

## CS 2850 – Networks HW 4

jfw225

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1. (a) Buyer  $y$  will bid the highest value at 7, and thus, win the auction because each buyer bids fairly in a second price auction. In addition,  $y$  will pay the second highest bid which is 5.  
(b) We start with creating two other fictional items  $b, c$ . After running the VCG procedure, we observe that item  $a$  goes to  $y$  for 5 as before, item  $b$  goes to  $x$  at 0, and item  $c$  goes to  $z$  at 0. Note that 5 is the harm that  $y$  causes to  $x, z$  because 5 is the value that  $a$  would be obtained at without  $y$ .
2. (a) The perfect matching that is yielded by treating the ALLOCATING SLOTS TO ADVERTISERS problem as a matching market is the following:  $x \rightarrow a$  at 0,  $y \rightarrow c$  at 8, and  $z \rightarrow b$  at 23.