NTNU

Methods for modeling data from multiple individuals

Implementation of SSFs in glmmTMB and INLA

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Recap – the model we want to fit

- Since conditional logistic regression is a special case of a multinomial model, and as such is likelihood-equivalent to a Poisson model with $E(y_{ntj}) = \mu_{ntj}$ (McCullagh and Nelder 1989)[1], we can fit

$$\mu_{ntj} = \exp(\alpha_{nt} + \boldsymbol{\beta}^\top \boldsymbol{x}_{ntj} + \boldsymbol{u}_n^\top \boldsymbol{z}_{ntj}) \ , \quad y_{ntj} \sim \text{Po}(\mu_{ntj}) \ ,$$

  with stratum-specific intercepts α_{nt}.
  Note: No global intercept.

- The intercepts are treated as random effects assuming $\alpha_{nt} \sim \mathsf{N}(0, \sigma_\alpha^2)$ with large σ_α^2 (*e.g.*, 10^6).

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[1]Chapter 6.4.2

The requirement on the software

Any software that fulfils the following two requirements can be used:

1. Capability to *fit mixed Poisson models*.
2. Possibility to *fix a random effect variance*.

- "Historically" (i.e., because of my background), it was most straightforward to use a Bayesian method. Fixing the prior on the variance is straightforward.

- But: of course this assumes that you are familiar with the rest of the Bayesian procedure.

- For some, it may be more staightforward to use a likelihood-based approach.

The Bayesian way: INLA

- Integrated nested Laplace approximations (Rue, Martino, and Chopin 2009).

- Idea: Fast approximations instead of MCMC sampling. A lot of mathy details.

- Some resources: www.r-inla.org

Hierarchical Bayesian models with INLA

INLA is able to deal with latent Gaussian *hierarchical models*, consisting of three sub-models:

- Observation model: Encodes information about data $\boldsymbol{y}|\boldsymbol{v},\boldsymbol{\theta}_1$
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- Hyperpriors: Models for the hyperparameters in the observation and latent processes $\boldsymbol{\theta}_1, \boldsymbol{\theta}_2$
  $\rightarrow$ Variances and other non-Gaussian paramters.

Understanding the "hyperparameters" in INLA

- Hyperparameters require integration in INLA. Time consuming!
- Simply speaking: Hyperparameters are the non-Gaussian unobserved variables.
- Typically (in SSFs): The (co)variance parameters.
- The number of (individual-specific) variances is therefore one of the most limiting factors for computational feasibility.

$\rightarrow$ *It is usually smart to carefully choose the variables that should be modeled with (animal-specific) random slopes.*

Pros and cons of INLA

Pros:
- Very flexible and modular toolset.
- Possible to combine with, *e.g.*, measurement error or spatially correlated random effects.
- Has most of the advantages Bayesian techniques have (priors, posteriors, joint modeling etc).
  $\rightarrow$ See the *coded session* for an example where we look at some posterior marginal distributions.

Cons:
- High threshold to get started, complex to use.
- Not very well documented.
- Slower than frequentist methods.

Bayesian SSFs using MCMC instead of INLA?

- Possible, but inefficient.
- We tried Stan, but the computation time was 1-2 orders of magnitues slower.

The frequentist way: glmmTMB

Brooks et al. (2017)

- Very fast frequentist inference.
- Easy to fix the random intercept variance.

$\rightarrow$ glmmTMB seems to be what most users of the Poisson-based SSF model prefer.

Brooks, Mollie E., Kasper Kristensen, Koen J. van Benthem, Arni Magnusson, Casper W. Berg, Anders Nielsen, Hans J. Skaug, Martin Mächler, and Benjamin M. Bolker. 2017. "glmmTMB Balances Speed and Flexibility Among Packages for Zero-inflated Generalized Linear Mixed Modeling." *The R Journal* 9: 378–400.

McCullagh, P., and J. A. Nelder. 1989. *Generalized Linear Models*. London: Chapman; Hall.

Rue, H, S Martino, and N Chopin. 2009. "Approximate Bayesian Inference for Latent Gaussian Models by Using Integrated Nested Laplace Approximations (with Discussion)." *Journal of the Royal Statistical Society. Series B (Methodological)* 71: 319–92.