2003 AP® CALCULUS AB FREE-RESPONSE QUESTIONS (Form B)

2. A tank contains 125 gallons of heating oil at time t = 0. During the time interval $0 \le t \le 12$ hours, heating oil is pumped into the tank at the rate

$$H(t) = 2 + \frac{10}{(1 + \ln(t+1))}$$
 gallons per hour.

During the same time interval, heating oil is removed from the tank at the rate

$$R(t) = 12 \sin\left(\frac{t^2}{47}\right)$$
 gallons per hour.

- (a) How many gallons of heating oil are pumped into the tank during the time interval $0 \le t \le 12$ hours?
- (b) Is the level of heating oil in the tank rising or falling at time t = 6 hours? Give a reason for your answer.
- (c) How many gallons of heating oil are in the tank at time t = 12 hours?
- (d) At what time t, for $0 \le t \le 12$, is the volume of heating oil in the tank the least? Show the analysis that leads to your conclusion.