Deep Learning Assignment 3

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1 1 General Questions

2 Softmax regression gradient calculation

з Given

$$\hat{y} = \sigma(Wx + b)$$
, where $x \in \mathbb{R}^d$, $W \in \mathbb{R}^{k \times d}$, $b \in \mathbb{R}^k$ (1)

4 where d is the input dimension, k is the number of classes, is the softmax function:

$$\sigma(a)_i = \frac{exp(a_i)}{\sum_j exp(a_j)} \tag{2}$$

- 5 Which means a given input x will output y with probability of each class
- 6 **2.1** Derive $\frac{\partial l}{\partial W_{ij}}$
- 7 If the given cross-entropy loss defined as followed:

$$l(y,y) = -\sum_{i} y_i \log \hat{y_i} \tag{3}$$

8 As W_{ij} will affect the prediction of class i by multipling index j in x, therefore we can derive:

$$\frac{\partial l}{\partial W_{ij}} = \frac{\partial l}{\partial \hat{y}_i} \frac{\partial \hat{y}_i}{\partial W_{ij}} \tag{4}$$

9 where:

12

$$l(y, \hat{y}) = -\sum_{i} y_{i} \log \hat{y}_{i} = -(y_{i} \log \hat{y}_{1} + y_{2} \log \hat{y}_{2} + \dots + y_{i} \log \hat{y}_{i} + \dots)$$
 (5)

10 and therefore

$$\frac{\partial l}{\partial \hat{y}_i} = \frac{-y_i}{\hat{y}_i \ln 10} \tag{6}$$

And we can rewrite (1) and (2) and care the value only for \hat{y}_i :

$$\hat{y_i} = \frac{e^{(W_{ij}X_j + b_i)}}{C + e^{(W_{ij}X_j + b_i)}}, \text{ where } C = \sum_k e^{W_{ik}X_k + b_i} - e^{(W_{ij}X_j + b_i)}$$
(7)

 $\frac{\partial \hat{y}_i}{\partial W_{ij}} = \frac{X_j e^{(W_{ij}X_j + b_j)}}{C + e^{(W_{ij}X_j + b_j)}} - \frac{X_j e^{2(W_{ij}X_j + b_j)}}{(C + e^{(W_{ij}X_j + b_j)})^2}$ (8)

13 Combining (6) and (8) to (4), and we will get the result

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14 3 Chain rule

15 4 Variants of pooling

5 Convolution

- 17 (a) As it is using 3x3 kernal along x and y axis of input, which is 5 and 5 respectively. The output of
- this layer will be $(5-3+1) \times (5-3+1)$ which is 3x3.
- (b) Assuming the kernel operation is point-point multiplication and summation, then the output of this layer is:

- 24 6 Optimization
- 7 Top-k error
- 26 8 t-SNE
- 9 Proximal gradient descent