Using the kcorebip package

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June 13, 2017

Introduction

This package performs the k-core decomposition analysis of a bipartite graph and provides two new kinds of plot: polar and ziggurat. It works for any kind of bipartite network, but we developed it to study ecological mutualistic communities, so we use terminology and examples of that research field [GA+17].

Decomposition and definition of k-magnitudes

The k-decomposition is an iterative algorithm that prunes links of nodes with degree equal or less than k [Sei83]. The process starts pruning nodes with k=1 until all the resting nodes have two or more links. Then it continues with k=2, and so on. After performing the k-decomposition, each species belongs to one of the k-shells. The highest value of k, i.e ks_{max} , corresponds to the innermost $core\ ks_{max} \equiv C^{A,B}$. For each k-shell there are two subsets, one per guild (A and B), that we call K_j^A, K_j^B where j is the k-shell index.

In order to quantify the distance from a node to the innermost shell of the partner guild, we calculate the average of the shortest paths to all the nodes in that set. We define the k_{radius} of node m of class A as the average distance to the species of C^B :

$$k_{radius}^{A}(m) = \frac{1}{|C^{B}|} \sum_{j \in C^{B}} dist_{mj} \qquad m \in A$$
 (1)

where $dist_{mj}$ is the shortest path from species m to each of the j species that belong to the set C^B . The same definition is valid for species of the guild B computing the average distance to C^A . The minimum possible radius value

is 1 for one node of the maximum shell directly linked to each one of the maximum shell set of the opposite guild.

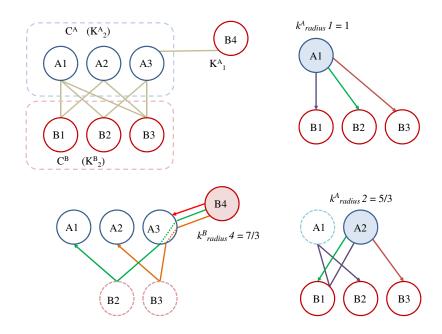


Figure 1: Examples of k_{radius} in a fictional network.

Figure ?? is a very simple fictional network, with only seven nodes. The upper left graph shows network structure. In the upper right figure, species A1 belongs to C^A . The distance to each of the nodes of C^B is 1, so its $k_{radius1}(1)$ is 1. In the bottom right figure, node A2 also belongs to C^A but there is not any direct link with B2, so the distance between them is 3 and $k_{radius}(2)$ is $\frac{5}{3}$. In the bottom left figure, node B4 is not part of C^B , and as may be expected, the value of its k_{radius} is higher.

A global value can be defined averaging this magnitude across network:

$$\overline{k}_{radius} = \frac{1}{|A \cup B|} \sum_{l \in A \cup B} k_{radius}(l) \tag{2}$$

In our example network of Figure $\ref{eq:1}$, the value is 11/7.

 k_{radius} is a useful magnitude to measure network compactness but it not a good measure of centrality. For instance, its value for an isolated specialist

linked to the maximum core is low. To attend this necessity, we define a second k-magnitude, the k_{degree} :

$$k_{degree}^{A}(m) = \sum_{j} \frac{a_{mj}}{k_{radius}j} \quad m \in A, \forall j \in B$$
 (3)

where a_{mj} is the element of the interaction matrix that represents the link. So the $k_{degree}m$ is the sum of the inverse of k_{radius} for each node linked to m. A node of the innermost shell will have a high degree, whereas specialists have only one or two links and so a low k_{degree} . In the example of Figure ??, this magnitude is 1 + 3/5 + 3/5 = 11/5 for node B3, while only 3/7 for node B4.

Input file format

We use the file format of web of life ecological data collection [Bas09]. Data are stored as .csv files. Species of guild a are distributed by colums, and those of guild b by rows. First colum contains the labels of guild b nodes, and first row, the labels of guild a. If the interaction matrix is binary, the cell of species_a_m, species_b_n will be set to 1. If it is weighted, to a real number different of 0.

The naming convention is $M_XX_NNN.csv$ where XX is the type, PL for pollinator networks and SD for seed dispersers, and NNN a serial number. Anyway, you can call your file whatever you want.

| | Α | В | С | D | E |
|---|-------------------|---------------------|----------------------|--------------|------------------------|
| 1 | | Juniperus phoenicea | Osyris quadripartita | Corema album | Phillyrea angustifolia |
| 2 | Turdus merula | 1 | 1 | 1 | 1 |
| 3 | Turdus iliacus | 1 | 1 | 0 | 0 |
| 4 | Turdus philomelos | 1 | 1 | 0 | 0 |
| 5 | Turdus torquatus | 1 | 0 | 0 | 0 |
| 6 | Turdus viscivorus | 1 | 0 | 0 | 0 |
| 7 | | | | | |

Figure 2: Examples of input file, the seed disperser network 029 of web of life site.

Network analysis

The function analyze_network performs the k-core decomposition and analysis.

Arguments:

- namenetwork: name of the file of the interaction matrix.
- directory: where the network file is stored.
- guild_a: prefix for the guild of nodes stored in rows.
- guild_b: prefix for the guild of nodes stored in columns.
- plot_graphs: plot kshell histogram and Kamada Kawai plots.
- only_NODF: just computes the *NODF* measurement of nestedness.

The function returns:

- calc_values, a list containing the following objects:
 - graph: an igraph::graph object. This is the additional information for each node, besides the regular of the object:
 - * V(result_analysis\$graph): list of node names
 - * $V(result_analysis\$graph)\$kdegree: list k_{degree}$
 - * $V(result_analysis\$graph)\$kradius: list k_{radius}$
 - * V(result_analysis\$graph)\$krisk: list k_{riks} , a measurement of vulnerability (See [GA+17])
 - max_core: maximum k shell index
 - nested_values: a list containing all the values provided by the bipartite::nested function, unless only_NODF set TRUE.
 - num_guild_a: number of nodes of guild a.
 - num_guild_b: number of nodes of guild b.
 - links: number of network links.
 - meandist: network average kradius.
 - meankdegree: network average kdegree.
 - spaths_mat: matrix with node to node shortest distance paths.
 - matrix: interaction matrix with nodes of guild a by columns and guild b by rows.
 - g_cores: list with the value of kshell for each node.
 - modularity_measure: value of igraph::modularity function.

The Polar Plot

The $Polar\ Plot$ shows nodes (species) centrality and provides an overview of network distribution. It was inspired by the fingerprint-like graph, developed by Alvarez-Hamelin $et\ al.\ [AH+05]$ to plot very large k-decomposed networks.

Nodes are depicted with their centers located at k_{radius} . Angles are assigned at random by the visualization algorithm and each guild lies inside one of the half planes. The size of each node is proportional to its k_{degree} and the color represents the k_{shell} . This visualization does not include links. The user may choose adding the histograms of k-magnitudes, a handy option because they convey a wealth of structural information.

The function call is:

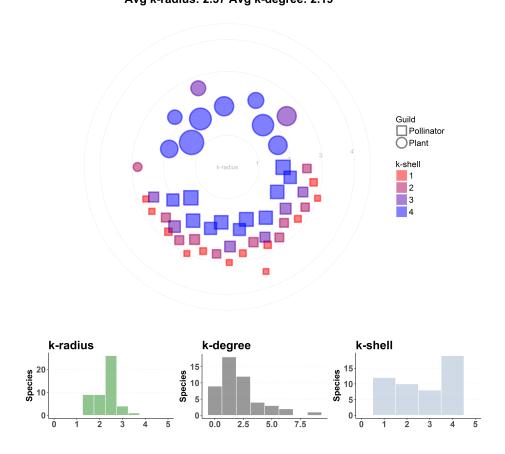
The parameters red, directorystr and plotsdir are the name of the interaction matrix, the directory where it is stored and the name of the plotting directory. If print_to_file is set to FALSE the polar plot will be displayed in the current R session. The name of the output file is that of the input file plus _polar.png. Paths are relative to the current working path in R but you may also specify absolute paths.

File plots have a resolution of 600 dots per inch, and a size of 12×12 inches. If the user wants to display the result in the current R session, label sizes may appear different depending on the installed fonts and size of the plotting window.

The following command creates the file M_PL_008_polar.png in the directory graphresults/

The plot title includes the network average k_{radius} and k_{degree} , a common measurement of nestedness called NODF [AN+08] and Modularity following the QanBiMo method [DS14].

Network M_PL_008 NODF: 35.97 Modularity: 0.2105 Avg k-radius: 2.37 Avg k-degree: 2.19



By default, nodes are unlabeled. You may choose to print some of them with the parameter printable_labels, but have in mind that the diagram may become messy. Guild labels are also configurable. The function will set automatically "Plant, Pollinator" and "Plant, Disperser" if the file follows the naming convention of the web of life site; you may choose any other pair of values with the input parameter glabels.

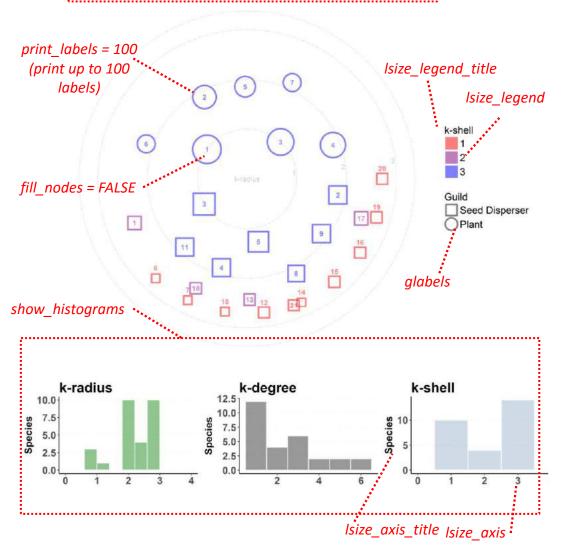
Three histrogams are displayed under the main plot, with the distributions of k_{radius} , k_{degree} and k_{shell} .

The configuration of a polar graph is quite simple. The following picture shows how and where the different input parameters modify the plot.

Network M_SD_001 NODF: 40.77 Modularity: 0.1752

Avg k-radius: 2.16 Avg k-degree: 2.33

print_title



The Ziggurat Plot

Ziggurat is the second type of visualization, created from scratch. Species are grouped by their k-shells. Each of these groups are represented as small ziggurats. The maximum k-shell is located on the left side, the other ones are arranged following an almond-like distribution.

Species of the maximum shell are ordered by their k_{degree} with the highest one leftmost. Areas do not convey meaning, their height decreases just by convenience of visualization.

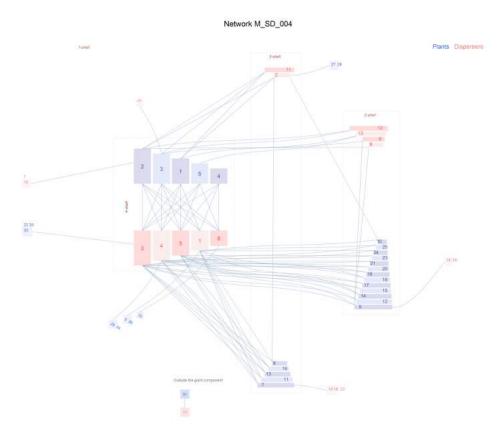


Figure 3: Ziggurat graph of an avian frugivore community in Puerto Rico with 54 species and 95 links [CCG03].

Nodes of 1-shell are scattered around the ziggurats. When multiple species of this shell are connected to the same node of any of the ziggurats they are clustered to reduce the number of lines. For instance, plants species

22, 30 and 33 are specialists linked to the generalist disperser 3. With this organization, we get a clear view of structure and interconnections. The almond shape leaves a wide space in the center of the graph to depict the links and they do not overcross the boxes of the different species. The function call is:

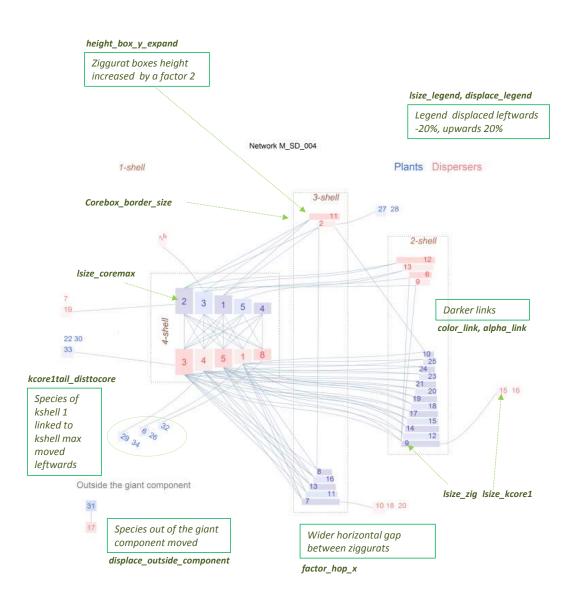
```
ziggurat_graph(datadir, filename, paintlinks = TRUE,
  displaylabelszig = TRUE, print_to_file = FALSE,
  plotsdir = "plot_results/ziggurat/", flip_results = FALSE,
aspect_ratio = 1, alpha_level = 0.2, color_guild_a = c("#4169E1",
  "#00008B"), color_guild_b = c("#F08080", "#FF0000").
  color_link = "slategray3", alpha_link = 0.5, size_link = 0.5,
displace_y_b = rep(0, 11), displace_y_a = rep(0, 11),
  labels_size = 3.5, lsize_kcoremax = 3.5, lsize_zig = 3,
  lsize_kcore1 = 2.5, lsize_legend = 4, lsize_core_box = 2.5,
  labels_color = c(), height_box_y_expand = 1, kcore2tail_vertical_separation = 1, kcore1tail_disttocore = c(1, 1), innertail_vertical_separation = 1, factor_hop_x = 1, displace_legend = c(0, 0), fattailjumphoriz = c(1, 1), fattailjumpvert = c(1, 1), coremax_triangle_height_factor = 1,
  coremax_triangle_width_factor = 1, paint_outsiders = TRUE,
  displace_outside_component = c(1, 1), outsiders_separation_expand = 1,
  outsiders_legend_expand = 1,
  weirdskcore2_horizontal_dist_rootleaf_expand = 1,
  weirdskcore2_vertical_dist_rootleaf_expand = 0,
  weirds_boxes_separation_count = 1, root_weird_expand = c(1, 1),
  hide_plot_border = TRUE, rescale_plot_area = c(1, 1), kcore1weirds_leafs_vertical_separation = 1, corebox_border_size = 0.2,
  kcore_species_name_display = c(), kcore_species_name_break = c(),
  shorten_species_name = 0, label_strguilda = "", label_strguildb = "",
  landscape_plot = TRUE, backg_color = "white", show_title = TRUE,
  use_spline = TRUE, spline_points = 100, file_name_append = "",
  svg_scale_factor = 10, progress = NULL, svg_scale_factor= 10,
weighted_links = "none", square_nodes_size_scale = 1,
  move_all_SVG_up = 0,)
```

The configuration of ziggurat plots is richer but also more complex than that of polar graphs. Some parameters are equivalent to those of the polar plot, such as filename, datadir and plotsdir that provide the input file, input directory and output directory. The output file is called as the input file plus _ziggurat.png and the user may also add the file_name_append label.

Graphical parameters provide a powerful toolset to improve visualizations. Figure ?? was created with the default call:

The same graph looks improved with some additional input data.

```
ziggurat_graph("data/","M_SD_004.csv", plotsdir = "grafresults/",
    height_box_y_expand = 2, factor_hop_x=1.5, color_link = "slategray3",
    alpha_link = 0.7, lsize_kcoremax = 6, lsize_zig = 5,lsize_kcore1 = 5,
    corebox_border_size=0.5, kcoreltail_disttocore = c(1.2,1),
    displace_outside_component = c(-0.3,1), lsize_legend = 7,
    lsize_core_box = 6, displace_legend = c(-0.2,0.2), print_to_file = TRUE)
```



Plot configuration may become quite complicated when network size grows, but we will show now the usefulness of another set of input parameters with a medium size example. Default function call provides a quite readable ziggurat plot of pollinator network number 12.

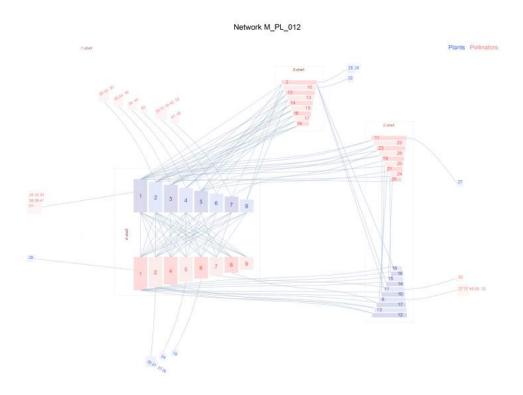
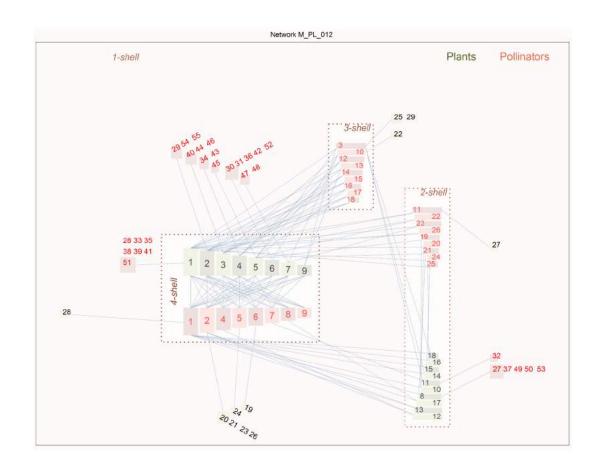


Figure 4: Ziggurat graph of a plant - pollinator network in Garajonay, La Palma (Spain). Olesen, unpublished.

This plot is nearly ready for publishing, some minor improvements would be nice, for instance increasing label sizes. However we are going to modify several input values to show how the picture changes.



We will not repeat the meaning of those that we have explained in the previous example. The role of some of the new ones are quite evident. We have changed the filling colors of ziggurats, providing the pairs color_guild_a and color_guild_b, and also the species label colors. A dime background is added as well. This trick shows the plotting area, that was horizontally increased a 20% with rescale_plot_area=c(1.2,1). This change only affects the plotting area, not the figure. The aspect ratio may be modified to flatten the plot is is lesser than 1 or to stretch it if bigger. The default value is 1, it is not mandatory to include, but we have added it to explain its meaning.

If you do not use splines, as in this example, links appear as straight lines. If you use splines you could also tell the function how many points they should have.

Fat tails are the two sets of 1-shell species eventually linked to highest k_{degree} generalists, those that are located leftmost in the max k-shell.

We saw how height_box_y_expand controls the height of outer ziggurat boxes. Height and width of rectangles of the max k-shell are modified with coremax_triangle_height_factor and coremax_triangle_width_factor.

The overall horizontal distance of 1-shell species linked to max k-shell (except fat tails) is increased or decreased with horiz_kcoremax_tails_expand.

Vertical separation of ziggurats is changed with vectors displace_y_a and displace_y_b. In this example, ziggurat of 2-shell plants is moved upwards by a 50%, 2-shell pollinators downwards 20% and 3-shell pollinators upwards 10%.

Finally, vertical separation of tails connected to inner ziggurats is increased with innertail_vertical_separation. See plant species 22 and 25.

Next example shows how to manage weird tails and outsiders. Weird tails are chains of species of 1-shell. They are rather unstable so they do not appear frequently. Outsiders are the species not connected to the giant component. Pollinator network 031 has species of both kinds.

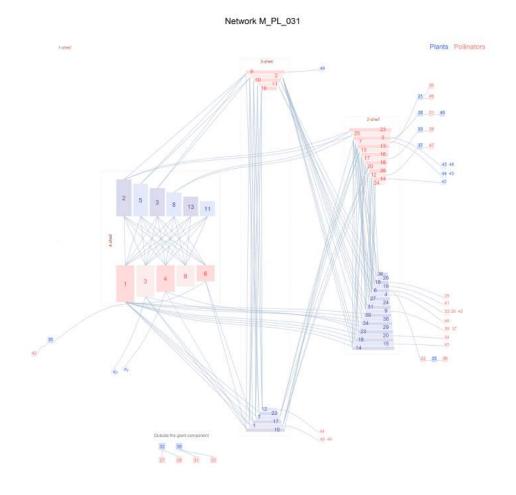
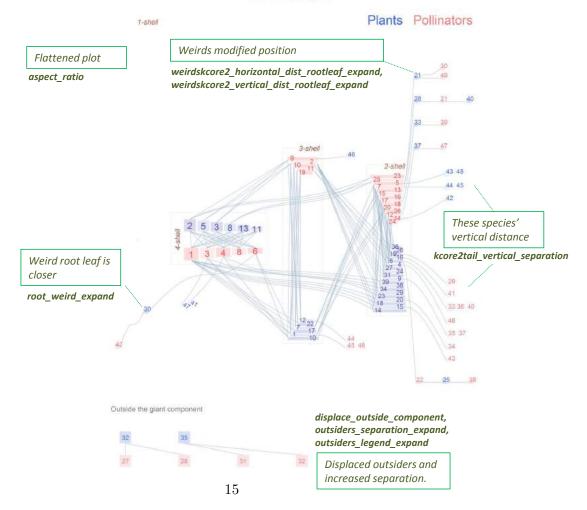


Figure 5: Default ziggurat graph of a plant - pollinator network in Alta Guyana (Venezuela) [Ram89].

Outsiders appear under the main plot. This network has a rich set of weird chains, linked both to ziggurats of 2-shell and to the max shell. If plant species 28 becomes extinct, it will also drag pollinator 21 and plant 40. This is an uncommon chain of specialists linked among them and very exposed to external perturbations.

The ziggurat_grap function offers input fields to manage the appearance and position of these species.

Network M_PL_031



It is possible to display the names of the species inside the ziggurat rectangles. Be careful, because they may make very difficult to understand the structure, we do not encourage using this feature unless the network is tiny. Species names of 1-shell cannot be displayed

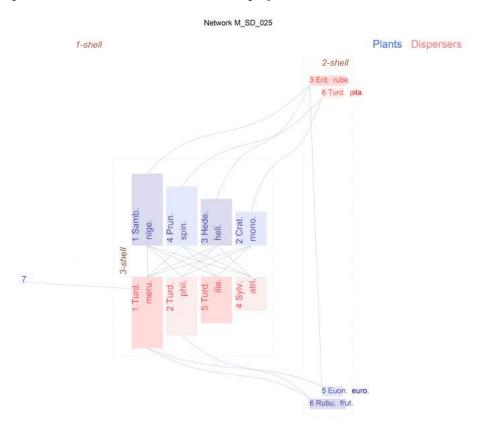


Figure 6: Ziggurat graph of a plant - disperser.

If the network is weighted, links width may be a function of the interaction strength, as in figure ??. There are two options, the natural or decimal logarithm of the weight.

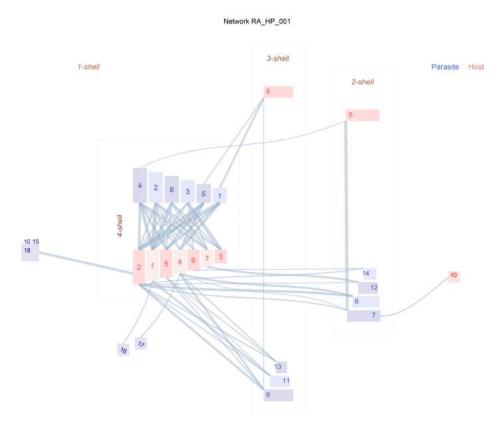


Figure 7: Ziggurat graph of a host - parasite network.

The function returns its own environment called zgg where configuration parameters and results are stored. If you are developing an application, you can retrieve:

- zgg\$plot: the ziggurat plot.
- zgg\$svg: the ziggurat plot as an SVG object.
- zgg\$results_analysis: the internal analyze_network call results.

Finally, this is the meaning of all the input parameters:

- datadir: name of the file of the interaction matrix.
- filename: file with the interaction matrix.
- print_to_file: if set to FALSE the plot is displayed in the R session window.
- plotsdir: the directory where the plot is stored.
- flip_results: displays the graph in portrait configuration.
- aspect_ratio: ziggurat plot default aspect ratio.
- alpha_level: transparency for ziggurats' filling.
- color_guild_a: default filling for nodes of guild_a.
- color_guild_b: default filling for nodes of guild_b.
- color_link default: link color.
- alpha_link: link transparency.
- size_link: width of the links.
- displace_y_b: relative vertical displacement of guild_b inner ziggurats.
- displace_y_a: relative vertical displacement of guild_a inner ziggurats.
- labels_size: default nodes labels size.
- lsize_kcoremax: nodes in kshell max label size.
- lsize_zig nodes: in inner ziggurats label size.
- lsize_kcore1: labels of nodes in kshell 1.
- lsize_legend: legend label size.
- lsize_kcorebox: default kshell boxes label size.
- labels_color: default label colors.
- height_box_y_expand: expand inner ziggurat rectangles default height by this factor.

- kcore2tail_vertical_separation: expand vertical of kshell 1 species linked to kshell 2 by this factor.
- kcore1tail_disttocore: expand vertical separation of kshell 1 species from kshell max (guild_a, guild_b).
- innertail_vertical_separation: expand vertical separation of kshell species connected to 2; kshell; kshell max.
- horiz_kcoremax_tails_expand: expand horizontal separation of weird tails connected to kshell max.
- factor_hop_x expand inner: ziggurats horizontal distance.
- displace_legend modify: legend position by these fractions.
- fattailjumphoriz: displace kshell 1 species linked to leftmost kshell max species.
- fattailjumpvert: idem for vertical position.
- coremax_triangle_width_factor: expand khsell max rectangles width by this factor.
- coremax_triangle_height_factor: expand khsell max rectangles height by this factor.
- paint_outsiders: paint species not connected to giant component.
- displace_outside_component: displace outsider species (horizontal, vertical).
- outsiders_separation_expand: multiply by this factor outsiders' separation.
- outsiders_legend_expand: displace outsiders legend.
- weirdskcore2_horizontal_dist_rootleaf_expand: expand horizontal distance of weird tail root node connected to kshell 2.
- weirdskcore2_vertical_dist_rootleaf_expand: expand vertical distance of weird tails connected to kshell 2.
- weirds_boxes_separation_count: weird species boxes separation count.
- root_weird_expand: expand root weird distances of tails connected to kshell != 2.
- hide_plot_border: hide border around the plot.
- rescale_plot_area: full plot area rescaling (horizontal, vertical).
- kcore1weirds_leafs_vertical_separation: expand vertical separation of weird tails connected to kshell 1 species.
- corebox_border_size: width of kshell boxes.

- kcore_species_name_display: display species names of shells listed in this vector.
- kcore_species_name_break: allow new lines in species names of shells listed in this vector.
- shorten_species_names: number of characters of species name to display.
- exclude_species_number: do not paste species number before species name.
- label_strguilda: string labels of guild a.
- label_strguildb: string labels of guild b.
- landscape_plot: paper landscape configuration.
- backg_color: plot background color.
- show_title: show plot title.
- use_spline: use splines to draw links.
- spline_points: number of points for each spline.
- file_name_append: a label that the user may append to the plot file name for convenience.
- svg_scale_factor: only for interactive apps, do not modify.
- weighted_links: weight function to display links, ("none","log10","ln")
- square_nodes_size_scale: scale the area of nodes in kshell 1 or outsiders.
- progress: only for interactive apps, do not modifiy.
- move_all_SVG_up: only for interactive apps, do not modifiy.

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