

# Correlation, Causation, and Causal networks

FW4001 Biometry

Department of Fisheries, Wildlife and Conservation Biology



# Learning objectives

1. Gain a deeper appreciation for why correlation (or association) is not the same as causation
2. Discover basic rules that allow one to determine dependencies (correlations) among variables from an assumed causal network
3. Understand how causal networks can be used to inform the choice of variables to include in a regression model

# Causation versus correlation

*Knowing what causes what makes a big difference in how we act. If the rooster's crow causes the sun to rise we could make the night shorter by waking up our rooster earlier and make him crow - say by telling him the latest rooster joke. - Judea Pearl (1936-), computer scientist*

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Regression coefficients change depending on what other variables are included.

# Regression and Causal Mechanisms

Often, we want to interpret models as capturing **causal mechanisms** so we can say what will happen if we **intervene** in the system:

- Will taking a daily vitamin improve long-term health?
- Will increasing the pay of teachers or reducing class size boost student performance?
- Will increasing taxes on the rich cause companies to relocate?
- Will we decrease deer population size if we institute an Earn-a-buck regulation?

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- The National Park Service commissioned a study to ask if fewer birds would have died from collisions had a bridge in Hastings MN been built differently.

These questions involve **counterfactuals** = something that did not happen, but would have happened if something had been different.

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Will taking a daily vitamin improve our long-term health?

People that take vitamins may have better health outcomes, but they may also...

- Exercise more
- Eat healthier
- Drive more cautiously

## Interventions: Direct and Indirect Effects

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Increasing taxes may allow a state to invest more in their schools.

- direct effect (negative) due to increased taxes
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Predicting the effect of an intervention requires something more complex...

# Campaign Spending: Correlation vs. Causation

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Campaign spending data from US Congressional elections

- Increased spending by those running for re-election (incumbents) is associated with lower vote percentages
- Does increased spending cause the incumbent to lose votes?
- Does the incumbent spend more when elections are tight?

# Causal Networks

**Causal network** = Hypothetical model of how the system works

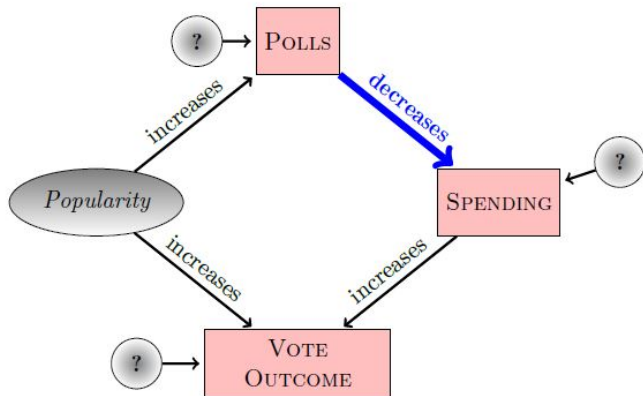


Figure 17.4: A hypothetical causal network describing how campaign spending by an incumbent candidate for political office is related to the vote outcome.



# Links and Nodes

Nodes: represent variables or components in a system

- Boxes = observed
- Ellipses = not observed (latent)
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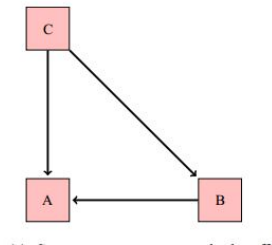
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Links: connections between nodes

- arrows = causal mechanistic connections
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Circles (things outside of the system) are said to be **exogenous**. Shapes with arrows pointing to them are influenced by things inside the system and are said to **endogenous**.

# Direct, indirect, and total effects



- A **direct effect** is one that is represented by a path between two nodes (without consideration of any intermediate nodes):  $C \rightarrow A$
- An **indirect effect** is one that connects two nodes, but where we also consider an intermediate node:  
 $C \rightarrow B \rightarrow A$ .  $B$  is called a **mediator** variable.
- The **total effect** is the sum of direct and indirect effects

# Using Simulation to Explore Campaign Spending

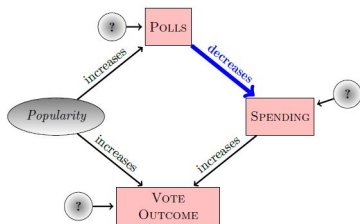


Figure 17.4: A hypothetical causal network describing how campaign spending by an incumbent candidate for political office is related to the vote outcome.

```
nsamps <- 435 # number of observations
popularity <- runif(nsamps, min=15, max=85)
polls <- popularity + rnorm(nsamps, sd=3)
spending <- 100 - polls + rnorm(nsamps, sd=10)
vote <- 0.75*popularity + 0.25*spending + rnorm(nsamps, sd=5)
votedat<-data.frame(popularity=popularity,
                    polls=polls, spending=spending, vote=vote)
```

# Linear Regression

```
fit.1<-lm(vote~spending, data=votedat)
summary(fit.1)
```

Call:

```
lm(formula = vote ~ spending, data = votedat)
```

Residuals:

Min	1Q	Median	3Q	Max
-31.771	-5.576	0.489	5.777	29.270

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	64.73715	0.99237	65.23	<2e-16 ***
spending	-0.31281	0.01844	-16.96	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.54 on 433 degrees of freedom

Multiple R-squared: 0.3992, Adjusted R-squared: 0.3978

F-statistic: 287.7 on 1 and 433 DF, p-value: < 2.2e-16

# What happens when we include polls?

```
fit2<-lm(vote~spending+polls, data=votedat)
summary(fit2)
```

Call:

```
lm(formula = vote ~ spending + polls, data = votedat)
```

Residuals:

Min	1Q	Median	3Q	Max
-26.2915	-3.6497	0.2508	3.5702	16.3300

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-0.41055	2.80020	-0.147	0.884
spending	0.27467	0.02738	10.031	<2e-16 ***
polls	0.72693	0.03039	23.922	<2e-16 ***

---

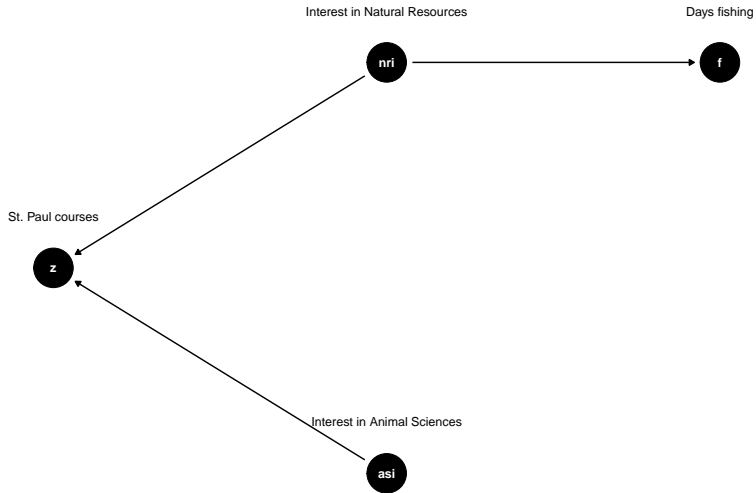
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.607 on 432 degrees of freedom

Multiple R-squared: 0.7416, Adjusted R-squared: 0.7404

F-statistic: 619.8 on 2 and 432 DF, p-value: < 2.2e-16

Consider the following DAG:





I've simulated data using these assumptions (note interest in nutrition and fishing are not causally connected):

```
# Set seed of random number generator
set.seed(1040)
# number of students
n <- 5000
# Interest in animal sciences
asi <- runif(n, 0, 10)
# Interest in natural resources
nri <- runif(n, 0, 10)
# Number of days fishing
f <- rpois(n, lambda=nri)
# Indicator variable (taking classes on St. Paul campus?)
p <- exp(-5 + 2*asi + 2*nri)/(1+exp(-5 + 2*asi + 2*nri))
z <- rbinom(n, 1, prob=p)
# Create data set
dagdata<-data.frame(animalsci.interest=asi, natresource.interest=nri,
```

## Fishing is unrelated to interest in the animal sciences

```
mod1 <- lm(fishing ~ animalsci.interest, data=dagdata)
summary(mod1)
```

```
##
## Call:
## lm(formula = fishing ~ animalsci.interest, data = dagdata)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.0049 -2.9686 -0.0049  2.0640 15.9993
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    4.926949   0.103496   47.60  <2e-16 ***
## animalsci.interest 0.007842   0.017838    0.44    0.66
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.646 on 4998 degrees of freedom
## Multiple R-squared:  3.867e-05, Adjusted R-squared: -0.0001614
## F-statistic: 0.1933 on 1 and 4998 DF, p-value: 0.6602
```

What if we “adjust” for whether the student is taking classes on the St. Paul campus?

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```
mod2 <- lm(fishing ~ animalsci.interest + stpaulcampus, data=dagdata)
summary(mod2)
```

```
##
## Call:
## lm(formula = fishing ~ animalsci.interest + stpaulcampus, data = da
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.4351 -2.9100 -0.3057  2.1591 16.1726
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      1.08727    0.26916   4.040 5.44e-05 ***
## animalsci.interest -0.06702    0.01810  -3.704 0.000215 ***
## stpaulcampus       4.37013    0.28389  15.394 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.563 on 4997 degrees of freedom
## Multiple R-squared:  0.04531,    Adjusted R-squared:  0.04493
## F-statistic: 118.6 on 2 and 4997 DF,  p-value: < 2.2e-16
```

# Confused?

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Should we adjust or not? It depends on one's hypothetical model of the system (i.e., the causal network)!

# Pathways

A **pathway** between two nodes is a route between them (may pass through other nodes along the way)

- **Correlating pathway** follows in the direction of causal links
- **Non-correlating pathway** one that does not follow in the direction of causal links.



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- **Witness:**  $A \Rightarrow C \Leftarrow B$

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- **Witness:**  $A \Rightarrow C \Leftarrow B$

Including  $C$  **opens** the pathway, which is otherwise blocked.

# Pathways

A pathway between two variables ( $A$  and  $B$ ) is correlating if there is a node on the pathway from which you can get to both variables.

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What about  $A \Leftarrow C \Leftarrow D \Leftarrow B$ ?

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Correlating!

# Circular Pathways, Correlation

**Recurrent** (closed loop):  $A \Rightarrow B \Rightarrow C \Rightarrow A$



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$A \Leftrightarrow B$  means that there is a **non-causal** connection between  $A$  and  $B$ .

# Circular Pathways, Correlation

**Recurrent** (closed loop):  $A \Rightarrow B \Rightarrow C \Rightarrow A$

Raise questions of “when”... we won't deal with these

$A \Leftrightarrow B$  means that there is a **non-causal** connection between  $A$  and  $B$ .

This must be because there is some unobserved variable,  $U$  producing the correlation:

- $A \Leftarrow U \Rightarrow B$

# Blocking Back Door Pathways

To determine whether to adjust or not, consider these rules and follow the pathways between variables.

- **Block correlating pathways: include** at least one of the interior nodes on the pathway as a covariate
- **DO not unblock non-correlating pathways: exclude** all the interior nodes on the pathway; do not include any of them as covariates.

# Back to Polls

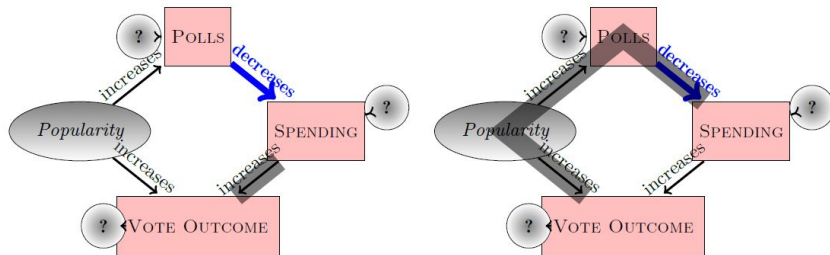
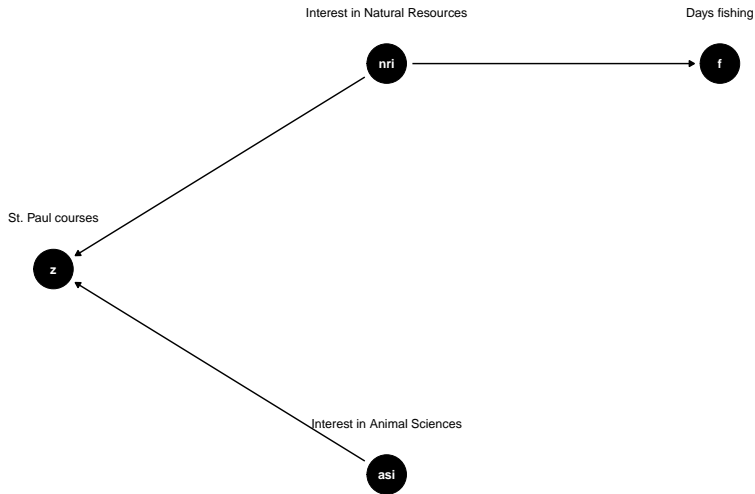


Figure 17.8: Pathways connecting **spending** to **vote outcome**. Both of these are correlating pathways.

# And fishing/nutrition example



# Selection Bias

What happens if we only survey students on the St. Paul campus?

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Selecting only individuals taking courses on the St. Paul campus has the same effect as adjusting for the variable in the regression.



# Selection Bias

```
summary(lm(fishing~animalsci.interest,  
           data=subset(dagdata, stpaulcampus==1)))
```

Call:

```
lm(formula = fishing ~ animalsci.interest, data = subset(dagdata,  
  stpaulcampus == 1))
```

Residuals:

Min	1Q	Median	3Q	Max
-5.4340	-2.9801	-0.3135	2.2062	16.1717

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	5.45626	0.10864	50.224	< 2e-16 ***
animalsci.interest	-0.06680	0.01841	-3.629	0.000287 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.619 on 4822 degrees of freedom

Multiple R-squared: 0.002724, Adjusted R-squared: 0.002518

F-statistic: 13.17 on 1 and 4822 DF, p-value: 0.000287

# Some (Summary) Comments on Regression Modeling

- Coefficients may change sign when we include or exclude other explanatory variables

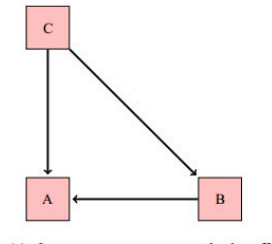
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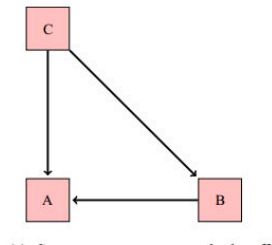
- Coefficients may change sign when we include or exclude other explanatory variables
- Whether we should include or exclude a particular variable depends on our hypothetical causal network
- Often useful to explore a few different hypothetical causal models, rather than fit (and average) over many models

# Estimates of Direct and Indirect Effects



What if we want to estimate the direct effect of C on A?

# Estimates of Direct and Indirect Effects

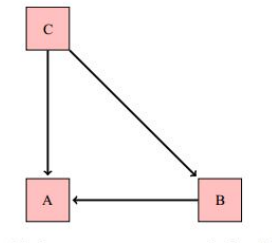


What if we want to estimate the direct effect of C on A?

Pathways:

- $C \Rightarrow A$  (correlating), and the effect of interest.

# Estimates of Direct and Indirect Effects

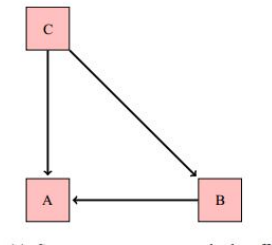


What if we want to estimate the direct effect of  $C$  on  $A$ ?

Pathways:

- $C \Rightarrow A$  (correlating), and the effect of interest.
- $C \Rightarrow B \Rightarrow A$  (correlating), an indirect effect of  $C$  on  $A$  that is mediated by  $B$

# Estimates of Direct and Indirect Effects



What if we want to estimate the direct effect of C on A?

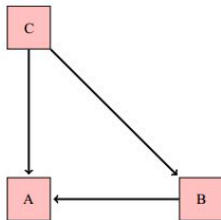
Pathways:

- $C \Rightarrow A$  (correlating), and the effect of interest.
- $C \Rightarrow B \Rightarrow A$  (correlating), an indirect effect of C on A that is mediated by B Include B to block!

$$\text{lm}(A \sim C + B)$$

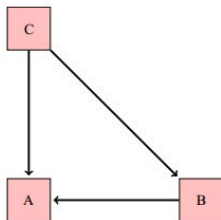


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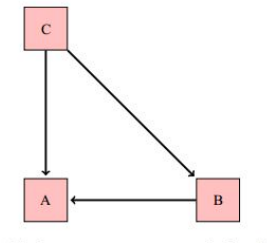


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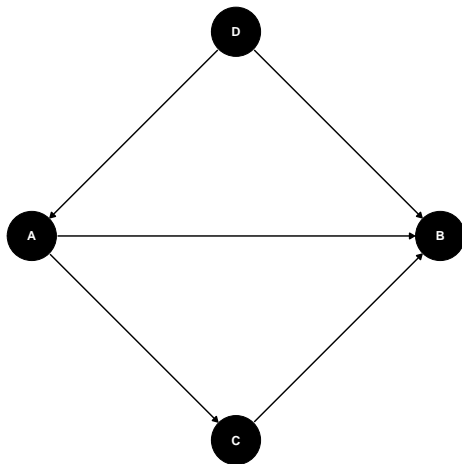
Pathways:

- $C \Rightarrow A$  (correlating)
- $C \Rightarrow B \Rightarrow A$  (correlating)

In this case, we would **not** want to include B as it would block the second pathway representing an indirect effect of C on A.

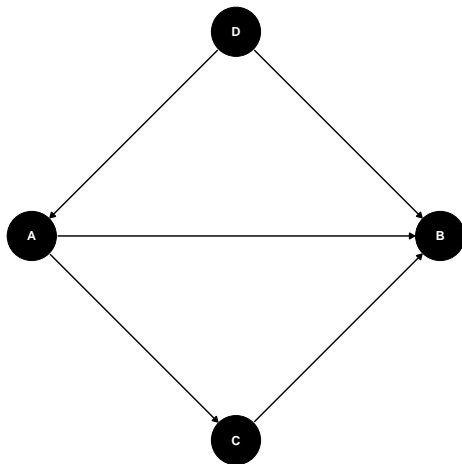
$lm(A \sim C)$

## Pathways and Choice of Covariates



Goal: study the direct effect of  $A$  on  $B$ .

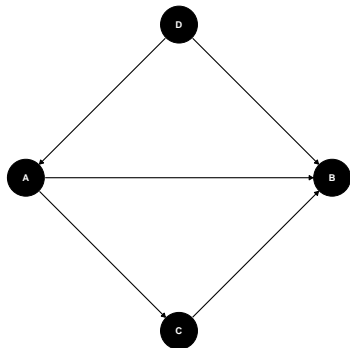
## Pathways and Choice of Covariates



Goal: study the direct effect of  $A$  on  $B$ .

Need to block all other pathways between  $A$  and  $B$ .

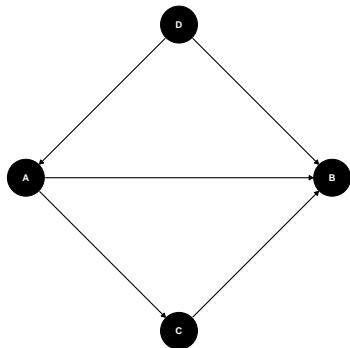
# Pathways and Choice of Covariates



Pathways:

- $A \Rightarrow B$  (correlating), effect of interest.

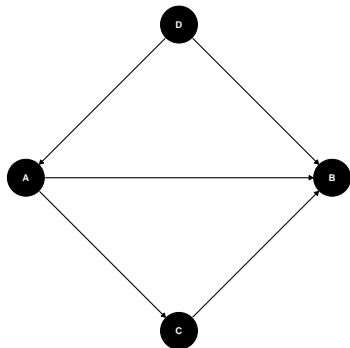
# Pathways and Choice of Covariates



Pathways:

- $A \Rightarrow B$  (correlating), effect of interest.
- $B \Leftarrow D \Rightarrow A$

# Pathways and Choice of Covariates

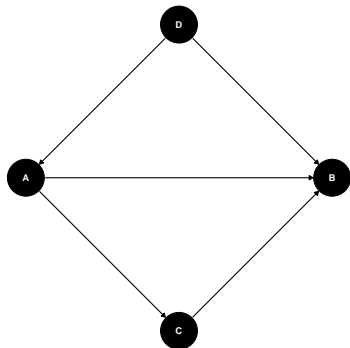


Pathways:

- $A \Rightarrow B$  (correlating), effect of interest.
- $B \Leftarrow D \Rightarrow A$  (correlating)



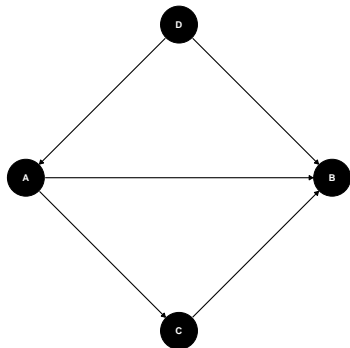
# Pathways and Choice of Covariates



Pathways:

- $A \Rightarrow B$  (correlating), effect of interest.
- $B \Leftarrow D \Rightarrow A$  (correlating) Include D to block!

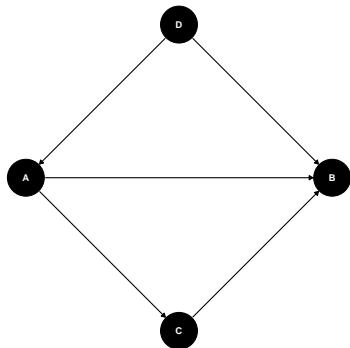
# Pathways and Choice of Covariates



Pathways:

- $A \Rightarrow B$  (correlating), effect of interest.
- $B \Leftarrow D \Rightarrow A$  (correlating) Include D to block!
- $A \Rightarrow C \Rightarrow B$

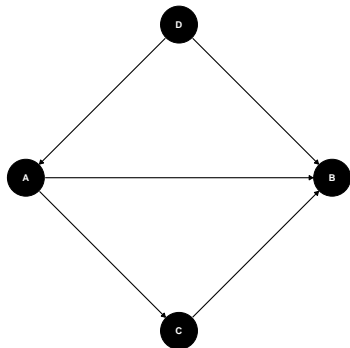
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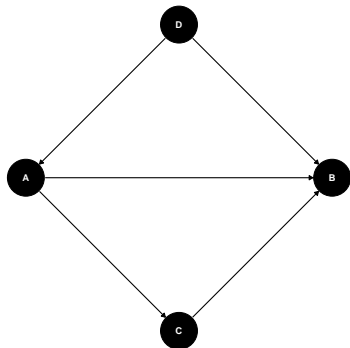
# Pathways and Choice of Covariates



Pathways:

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- $A \Rightarrow C \Rightarrow B$  (correlating) Include  $C$  to block!

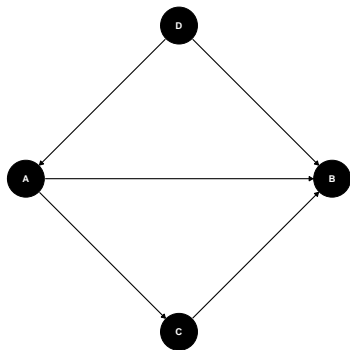
# Pathways and Choice of Covariates



Pathways:

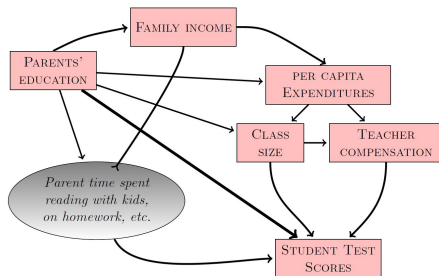
- $A \Rightarrow B$  (correlating), effect of interest.
- $B \Leftarrow D \Rightarrow A$  (correlating) Include  $D$  to block!
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$\text{lm}(B \sim A + C + D)$



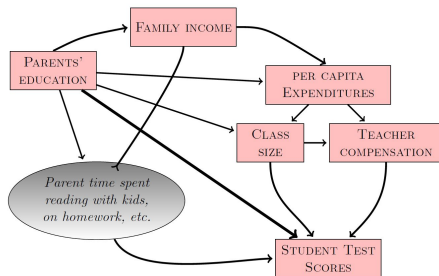
To study the **total effect** of  $A$  on  $B$ , we would use  $\text{lm}(B \sim A + D)$ .

# Student Test Scores



Effect of per-capita expenditures on Student Test Scores:

# Student Test Scores

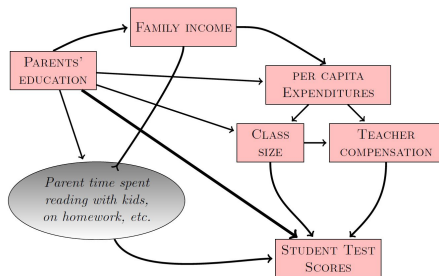


Effect of per-capita expenditures on Student Test Scores:

- Include Class Size?
- Include Teacher Compensation?



# Student Test Scores

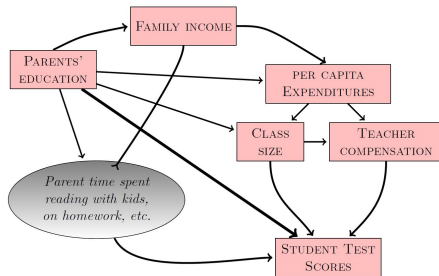


Effect of per-capita expenditures on Student Test Scores:

- Include Class Size?
- Include Teacher Compensation? (No and No)

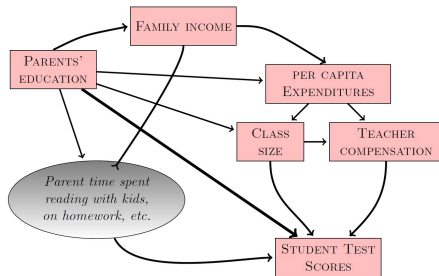
Per-capita expenditures  $\Rightarrow$  (Class Size, Teacher Compensation)  
 $\Rightarrow$  Test Scores

# Student Test Scores



Include Parents' Education?

# Student Test Scores

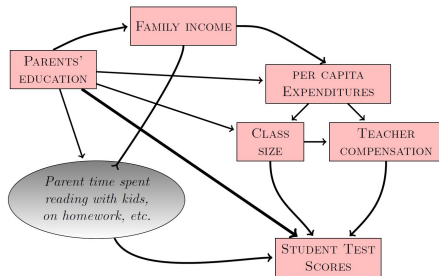


Include Parents' Education?

Consider the path:

Per-capita expenditures  $\leftarrow$  Parents' education  $\Rightarrow$  Test scores

# Student Test Scores



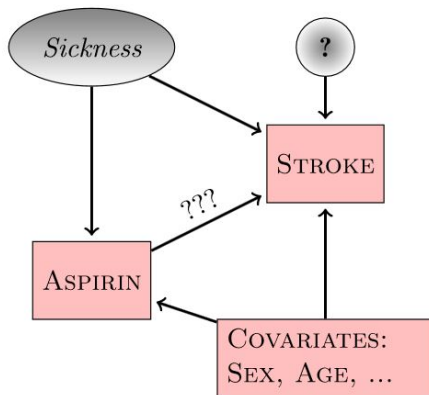
Include Parents' Education?

Consider the path:

Per-capita expenditures  $\leftarrow$  Parents' education  $\Rightarrow$  Test scores

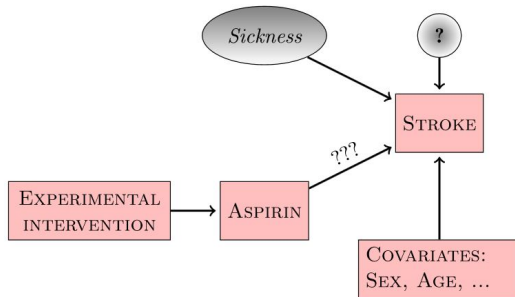
Include Parents' education to block the path!

# Experiments



How do we measure “sickness” to block the backdoor pathway?

# Experiments revisited



Randomly assigning aspirin (treatment) eliminates the connection between Sickness and Aspirin!