

o.o.1 System: The 2D Ising model

```
1 import numpy as np
2 from numba.experimental import jitclass
3 from numba import int64
4 integer = int64

1 __all__ = ['IsingModel']
2 @jitclass([
3     ('spins', integer[:, :]),
4     ('L', integer),
5     ('sweep_steps', integer),
6     ('E', integer),
7     ('Ev', integer),
8     ('dE', integer),
9     ('i', integer),
10    ('j', integer)
11 ])
12 class IsingModel:
13     def __init__(self, spins):
14         shape = np.shape(spins)
15         if len(shape) != 2 or shape[0] != shape[1]:
16             raise ValueError('IsingModel spin array is not a square.')
17         self.spins = spins
18         self.L = shape[0]
19         self.sweep_steps = shape[0]**2
20         self.E = self.energy()
21         self.Ev = self.E
22         self.dE = 0
23         self.i = 0
24         self.j = 0
25     def state(self):
26         return (self.spins.copy(),)
27     def state_names(self):
28         return ('spins',)
29     def copy(self):
30         return IsingModel(*self.state())
31     def energy_bins(self):
32         Ex = 2 * self.L**2
33         ΔE = 4
34         Es = np.arange(-Ex, Ex + ΔE + 1, ΔE)
35         # Penultimate indices are not attainable energies
36         return np.delete(Es, [1, -3])
37     def neighbors(self, i, j):
38         return np.array([
39             self.spins[i-1, j],
40             self.spins[(i+1) % self.L, j],
41             self.spins[i, j-1],
42             self.spins[i, (j+1) % self.L],
43         ])
44     def energy(self):
45         E = 0
46         for i in range(self.L):
47             for j in range(self.L):
48                 E -= np.sum(self.spins[i, j] * self.neighbors(i, j))
49         return E // 2
50     def propose(self):
51         i, j = np.random.randint(self.L), np.random.randint(self.L)
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52     self.i, self.j = i, j
53     dE = 2 * np.sum(self.spins[i, j] * self.neighbors(i, j))
54     self.dE = dE
55     self.Ev = self.E + dE
56     def accept(self):
57         self.spins[self.i, self.j] *= -1
58         self.E = self.Ev
```