

# Regional Disparities, Aggregation Effects and the Role of Space

Evidence from Homicide Rates in Colombia 2010-2018

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July 24th 2019

## Motivation:

- Beyond GDP, social variables and their convergence are relevant for development studies (Royuela et al 2015)
- Persistent income differences, differences in health indicators and in "general" regional inequality in Colombia.
- Scarce academic literature on inequality (convergence approach) at the municipality level.

## Research Objective:

- Study convergence/divergence of homicide rates across municipalities and departments in Colombia 2010-2018
- Analyze spatial autocorrelation and its robustness at different disaggregate levels

## Methods:

- Classical convergence framework (Barro and Sala-i-Martin 1992)
- Distributional convergence framework (Quah 1996; Hyndman et. al 1996)
- Spatial autocorrelation (Moran's I)

# Main Results:

1. **Sigma Convergence** for homicide rates at the state level, **Beta Convergence** at the municipality level
2. Regional disaggregation matters: **Local convergence clusters**
3. **Clustering dynamics**
  - State level: 4+? convergence clusters
  - Municipality level: 2+? convergence clusters
4. **Spatial Autocorrelation** robust only at the municipality level

# Outline of this presentation

1. **Data description** Survival rates (not homicide rates)
2. **Global convergence:** Using classical summary measures
  - Beta convergence
  - Sigma convergence
3. **Regional disaggregation:**
  - Distribution dynamics framework
  - Distributional convergence
4. **Local convergence clusters**
5. **Global spatial autocorrelation:**
  - Disaggregation effects
6. **Concluding Remarks**

## Data:

- Total number of homicides in Colombia per year from 2010 until 2018 (data taken from the National police).
- Data is aggregated at the municipality and departament level.
- Population census and estimates for states and municipalitites.
- Raw rates computed

$$Hrate = homicides/population$$

- Survival rates (non- murder rates) computed

$$NMR = 10000 - raw\ rate * 10000$$

- **Survival rates** are chosen because positively defined variables are a **standard** in the convergence literature.

## (2) Global convergence:

Using classical summary measures

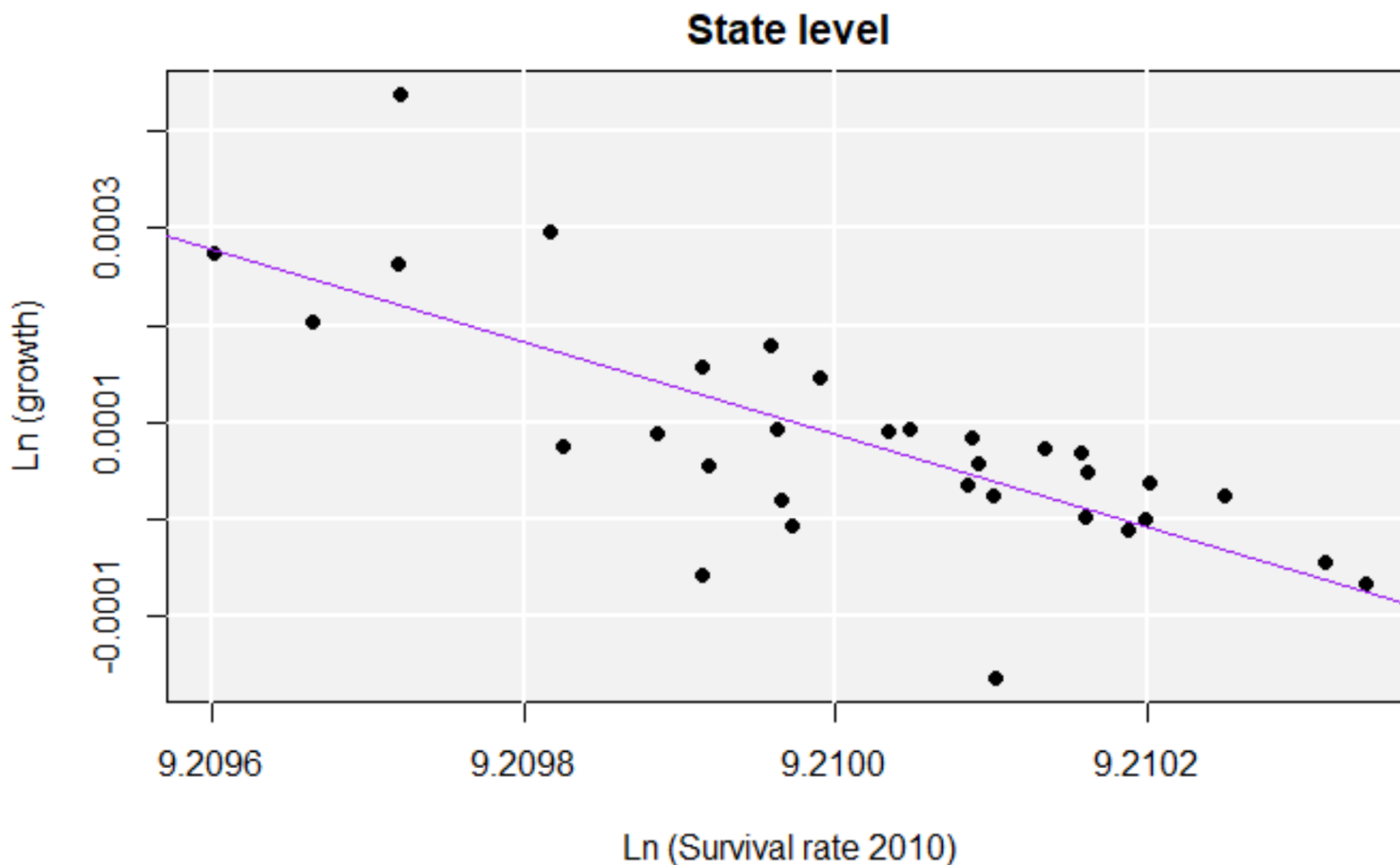
Beta convergence

Sigma convergence

## States-Sigma and Beta convergence

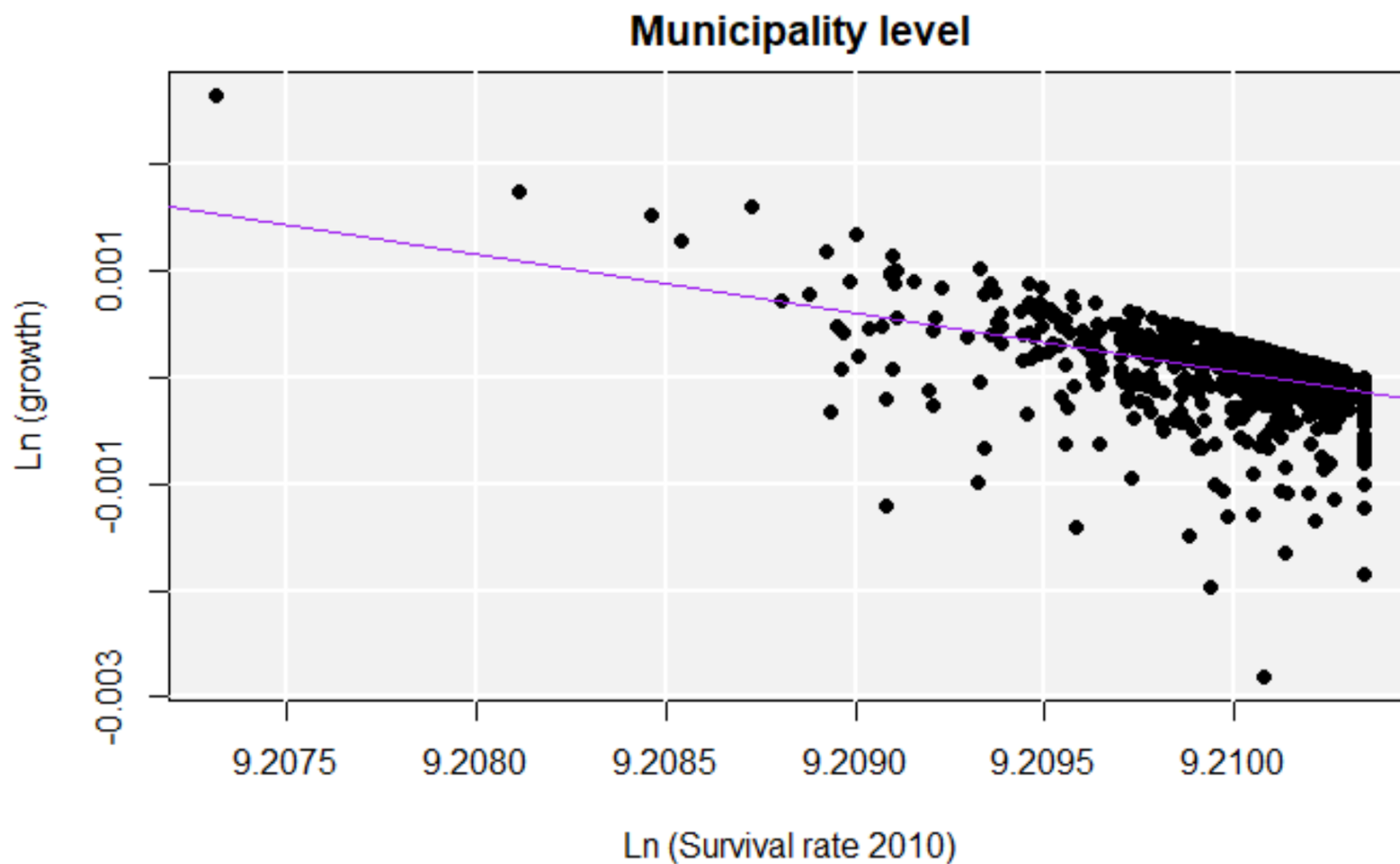
$\sigma$ (Standard deviation)  $\sigma_{2010} = 1.84$   $\sigma_{2018} = 1.26$

$$\log \frac{Y_t}{Y_0} = \alpha + \beta * \log Y_0 + \epsilon \quad \beta = -0.476^{***} \quad \text{halflife} = 8.59 \text{ years}$$



## Municipalities - Beta convergence (only)

$$\log \frac{Y_t}{Y_0} = \alpha + \beta * \log Y_0 + \epsilon \quad \beta = -0.551^{***} \quad \text{half life} = 6.92 \text{ years}$$





## (3) State and Municipality disaggregation:

Distribution dynamics framework

Distributional convergence class: middle

## Regional heterogeneity matters

Dynamics of the **entire regional distribution**

**conditional density** estimation

## The distribution dynamics framework

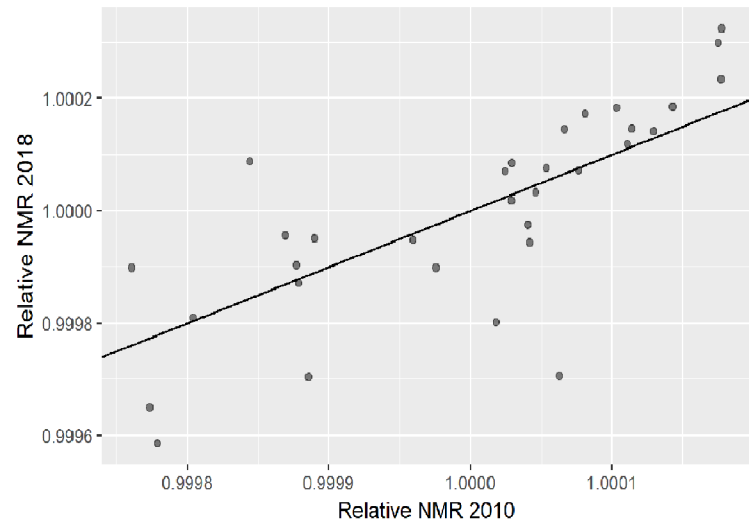
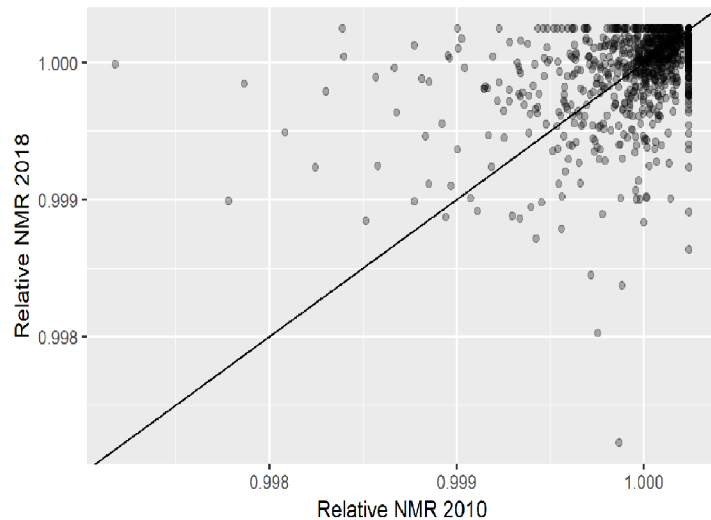
## (4) Local convergence clusters

State level: 4+? convergence clusters

Municipality level: 2+? convergence clusters

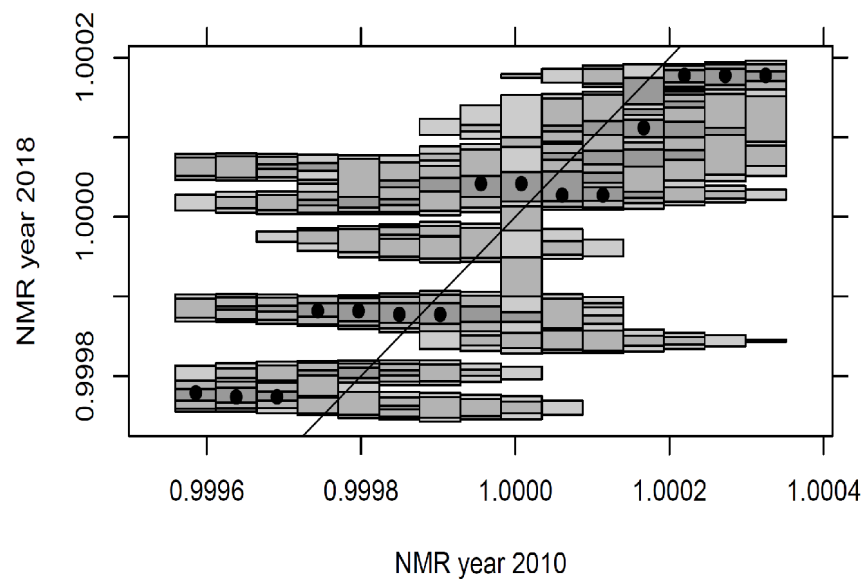
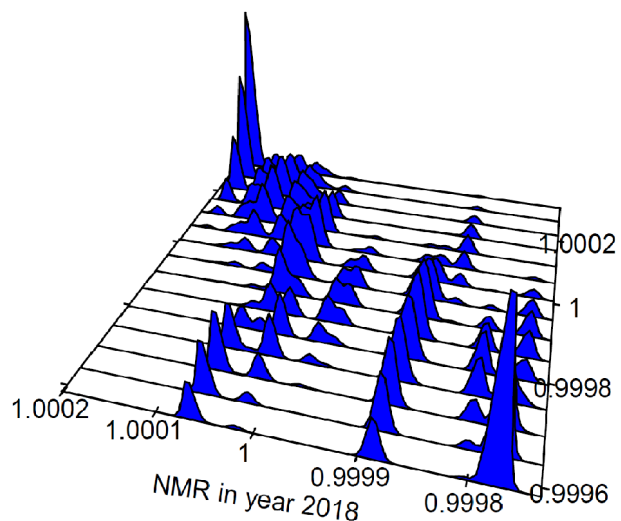
# Where are the clusters?

Municipality level ----- Department Level



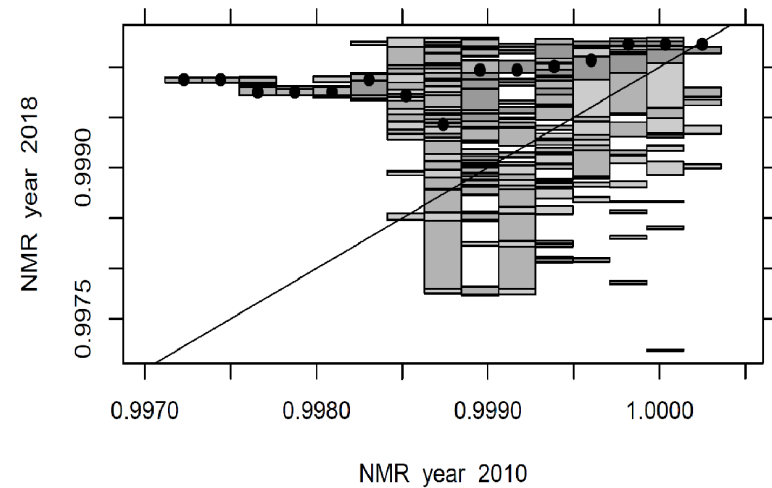
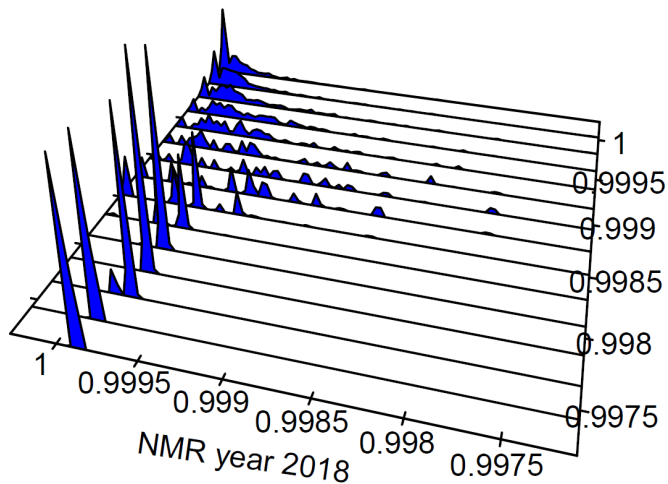
Those lines are not regression trends!

## State level: 4+? convergence clusters



Multimodal distribution with sigma convergence

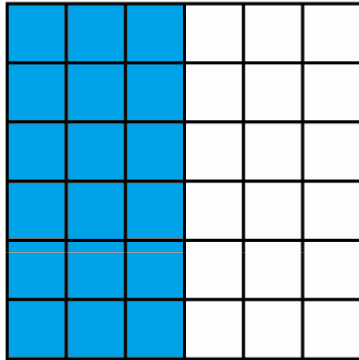
## Municipality level: 2+? convergence clusters



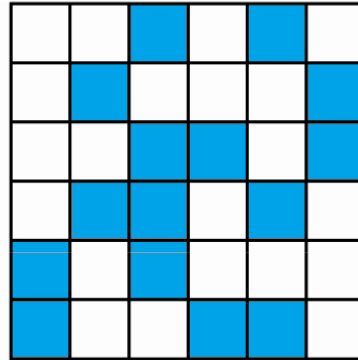
Interesting results; there are fewer clusters but sigma convergence is not present.

## (4) Spatial Autocorrelation (morán I definition)

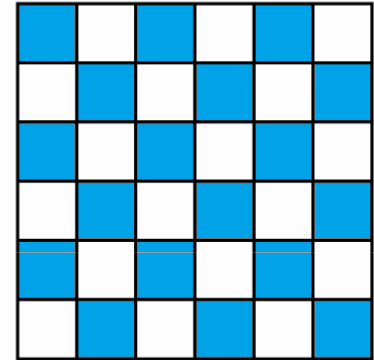
### High Intuition Concept



Positive spatial  
autocorrelation



No spatial  
autocorrelation



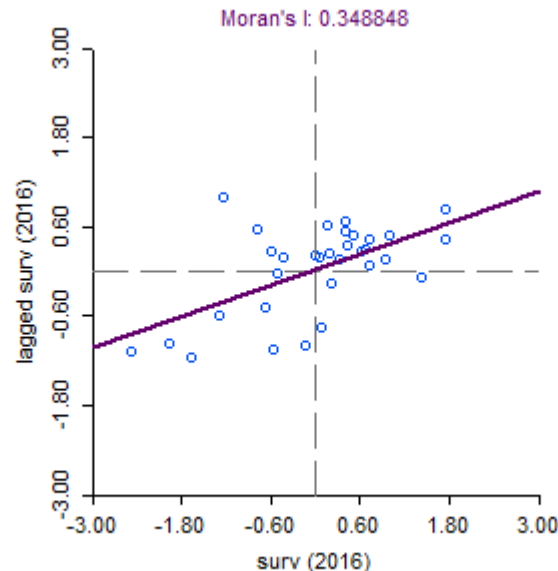
Negative spatial  
autocorrelation

Source: adapted from Radill (2011)

### More Formal (less intuitive)

$$I = \frac{\sum_i \sum_j w_{ij} z_i \cdot z_j}{\sum_i z_i^2} = \frac{\sum_i (z_i \times \sum_j w_{ij} z_j)}{\sum_i z_i^2}.$$

In the linear regression  $y = \alpha + \beta x$ , the estimate for  $\beta$  is  $\sum_i (x_i \times y_i) / \sum_i x_i^2$ . In the Moran scatter plot shown below,  $y$  is the spatial lag variable  $\sum_j w_{ij} z_j$



### Differential Moran Scatter Plot ( $y_{i,t} - y_{i,t-1}$ )

Differencing the variable to control for the locational fixed effects: We compute the Moran's I for the variable  $y_{i,t} - y_{i,t-1}$ . If we consider there is a fixed effect  $\mu_i$  related to location  $i$ , it is possible to present the value at each location for time  $t$  as the sum of some intrinsic value and the fixed effect.  $y_{i,t} = y *_{i,t} + \mu_i$  (Geoda documentation 2019)



## (4) Spatial autocorrelation

**State level:** Moran's I statistic significant from 2012, differential Moran's I is not significant  
(not robust)

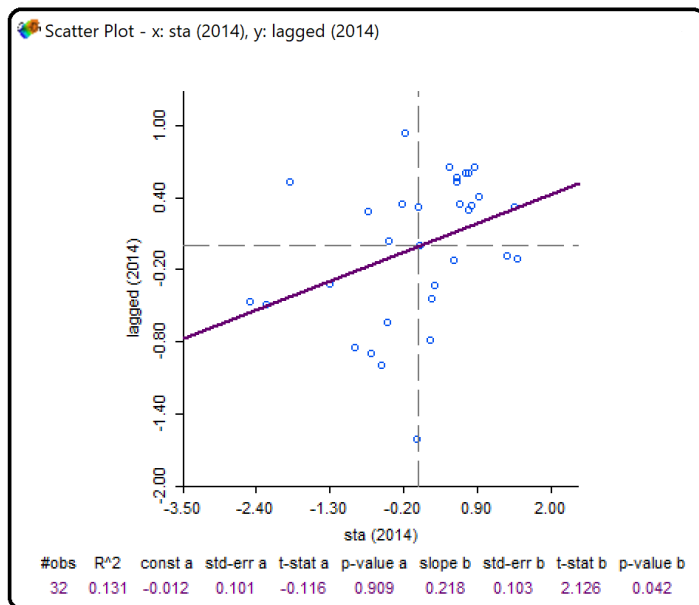
**Municipality level:** Differential Moran's I significant from 2010 (robust)

## (4) Spatial autocorrelation

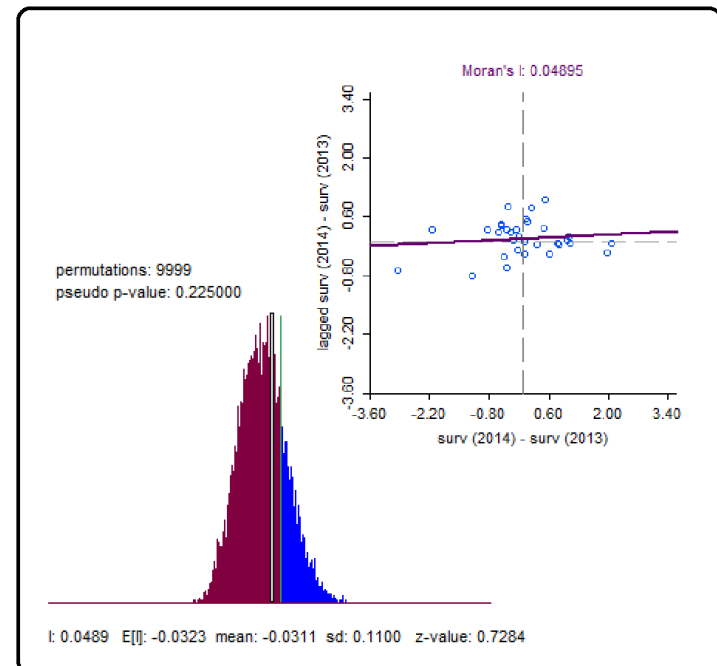
### State level (not robust)

- Univariate Moran's I is significant from 2012.
- But, **The differential moran statistic is not significant.** It is then considered that the significance of Spatial Autocorrelation is **not robust**.
- See plots for 2014 and 2014-2013, similar for other years (standardized variables)

Univariate Moran



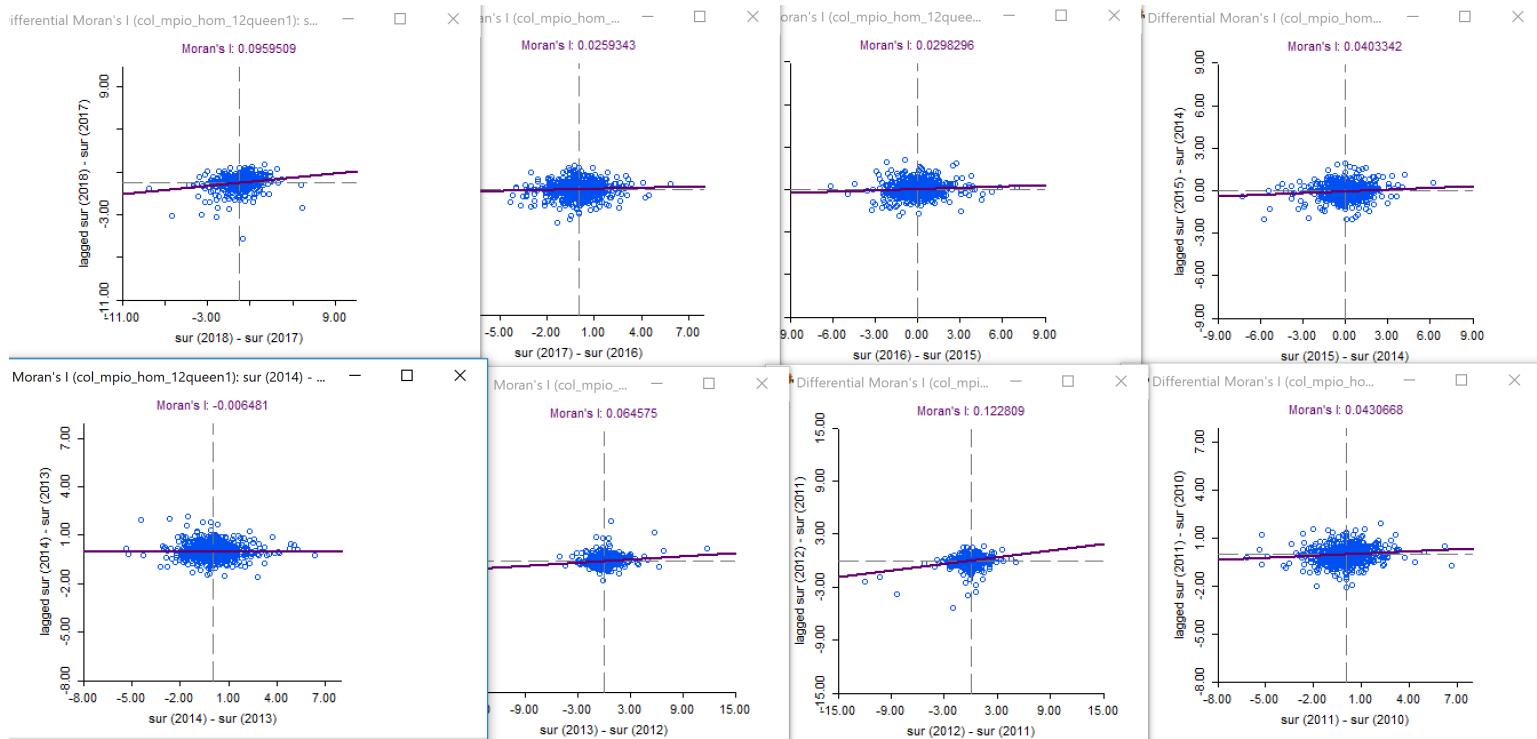
Differential Moran



## (4) Spatial autocorrelation

### Municipality level (Robust)

- The univariate Moran's I is not significant in 2010 and 2011. however, it is significant from 2012 to 2018; reaching a maximum value in 2016.
- Differential Moran's I (  $sur_{2018} - sur_{2010}$  ) is significant  $Moran's I = 0.22^{***}$
- Subsequent Differential Moran's I  $sur_t - sur_{t-1}$  statistically significant at the municipality level. Except 2014-2013 (not statistically significant) see graphs



## (5) Concluding Remarks

### Uplifting results "on average" :

- Differences in overall raw rates at the state level **have decreased** and the means at both levels have increased (survival rate)
- **Global convergence on average at the state level**, while fast beta convergence at the municipality level.

### Beyond classical convergence :

- Regional differences matter in **both disaggregation levels**.
- **Multiple local convergence clubs**; with more clubs at the state level.

### The Role of Space

- Subsequent Differential Moran's I are robust and significant at the **municipality level only**
- Results at the **state level** are not conclusive and similar to the ones reported by Royuela et al 2015.

## (5) Concluding Remarks

### Implications and further research

- Strong spatial autocorrelation suggest the possibility of applying the Getis filtering in order to filter the spatial component of homicide variables.
- Convergence clusters help us to find regions with similar outcomes, coordination among them can be promoted.
- Has crime followed a trajectory? can a speed and direction of contagious patterns be found?
- At the state or department level (including more variables) can a probit model help us to find the determinants for a conditional "jump" to the upper clusters.

# Thank you very much for your attention

If you are interested in our research, please check Prof. Carlos Mendez website

<https://carlos-mendez.rbind.io>

And the research seminar's website <https://carlos-seminar.rbind.io/>

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Stay tuned for my Felipe's Master's thesis

**Will the SGDs be Achieved in Colombia? A Study of National Convergence and Regional differences.**

Gender inequality, Income, Education, Crime... Classical convergence, Distributional Dynamics, Spatial Filtering, Spatial econometrics, long-run Filtering...