

Math 324 A - Summer 2017
Midterm exam 1
Friday, June 7th, 2017

Name: _____

Problem 1	14	
Problem 2	12	
Problem 3	12	
Problem 4	12	
Total	50	

- There are 4 questions on this exam. Make sure you have all four.
- **You must show your work on all problems.** The correct answer with no supporting work may result in no credit. Put a box around your FINAL ANSWER for each problem and cross out any work that you don't want to be graded.
- Give exact answers, and simplify as much as possible. For example, $\frac{\pi}{\sqrt{2}}$ is acceptable, but $\frac{1}{2} + \frac{3}{4}$ should be simplified to $\frac{5}{4}$.
- If you need more room, use the backs of the pages and indicate to the grader that you have done so.
- Raise your hand if you have a question.
- Any student found engaging in academic misconduct will receive a score of 0 on this exam.
- You have 60 minutes to complete the exam. Budget your time wisely!

GOOD LUCK!

1. (a) (7 pts) Let $B \subset \mathbb{R}^3$ be the region inside the sphere $x^2 + y^2 + z^2 = 16$, outside the sphere $x^2 + y^2 + z^2 = 1$, and inside the cone $x^2 = 3y^2 + 3z^2$. Set up an integral to find the volume of B . **You do not need to evaluate it.**

- (b) (7 pts) Let S denote the sphere of radius 2 centered at $(0, 0, 0)$, and imagine that S is filled with a fluid with density function $f(x, y, z) = z^3 - z + 2$. Find the total mass of fluid inside S by integrating the function f over S .

2. (12 pts) Use cylindrical coordinates to evaluate

$$\iiint_E e^z dV,$$

where E is the region enclosed by the paraboloid $z = 4 + x^2 + y^2$, the cylinder $x^2 + y^2 = 2$, and the plane $z = 0$.

3. (12 pts) Consider the tetrahedron $E \subset \mathbb{R}^3$ bounded by the planes $x = 0, z = 0, z = 2y$ and $2x + 2y + z = 4$. Set up the triple integral

$$\iiint_E xz \, dV$$

with the two given orders of integration. **You do not need to evaluate the integrals.**

(a) $dx \, dy \, dz$.

(b) $dy \, dz \, dx$.

4. (12 pts) Consider the region in the x - y plane inside the circle $x^2 + (y - 1)^2 = 9$ and above the line $y = x\sqrt{3}$.

(a) Re-write the circle equation using polar coordinates.

(b) Solve the equation you got in part *a* for r as a function of θ .

(c) Draw a picture of D , and set up an integral in polar to find the area of D using your answer from part *b*. **You do not need to evaluate it.**