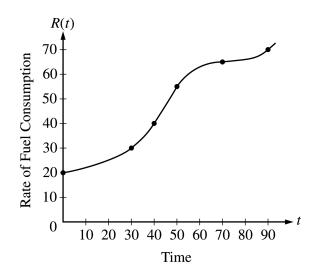
2003 AP® CALCULUS AB FREE-RESPONSE QUESTIONS



(minutes)	R(t) (gallons per minute)
0	20
30	30
40	40
50	55
70	65
90	70

- 3. The rate of fuel consumption, in gallons per minute, recorded during an airplane flight is given by a twice-differentiable and strictly increasing function R of time t. The graph of R and a table of selected values of R(t), for the time interval $0 \le t \le 90$ minutes, are shown above.
 - (a) Use data from the table to find an approximation for R'(45). Show the computations that lead to your answer. Indicate units of measure.
 - (b) The rate of fuel consumption is increasing fastest at time t = 45 minutes. What is the value of R''(45)? Explain your reasoning.
 - (c) Approximate the value of $\int_0^{90} R(t) dt$ using a left Riemann sum with the five subintervals indicated by the data in the table. Is this numerical approximation less than the value of $\int_0^{90} R(t) dt$? Explain your reasoning.
 - (d) For $0 < b \le 90$ minutes, explain the meaning of $\int_0^b R(t) dt$ in terms of fuel consumption for the plane. Explain the meaning of $\frac{1}{b} \int_0^b R(t) dt$ in terms of fuel consumption for the plane. Indicate units of measure in both answers.

END OF PART A OF SECTION II

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