Stat 610 Homework 7

Due Wednesday, November 6, 11:59pm

Assignment

You will experiment with fitting distributions to some baseball statistics. In particular, we will look at how well the number of home runs a player hits in a season can be modeled by the Poisson and negative binomial distributions.

- The data are available in the Lahman package. Install with install.packages('Lahman'), and then get the data using library(Lahman) and data(Batting). The data command will add a data frame called Batting to your environment.
 - We will be interested in modeling the number of home runs hit by each player in 2018. These are available with subset(Batting, yearID == '2018')\$HR. You should save them as something, e.g. hrs <- subset(Batting, yearID == '2018')\$HR.
- 2. Fitting a Poisson by eye: Suppose that we are modeling hrs as coming from a Poisson distribution. Make a plot like we did in class that shows the empirical and expected fraction of the time we observe hrs = i, for i between o and 30. For the "expected" part of the plot, you will need to choose what mean parameter to pick for the Poisson. Experiment with a couple and pick the one that you like the best.
- 3. "Best-fitting" Poisson: It turns out that both method of moments and maximum likelihood estimation tell you that the "best-fitting" Poisson will be the one whose mean parameter matches the empirical mean (the mean of hrs).
 - Make the same sort of plot you did in the previous question, but with the mean of the Poisson set to be the mean of hrs. What do you think of the fit?
- 4. Negative binomial by eye: The negative binomial, like the Poisson, is a distribution that is supported on 0,1,2,.... However, it has two parameters instead of just one, meaning that its variance can be different from its mean (for the Poisson distribution the mean equals the variance).

There are a number of different parameterizations of the negative binomial, but for the purposes of this exercise the easiest is probably the one given at https://mc-stan.org/docs/2_20/functions-reference/nbalt.html. The parameter μ at the linked site is called mu in the dnbinom function in R, and the parameter ϕ at the linked site is called size. μ gives the mean of the distribution, and the variance is $\mu + \mu^2/\phi$. Note that since ϕ is always positive, the variance of a negative binomial distribution is always larger than its mean, and how much larger is determined by ϕ .

Make the same sort of plot as in question 2, using the dnbinom function, setting mu to equal the empirical mean, and experimenting with different values of size.

5. Negative binomial by method of moments: Remember that in method of moments, we choose parameters for the distribution by matching the theoretical moments of the distribution to the empirical moments of the data. Find parameters μ and ϕ (mu and size) so that the mean and variance of a NegativeBinomial(μ , ϕ) distribution match the empirical mean and variance of hrs. Make the empirical/expected plot one last time, and compare the fit of this negative binomial to the Poisson fit in question 3.

Submission parameters

 Submit an .Rmd and .pdf or .html file with your answers to the questions, your code, and a description of what it is doing.