2007 AP® CALCULUS AB FREE-RESPONSE QUESTIONS

CALCULUS AB SECTION II, Part B

Time—45 minutes
Number of problems—3

No calculator is allowed for these problems.

- 4. A particle moves along the x-axis with position at time t given by $x(t) = e^{-t} \sin t$ for $0 \le t \le 2\pi$.
 - (a) Find the time t at which the particle is farthest to the left. Justify your answer.
 - (b) Find the value of the constant A for which x(t) satisfies the equation Ax''(t) + x'(t) + x(t) = 0 for $0 < t < 2\pi$.

t (minutes)	0	2	5	7	11	12
r'(t) (feet per minute)	5.7	4.0	2.0	1.2	0.6	0.5

- 5. The volume of a spherical hot air balloon expands as the air inside the balloon is heated. The radius of the balloon, in feet, is modeled by a twice-differentiable function r of time t, where t is measured in minutes. For 0 < t < 12, the graph of r is concave down. The table above gives selected values of the rate of change, r'(t), of the radius of the balloon over the time interval 0 ≤ t ≤ 12. The radius of the balloon is 30 feet when t = 5.
 (Note: The volume of a sphere of radius r is given by V = 4/3 πr³.)
 - (a) Estimate the radius of the balloon when t = 5.4 using the tangent line approximation at t = 5. Is your estimate greater than or less than the true value? Give a reason for your answer.
 - (b) Find the rate of change of the volume of the balloon with respect to time when t = 5. Indicate units of measure.
 - (c) Use a right Riemann sum with the five subintervals indicated by the data in the table to approximate $\int_0^{12} r'(t) dt$. Using correct units, explain the meaning of $\int_0^{12} r'(t) dt$ in terms of the radius of the balloon.
 - (d) Is your approximation in part (c) greater than or less than $\int_0^{12} r'(t) dt$? Give a reason for your answer.

WRITE ALL WORK IN THE PINK EXAM BOOKLET.