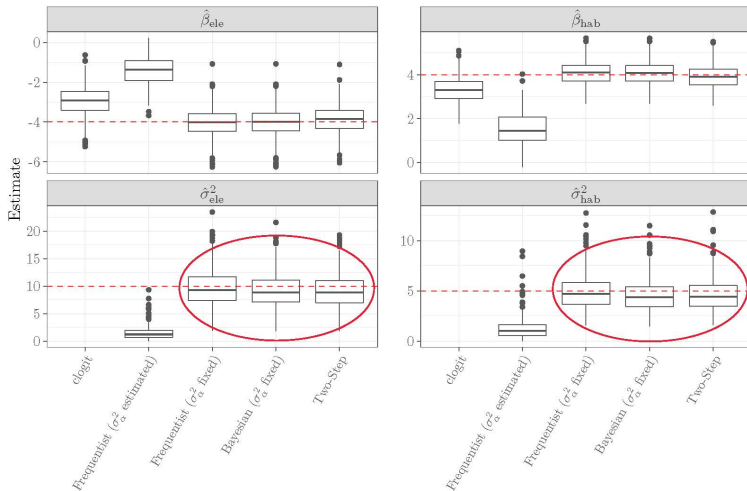
Random Effects with Fixed Large Variance



Two-step



Variance Parameters



Applied Example



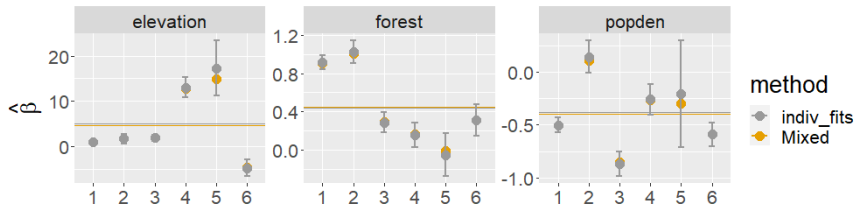
Covariates:

- ▶ elevation
- ▶ population density
- ▶ forest (yes/no)

Compare two-step approaches and mixed models:

- ▶ estimates of individual coefficients
- ▶ mean and variance of the coefficients across animals

Resource-Selection Functions



Variance estimates	$sd(\beta_{\text{elevation}})$	$sd(\beta_{\text{popden}})$	$sd(\beta_{\text{forest}})$
naive two-step (indiv_fits)	8.35	0.352	0.428
mixed model	7.07	0.315	0.382

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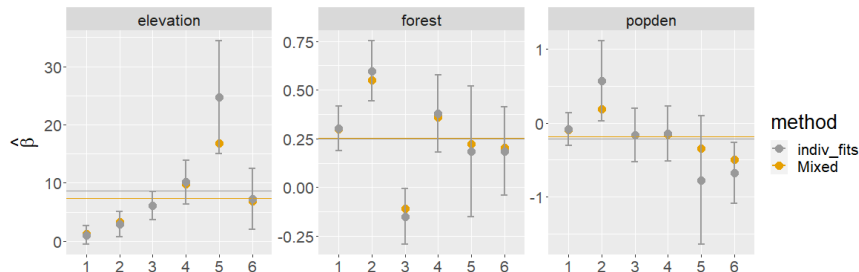
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- ▶ two-step approach + bootstrap (resampling individuals) could relax the assumption of independence within an individual

Step-Selection Functions



Variance estimates	$sd(\beta_{\text{elevation}})$	$sd(\beta_{\text{popden}})$	$sd(\beta_{\text{forest}})$
naive two-step (indiv_fits)	7.67	0.465	0.282
mixed model	4.91	0.293	0.252

Step-Selection Functions

Here, there are clear advantages to using mixed-model:

- ▶ beneficial shrinkage (due to smaller sample sizes since we are modeling transitions requiring equally-spaced time points)
- ▶ estimates of variance parameters are not biased by sampling variability
- ▶ BUT: steps may still be autocorrelated depending on the sampling frequency

Next steps

We will explore code for:

- ▶ implementing a two-step approach using tidyverse principles
- ▶ fitting mixed SSFs using glmmTMB (frequentist)
- ▶ fitting mixed SSFs using INLA (Bayesian)

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- ▶ Is it OK to assume turn angles and step lengths are independent?
- ▶ Should we incorporate longer-term dependencies, and if so, how?
- ▶ How should we account for changes in animal movement and habitat selection patterns?
 - ▶ over time (diurnally, seasonally)
 - ▶ across different behavioral states