

# Investment Funds Risks

University of Luxembourg

Juan F. Imbet *Ph.D.*

## About Me

- Assistant Professor of Finance at Paris Dauphine University - Paris Sciences et Lettres.
- Ph.D. in Finance from Pompeu Fabra Universit and the Barcelona School of Economics.
- External Member of the Institute for Advanced Studies in Luxembourg.
- Researcher in Financial Economics and Asset Management.
- Instructor of courses on Data Science and Finance (Python).
- [juan.imbet@dauphine.psl.eu](mailto:juan.imbet@dauphine.psl.eu)

# Outline

- 25/11/2024: Active Investment
- 26/11/2024: Equity Strategies
- 27/11/2024: Asset Allocation and Macro Strategies
- 29/11/2024: Arbitrage Strategies

## References

- Pedersen L. H. (2019). Efficiently Inefficient: How Smart Money Invests and Market Prices Are Determined. Princeton University Press.

## Requirements

- Statistics: Confidence intervals, t-tests, regressions.
- Asset Pricing: CAPM, Fama-French 3-factor model.
- Any programming language (Python, R, Matlab).
- Basic Finance: Risk, Return, Portfolio Theory.

# Part 1: Active Investment

# Understanding Hedge Funds

# Introduction

- There are many types of active investors. Some of them are classified as **Hedge Funds**
- Hedge funds are investment pools that are relatively unconstrained in what they do.
- They are relatively unregulated (for now), charge very high fees, and will not necessarily give you your money back when you want it.
- They are supposed to make money all the time, and when they fail at this, their investors tend to redeem.
- They are generally run for rich people by rich people. (e.g. clients in Geneva and run in Greenwich Connecticut).

## Hedge Funds vs Mutual Funds

- Hedge funds have a lot of freedom in the trading that they do, as well as limited requirements.
- In exchange for this freedom they are restricted in how they can raise money.
- In terms of freedom, hedge funds can use leverage, short-selling, derivatives, and incentive fees.
- Hedge fund investors must be accredited investors (they need to be rich).
- The first formal hedge fund is believed to have been a fund created by Alfred Winslow Jones in 1949.
- In the 1990s the hedge fund industry saw a dramatically increased interest as institutional investors began to embrace hedge funds.



## Objectives and Fees

- The objective of asset managers is to add value tot heir investors by making money relative to a becnhmark.
- Mutual funds typically have a market index as a benchmark.
- Hedge funds are not trying to beat the stock market but, ather, trying to make money in any environment.
- This is where the **Hedge** term comes from.
- E.g. hedge fund investors would normally punish a hedge fund which is down by 10% even if the stock market is down by 20%.

## Objectives and Fees

- While fees vary greatly across funds, the classic hedge fund fee structure has been "2 and 20". A 2% management fee paid regardless of returns, and a 20% performance fee.
- A hedge fund's performance fee is often subject to a high-water mark, which means that the fund must make up for losses before it can collect a performance fee.
- This means that it normally only collects profits when it reaches a new high in terms of the value of the fund.

# Performance

- A number of famous hedge fund managers have produced spectacular returns over the years. But these managers do not represent the typical hedge fund. Are they good or just lucky?
- This question is very hard to answer for several reasons. First, the data on hedge fund returns are rather poor as they are available only over a limited time period and subject to important **biases**,
- Hedge funds report their returns to promote themselves in many cases.
- When they decide to start reporting information to data providers, the information is backfilled. This means that they might only decide to report their returns when they have a good track record.

## Organization of Hedge Funds

Hedge funds are contractually organized in different ways, but the typical **master-feeder** structure (in the US, but in many cases also in Europe) is as follows:

# Explanation

- The structure is not as complicated as it looks.
- Contractually there is a distinction between the *fund*, where the money is, and the *management company*, where the traders and other staff are.
- An investor in a hedge fund invests in a *feeder fund*, whose sole purpose in life is to invest in the *master fund* where the trading is done.
- This structure is useful since it allows the manager to focus on running a single master fund while at the same time creating different investment products (the feeder funds) for different types of investors.
- Typically US investors prefer a feeder fund that is registered in the US, while non residents prefer an offshore feeder fund.
- These offshore funds are typically domiciled in the Cayman Islands.
- For different currencies, there can be different feeder funds each one hedged to the currency of the investor.

## Explanation

- This feeder/master structure is also useful for risk management. If the master fund has a volatility of 20%, the feeder fund can have half the volatility by investing half the money in the master fund and the other half in money market funds.
- The master fund has a pool of money, and this is where all the trades are carried out.
- The fund has an Investment Management Agreement (IMA) with the management company. The MC provides investment services, including strategy development, implementation, and trading. This is where all the employees work.
- The master fund is typically organized as a partnership, where the feeder funds are the limited partners, and the general partner is the company that owns the management company. (E.g. JP Morgan Chase and Jp Morgan Chase Investment Management).

## Explanation

- The hedge fund also contracts with agents who handle trading, custody, clearing, and other services.
- For exchange-traded instruments, the hedge fund will typically have a prime broker who will provide leverage, short-selling, and other services.

Some nomenclature:

- NYSE: New York Stock Exchange
- CME: Chicago Mercantile Exchange
- DTCC: Depository Trust & Clearing Corporation
- OCC: Options Clearing Corporation

## Hedge Funds' Role in the Economy

- Hedge funds often face criticism in the media.
- Companies do not like to see their shares shorted, since this indicates a belief that the company's share price could go down.
- Short sellers, including hedge funds, are sometimes accused of being the source of a company's problem.
- However, hedge funds play several useful roles in the economy.
- They make markets more efficient by collecting information.
- They also provide diversification to accredited investors.



# Evaluating Trading Strategies

## Performance Measures

# Alpha and Beta

- The most basic measure of trading performance is, ofcourse, the return  $R_t$  in a period  $t$ . The return is often separated into its alpha and beta (abussing notation a bit). Beta is the strategy's market exposure, while alpha is the excess return after accounring for performance due to market movements.
- Defining the excess return on top of the risk free rate  $R_t^e = R_t - R^f$

$$R_t^e = \alpha + \beta R_t^{me} + \epsilon_t$$

-where  $R_t^{me}$  is the market excess return and  $\epsilon_t$  is the residual return.

- Here beta measures the strategy's tendency to follow the market. While  $\epsilon_t$  measures the idiosyncratic return.
- The idiosyncratic return can be positive or negative but in average is zero.

# Alpha and Beta

- Knowing a strategy's beta is useful for many reasons.
- If you want to mix a hedge fund with another investment, the beta risk is not diversified away while idiosyncratic risk is.
- Furthermore, market exposure ("beta risk") is easy to obtain at very low fees, for example, by buying index funds. *You should not be paying large fees for beta risk.*
- Many hedge funds are ( or claim to be) market neutral. This means that their performance is independent of what happens in the market (i.e.  $\beta = 0$ ).
- Another use of beta is that it tells us how to make a strategy market neutral. If a strategy has a beta of 2, we can make it market neutral by shorting twice the market.

$$\text{market-neutral excess return} = \alpha + \epsilon_t$$

$$\mathbb{E}[\text{market-neutral excess return}] = \alpha$$

# Alpha and Beta

- Alpha is clearly the sexiest term in the regression.
- It is the Holy Grail all active managers seek.
- A hedge-fund's quest for alpha *defies* the Capital Asset Pricing Model (CAPM), since they would be compensated for risk that is not systematic.
- A hedge fund's alpha and beta are estimated with significant error. Hence if a hedge fund has an estimated alpha of 6%, how do we know if this is luck or skill?
- Researchers often look at the t-statistic.
- We can also compute a strategy's excess return above and beyond several risk exposures, e.g. the Fama-French 3-factor model.

$$R_t^e = \alpha + \beta R_t^{me} + \beta^{smb} R_t^{smb} + \beta^{hml} R_t^{hml} + \epsilon_t$$

## Risk-reward ratios

- As we have seen, a positive alpha is good while a negative alpha is bad.
- However, is a high positive alpha always better than a low positive alpha? Not always.
- The alpha tells you the size of the market-neutral returns that a strategy delivers, it does not say at what risk.
- Second, alpha depends on how a strategy is scaled. For instance, a twice-leveraged strategy has twice the alpha of an unlevered version.
- Risk-reward ratios resolve these issues. At a basic level, potential investors in a hedge fund want to know how the future expected excess returns compare to the risk that the hedge fund is taking.
- The Sharpe Ratio (SR) is a measure of just that (some people call it the risk adjusted return, but again this is a misnomer).

## Sharpe Ratio

$$SR = \frac{\mathbb{E}[R_t^e]}{\sigma(R_t^e)}$$

## The Information Ratio

- The SR gives the hedge fund credit for all excess returns, but we learned that some of these excess returns are due to market exposure.
- The IR addresses this by focusing on the risk-adjusted *abnormal* return, or just the risk-adjusted alpha

$$IR = \frac{\mathbb{E}[\alpha]}{\sigma(\epsilon)}$$

- If the hedge fund has a benchmark which is not the market, the IR is computed with respect to this benchmark.

## You can't eat alpha

- Suppose, for instance, that a hedge fund beats the risk-free rate by 3% at a tiny risk of 2% with a great SR of 1.5. Some investors might say, "Well, it's still just 3%. I was hoping for more return".
- Whether this is a fair criticism or not depends on several things. In particular if the low risk is long-term or short-term.
- If we suppose the risk is really that low, you can apply leverage to the strategy to achieve higher return and risk.



## alpha-to-margin (AM) ratio

$$AM = \frac{\alpha}{\text{margin}}$$

- The idea behind is to compute the return on a "maximally leveraged" version of a market neutral strategy.
- While hedge funds can apply leverage to any strategy, there is a maximum amount of leverage that depends on their margin requirements (more on this later). The maximum leverage is therefore  $1/\text{margin}$ .
- There is a close relationship between the AM ratio and the IR

$$AM = IR \times \frac{\sigma(\epsilon)}{\text{margin}}$$

## Time horizons (annualization)

- The horizon we use to compute performance/risk measures matters.
- Some of them can be annualized easily (assuming 252 trading days)

$$E[R_{\text{annualized}}^e] = 252 \times E[R_{\text{daily}}^e]$$

$$\sigma(R_{\text{annualized}}^e) = \sqrt{252} \times \sigma(R_{\text{daily}}^e)$$

$$SR_{\text{annualized}} = \sqrt{252} \times SR_{\text{daily}}$$

## Strategies seem riskier the higher the frequency

- Consider estimating the probability of having negative excess returns. Assume excess returns follow a normal distribution (not always realistic), call  $z$  the standard normal distribution

$$Pr(R^e < 0) = Pr(E[R^e] + \sigma z < 0) = Pr(z < -SR)$$

- A high frequency trader can observe very frequent losses even on a highly profitable strategy.

## High Water Mark

- The highest price (cumulative return) achieved in the past

$$HWM_t = \max_{s \leq t} P_s$$

## Drawdown

$$DD_t = \frac{HWM_t - P_t}{HWM_t}$$

## Maximum Drawdown

$$MDD_T = \max_{t \leq T} DD_t$$

## Adjusting for Stale Prices

- Hedge funds' investments are often illiquid, and their prices are not always available.
- How would you compute a beta if data is not available at every frequency?

$$R_t^e = \alpha^{\text{adjusted}} + \beta_0 R_t^{me} + \beta_1 R_{t-1}^{me} + \dots + \beta_k R_{t-k}^{me} + \epsilon_t^{\text{adjusted}}$$

$$\beta^{\text{all-in}} = \beta_0 + \beta_1 + \dots + \beta_k$$

- Adjust ratios accordingly.

$$IR^{\text{adjusted}} = \frac{\alpha^{\text{adjusted}}}{\sigma(\epsilon^{\text{adjusted}})}$$

# Finding and Backtesting Investment Strategies

## Good Strategies are Hard (but not impossible) to Find

- Production of information.
- Access to information (legal vs illegal).
- Behavioral biases and limits to arbitrage.
- Compensation for liquidity.
- Compensation for funding costs.

## How to backtest a strategy

- Universe
- Signals
- Trading Rules
- Time Lags
- Portfolio Rebalancing
- Enter/Exit Rules



## identifying good signals.

Consider a signal  $S_t$  that predicts returns

$$R_{t+1}^e = a + bS_t + \epsilon_{t+1}$$

OLS estimator

$$\hat{b} = \frac{\sum_{t=1}^T (S_t - \bar{S}) R_{t+1}}{\sum_{t=1}^T (S_t - \bar{S})^2} = \sum_t x_t R_{t+1}$$

where

$$x_t = k \times (S_t - \bar{S})$$

$$k = \frac{1}{\sum_{t=1}^T (S_t - \bar{S})^2}$$

## Identifying good signals

- In a time series regression the OLS estimate of the regression gives you the cumulative return of a timing strategy.
- For the strategy to be profitable, it must be positive.
- However, it only provides evidence insample, since it assumes that the unconditional mean of the signal is known in advance.

## Cross sectional signals

$$R_{t+1}^i = a + bS_t^i + \epsilon_{i,t+1}$$

Fix a date  $t$  and estimate the regression for all assets  $i$  in the universe.

$$\hat{b}_t = \frac{\sum_{i=1}^N (S_t^i - \bar{S}) R_{t+1}^i}{\sum_{i=1}^N (S_t^i - \bar{S})^2} = \sum_i x_t^i R_{t+1}^i$$

where

$$x_t^i = k \times (S_t^i - \bar{S})$$
$$k = \frac{1}{\sum_{i=1}^N (S_t^i - \bar{S})^2}$$

## Fama MacBeth regressions use the same concept

$$\hat{b} = \sum_t \hat{b}_t / T$$

$$\sigma(\hat{b}) = \sqrt{\sum_t (\hat{b}_t - \hat{b})^2 / (T - 1)}$$

- The SR of the security selection strategy is

$$SR = \frac{\hat{b}}{\sigma(\hat{b})}$$

which is related to the  $t$ -statistic of the cross-sectional regression.

$$t = \sqrt{T} \frac{\hat{b}}{\sigma(\hat{b})}$$

## Portfolio Management - Basics

- Consider the following static portfolio allocation problem:
  - Universe of  $i \in \{1, \dots, N\}$  tradeable assets with random return  $r_i$ .
  - Finite first and second moments:  $\mathbb{E}[r_i] < \infty, \mathbb{E}[r_i^2] < \infty$ .
  - No transaction costs or short-sell restrictions.
  - Investors maximize a utility function  $U : \mathbf{R}^N \rightarrow \mathbf{R}$  dependent on moments of  $r_i$  and possibly other characteristics.

## Example

$$\max_{\theta} \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta$$

Subject to  $\theta' \mathbf{u} = 1$

where

$$\theta = \begin{bmatrix} \theta_1 \\ \vdots \\ \theta_N \end{bmatrix}, \quad \mathbf{u} = \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix}, \quad \mu = \begin{bmatrix} \mathbb{E}[r_1] \\ \vdots \\ \mathbb{E}[r_N] \end{bmatrix}, \quad \Sigma = \begin{bmatrix} \sigma_1^2 & \dots & \sigma_{1N} \\ \vdots & \ddots & \vdots \\ \sigma_{N1} & \dots & \sigma_N^2 \end{bmatrix}.$$

Parameter  $\gamma$  captures risk aversion.

## Closed Form Solution

The problem allows for a closed-form solution ( $\gamma > 0$ ):

$$\mathcal{L} = \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta - \lambda (\theta' \mathbf{u} - 1)$$

$$\mathcal{L}_\theta = \mu - \gamma \Sigma \theta - \lambda \mathbf{u} = 0 \implies \theta = \frac{1}{\gamma} \Sigma^{-1} (\mu - \lambda \mathbf{u})$$

$$\lambda = \frac{\mathbf{u}' \Sigma^{-1} \mu - \gamma}{\mathbf{u}' \Sigma^{-1} \mathbf{u}}$$

$$\theta = \frac{1}{\gamma} \Sigma^{-1} \left( \mu - \frac{\mathbf{u}' \Sigma^{-1} \mu - \gamma}{\mathbf{u}' \Sigma^{-1} \mathbf{u}} \mathbf{u} \right).$$

## Is it realistic?

This simple portfolio allocation problem often fails to capture the complexity of financial markets:

- Irrelevant for asset managers using numerical methods.
- Realistic models can be solved with state-of-the-art methods and solvers.
- Bottlenecks occur when  $N$  is large, as complex problems are often NP-Hard.
- Realistic problems require convex and mixed-integer formulations.
- Risk management decisions influence portfolio manager strategies.



## Risk Management Decision: Market Exposure

To control market risk ( $\beta$ ):

$$\max_{\theta} \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta$$

$$\text{Subject to } \theta' \mathbf{u} = 1, \quad \theta' \beta = \bar{\beta}$$

where  $\bar{\beta} \in \mathbb{R}$  and  $\beta = [\beta_1, \dots, \beta_N]$ .

## Factor Exposure and Concentration

Consider a multi-factor model with  $K$  factors:

$$r_t = \mathbf{B}f_t + \epsilon_t$$

where  $\mathbf{B} \in \mathbb{R}^{N \times K}$  and  $\bar{\beta} \in \mathbb{R}^K$ .

$$\max_{\theta} \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta$$

Subject to  $\theta' \mathbf{u} = 1$ ,  $\mathbf{B}'\theta = \bar{\beta}$ ,  $\bar{b} \geq \theta \geq \underline{b}$ .

## Value at Risk (VaR)

VaR measures the risk of loss for an investment:

$$VaR_{\alpha}(X) = -\inf\{x \in \mathbb{R} : F_X(x) > \alpha\}.$$

For a given portfolio, time horizon, and probability  $\alpha$ ,  $\alpha$ -VaR is the maximum possible loss, excluding worse outcomes with a combined probability of at most  $\alpha$ .

Approaches to compute  $F_X$ :

- Historical data
- Distribution assumptions
- Non-parametric methods

## Leverage

Leverage boosts investment performance at the expense of higher risk:

$$L = \frac{\text{Total Value of Positions}}{\text{Capital}}.$$

For a fund receiving  $X$  dollars:

$$L = \theta^+ + \theta^-$$

where  $\theta^+$  and  $\theta^-$  are the fractions for long and short positions, respectively.

## Introducing Leverage

To model leverage with cash ( $\theta_c$ ):

$$\max_{\theta} \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta$$

Subject to  $\theta' \mathbf{u} + \theta_c = 1$ ,  $\theta = \theta^+ - \theta^-$ ,  $\theta^+ \geq 0$ ,  $\theta^- \geq 0$ .

## Controlling Leverage

$$\max_{\theta} \theta' \mu - \frac{\gamma}{2} \theta' \Sigma \theta$$

$$\text{Subject to } \theta' \mathbf{u} + \theta_c = 1, \quad \mathbf{u}'(\theta^+ + \theta^-) \leq L.$$

Arbitrage funds may use leverage up to  $\times 10$ , while mutual funds tend to have leverage close to 1.

## Liquidity

Introducing cash allows liquidity management, essential for institutions facing withdrawals:

$$\theta_c \geq \bar{c} \geq 0.$$

# Non-Convex Non-Linear Dynamics

Real-world features requiring advanced modeling include:

- Sector concentration
- Portfolio size
- Higher moments
- Transaction costs
- Asset liquidity
- Heterogeneous preferences