

2003 AP<sup>®</sup> CALCULUS AB FREE-RESPONSE QUESTIONS (Form B)

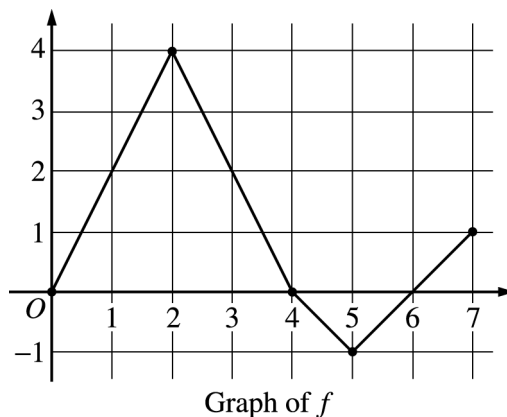
CALCULUS AB  
SECTION II, Part B

Time—45 minutes

Number of problems—3

No calculator is allowed for these problems.

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4. A particle moves along the  $x$ -axis with velocity at time  $t \geq 0$  given by  $v(t) = -1 + e^{1-t}$ .
- (a) Find the acceleration of the particle at time  $t = 3$ .
  - (b) Is the speed of the particle increasing at time  $t = 3$ ? Give a reason for your answer.
  - (c) Find all values of  $t$  at which the particle changes direction. Justify your answer.
  - (d) Find the total distance traveled by the particle over the time interval  $0 \leq t \leq 3$ .
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5. Let  $f$  be a function defined on the closed interval  $[0, 7]$ . The graph of  $f$ , consisting of four line segments, is shown above. Let  $g$  be the function given by  $g(x) = \int_2^x f(t) dt$ .
- (a) Find  $g(3)$ ,  $g'(3)$ , and  $g''(3)$ .
  - (b) Find the average rate of change of  $g$  on the interval  $0 \leq x \leq 3$ .
  - (c) For how many values  $c$ , where  $0 < c < 3$ , is  $g'(c)$  equal to the average rate found in part (b)? Explain your reasoning.
  - (d) Find the  $x$ -coordinate of each point of inflection of the graph of  $g$  on the interval  $0 < x < 7$ . Justify your answer.
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