

GETTING STARTED EXERCISES

Here is a collection of basic ‘number-crunching’ exercises that are typical of statistical tasks performed in R every day. Try to do them all in the accompanying exercise R script file (see exercise folder for session 1).

(Normal percentiles). The `qnorm` function returns the percentiles (quantiles) of a normal distribution. Use the `qnorm` function to find the 95th percentile of the standard normal distribution. Then, use the `qnorm` function to find the quartiles of the standard normal distribution (the quartiles are the 25th, 50th, and 75th percentiles). Note that you can use `c(.25, .5, .75)` as the first argument to `qnorm`.

(Chi-square density curve). Use the `curve` function to display the graph of the $\chi^2(1)$ density. The chi-square density function is `dchisq`.

(Gamma densities). Use the `curve` function to display the graph of the gamma density with shape parameter 1 and rate parameter 1. Then use the `curve` function with `add=TRUE` to display the graphs of the gamma density with shape parameter k and rate 1 for $k = 2, 3$, all in the same graphics window. The gamma density function is `dgamma`. Consult the help file `?dgamma` to see how to specify the parameters.

(Binomial probabilities). Let X be the number of “ones” obtained in 12 rolls of a fair die. Then X has a `Binomial($n = 12, p = 1/3$)` distribution. Compute a table of binomial probabilities for $x=0,1, \dots, 12$ by two methods:

a. Use the probability density formula

$$P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$$

and vectorized arithmetic in R. Use `0:12` for the sequence of x values and the `choose()` function to compute the binomial coefficients (n over k)

b. Use the `dbinom` function provided in R and compare your results using both methods.

(Binomial CDF). Let X be the number of “ones” obtained in 12 rolls of a fair die. Then X has a `Binomial($n = 12, p = 1/3$)` distribution. Compute a table of cumulative binomial probabilities (the CDF) for $x = 0,1, \dots, 12$ by two methods: (1) using `cumsum` and the result of the previous exercise, and (2) using the `pbinom` function. What is $P(X > 7)$?

(Presidents’ heights). Refer to the data on the heights of the United States Presidents compared with their main opponent in the presidential election. Create a scatterplot of the loser’s height versus the winner’s height using the `plot` function.