# Scan pattern

By using the scan pattern, give a parallel solution for the following problems.

#### **Prefix sum**

The prefix sum operation takes a binary associative operator  $\oplus$  and an ordered set of n elements  $[a_0,a_1,...,a_{n-1}]$  and returns the ordered set

$$[a_0, (a_0 \oplus a_1), ..., (a_0 \oplus a_1 \oplus ... \oplus a_{n-1})]$$

Design and implement a parallel algorithm to compute the prefix sum operation, assuming that the binary operator  $\oplus$  corresponds to the addition.

## List ranking

The list ranking operation takes a binary associative operator  $\oplus$  and a linked list L with n nodes. Let a be an element of L, where next(a) is the position of the node following a on L, and val(a) is the value stored in the node a. The linked list operations is defined as the computation of the distance of each node of L from the head of the list. An alternative definition is this: The computation of the prefix sum operation over the values val(), using the operator  $\oplus$ , by following the references given by the next() function.

Design and implement a parallel algorithm to compute the list ranking operation, assuming that the binary operator  $\oplus$  corresponds to the addition.

## **Filtering**

Given an array of integers, implement a parallel algorithm to filter of the elements that meet a given condition. The output of the algorithm must a an array with all the elements that meet the condition.

**Note:** The pattern to reduce the size of an array, by deleting unused elements is called **pack** 

**Hint:** Use the prefix sum operation.

# **Graph to tree**

Given a the adjacency list representation of a graph G and the list of visited edges after a DFS traversal, implement a parallel algorithm to construct an spanning tree of G using the visited edges.

**Note:** Assume the adjacency list representation given in <u>www.josefuentes.cl/datasets/graphs.php</u>. To test your algorithm, use the datasets given in the same web page.

**Hint:** Use the prefix sum operation.

### **Euler tour**

Given a tree T, design and implement a parallel algorithm to compute the Euler Tour of T.

**Note:** Assume the adjacency list representation given in <u>www.josefuentes.cl/datasets/trees.php</u>. To test your algorithm, use the datasets given in the same web page.

**Hint:** Use the list ranking operation.