

MARE-Madeira 2025

# *Movement speed estimation*

Using the 'ctmm' R package



*Inês Silva*

✉ [i.simoes-silva@hzdr.de](mailto:i.simoes-silva@hzdr.de)



## Vectors

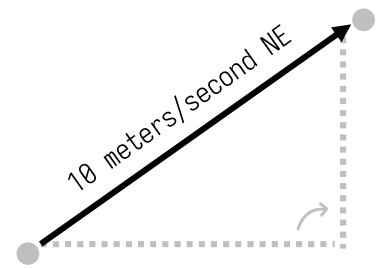
Specified by both **magnitude** (value + unit)  
and **direction**

Displacement

**Velocity**

Acceleration

N/A



magnitude of **velocity** vector



## Scalars

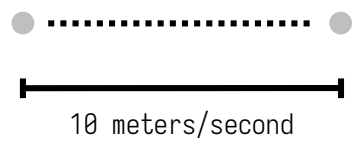
Specified by only **magnitude** (value + unit)

Distance

**Speed**

Acceleration/deceleration

Time





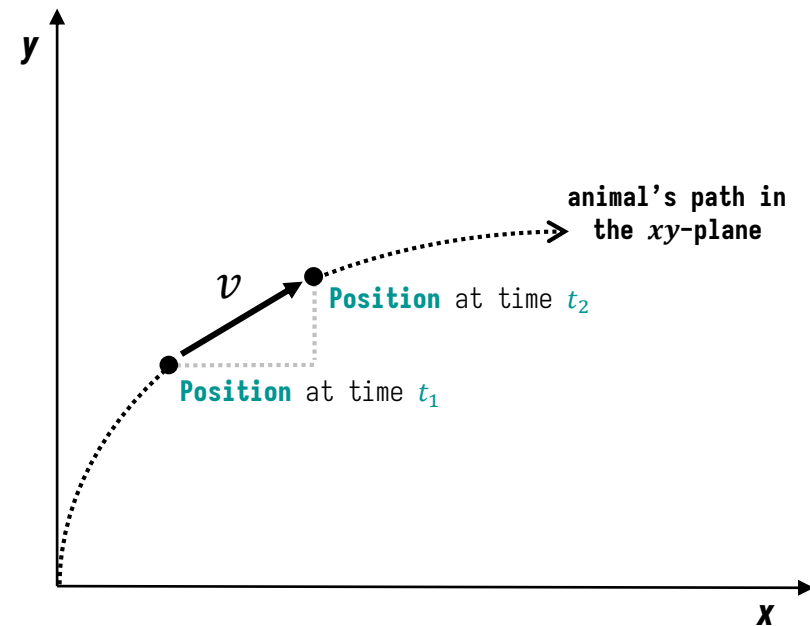
### Average **velocity**

*Displacement* divided by *time*

### Instantaneous **velocity**

The instantaneous rate of change of the **position vector** with respect to **time**  
(i.e., examined for a **very small time interval**)

$$\mathbf{v}_t = \lim_{\Delta t \rightarrow 0} \frac{\Delta \mathbf{r}}{\Delta t}$$



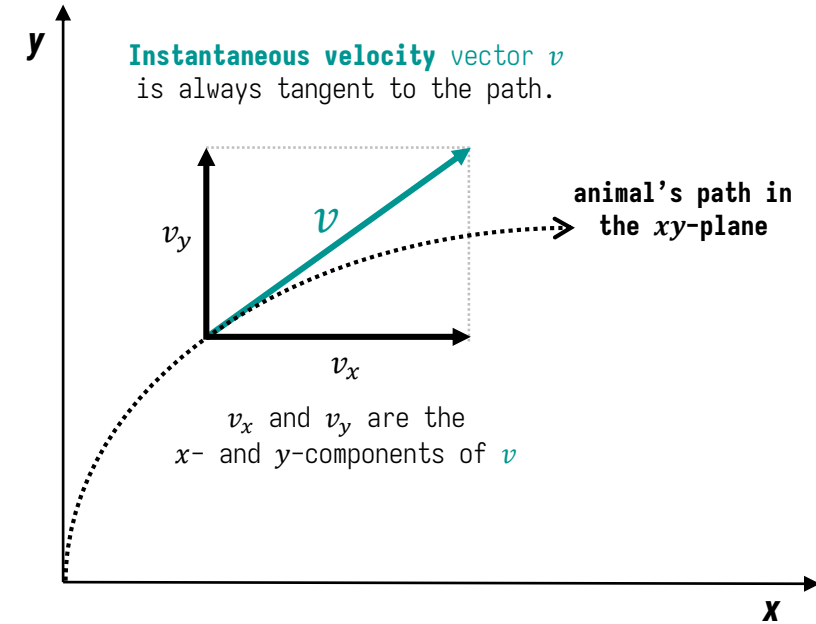
↪ For **speed**, take the magnitude only.

Average **velocity**  
*Displacement* divided by *time*

Instantaneous **velocity**

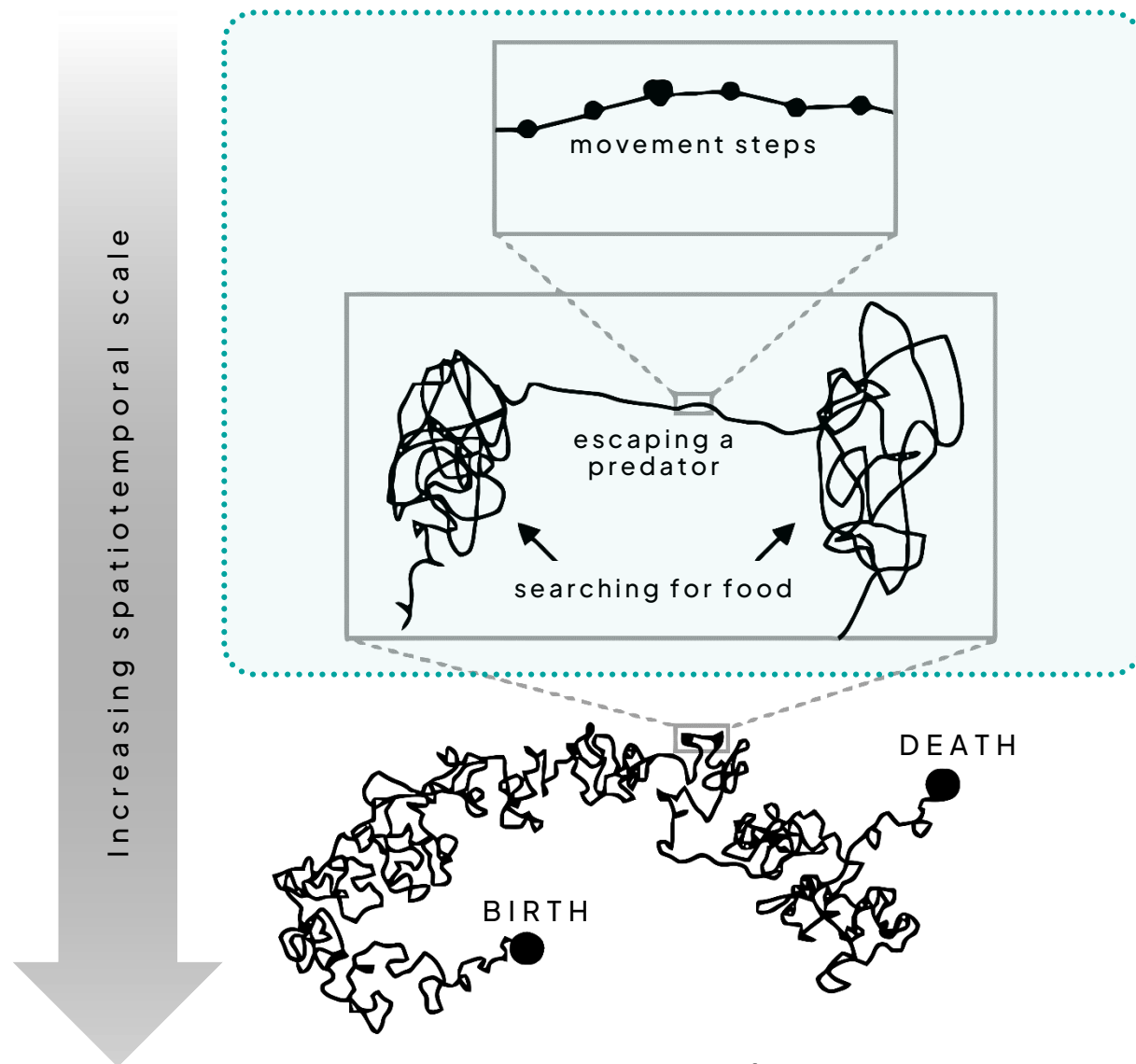
The instantaneous rate of change of the **position vector** with respect to **time**  
(i.e., examined for a **very small time interval**)

$$\mathbf{V}_t = \lim_{\Delta t \rightarrow 0} \frac{\Delta \mathbf{r}}{\Delta t}$$

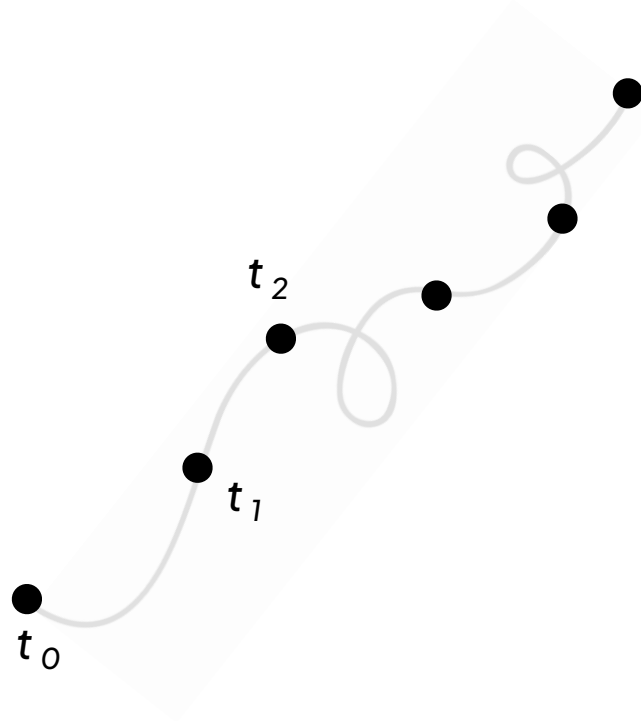




Speed- and distance-related metrics provide quantifiable links between **behavior and energetics**, can inform on risk/reward tradeoffs or as signals of **anthropogenic disturbance**.



Adapted from Nathan *et al.* (2008)

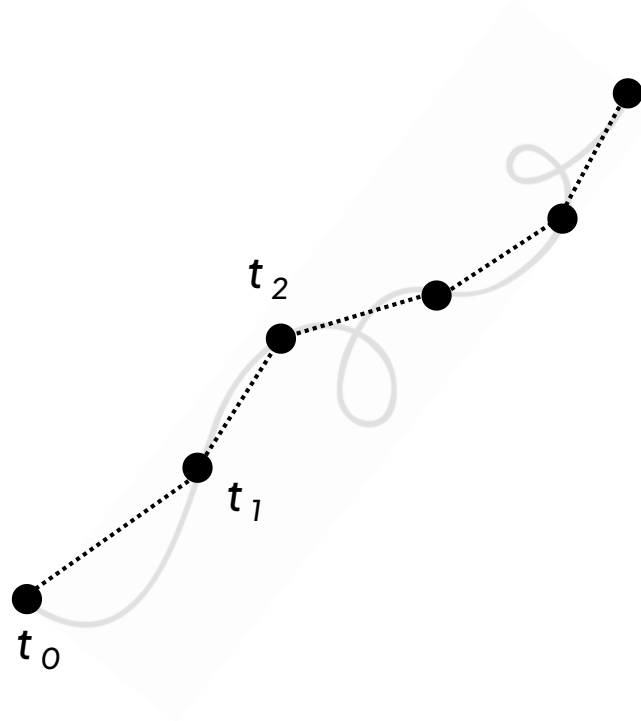


**Speed and distance traveled** are among the most routinely estimated metrics from animal tracking data.

Usually estimated by summing the **straight-line distance (SLD)** between location estimates...

$$\hat{d} = |\Delta \mathbf{r}| = \sqrt{\Delta x^2 + \Delta y^2}$$

... and divide that by  $\Delta t$  if speed is the desired metric.

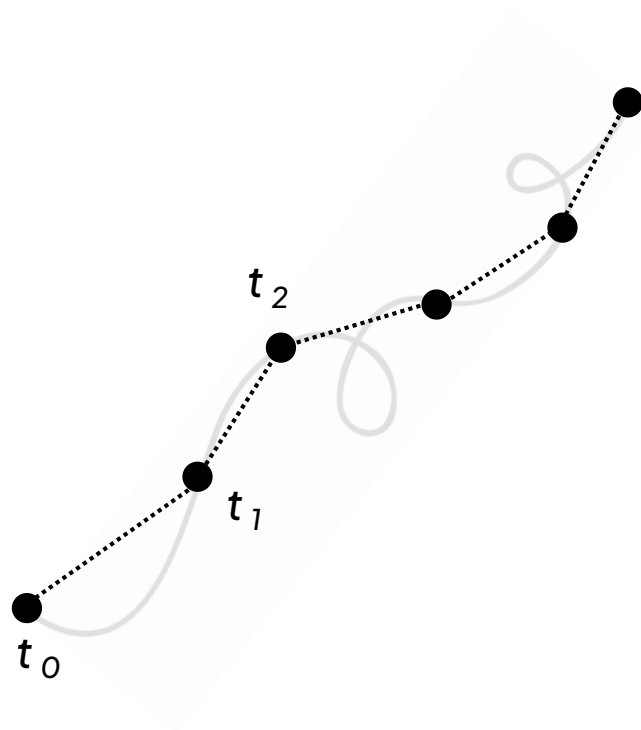


**Speed and distance traveled** are among the most routinely estimated metrics from animal tracking data.

Usually estimated by summing the **straight-line distance (SLD)** between location estimates...

$$\hat{d} = |\Delta \mathbf{r}| = \sqrt{\Delta x^2 + \Delta y^2}$$

... and divide that by  $\Delta t$  if speed is the desired metric.



**Speed and distance traveled** are among the most routinely estimated metrics from animal tracking data.

Usually estimated by summing the **straight-line distance (SLD)** between location estimates...

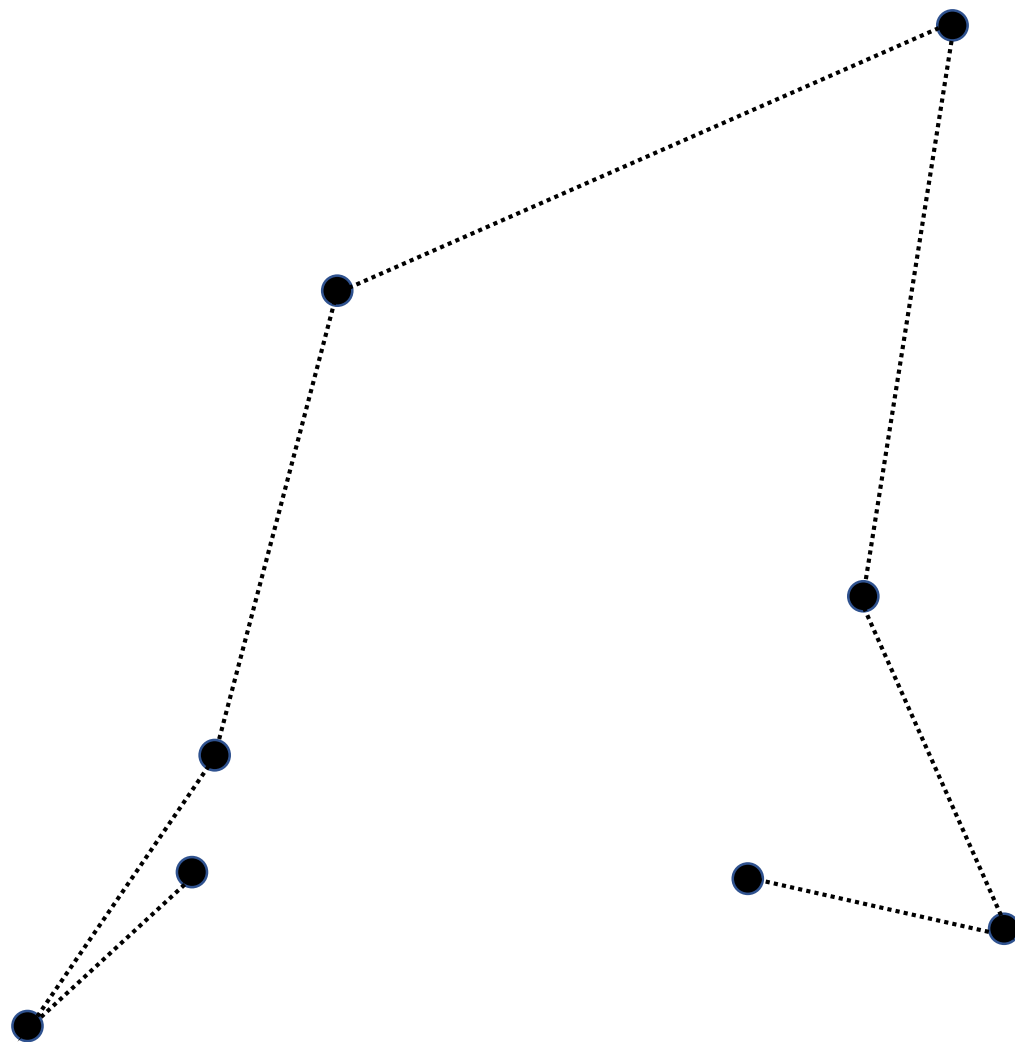
$$\hat{d} = |\Delta \mathbf{r}| = \sqrt{\Delta x^2 + \Delta y^2}$$

... and divide that by  $\Delta t$  if speed is the desired metric.

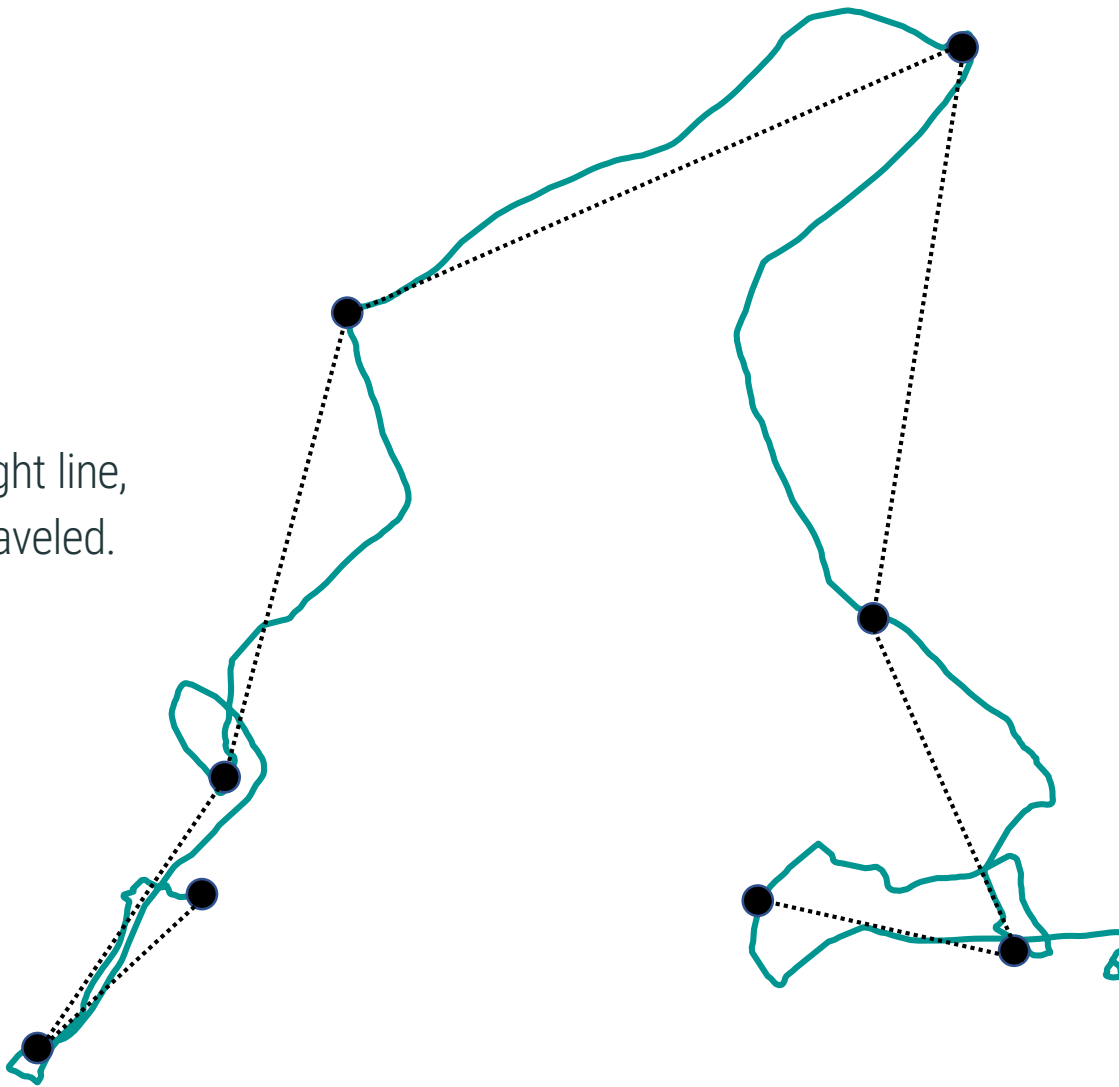


Although SLD is easy to quantify,  
it is also **heavily biased**.

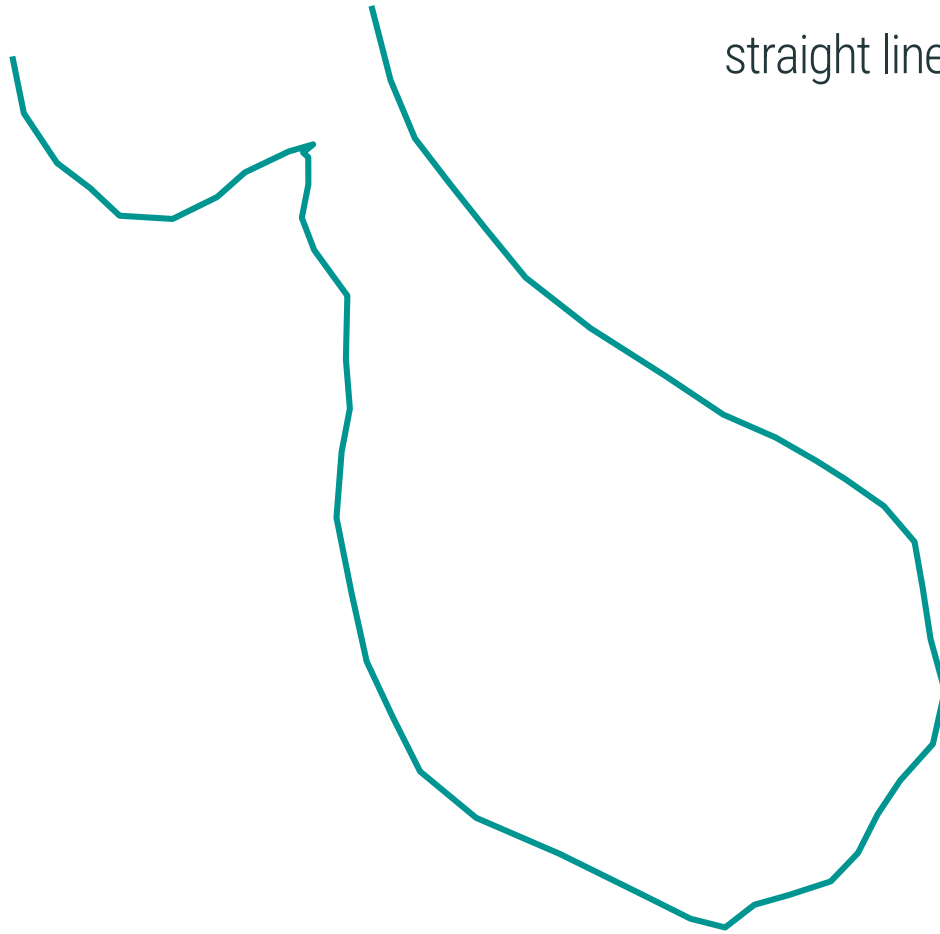


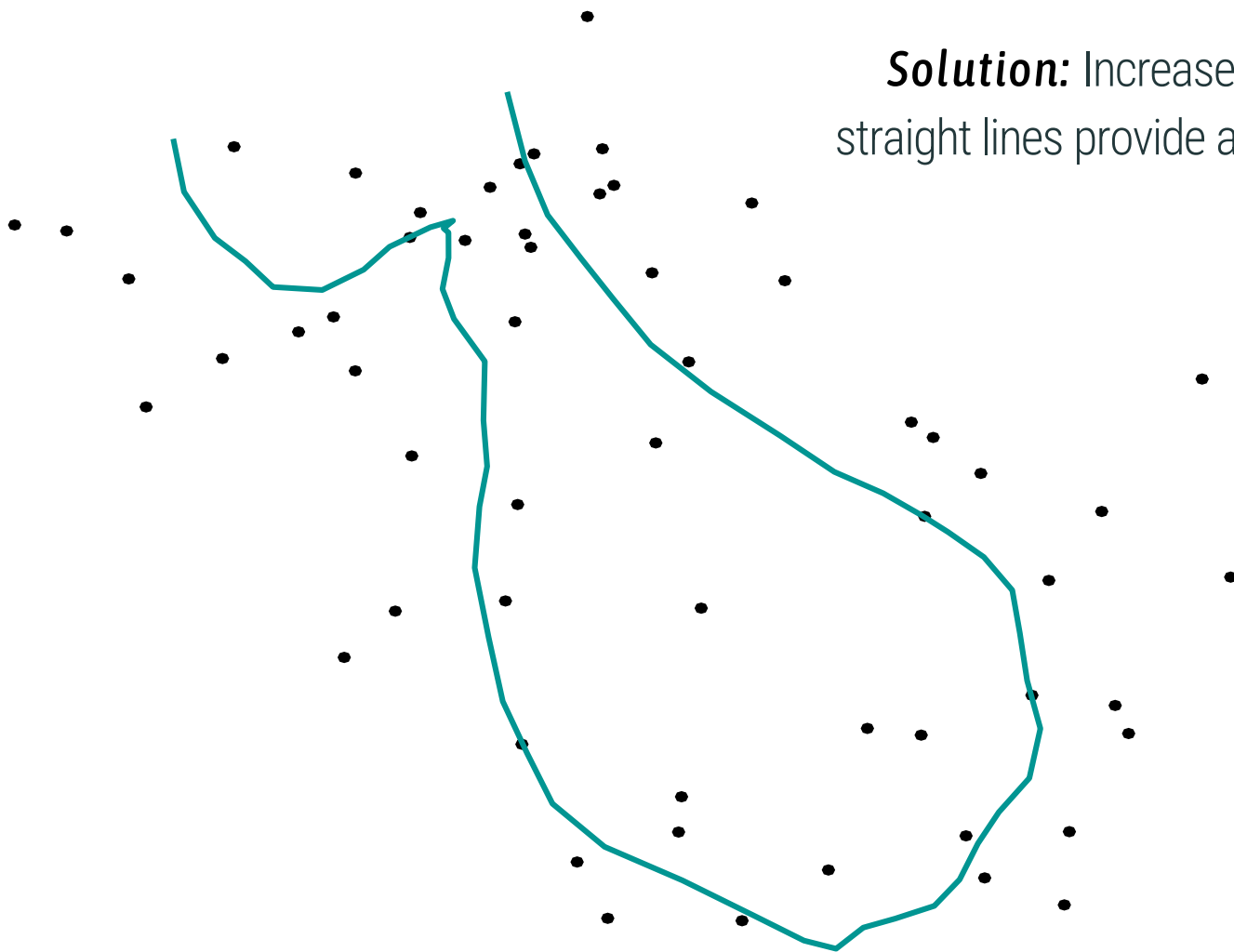


Unless the animal moved in a perfectly straight line, this will always **underestimate** distance traveled.

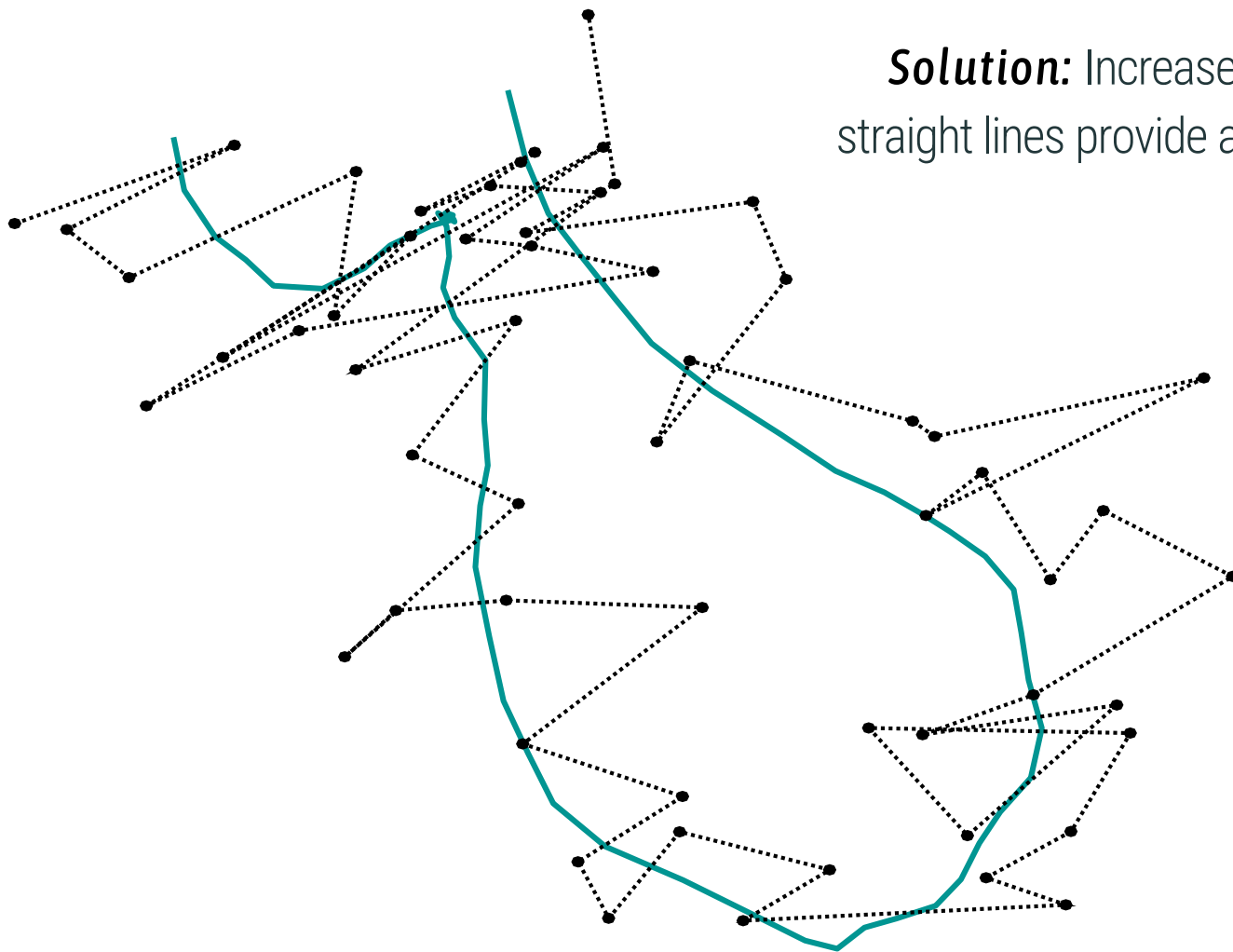


**Solution:** Increase the sampling frequency until the straight lines provide a better *approximation* of a curve?

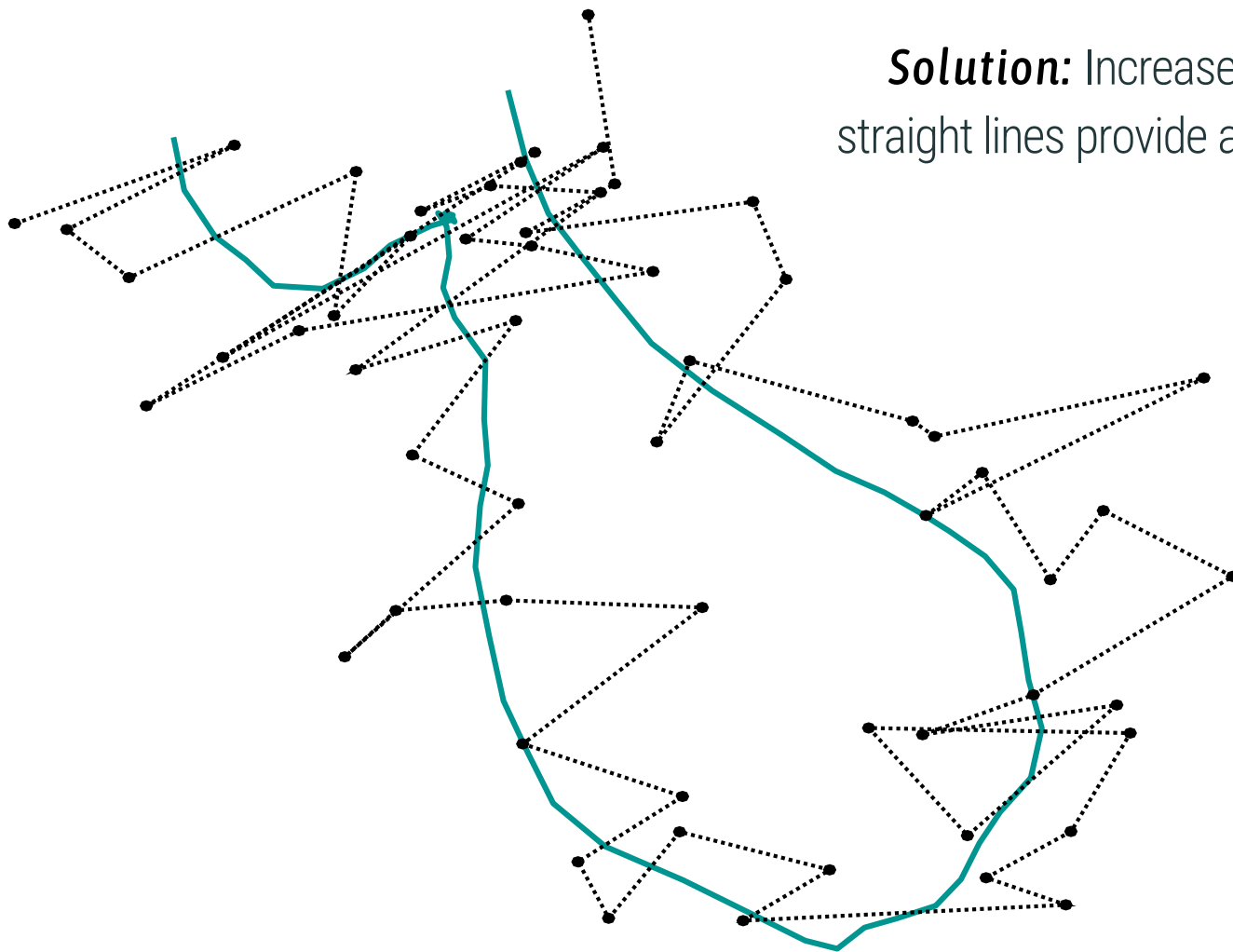




**Solution:** Increase the sampling frequency until the straight lines provide a better *approximation* of a curve?



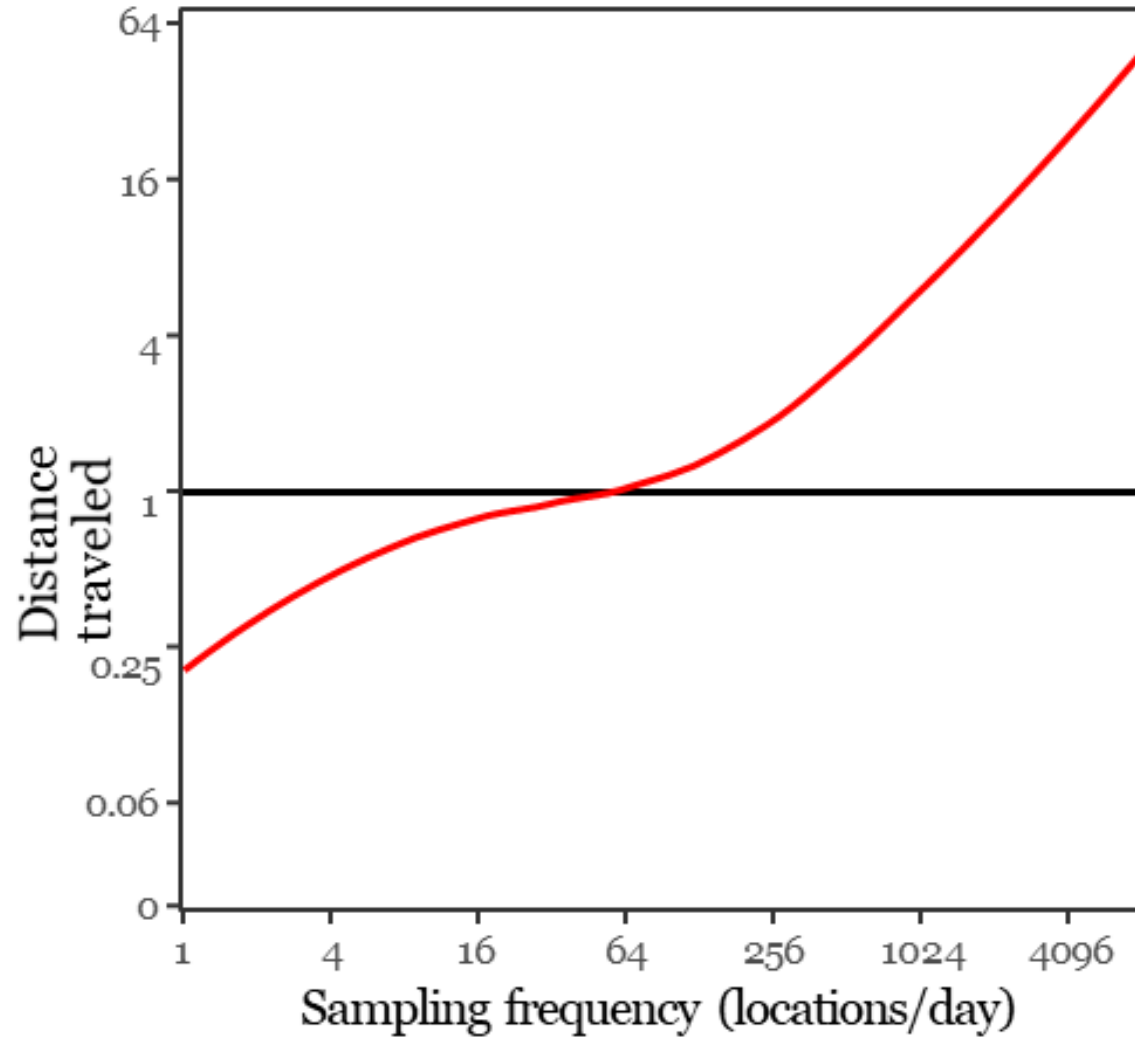
**Solution:** Increase the sampling frequency until the straight lines provide a better **approximation** of a curve?



**Solution:** Increase the sampling frequency until the straight lines provide a better **approximation** of a curve?

**However,**  
If error is uncorrelated in time, estimates converge to **infinity** with infinite sampling frequency ( $\Delta t \rightarrow 0$ ).

**Why?** The actual distance traveled by the animal goes to **0** in the limit where  $\Delta t \rightarrow 0$ , but the magnitude of uncorrelated measurement error is **independent of  $t$** .



## Continuous-time speed and distance (CTSD)

Noonan *et al.* (2020)

Model	Autocorrelation			Parameters:
	Position	Velocity	Restricted	
IID	No	No	Yes	$\tau = \text{NULL}$
BM	Yes	No	No	$\tau = \infty$
OU	Yes	No	Yes	$\tau = \tau_p$
IOU	Yes	Yes	No	$\tau = \{\infty, \tau_v\}$
OUF	Yes	Yes	Yes	$\tau = \{\tau_p, \tau_v\}$



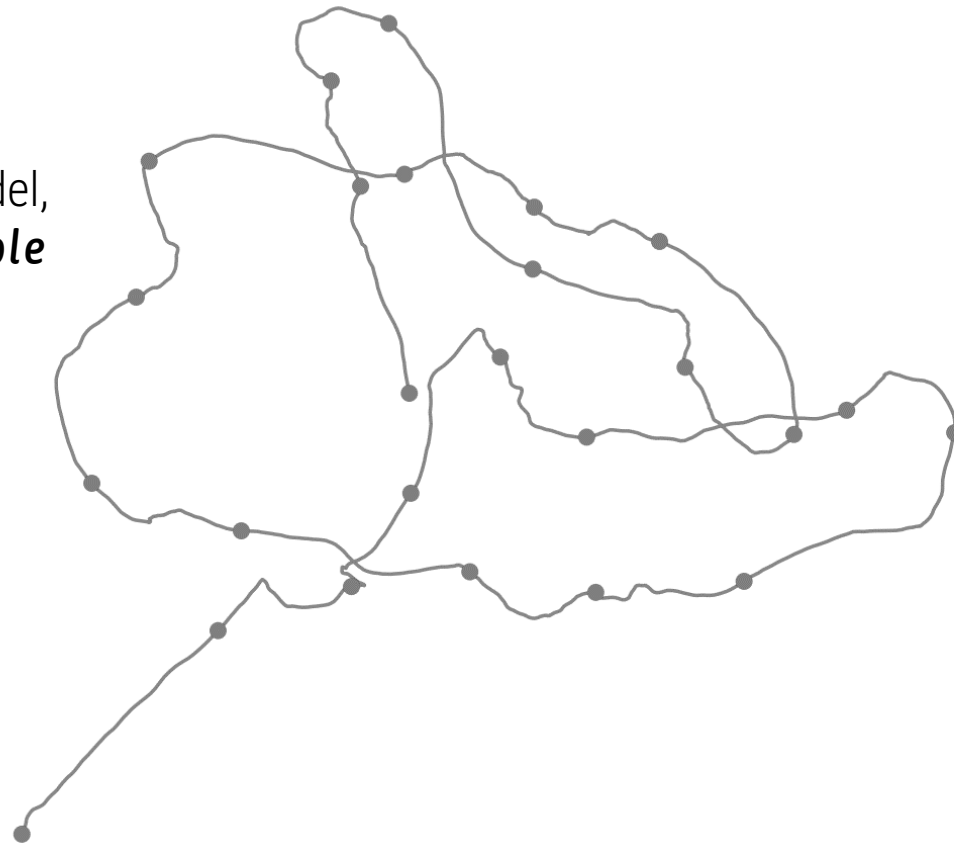
Requires a *correlated velocity model*.



## Continuous-time speed and distance (CTSD)

 Noonan *et al.* (2020)

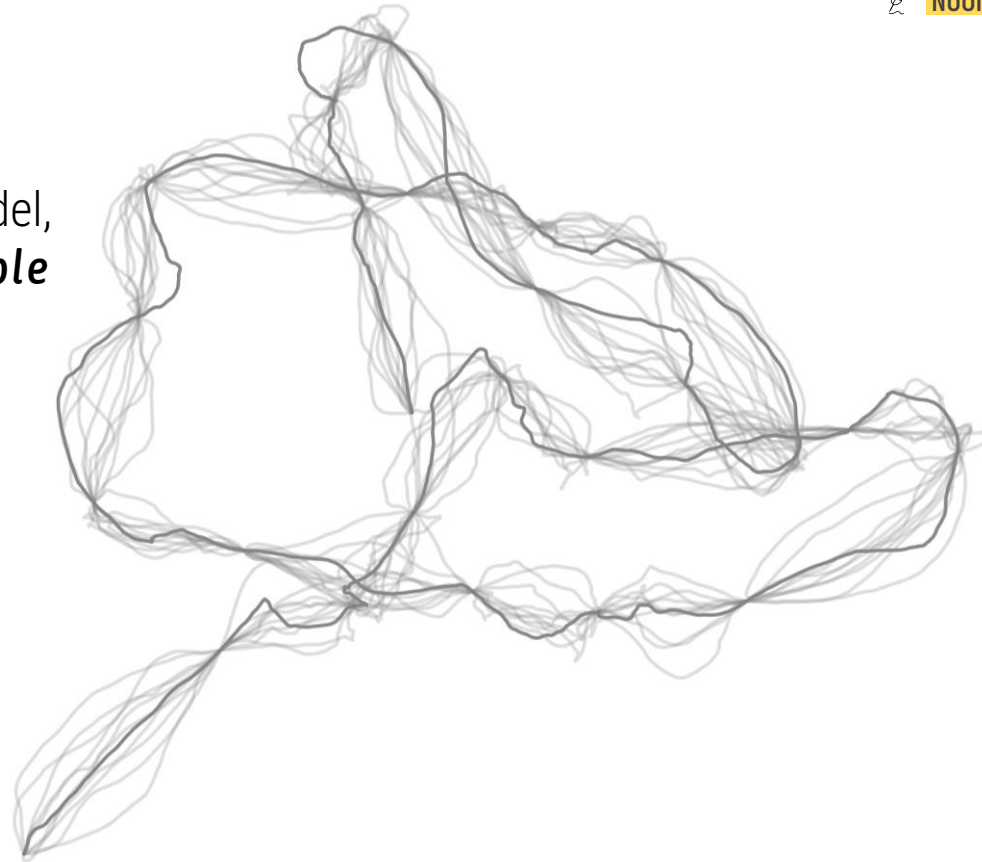
Select best-fit movement model,  
so we can repeat over **multiple  
rounds of simulations**.



## Continuous-time speed and distance (CTSD)

 Noonan *et al.* (2020)

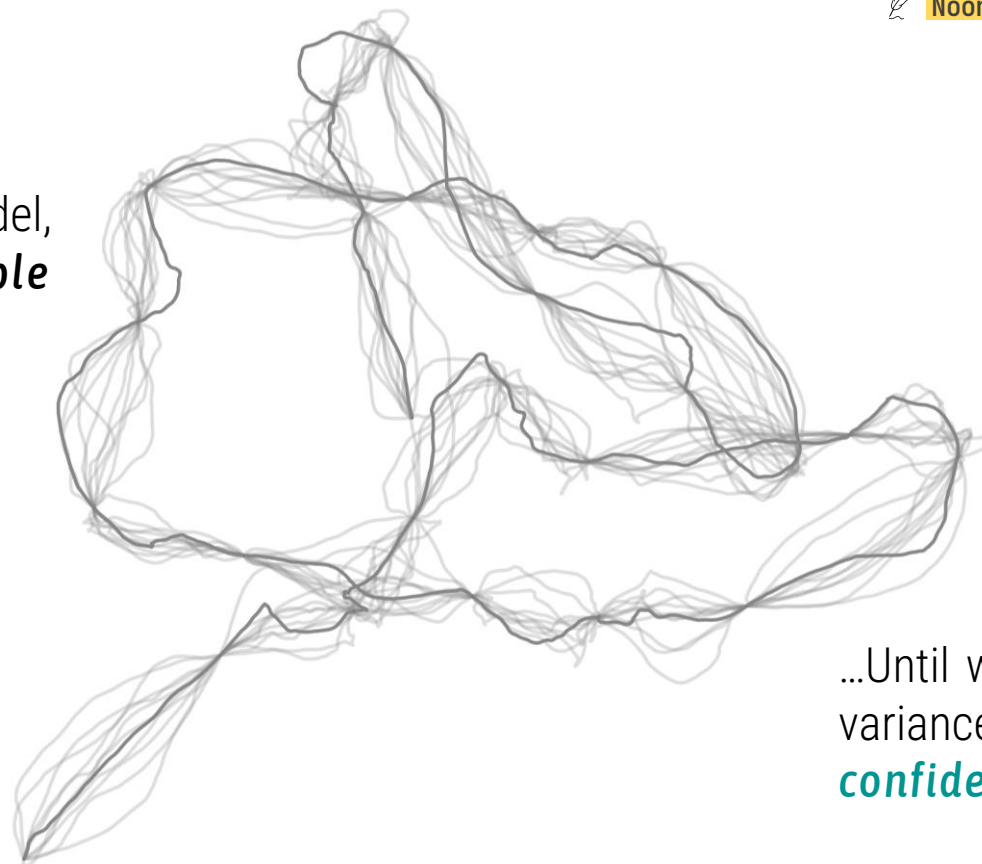
Select best-fit movement model,  
so we can repeat over **multiple  
rounds of simulations**...



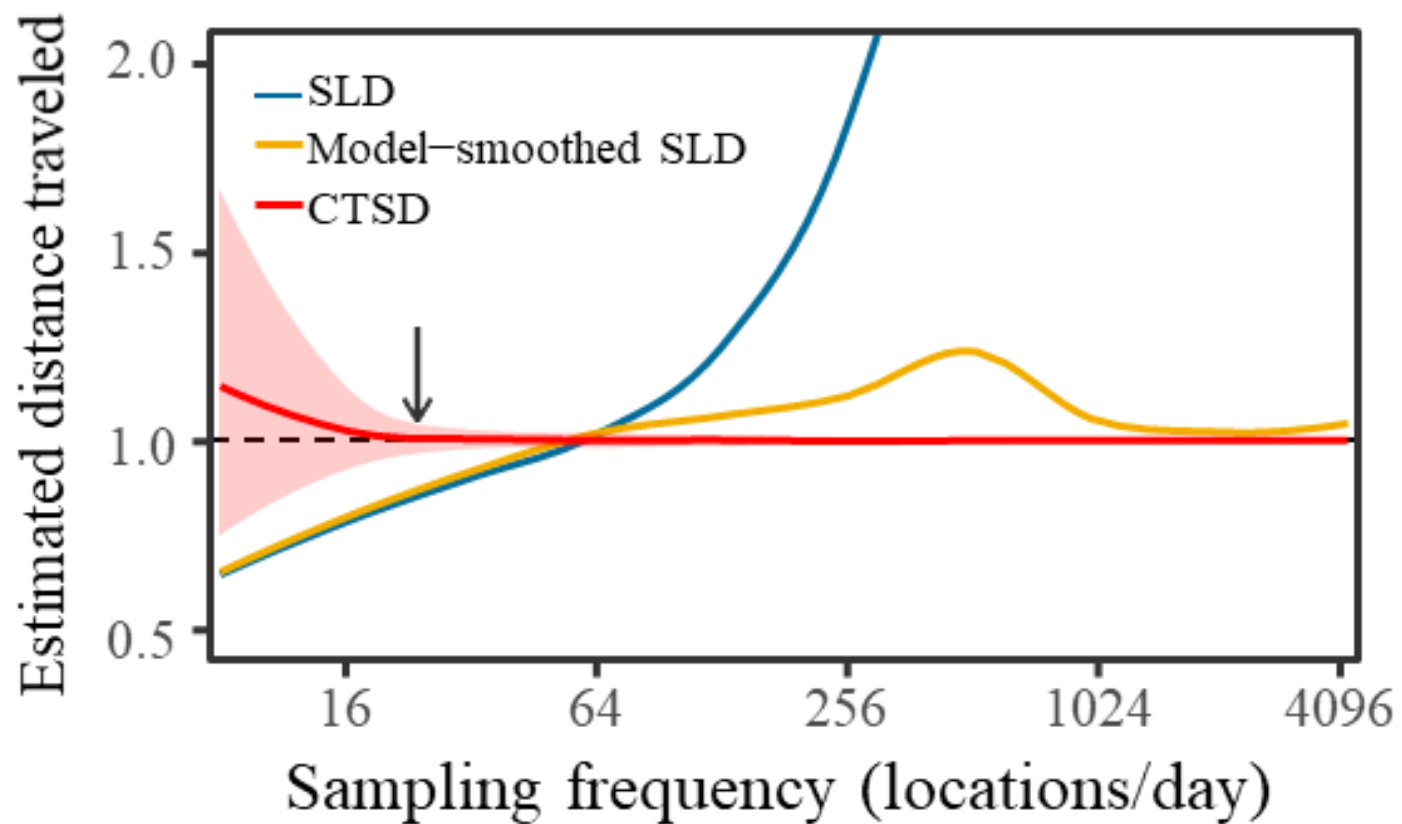
## Continuous-time speed and distance (CTSD)

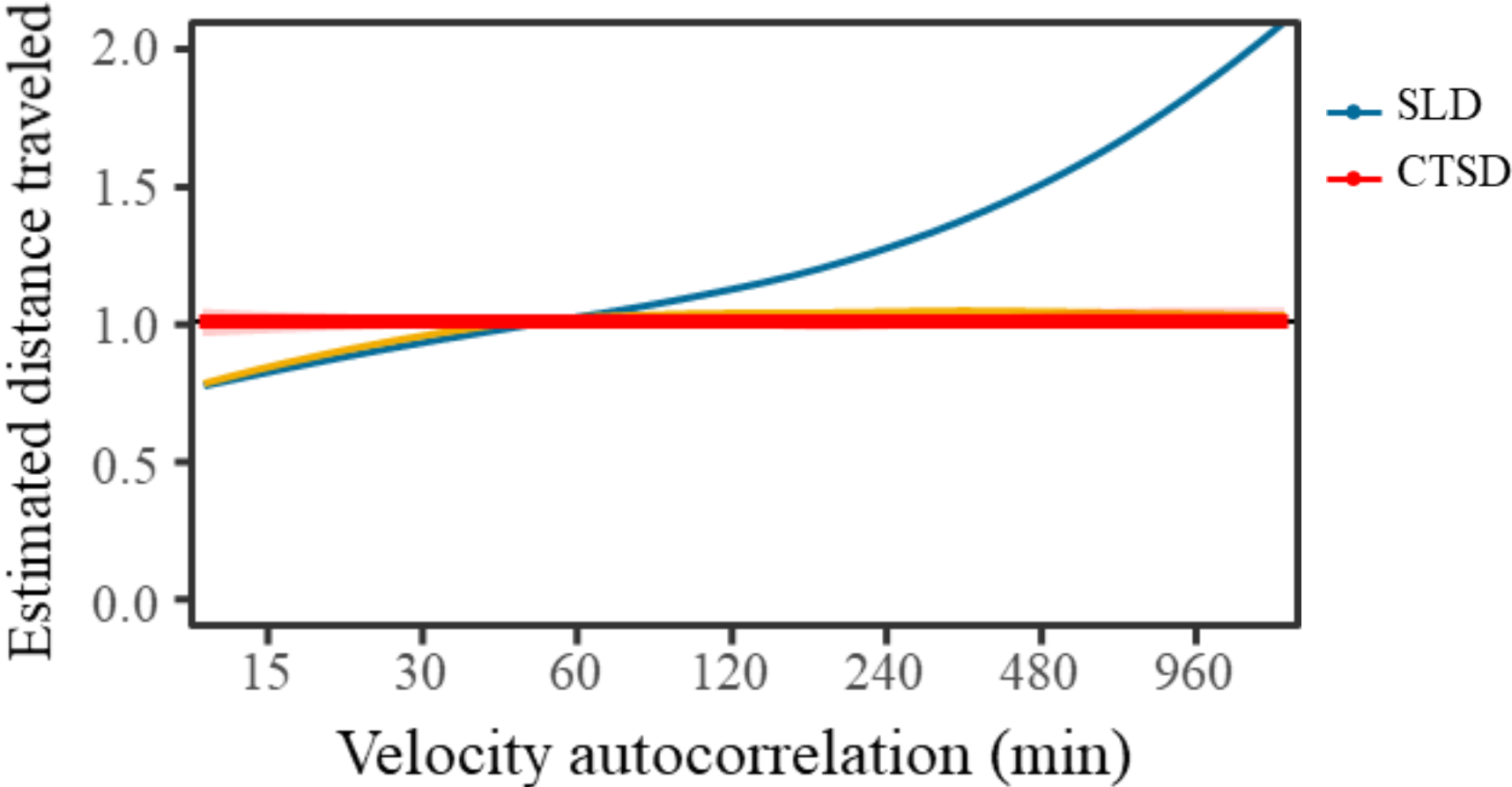
 Noonan *et al.* (2020)

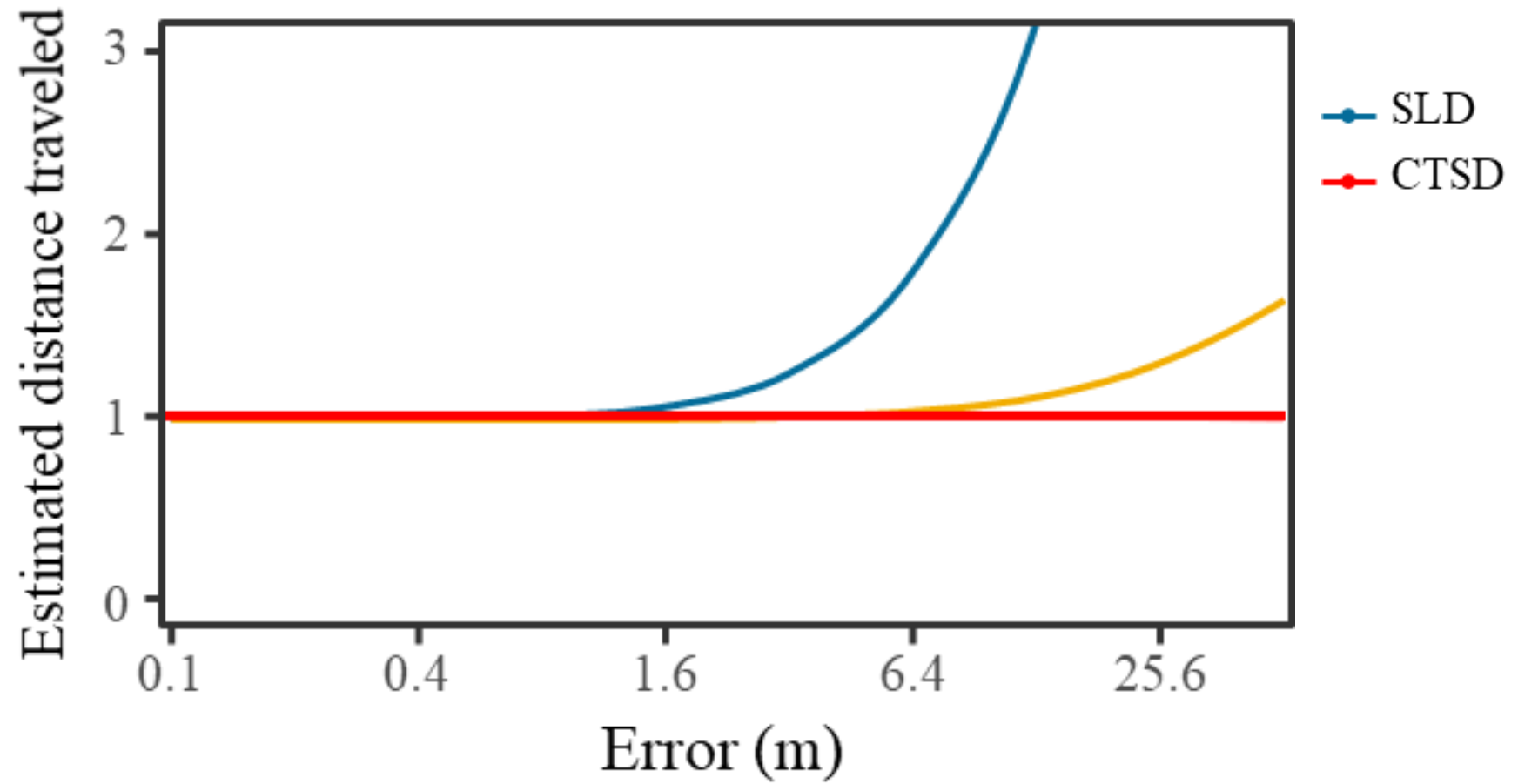
Select best-fit movement model,  
so we can repeat over **multiple  
rounds of simulations**...

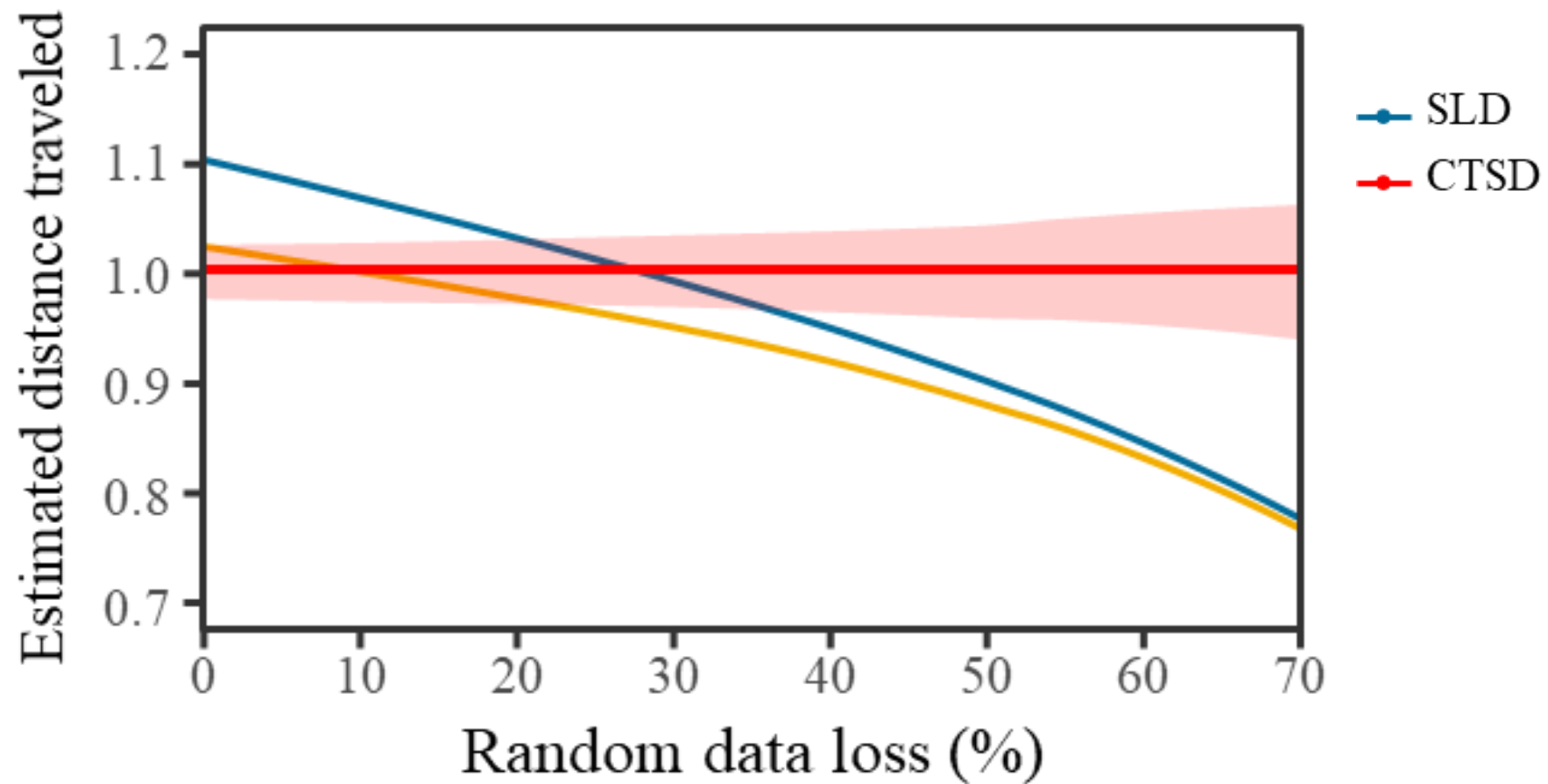


...Until we get a **point estimate**, and  
variance around the estimate (for the  
**confidence intervals**).





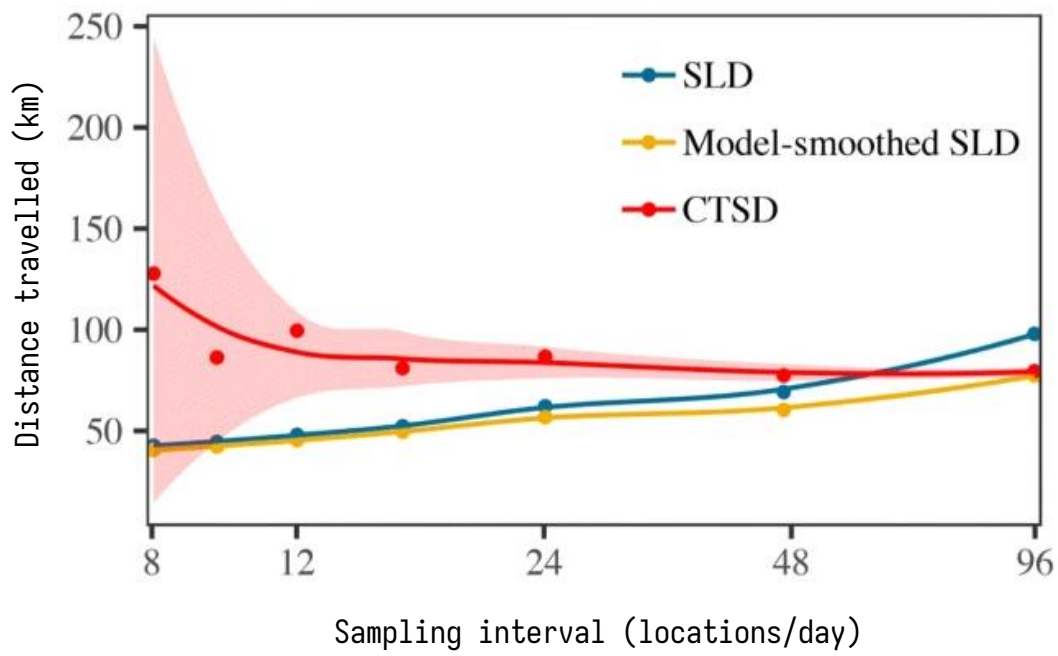
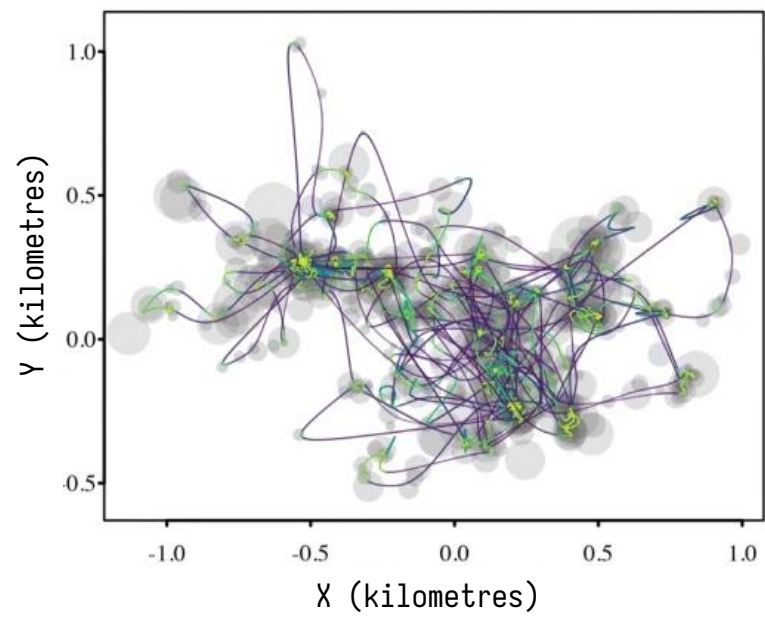






Sampling frequency (max)

1 fix every 15 minutes



Chuck Homler



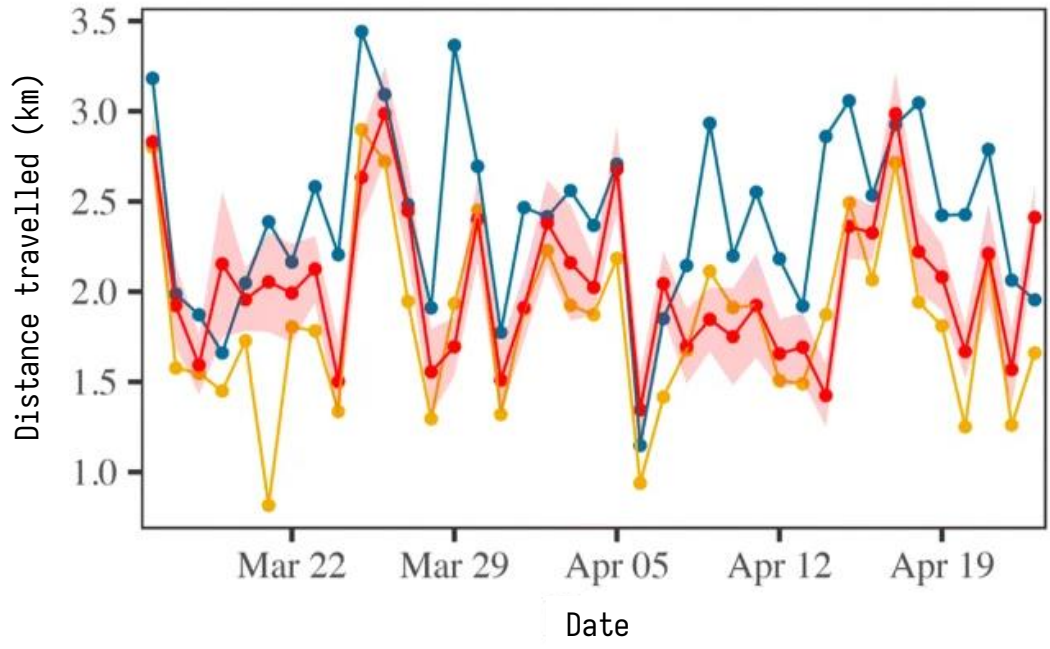
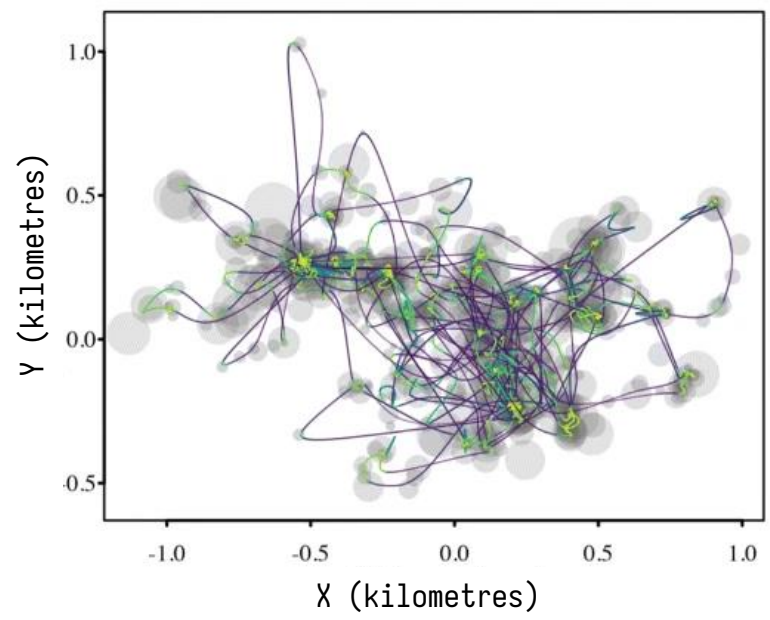
**White-nosed coati**  
(*Nasua narica*)





Sampling frequency (max)

1 fix every 15 minutes



Chuck Homler



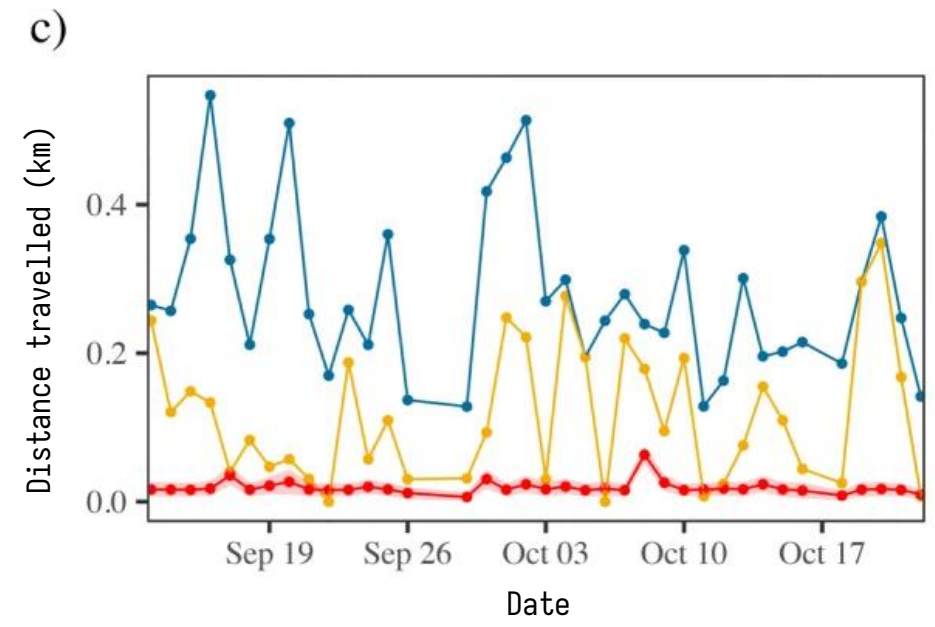
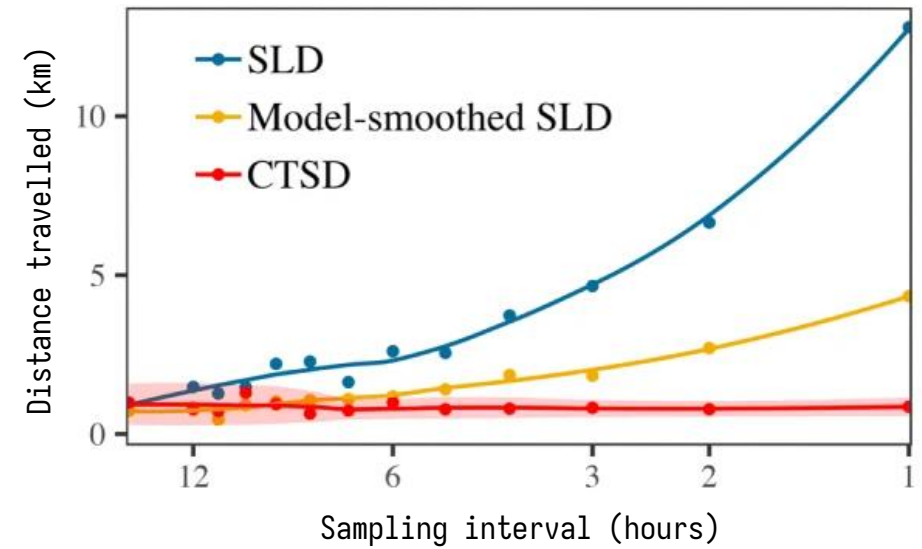
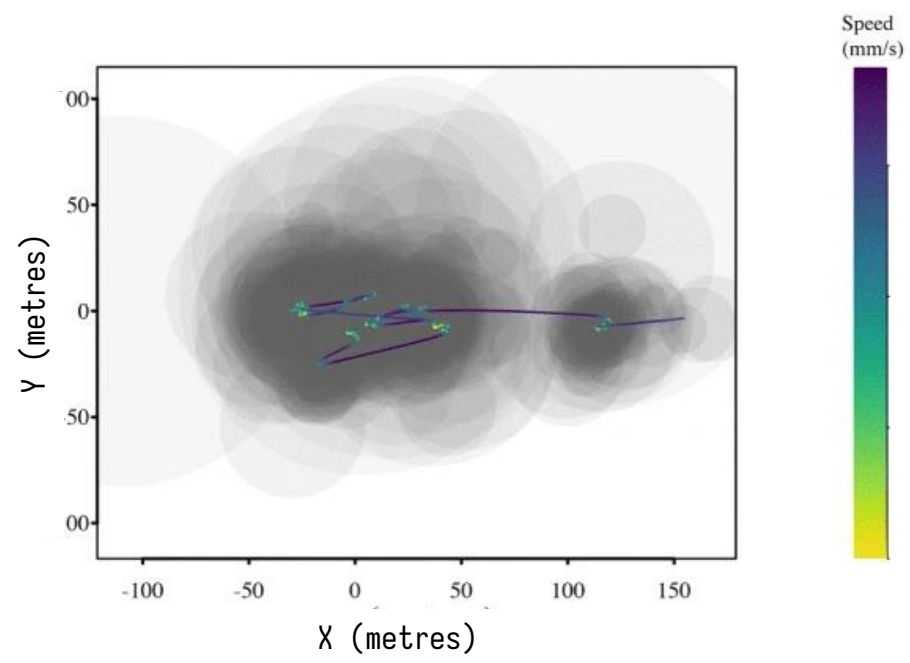
**White-nosed coati**  
(*Nasua narica*)



# Wood turble

(*Glyptemys insculpta*)

EN





*To keep in mind...*

