Spatial modelling of the two-party preferred vote in Australian federal elections: 2001–2016

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5 Summary

- We examine the relationships between electoral socio-demographic characteristics and
- two-party preferences in the six Australian federal elections held between 2001 and
- 8 2016. Socio-demographic information is derived from the Australian Census which
- 9 occurs every five years. Since a Census is not directly available for each election,
- an imputation method is employed to estimate Census data for the electorates at the
- time of each election. This accounts for both spatial and temporal changes in electoral
- 12 characteristics between Censuses. To capture any spatial heterogeneity, a spatial error
- model is estimated for each election, which incorporates a spatially structured random
- effect vector. Over time, the impact of most socio-demographic characteristics that
- affect electoral two-party preference do not vary, with age distribution, industry of work,
- incomes, household mobility and relationships having strong effects in each of the six
- elections. Education and unemployment are amongst those that have varying effects. All
 - data featured in this study has been contributed to the eechidna R package (available
- 19 on CRAN).

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- 20 Keywords: federal election, Census, Australia, spatial modelling, imputation, data
- 21 science, socio-demographics, electorates, R, eechidna

1. Introduction

- Australia has changed in many ways over the last two decades. Rising house prices,
- 24 country-wide improvements in education, an ageing population, and a decline in
- 25 religious affiliation, are just a few facets of the country's evolving socio-demographic

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characteristics. At the same time, political power has moved back and forth between the 26 two major parties. In the 2007 and 2010 federal elections, the Australian Labor Party 27 (hereafter Labor) was victorious, whereas the 2001, 2004, 2013 and 2016 elections were 28 won by the Liberal National coalition (hereafter Liberal). The two-party preferred vote, 29 a measure of support between these two parties, fluctuated between 47.3% and 53.5% 30 (in favour of the Liberal party) over this period. This study explores how electoral 31 (aggregate) socio-demographic characteristics relate to two-party preferences, and 32 whether their effects have changed over time. 33

The Australian Electoral Commission (AEC) divides Australia into 150 regions, called 34 electorates, with each corresponding to a single seat in the House of Representatives. If 35 a party wins a majority of seats, they become the governing party. Data on the socio-36 demographics of these electorates are derived from the Australian Census, and vote 37 counts are obtained from Australian federal elections. Joining these two data sources is 38 problematic as there is an inherent asynchronicity in the two types of events. A Census 39 is conducted by the Australian Bureau of Statistics (ABS) every five years, whereas 40 federal elections, conducted by the AEC, usually occur every three years or so. The 41 first problem addressed is that of constructing appropriate Census data for the 2004, 42 2007, 2010 and 2013 elections — election years in which a Census did not occur. The 43 predominant approach in previous studies was to join voting outcomes to the nearest Census, without accounting for any temporal differences (see Davis & Stimson 1998; 45 Stimson, McCrea & Shyy 2006; Liao, Shyy & Stimson 2009; Stimson & Shyy 2009). 46 Furthermore, electoral boundaries change regularly, so spatial discrepancies also arise when matching with electoral data. To obtain appropriate "Census-like" data for these 48 four elections, electoral socio-demographics are constructed using a spatio-temporal 49 imputation that combines areal interpolation (Goodchild, Anselin & Deichmann 1993) 50 and linear time-interpolation. Collecting and wrangling the raw data, along with the 51 imputation process, are detailed in Section 2. All data and associated documentation 52 relating to this procedure are available in the eechidna R package (Forbes et al. 2019), 53 providing a resource for any future analysis. 54

Previous work on modelling Australian federal elections has found that aggregate sociodemographics are relatively good predictors of voting outcomes. Forrest et al. (2001) used multiple regression to model the Liberal and Labor primary vote for polling booths in the Farrer electorate in 1998 as a function of Census variables from 1996. Stimson, McCrea & Shyy (2006), Stimson & Shyy (2009) and Stimson & Shyy (2012) used principal component analysis of polling booths in the 2001, 2004 and 2007 elections respectively, also finding that socio-demographic characteristics of polling booths are linked to their two-party preferred vote. In contrast, Stimson & Shyy (2009) models the polling booth swing vote (change in the two-party preferred vote) in the 2007 election, finding that little of the swing vote can be explained by Census data.

Instead of analyzing a single election in isolation, this paper employs a consistent 65 model framework across six elections so that temporal changes in the effects of socio-66 demographics can be observed. Each federal election is modelled with a cross-sectional 67 dataset, where each observation is one of the 150 electorates. This dataset consists of the two-party preferred vote (as the response variable) and a set of common socio-69 demographic variables (as the explanatory variables). To prepare these datasets, socio-70 demographic variables are first standardized, and then a principal component analysis 71 is used to group many of the variables into "factors". To account for the inherent 72 spatial structure of the data, a spatial error model is then estimated for each election. In 73 interpreting these models, it is important to be mindful of the ecological fallacy. Insights 74 are being drawn at the electorate level and cannot be inferred for another disaggregate 75 level (in particular, drivers of individual voter behaviour may vary from what is observed 76 at the electorate level). 77

The paper is organised as follows. Section 2 describes the data collection, joining and cleaning, while model details are discussed in Section 3. Section 4 describes the inference conducted to determine significance of effects and how these change over time, as well as including details on model robustness. Section 5 summarises the work.

Two supplementary sections document the contributions of others to this work and the software.

2. Data collection, wrangling and imputation

2.1. Collecting the data

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The voting outcome of interest is the electoral two-party preferred vote, which is 86 provided by the Australian Electoral Commission (AEC) for the 2001, 2004, 2007, 2010, 87 2013 and 2016 elections via the AEC Tally Room. The AEC divides Australia into 150 88 regions, called electorates, with each corresponding to a single seat in the House of 89 Representatives. Voting is compulsory in Australia, and each voter assigns a numbered 90 preference to each available candidate in their electorate. The two-party preferred vote 91 is determined by a tally of these preferences where, by convention, only the ranks of the 92 Labor and Liberal candidates are considered. This is recorded as a percentage preference 93 in favour of the Liberal party.

Socio-demographic variables are derived from the Australian Census of Population 95 and Housing (Census), which is a survey of every household in Australia, recording 96 information such as age, gender, ethnicity, education level and income. There have 97 been four Censuses so far in the 21st century, conducted in 2001, 2006, 2011 and 98 2016. The Australian Bureau of Statistics (ABS) conducts the Census and publishes aggregated information. The ABS uses electoral boundaries as defined by the AEC at 100 the time of each Census, which may not match those in place at the subsequent and 101 previous elections. From the available Census information aggregated at the electorate 102 level, 50 socio-demographic variables are defined for each of the electorates to be 103 used in the analysis. These variables include information relating to electoral age 104 distributions, income, education qualifications, employment industries and job types, 105 religion, birthplace, household characteristics and relationships. 106

Raw data is sourced online from the AEC and ABS websites in .csv and .xlsx 107 files. The formats of these files differ over the years, making extracting the appropriate 108 information a big task. The functions available in the dplyr (Wickham et al. 2019b) 109 and readx1 (Wickham et al. 2019a) R packages are particularly useful, as they provide 110 fast consistent tools for data manipulation and functions to import .xlsx files. The 111 2001 and 2006 Census data are published in a format where the information for each 112 electorate is held in a separate document making it difficult to use the dplyr tools. 113 Instead, cells have to be selected from each individual file to construct the desired 114 variables. All scripts required for the data wrangling process can be found in the github 115 repository for the eechidna R package (Forbes et al. 2019), along with the raw data. 116 The eechidna package makes this study entirely reproducible and provides a resource 117 to help wrangle data for future Censuses and elections, when they become available. 118

119 2.2. Joining Census and election data

120 Differences between Census and election data

Between 2001 and 2016 there were six elections and four Censuses (see Figure 1). 121 Electoral boundaries are redistributed regularly by the AEC, meaning that only in the 122 years where both a Census and an election occur are all boundaries likely to match — the 123 case for the 2001 and 2016 elections. Therefore, for the four elections between 2004 and 124 2013, both temporal and spatial differences in electorates need to be accounted for when 125 joining the electoral two-party preferred vote with Census data. For these elections a 126 spatio-temporal imputation method is employed to obtain electoral socio-demographics. 127 This method uses Census information from both before and after the election of interest. 128

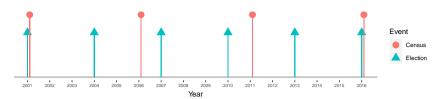


Figure 1. Timeline of Australian elections and Censuses. They do not always occur in the same year.

Spatio-temporal imputation

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For each election, neighbouring Census information has to be combined in some way so that it represents the boundaries in place at the time of the election. This is done by taking the electoral boundaries and imputing the corresponding socio-demographic characteristics for each of the neighbouring Censuses, thereby addressing the spatial aspect. Next, to deal with the temporal component, characteristics at the time of the election are constructed using linear interpolation between the spatially imputed neighbouring Census variables.

The finest level of disaggregation available for Census data is the region classification called Statistical Area 1 (SA1). In 2016, Australia was divided into over 55,000 SA1s. Consider each of these SA1 regions as a source zone, $s=1,\ldots,S$, for which sociodemographic information is available. For simplicity, let each source zone be wholly summarised by its centroid. A set of target zones, $t=1,\ldots,T$, are defined as regions for which information is to be imputed — these are the electoral boundaries for a particular election.

Take the example of the Melbourne Ports electorate from the 2013 federal election, illustrated in Figure 2. The purple region in this figure represents the target zone and the source zones are the centroid locations from the 2016 Census SA1 areas.

Furthermore, let $I_{s,t}$ be an indicator variable, for which $I_{s,t}=1$ if the centroid of source zone s falls within target zone t, and 0 otherwise. Additionally, let the population of the source zone s be U_s and the population of target zone t be P_t .

In order to calculate socio-demographic information for each of the target zones, a weighted average of source zones is taken using their populations as weights. Denote a given Census variable for the target zone by C_t , and the same Census variable for the source zone as D_s . Then, estimate C_t using

$$\hat{C}_t = \frac{\sum_{s=1}^{S} I_{s,t} * D_s * U_s}{\sum_{s=1}^{S} I_{s,t} * U_s}, \quad \text{for each } t = 1, \dots, T.$$

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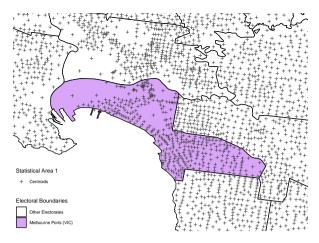


Figure 2. The electoral boundaries for Melbourne Ports (shown in purple) and surrounding electorates, with centroids for Statistical Area 1 regions from the 2016 Census overlaid. The centroids falling within the purple region are attributed to Melbourne Ports.

This concludes the spatial imputation of the socio-demographic characteristics for one target zone (a single electoral boundary), at the time of only one of the neighbouring Censuses. This process is repeated for all of the target zones, and then for the other neighbouring Census.

To account for temporal changes, linear interpolation is used between Census years to get the final estimate of a Census variable for the target zone in the election year. Let y_1 be the year of the Census preceding an election, let y_2 be the year of the election, and y_3 be the year of the Census that follows. Add this year subscript to the Census variable estimate \hat{C}_t , resulting in $\hat{C}_{t,y}$. Linear interpolating between these Census years results an imputed value for the election year, given by

$$\hat{C}_{t,y_2} = \frac{y_3 - y_2}{y_3 - y_1} \hat{C}_{t,y_1} + \frac{y_2 - y_1}{y_3 - y_1} \hat{C}_{t,y_3}.$$

164 Implicitly this assumes that population characteristics change in a linear manner over 165 time.

Continuing with the example of Melbourne Ports in the 2013 election, the estimate for a given Census variable in 2016, $\hat{C}_{\text{MelbPorts},2016}$ would be obtained by computing the weighted average of this variable amongst the SA1s within the purple region shown in Figure 2. This would be repeated with the 2011 Census SA1s to obtain $\hat{C}_{\text{MelbPorts},2011}$, from which the final estimate is given by

$$\hat{C}_{\text{MelbPorts},2013} = \frac{3}{5}\hat{C}_{\text{MelbPorts},2011} + \frac{2}{5}\hat{C}_{\text{MelbPorts},2016}.$$

This is done for each of the socio-demographic variables, and is repeated for each of the 149 remaining target zones corresponding with 2013 electorates.

3. Modelling

From this imputation process, electoral socio-demographic variables are available for each of the six elections and can be joined with their corresponding two-party preferred votes. Before choosing an appropriate model, two issues with the socio-demographic variables need to be addressed. First, variable scales change over the years, making it important to standardize variables. Second, many variables represent similar information and where appropriate, will be grouped together. To determine which variables should be grouped, principal component analysis (PCA) is used to guide the construction of specific factors. The intuition here is that PCA will identify which variables covary, from which intuitive groupings of variables can be chosen to combine into individual variables. Details are given in Section 3.2. After these steps, a model specification is chosen.

3.1. Standardizing variables

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Many of the socio-demographic variables have changing scales over the years. For example, inflation-adjusted median rental prices increased across almost all electorates, with median rent of 225 dollars per week placing an electorate in the 90th percentile in 2001, but only the 45th percentile in 2016. In order for socio-demographic effects to be comparable across years, all explanatory variables are standardized to have mean zero and variance one within each election year. By standardizing, each variable is reported as a relative measure compared to all other electorates in the same year.

3.2. Creating factors

There are only N=150 observations (electorates) in each election and p=50 socio-demographic variables in each cross-section, with many variables representing similar information about an electorate. Any model that uses all variables would face problems with multi-collinearity and over-fitting, which would likely lead to erroneous conclusions regarding variable significance. To address this, variables that represent similar information are combined into a single variable, which will be referred to as a "factor".

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A factor is created from a group of variables if there is an intuitive reason as to why these variables should represent similar information and if there is evidence to suggest that they covary. For example, a potential group would be variables relating to electoral incomes — median family, household and personal incomes. To determine which variables covary, principal component analysis is used on a combined dataset of sociodemographic variables from all six elections*. The only variables exempted from the principal component analysis are the four variables representing age brackets (the proportion of the population aged 0–19 years old, 20–34 years old, 45–54 years old and 55 years plus), which are included in the model as separate variables.

Only the first four principal components from the combined dataset are considered, as the scree plot levels off after the fourth component. Variables that have a large loading in a particular component are deemed to covary, with a loading with magnitude greater than 0.15 being considered large. Each principal component is considered separately. If a subset of variables have large loadings (positive or negative) in a given component, and there is an intuitive reason as to why they should be grouped together, then this subset of variables will be combined to become a factor. Note that more than one factor can be deduced from a principal component (i.e. two non-overlapping subsets of variables), and that any variables not included in a factor are not discarded.

Six factors are created using this approach. These are: Incomes (median personal income, median household income, median family income); Unemployment (unemployment rate, labour force participation rate); PropertyOwned (proportion of dwellings that are owned, proportion of dwellings that are mortgages, proportion of dwellings that are rented, proportion of dwellings that classified as government housing); RentLoanPrice (median rental payment amount, median loan repayment amount); FamHouseSize (average household size, ratio of people to families, incidence of single person households, incidence of households containing a couple with kids, incidence of households containing a couple without kids); and Education (high school completions, undergraduate and postgraduate degrees, proportion of employed people working as professionals, proportion of jobs in finance, proportion of workers who are labourers, proportion of workers who work as a tradesperson, diploma and certificate qualifications).

For each of these groupings, a factor is created by taking a weighted sum of the variables.

The weightings are allocated on the basis of whether the variable had a positive or

^{*}It is appropriate to compute principal components on a combined dataset of all six elections because when computed separately for each election, scree plots level off after four components and the loadings of the first four components are similar across the elections.

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negative loading in the principal component from which the grouping was identified. Variables with a positive loading are allocated a weight of +1 and those with negative loadings are allocated a weight of -1. After computing these weighted sums, the factor

is standardized to have mean zero and variance one, within each election.

The final predictor set contains p = 32 variables[†] which are listed in Table 1.

3.3. Regression incorporating spatially dependent errors

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An identical model specification is used for each of the six elections, with each election 240 modelled separately. Separate models are preferred to a single model because of how 241 frequently electoral boundaries change, noting that electorates with the same name 242 across elections are not guaranteed to represent the same geographic region. Therefore 243 any fixed or random effects models would be difficult to estimate without implementing 244 consistent boundaries, which would require further imputation (of voting information). 245 The separate models also allow the socio-demographic effects to be estimated separately 246 for each election year, facilitating analysis of temporal changes in variable effects. This 247 can be considered a special case of a longitudinal model where all coefficients are 248 time-varying and heteroskedasticity is time-varying. 249

For each cross-section, let the response y be the vector two-party preferred vote in favour 250 of the Liberal party; for example, $y_i = 70$ represents a 70% preference for Liberal, 30% 251 for Labor, in electorate i. Although y_i lies in the interval (0, 100), observed values are 252 never close to 0 or 100 (minimum 24.05% and maximum 74.90%), so there is no need 253 to formally impose the constraint of $y_i \in [0, 100]$. Furthermore, the responses are found 254 to be spatially correlated in each election (Moran's I test, $p \le 7 \cdot 10^{-15}$). This is not 255 surprising as electorates are aggregate spatial units, and hence the spatial structure of 256 the data must be modelled appropriately. 257

The spatial error model (Anselin 1988) is chosen because it captures spatial heterogeneity by incorporating a spatially structured random effect vector (LeSage, Kelley Pace & Pace 2009). In this context, the random effect can be thought of as capturing the effect of any characteristics that neighbourhoods share that have not been addressed by the independent variables included in the model.

[†]The factor creation procedure reduced the variable set to p=33, however one of the age brackets (Pop_55_plus) is not included as a variable to avoid multicollinearity, because the other three age brackets are included.

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10 SPATIAL MODELLING OF AUSTRALIAN FEDERAL ELECTIONS: 2001–2016 Table 1. Estimated spatial error model parameters (standard errors) for each of the six election years.

<u>-</u>	2001	2004	2007	2010	2013	2016
ρ	0.53***	0.33**	0.21	0.17	0.27	0.39**
AugCitigon	(0.15)	(0.16)	(0.18)	(0.17)	(0.17)	(0.17)
AusCitizen	-3.94* (2.27)	-1.39 (2.44)	-2.18 (2.21)	-1.28 (2.69)	-3.89 (2.51)	-2.66 (2.61)
Pop_00_19	0.49	2.66	9.39***	5.25	3.31	0.88
Pop_20_34	(2.54)	(3.91)	(3.63)	(3.64)	(2.91)	(2.62)
	-8.04*** (1.80)	-7.72*** (2.21)	-8.34*** (2.18)	-11.68*** (2.90)	-9.29*** (2.62)	-9.21*** (2.37)
Pop_35_54	-2.64***	-2.78***	-3.62***	-3.13***	-2.76**	-2.13**
	(0.84)	(0.89)	(0.83)	(1.10)	(1.11)	(1.06)
BornAsia	3.58*	-1.09	0.66	-1.78	-1.08	-0.14
BornMidEast	(2.09) -1.02	(2.52) -1.75	(1.99) -0.98	(2.74) -1.00	(2.54) -1.66	(2.17) -1.31
BornSEEuro	(1.00)	(1.17)	(1.09)	(1.33)	(1.23)	(1.11)
	-1.63	-3.17*	-1.07	-2.04	-2.89***	-2.53***
BornUK	(1.37) 0.29	(1.68) 0.31	(1.06) 0.32	(1.29) 0.28	(1.11) -0.15	(0.97) -0.61
Bomok	(1.02)	(1.04)	(0.87)	(1.06)	(0.99)	(0.99)
BornElsewhere	-4.13	-1.51	-1.03	2.45	-4.21	-2.17
Buddhism	(3.14) -0.07	(3.62) 0.80	(3.18) 0.58	(4.13) -0.14	(3.90) -0.43	(3.76) -1.16
	(1.31)	(1.54)	(1.39)	(1.66)	(1.60)	(1.58)
Christianity	-1.70	-1.01	-0.45	0.13	2.03	3.76**
G 4.6: 1:	(1.62)	(1.75)	(1.60)	(1.85)	(1.68)	(1.83)
CurrentlyStudying	-2.20^* (1.22)	-0.01 (1.50)	-0.14 (1.39)	1.35 (1.41)	0.32 (1.35)	0.22 (1.56)
DeFacto	-3.24	-2.25	-4.67**	-7.75**	-7.82**	-10.39***
DiffAddress Distributive	(2.07)	(2.62)	(2.27)	(3.09)	(3.08)	(3.15)
	3.06*** (0.94)	2.75** (1.20)	0.73 (1.24)	2.55 (1.79)	2.27 (1.67)	5.20*** (1.51)
	1.60	1.89*	0.50	0.62	1.59	1.31
Education	(1.06)	(1.14)	(0.99)	(1.27)	(1.20)	(1.18)
	-0.37	-0.26	-6.72**	-7.31*	-7.31**	-8.55**
Extractive	(2.35) 3.74***	(3.34) 4.96***	(3.00) 4.64***	(3.90) 6.46***	(3.63) 5.97***	(3.37) 6.38***
Extractive	(1.43)	(1.47)	(1.20)	(1.45)	(1.35)	(1.38)
FamHouseSize	1.94	-2.55	-6.47**	-3.84	-3.12	-2.00
Incomes	(2.61) 4.36***	(3.66) 2.42	(3.28) 5.52**	(3.87) 5.63*	(3.52) 8.02***	(3.06) 12.70***
meones	(1.69)	(3.00)	(2.42)	(3.15)	(2.78)	(2.64)
Indigenous	1.26	1.96	2.41	2.38	0.46	-0.22
Y-1	(1.61)	(1.89)	(1.59)	(2.00)	(1.88)	(1.90)
Islam	-0.75 (1.14)	-0.91 (1.28)	-0.60 (1.14)	-2.01 (1.41)	-0.88 (1.26)	-1.09 (1.30)
Judaism	1.32	0.93	1.47	0.28	1.35	1.15
	(1.01)	(1.08)	(0.92)	(1.10)	(1.02)	(0.97)
ManagerAdmin	2.62*** (0.67)	4.67*** (1.06)	7.47*** (0.95)	7.05*** (1.16)	5.93*** (1.06)	5.64*** (0.97)
Married	-3.93	-2.72	-9.35***	-10.12***	-7.91**	-9.47**
	(2.51)	(3.56)	(3.12)	(3.55)	(3.57)	(3.85)
NoReligion	-0.73	0.04	1.32	0.37	1.41 (1.74)	2.94 (2.03)
OneParentHouse	(1.50) -4.77***	(1.65) -3.23	(1.51) $-6.55***$	(1.75) -7.03***	-5.32***	-4.94**
OtherLanguage	(1.49)	(1.99)	(1.81)	(2.04)	(1.97)	(2.03)
	-1.02	6.88	6.21	7.80	10.13**	9.98**
PropertyOwned	(3.00) -2.01	(4.93) -0.30	(3.97) 0.74	(5.25) -1.92	(5.09) -1.05	(4.26) 0.73
TropertyOwned	(1.35)	(1.49)	(1.36)	(1.74)	(1.67)	(1.48)
RentLoanPrice	-2.17	0.37	1.23	3.08	1.36	-2.04
SocialServ	(1.46) 3.31***	(1.93)	(1.76) 3.46***	(2.23) 3.72**	(2.20) 2.98**	(2.07) 4.04***
SUCIALSEL V	(1.27)	2.85** (1.40)	(1.17)	(1.46)	(1.28)	(1.15)
Transformative	2.30	4.71***	4.58***	4.55**	3.63**	4.05***
TY 1	(1.48)	(1.77)	(1.51)	(1.87)	(1.67)	(1.47)
Unemployment	-3.39** (1.37)	-3.47** (1.69)	-0.40 (1.45)	-0.68 (1.80)	0.81 (1.47)	1.93 (1.32)
Constant	50.80***	52.63***	(1.45) 47.31***	49.92***	53.52***	50.46***
	(0.76)	(0.59)	(0.44)	(0.52)	(0.54)	(0.64)
Residual Standard Error (GLS)	4.34	4.82	4.32	5.30	4.82	4.76
Observations	150	150	150	150	150	150

*p<0.1; **p<0.05; ***p<0.01

Spatial weights are calculated in accordance with the assumption that an electorate is equally correlated with any electorate that shares a part of its boundary. Let ρ be the spatial autoregressive coefficient, v be a spherical error term, w be a matrix of spatial weights (containing information about the neighbouring regions), w be a matrix of socio-demographic covariates, w be a vector of regression coefficients and w be a spatially structured random effect vector.

$$y = X\beta + a$$

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$$a = \rho W a + v$$

where $\boldsymbol{v} \sim N(\boldsymbol{0}, \sigma^2 \boldsymbol{I_n})$, and hence

$$\boldsymbol{y} = \boldsymbol{X}\boldsymbol{\beta} + (\boldsymbol{I}_n - \rho \boldsymbol{W})^{-1}\boldsymbol{v}.$$

Estimation of the above spatial error model is undertaken using feasible generalized least squares.

Table 1 details the estimated model coefficients and their estimated standard errors, for each of the six elections. An interpretation of these estimated values is provided in the next section.

4. Results

4.1. Spatial autoregressive parameter

The spatial autoregressive coefficient ρ is positive and significant in the 2001, 2004 and 2016 elections (Figure 3). In these three elections, there is evidence to suggest that neighbours share some influential characteristics outside the explanatory variables, which affect the two-party preferred vote. Conversely, in the other three elections, the spatial effect weakens to become insignificant (although still positive).

4.2. Country-wide trend

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Since all socio-demographics have been standardized to have a mean of zero and a variance of one, the intercept in each model can be interpreted as the estimated

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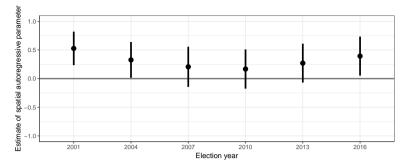


Figure 3. Estimates of the spatial autoregressive parameter for each of the six elections, reported with their individual 95% confidence intervals. Only in 2001 and 2016 is there a significant spatial component.

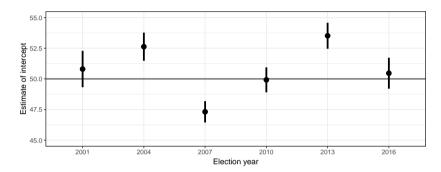


Figure 4. Estimated intercept for each election, which represents the two-party preferred vote for an electorate with mean characteristics.

two-party preferred vote for an electorate with mean characteristics[‡]. Figure 4 shows that the baseline of party preference has varied over the elections, with the biggest swing occurring in the 2007 election where the mean electorate shifted more than five percentage points in favour of the Labor party.

4.3. Influential socio-demographics

To investigate the socio-demographics that have a strong effect on the two-party preferred vote, partial residual plots are used and shown in Figures 5 and 6. Partial residuals, for a given variable, are the residuals from the fitted model with the estimated effect of that variable added to it. These plots show the direction, size and significance of an estimated effect, as well as any deviations from linearity. In each plot, the slope of the prediction line matches the estimated coefficient and the shaded region represents a 95% confidence

 $^{^{\}ddagger}$ Mean of all variables aside from Judaism, Indigenous, Islam and Buddhism, where it assumes the mean of the log value.

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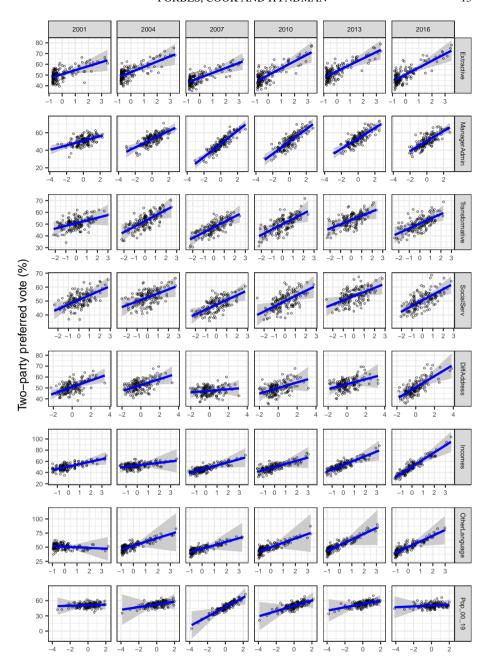


Figure 5. Partial residual plots by election year for a selection of predictors. Linear model with 95% confidence bands overlaid. Most predictors have a positive relationship: the larger the value the more likely the electorate preferences the Coalition. The relationship is relatively robust over time, with the exception of <code>DiffAddress</code>, <code>Incomes</code>, <code>OtherLanguageHome</code> and <code>Pop_00_19</code>.

band. Plots are computed using the method in Breheny & Burchett (2017). If a horizontal line can be drawn through the confidence band, then the effect is insignificant. The

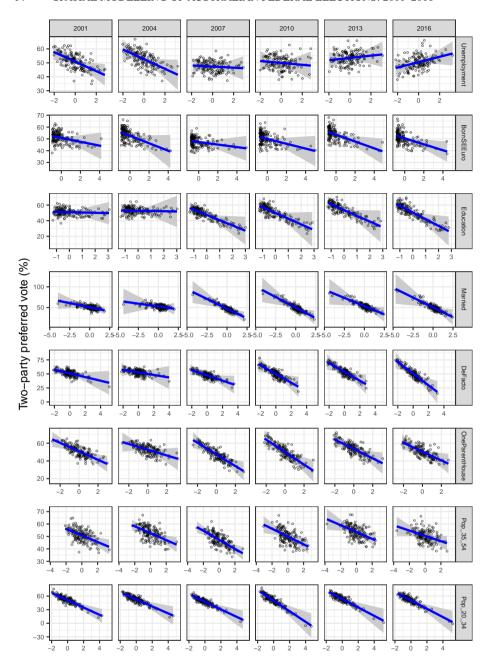


Figure 6. Partial residual plots by election year for a selection of predictors. Linear model with 95% confidence bands overlaid. Several predictors have a negative relationship: with larger values indicating the electorate more likely preferences Labor. Most relationships are relatively stable over elections, except Unemployment and Education."

estimated intercept is also added to the partial residuals for interpretability. Plots for each election are faceted to compare the effects over time in Figures 5 and 6. Only

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socio-demographics that have a significant effect in at least two elections are displayed in Figures 5 and 6.

303 Industry and type of work

Electorates with higher proportions of workers in mining, gas, water, agriculture, waste 304 and electricity (grouped as Extractive industries) are consistently linked with higher 305 support for the Liberal party, with the magnitude of this effect slightly increasing over 306 the years (see row 3 in Figure 5). This is unsurprising, as the Liberal party has close ties 307 with these traditional energy industries, and typically present policies to reduce taxation 308 on energy production. Furthermore, electorates with more workers in construction or 309 manufacturing industries (Transformative) are also more likely to support the 310 Liberal party (see row 4 in Figure 5), from 2004 onwards. 311

Similarly, the proportion of workers in managerial, administrative, clerical and sales roles (ManagerAdmin), is also a significant predictor of two-party preference vote across all six elections, with a higher proportion of people working these jobs increasing Liberal support.

Of these job related variables, the most surprising effect is that associated with the proportion of workers in education, healthcare, social work, community and arts (SocialServ). Typically the Labor party has more generous funding schemes affecting these areas of work, so one might expect SocialServ to have a negative effect on two-party preference. However, in every election this effect is found to be positive and significant.

2 Income and unemployment

Typically the Labor party campaigns on more progressive policies, which often include 323 tax reform that adversely affects higher income earners, and more generous social 324 assistance programs. Perhaps it is due to these policies that higher income electorates 325 appear more likely to support the Liberal party, as the Incomes factor has a positive 326 effect on Liberal preference (see row 1 in Figure 5). This effect is significant in every 327 election aside from 2004 and 2010. Unemployment however, is not as influential. In 328 2001 and 2004, electorates with higher unemployment align with Labor, but over time 329 this shifts towards support for the Liberal party, culminating in a positive (insignificant) 330 effect in 2016. 331

332 **Age**

The older Australian population is often believed to be more conservative, and the left 333 leaning political parties (including Labor) typically have a stronger appeal to younger 334 people. This effect is indeed observed across the six elections, with populations between 335 20 and 34 years of age (Pop_20_34) being very strongly aligned with Labor preference 336 (bottom row in Figure 6). Larger populations of 35 to 54 year olds (Pop 35 54) are 337 also associated with Labor, but the magnitude of this effect is far smaller. Populations 338 under 20 years of age is only significant in 2007, where Pop 00 19 increased Liberal 339 support. 340

341 Education

Since 2007, electorates with higher education levels are associated with supporting the Labor party, with this effect being significant in 2007, 2013 and 2016 and only marginally insignificant in 2010. In the elections before 2007, education has a negligible effect (see row 3 in Figure 5). Additionally, student populations (CurrentlyStudying) do not affect electoral party preference in any election (not shown).

347 Diversity

Larger migrant populations from Asia, the Middle East, South-Eastern Europe, the 348 United Kingdom and elsewhere, are either associated with Labor support, or have no 349 effect. Of these areas, only South-Eastern European populations significantly affect 350 party preference, with larger populations associating with Labor in 2013 and 2016 (row 351 2, Figure 6). Speaking other languages (aside from English) however, appears to have 352 a far stronger effect, as observed through the OtherLanguage variable. Electorates 353 with more diverse speech are associated with higher support for the Liberal party from 354 2004 onwards, with this effect being significant in 2013 and 2016 (see row 7, Figure 5). 355 Furthermore, none of the variables relating to religious beliefs aside from Christianity 356 have a material effect in any election (this includes the Buddhist, Muslim, Jewish, non-357 religious and Indigenous Australian populations). The association between Christian 358 populations (Christianity) and the Liberal party steadily increases over the years, 359 becoming positive and significant in 2016. 360

361 Households

- In 2001, 2004 and 2016, higher proportions of people that have recently (in the past five years) moved house (DiffAddress) increased electoral support for the Liberal party (see row 5 in Figure 5). This is somewhat surprising as one might expect house ownership and rental prices to be linked to two-party preference, rather than household mobility (PropertyOwned and RentLoan are not significant in any election).
- Higher proportions of single parent households are associated with Labor support in all elections (albeit insignificant in 2004, see row 6 in Figure 6), whereas the electoral family and household sizes (via the FamHouseSize variable) do not appear to be associated with either party.

371 Relationships

- From 2007 onwards, both marriages (Married) and de facto relationships (DeFacto)
- are found to be strong predictors of the two-party preferred vote in favour of the Labor
- party. In 2001 and 2004 neither of these variables are significant (see rows 4 and 5 in
- 375 Figure 6).

376 4.4. A closer look at the residuals

377 Residuals by state

It is often hypothesized that states have a systematic bias towards one of the two major parties. Boxplots of residuals grouped by state (Figure 7) show that the data reflects this to only a limited extent. Tasmania and the Australian Capital Territory appear to have a bias towards Labor, whereas the South Australia and the Northern Territory tend towards voting Liberal. However, there are relatively few electorates in each of these states (five, two, eleven and two respectively), so this apparent result may be due to incumbent effects rather than an actual state-specific bias.

385 Residuals by party incumbency

The incumbent party appears to have a distinct advantage at the next election. The boxplots in Figure 8 show that if either of the Labor or Liberal parties won the seat at

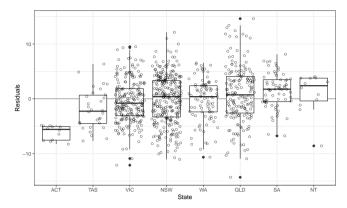


Figure 7. Boxplot of residuals by state with jittered points. States ordered by median residual. A state-specific bias present only in the smaller states appears to have not been captured by the model.

the previous election, the electorate is likely to vote in their favour, over and above any socio-demographic effects — this effect has not been captured by the model.

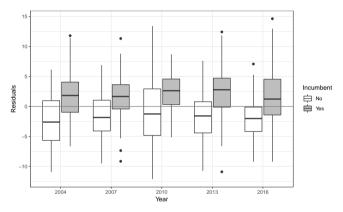


Figure 8. Boxplot of residuals for incumbent and non-incumbent parties each year. An incumbent advantage is evident and has not been captured by the model.

4.5. Robustness

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391 Multicollinearity

Three robustness checks are conducted to confirm model stability. First, a model for each election is re-estimated using only the variables that are found to be significant in at least one of the six elections. The estimated coefficients of the variables in the re-estimated models all fall within their respective 95% confidence intervals from the full models. The second check involves the ten largest pairwise correlations. For each

pair, a model for each election is re-estimated omitting one of the two variables. It is found that for each of these pairs, the estimated effect of the remaining variable in the reduced model lies within the 95% confidence interval from the full model. The final check is a visual exploration of different variable projections using a tour (Wickham et al. 2011) for each election. No definitive signs of multicollinearity are observed, and as expected (given the nature of spatial data), there is some clumping of electorates for certain projections.

Influential and outlier electorates

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Based on the distribution of the Cook's distance values and the distribution of hat values, a Cook's distance greater than 0.1 is considered to be influential, and a hat value greater than 0.5 is considered to have high leverage. Electorates fitting these criteria are flagged and investigated to examine the characteristics driving these values.

The electorate of Sydney (NSW) has a large Cook's distance and high leverage from 2001 409 to 2007, due to its diverse population (languages, birthplace and religion), high density 410 of young adults (20 to 34 years old), high number of defacto relationships, high income, 411 high household mobility and small amount of workers in extractive and transformative jobs. It has remained a strong supporter of the Labor party and the extent of this support 413 is underpredicted by the model, making it an outlier. Nearby in metropolitan NSW, 414 the electorate of Wentworth is found to be an outlier in the 2013 and 2016 elections. 415 Although historically Liberal, its two-party vote jumped by over 10 percentage points 416 in 2010 without experiencing any notable changes in its socio-demographic makeup — 417 implying that this may be the direct effect of its Liberal member, Malcolm Turnbull, 418 becoming the leader of the Liberal party. In the elections since, the model underpredicts Wentworth's Liberal support. 420

Lingiari, an electorate taking up almost all of the Northern Territory, has consistently 421 high leverage (all years) and is an outlier in all but the 2013 election due to its large 422 Indigenous population, low rates of property ownership and few workers in management 423 or administrative jobs. Fowler (NSW) has a diverse population with a high proportion 424 of migrants, many Buddhists and Muslims, as well as a high proportion of single parent 425 households. These characteristics explain its high leverage in 2001, 2004, 2010 and 426 2013, and its strong Labor support makes it influential in 2001, 2004 and 2010. Other 427 electorates with large Cook's distance are Canberra (ACT) and Durack (WA) in 2013, 428 and Solomon (NT) in 2016. 429

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All of the electorates examined are not unduly influential in the model and therefore no action is required.

432 **5. Conclusion**

This paper explores the effects of electoral socio-demographic characteristics on the two-party preferred vote in the 2001–2016 elections, using information from the corresponding Australian federal elections and Censuses. As a Census does not always occur in the same year as an election, Census data for the 2004–2013 elections are generated by employing a method of spatio-temporal imputation. This imputes electoral socio-demographics for the electoral boundaries in place at the time of the election — an approach that is distinctly different from previous work on modelling election outcomes, where Census and election data are typically joined without addressing their temporal differences. Before estimating a model, these socio-demographic variables are standardized (to adjust for changing variable scales) and many variables (representing similar information) are combined into factors, resulting in a reduced predictor set. A spatial error model is then estimated for each election, accounting for the inherent spatial structure of the data.

Across the past six elections, most of the socio-demographics that drive the electoral two-party preferred vote are found to remain steady, whilst a few (typically weaker) effects vary over time. Industry and type of work are particularly influential. Energyrelated and manufacturing/construction jobs, as well as administrative roles and jobs in education and social services are strongly linked with the Liberal party in all elections. Incomes have a similarly consistent effect, with higher income areas supporting Liberal. Higher levels of unemployment shift from weak association with Labor to a significant Liberal effect over the years, and higher education levels are associated with Labor from 2007 (although marginally insignificant in 2010). Electorates with large populations 20 to 34 years are strongly associated with Labor, whilst the 35 to 54 year old bracket also increases Labor support, but to a lesser extent. It is also found that birthplace diversity slightly favours Labor, relationships (both marriages and de facto relationships) align with Labor preference from 2010 onwards, and the influence of Christian populations has trended towards Liberal support whilst other religions have negligible effects. Family and household sizes have minimal influence, although electorates with more single parent households are linked with Labor support. Furthermore, the spatial effects are found to be positive in all elections and significant in 2001, 2004 and 2016, meaning

that other characteristics that neighbours have in common (outside of the variables in 463 the model) appear to be influential in those years. 464

The findings in this paper complement the existing literature by modelling temporal 465 trends, which as far as the authors are aware, has not been done previously for Australian 466 elections using a regression framework. It is also the first study to model any Australian 467 election since 2010 using Census information. 468

Additionally, a key contribution of this research is the wrangling of the raw data and 469 imputed data sets for the 2004, 2007, 2010 and 2013 elections, which have been 470 contributed to the eechidna R package — providing a rich, accessible data resource 471 for any future Australian electoral analysis.

6. Acknowledgements

This paper was produced using RMarkdown (Allaire et al. 2019) and knitr (Xie 474 2015). All corresponding code for this paper can be found in the github repository 475 github.com/jforbes14/eechidna-paper, and the data used is available in the eechidna 476 package (Forbes et al. 2019). All raw data was obtained from the Australian Electoral Commission, the Australian Bureau of Statistics and the Australian Government. 478

The authors would like to sincerely thank the editor and associate editor of the Australian 479 & New Zealand Journal of Statistics and the two anonymous reviewers for providing 480 helpful comments and suggestions on earlier drafts of this manuscript. Additionally, 481 the authors would like to thank Anthony Ebert, Heike Hofmann, Thomas Lumley, Ben 482 Marwick, Carson Sievert, Mingzhu Sun, Dilini Talagala, Nicholas Tierney, Nathaniel 483 Tomasetti, Earo Wang and Fang Zhou, all of whom have contributed to the eechidna 484 package. 485

7. Software 486

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All election and Census datasets, along with electoral maps and more, are available in the eechidna (Exploring Election and Census Highly Informative Data Nationally 488 for Australia) R package, which can be downloaded from CRAN. The eechidna 489 package makes it easy to look at the data from the Australian Federal elections and Censuses that occurred between 2001 and 2016. This study contributed a large revision to the eechidna package, which included the addition of election and Census data for

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- 493 2001–2010, voting outcomes for polling booths and imputed Census data for election
- years. For more details on using eechidna, please see the articles (vignettes) on the
- github page ropenscilabs.github.io/eechidna/.

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