Using the kcorebip package Version 1.0

Javier Garcia-Algarra jgalgarra@gmail.com

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1 Introduction

This package performs the k-core decomposition analysis of a bipartite graph and provides four ways to plot it: bipartite, matrix, ziggurat and polar. It works for any kind of bipartite network but as it was developed to study ecological mutualistic communities you will find terminology and examples of that research field throughout the text [GA+18; GA+17].

There is an user-friendly interactive application based on kcorebip, called *BipartGraph*, to create plots from a web interface. It is available at http://jgalgarra.gihutb.io/bipartgraph.

2 Install kcorebip

The package devtools must be installed in your computer. To load it type:

library("devtools")

and then issue the following command:

install_github("jgalgarra/kcorebip")

Warning. A gcc compiler is required to install the package. If you are a developer and you know you do have it, kcorebip will install smoothly. Otherwise, you will get a message telling that Rtools is not available. In that case follow the instructions of the following page to install Rtools:

https://cran.r-project.org/bin/windows/Rtools/

3 Decomposition and definition of k-magnitudes

The rationale behind this package is that, as biological networks are not random, this fact should provide a natural way to group nodes using their topological properties. These groups must be the basis for a spatial distribution that improves network visualization and, in addition, makes structural sense.

The k-core decomposition is a technique to cluster nodes by their connectivity properties [Sei83; BZ03]. The k-core of a graph G is a maximal connected subgraph of degree k. Each node of the core of order m (called m-shell) has links with at least m other nodes that belong to that same core. The practical implication of this definition is that nodes are classified according to their connectivity. The innermost shell is the set of highest k index nodes. Nodes with higher degrees are the g-eneralists. As k index decreases, nodes become more specialist.

The k-decomposition is an iterative algorithm that prunes links of nodes with degree equal or less than k [Sei83]. The process starts pruning nodes with degree 1 until all the remaining nodes have two or more links. Then it with k = 2, and so on. After performing the k-decomposition, each species belongs to one of the k-shells. The highest value of k, i.e ks_{max} , corresponds to the innermost core $ks_{max} \equiv C^{A,B}$. For each k-shell there are two subsets, one per guild (A and B), that we call K_j^A, K_j^B where j is the k-shell index.

In order to quantify the distance from a node to the innermost shell of the partner guild, we compute the average of the shortest paths to each node within that set. We define the k_{radius} of node m of class A as the average distance to the species of C^B :

$$k_{radius}^{A}(m) = \frac{1}{|C^{B}|} \sum_{j \in C^{B}} dist_{mj} \qquad m \in A$$
 (1)

where $dist_{mj}$ is the shortest path from species m to each of the j species that belong to C^B . The same definition is valid for species of guild B computing the average distance to C^A instead. The minimum possible radius value is 1 for a node of the maximum shell that is directly linked to each node of the maximum shell set of the opposite guild.

Figure 1 is a toy bipartite network, with only seven nodes. The upper left graph shows network structure. In the upper right figure, species A1 belongs to C^A . The distance to each node of C^B is 1, so its $k_{radius1}(1)$ is 1. In the bottom right figure, node A2 also belongs to C^A but there is not any direct link with B2, so the distance between them is 3 and $k_{radius}(2)$ is $\frac{5}{3}$. In the bottom left figure, node B4 is not part of C^B , and as may be expected, the value of its k_{radius} is higher.

A global value can be defined averaging this magnitude across network:

$$\overline{k}_{radius} = \frac{1}{|A \cup B|} \sum_{l \in A \cup B} k_{radius}(l) \tag{2}$$

For the network in Figure 1, the value is 11/7.

 k_{radius} is a useful measure of network compactness but it does not work as measure of centrality. For instance, its value for an isolated specialist linked to the maximum core is low. To address this issue, we define a second k-magnitude, called k_{degree} :

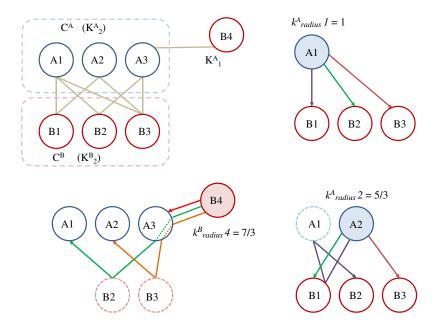


Figure 1: Examples of k_{radius} in a fictional network.

$$k_{degree}^{A}(m) = \sum_{j} \frac{a_{mj}}{k_{radius}j} \quad m \in A, \forall j \in B$$
 (3)

where a_{mj} is the element of the interaction matrix that represents the link. So the $k_{degree}m$ is the sum of the inverse of k_{radius} for each node linked to m. A node of the innermost shell will have a high degree, whereas specialists have only one or two links and so a low k_{degree} . In the example of Figure 1, this magnitude is 1 + 3/5 + 3/5 = 11/5 for node B3, while only 3/7 for node B4.

3.1 Input file format

We use the file format of web of life ecological data collection [Bas09]. Data are stored as .csv files. Species of guild a are distributed by colums, and those of guild b by rows. Field separator can be a semicolon (by default), a comma or a tabulator. If the file is labeled, first colum contains the labels of guild b nodes, and first row, the labels of guild a. If the interaction matrix is binary, the cell of $species_a_m, species_b_n$ will be set to 1. If it is weighted, to a positive real number, its meaning depends on the type of interaction.

The file naming convention is $M_XX_NNN.csv$ where XX is the type, PL for pollinator networks and SD for seed dispersers, and NNN a serial number. Anyway, you are free to call your file in the most convenient way for you.

	Α	В	С	D	E
1		Juniperus phoenicea	Osyris quadripartita	Corema album	Phillyrea angustifolia
2	Turdus merula	1	1	1	1
3	Turdus iliacus	1	1	0	0
4	Turdus philomelos	1	1	0	0
5	Turdus torquatus	1	0	0	0
6	Turdus viscivorus	1	0	0	0
7					

Figure 2: Examples of input file, the seed disperser network 029 of web of life site.

3.2 Network analysis

The function analyze_network performs the k-core decomposition and analysis.

Arguments:

- namenetwork: name of the interaction matrix file.
- directory: folder where the network file is stored.
- guild_a: prefix for the guild of nodes stored in rows.
- guild_b: prefix for the guild of nodes stored in columns.
- plot_graphs: plot kshell histogram and Kamada Kawai plots.
- only_NODF: just computes the *NODF* measurement of nestedness.

The function returns:

- calc_values, a list containing the following objects:
 - graph: an igraph::graph object. This is the additional information for each node, besides the regular of the object:
 - * V(result_analysis\$graph): list of node names
 - * $V(result_analysis\$graph)\$kdegree:$ list k_{degree}
 - * V(result_analysis\$graph) $kradius: list k_{radius}$
 - * V(result_analysis\$graph)\$krisk: list k_{riks} , a measurement of vulnerability (See [GA+17])
 - max_core: maximum k shell index
 - nested_values: a list containing the values provided by the bipartite::nested function, unless only_NODF set TRUE.
 - num_guild_a: number of nodes of guild a.
 - num_guild_b: number of nodes of guild b.
 - links: number of network links.
 - meandist: network average kradius.
 - meankdegree: network average kdegree.
 - spaths_mat: matrix with node to node shortest distance paths.
 - matrix: interaction matrix with nodes of guild a by columns and guild b by rows.
 - g_cores: list with the value of kshell for each node.
 - modularity_measure: value of igraph::modularity function.

4 The Ziggurat Plot

Ziggurat is a visualization created from scratch. Species are grouped by their k-shells. Each of these groups are plotted as small ziggurats. The maximum k-shell is located on the left side, the other ones are arranged following an almond-like distribution.

Species within the maximum shell are ordered by their k_{degree} with the highest one leftmost. Areas do not convey meaning, their height decreases just by convenience of visualization.

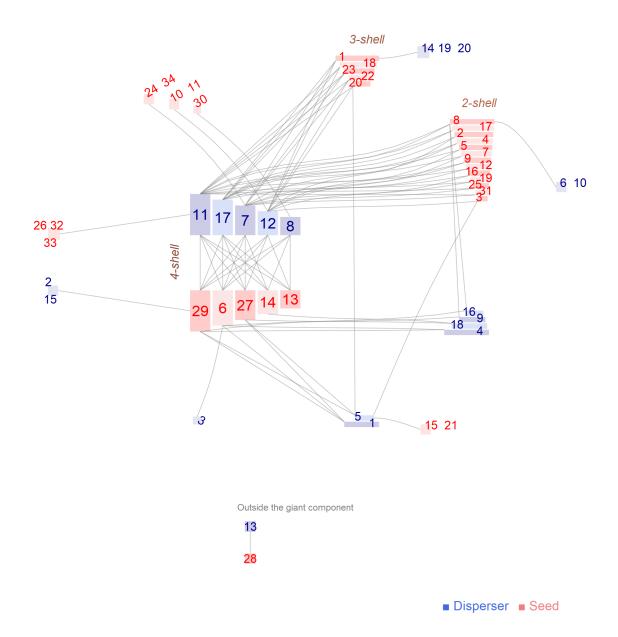


Figure 3: Ziggurat graph of an avian frugivore community in Puerto Rico with 54 species and 95 links [CCG03].

Nodes of 1-shell are scattered around the ziggurats. When multiple species of this shell are connected to the same node of any of the ziggurats they are plotted inside a common node to reduce the number of lines. For instance, seed producer species 26, 32 and 33 are specialists linked to the generalist disperser 11. With this organization, we get a clear view of structure and interconnections. The almond shape leaves a wide space in the center of the graph to depict the links and they do not overcross the boxes of the different species. The function call is:

The configuration of ziggurat plots is quite flexible. There are just two mandatory parameters, datadir and filename, that provide the input directory and input file. The output file is named as the input file plus _ziggurat.png and the user may also add the file_name_append label.

Graphical parameters provide a powerful toolset to improve visualizations. Figure 3 is the result of the default call:

```
ziggurat_graph("../data/","M_SD_004.csv", plotsdir = "grafresults/",
print_to_file = TRUE, label_strguilda = "Disperser", label_strguildb = "Seed")
```

The same graph looks improved tweaking some input parameters.

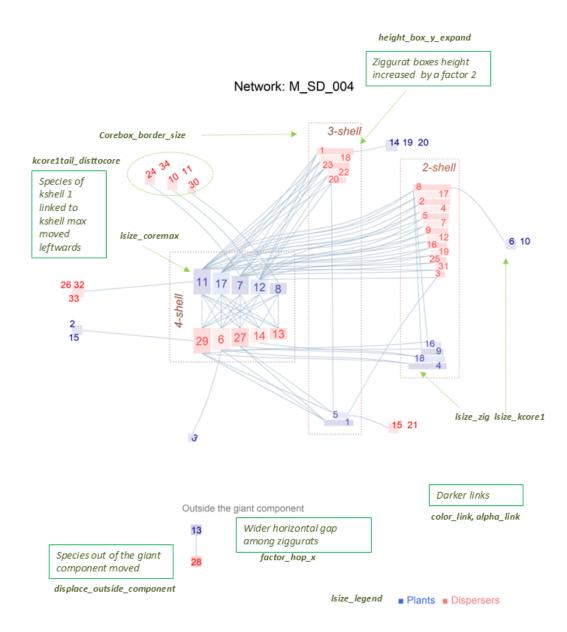


Figure 4: Improved ziggurat graph of an avian frugivore community in Puerto Rico

Plot configuration becomes harder when network size grows. We show now the usefulness of another set of input parameters with a mid-sized example. Default function call provides a quite readable ziggurat plot of pollinator network number 12.

ziggurat_graph("data/","M_PL_012.csv", plotsdir = "grafresults/", print_to_file = TRUE)

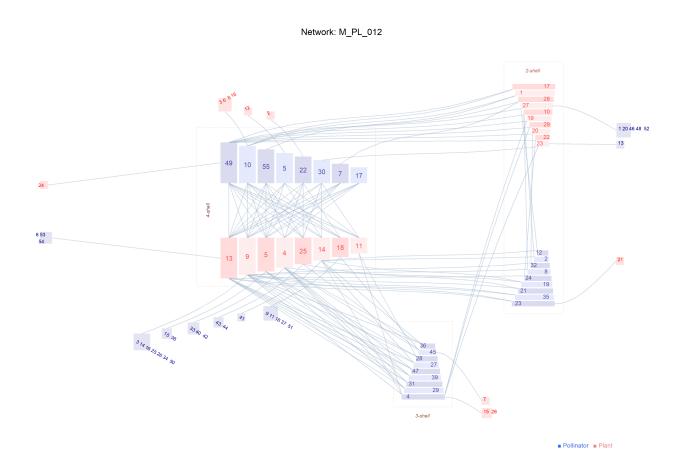
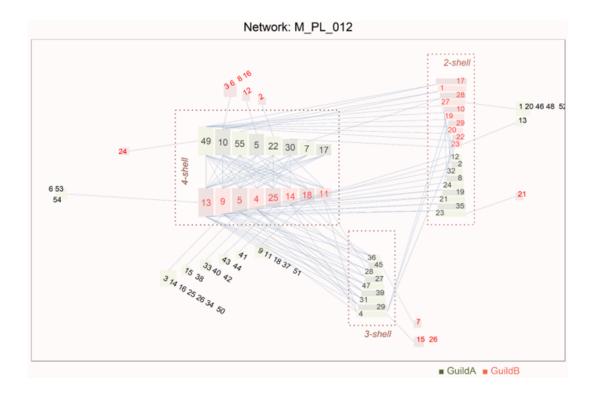


Figure 5: Ziggurat graph of a plant - pollinator network in Garajonay, La Palma (Spain). Olesen, unpublished.

This plot is nearly ready for publishing, some minor improvements would be nice, for instance increasing label sizes. However we are going to modify several input values to show how the picture changes.

We have changed the filling colors of ziggurats, providing the pairs color_guild_a and color_guild_b, and also the species label colors. A dime background is added as well. This trick shows the plotting



area, that was horizontally increased by a 20% with rescale_plot_area=c(1.2,1). This change only affects the plotting area, not the figure. The aspect ratio may be modified to *flatten* the plot if is smaller than 1 or to *stretch* it if larger.

If you do not use splines, as in this example, links appear as straight lines. If you use splines you could also tell the function how many points they should have.

Fat tails are the two sets of 1-shell species eventually linked to highest k_{degree} generalists, those that are located leftmost in the max k-shell.

We saw how height_box_y_expand controls the height of outer ziggurat boxes. Height and width of rectangles of the max k-shell are modified with coremax_triangle_height_factor and coremax_triangle_width_factor.

The overall horizontal distance of 1-shell species linked to max k-shell (except fat tails) is increased or decreased with horiz_kcoremax_tails_expand.

Vectors displace_y_a and displace_y_b control the vertical separation of ziggurats. In this example, ziggurat of 2-shell plants moves upwards by a 50%, 2-shell pollinators downwards 20% and 3-shell pollinators upwards 10%. The parameter innertail_vertical_separation resizes the vertical separation of tails connected to inner ziggurats.

Next example shows how to manage *specialist tails* and *outsiders*. specialist tails are chains of species of *1-shell*. They are rather unstable so they do not appear frequently. Outsiders are the species not connected to the giant component. Pollinator network 031 has species of both kinds.

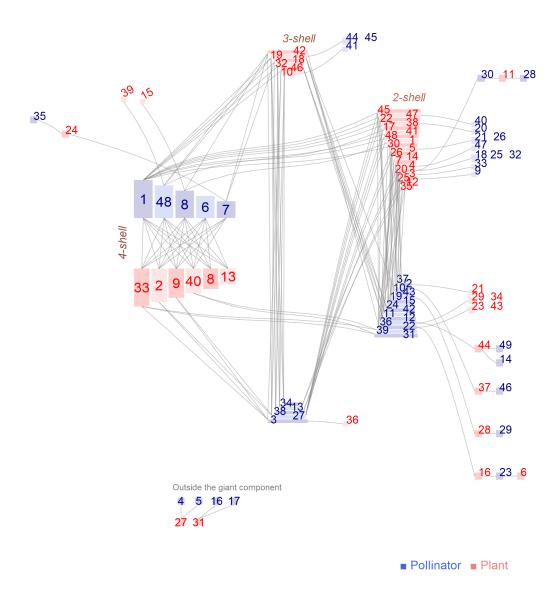
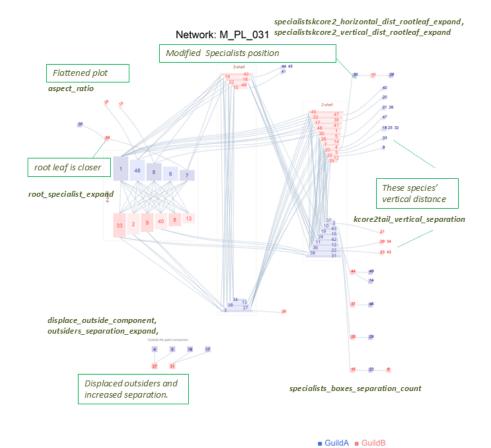


Figure 6: Default ziggurat graph of a plant - pollinator network in Alta Guyana (Venezuela) [Ram89].

Outsiders appear under the main plot. This network has a rich set of specialist chains, linked both to ziggurats of 2-shell and to the max shell. If plant species 16 becomes extinct, it will also drag pollinator 23 and plant 6. This chain of specialists is exposed to external perturbations.

The ziggurat_grap function offers input fields to manage the appearance and position of these species.



It is possible to display the names of the species inside the ziggurat rectangles. Be careful, because they may make hard to understand the structure, we do not encourage using this feature unless the network is tiny. Species names of 1-shell cannot be displayed.

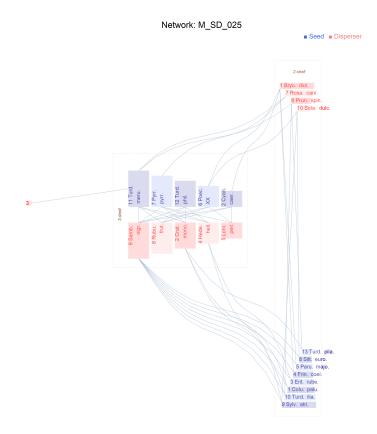


Figure 7: Ziggurat graph of a plant - disperser network. [Sor81]

If the network is weighted, links width may appear as a function of the interaction strength, as in figure 8. There are three options: square root, natural logarithm or decimal logarithm of the weight.

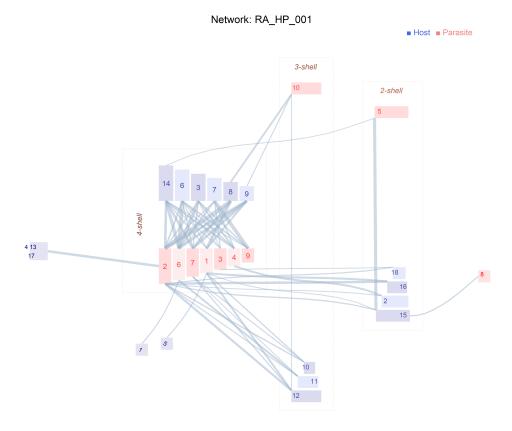


Figure 8: Ziggurat graph of a host - parasite network [Had+14]

The function returns its own environment called **zgg** where configuration parameters and results are stored. If you are developing an application, you can retrieve:

- zgg\$plot: the ziggurat plot.
- zgg\$svg: the ziggurat plot as an SVG object.
- zgg\$results_analysis: the internal analyze_network call results.

The default $ziggurat_graph$ prints the plot in png format with a resolution of 300dpi, but you can save zgg\$plot outside the function in any other format and resolution. Finally, this is the meaning of all the input parameters:

- datadir: name of the file of the interaction matrix.
- filename: file with the interaction matrix.
- paintlinks: if set to FALSE links will be hidden. It is useful to test the plot appearance when the network is huge.
- print_to_file: if set to FALSE the plot is displayed in the R session window.
- plotsdir: the directory where the plot is stored.
- flip_results: displays the graph in portrait configuration.
- aspect_ratio: ziggurat plot default aspect ratio.
- alpha_level: transparency for ziggurats' filling.
- color_guild_a: default filling for nodes of guild_a.
- color_guild_b: default filling for nodes of guild_b.
- color_link default: link color.
- alpha_link: link transparency.

- size_link: width of links.
- displace_y_b: relative vertical displacement of guild_b inner ziggurats.
- displace_y_a: relative vertical displacement of guild_a inner ziggurats.
- labels_size: default node label size.
- lsize_kcoremax: nodes in max-kshell label size.
- lsize_zig nodes: in inner ziggurats label size.
- lsize_kcore1: labels of nodes in 1-shell.
- lsize_legend: legend label size.
- lsize_kcorebox: default kshell boxes label size.
- labels_color: default label colors.
- height_box_y_expand: expand inner ziggurat rectangles default height by this factor.
- $\bullet \ \ \text{kcore2tail_vertical_separation: expand vertical of } 1\text{-}shell \ \ \text{species linked to } 2\text{-}shell \ \ \text{by this factor.}$
- kcore1tail_disttocore: expand vertical separation of 1-shell species from max-shell (guild_a, guild,b).
- innertail_vertical_separation: expand vertical separation of kshell species connected to 2-shell < kshell < max-shell.
- horiz_kcoremax_tails_expand: expands horizontal separation of specialist tails connected to max-shell.
- factor_hop_x expand inner: expands ziggurats horizontal distance.
- fattailjumphoriz: displace species linked to leftmost max-shell species.
- fattailjumpvert: idem for vertical position.
- coremax_triangle_width_factor: expand khsell max rectangles width by this factor.
- coremax_triangle_height_factor: expand khsell max rectangles height by this factor.
- paint_outsiders: paint species disconnected of the giant component.
- displace_outside_component: displace outsider species (horizontal, vertical).
- outsiders_separation_expand: multiply by this factor outsiders' separation.
- outsiders_legend_expand: displace outsiders legend.
- specialistskcore2_horizontal_dist_rootleaf_expand: expand horizontal distance of specialist tail root node connected to 2-shell.
- specialistskcore2_vertical_dist_rootleaf_expand: expand vertical distance of specialist tails connected to 2-shell.
- specialists_boxes_separation_count: specialist species boxes separation count.
- root_specialist_expand: expand root specialist distances of tails connected to $kshell \neq 2$.
- hide_plot_border: hide border around the plot.
- rescale_plot_area: full plot area rescaling (horizontal, vertical).
- kcore1specialists_leafs_vertical_separation: expand vertical separation of specialist tails connected to 1-shell species.
- corebox_border_size: width of kshell boxes.
- kcore_species_name_display: display species names of shells listed in this vector.
- kcore_species_name_break: allow new lines in species names of shells listed in this vector.
- shorten_species_names: number of characters of species name to display.
- label_strguilda: string labels of guild a.
- label_strguildb: string labels of guild b.
- landscape_plot: paper landscape configuration.
- backg_color: plot background color.

- show_title: show plot title.
- use_spline: use splines to draw links.
- spline_points: number of points for each spline.
- file_name_append: a label that the user may append to the plot file name for convenience.
- svg_scale_factor: only for interactive apps, do not modify.
- weighted_links: weight function to display links, ("none","log10","ln","sqrt")
- \bullet square_nodes_size_scale: scale the area of nodes in 1-shell or outsiders.
- progress: only for interactive apps, do not modifiy.

5 Bipartite Plot

The bipartite plot is the conventional way to depict a bipartite network. Nodes of both guilds are aligned in two parallel lines (horizontal or vertical is a matter of taste), orderded by degree. A straight line between two nodes of different guilds means that there is a link and its width may be proportional to the weight of the interaction. The bipartite plot becomes a hair ball as the number nodes and links increases. There are some minor mitigation strategies to overcome this problem. This package offers the legacy style for bipartite plot, following the traditional layout, but distributing evenly the nodes of the smallest guild. This solution makes the diagram more readable.

bipartite_graph("../data/", "M_SD_004.csv", style = "legacy", print_to_file = TRUE)

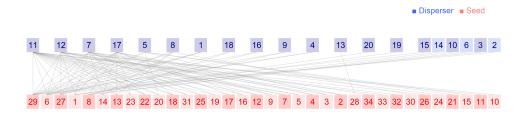


Figure 9: Legacy bipartite graph of an avian frugivore community in Puerto Rico with 54 species and 95 links [CCG03].

There are some details that we can deduce at a glance. The more generalist species are those that lay on the left side of the plot and the pair disperser 13/plant 28 is disconnected of the giant component of the network. We can get further visual information tunning input parameters.

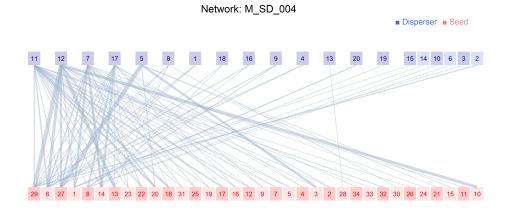


Figure 10: Improved bipartite graph.

The spatial gap between guild lines is now wider. Lilnks width is proportional to the weight and labels size is larger. But the information is harder to discover in this plot than in its ziggurat counterpart (fig. 4). The difference between both kind of graphs is that bipartite is essentially a linear plot, while ziggurat is bidimensional. In addition, nodes in ziggurat are clustered by its k-shell number. This package provides a new style of bipartite plot, named kcoreorder, where nodes are ordered and grouped following this criterion. Moreover, nodes of 1-shell are ploted on the left side to shorten their links length towards the max shell of the network.

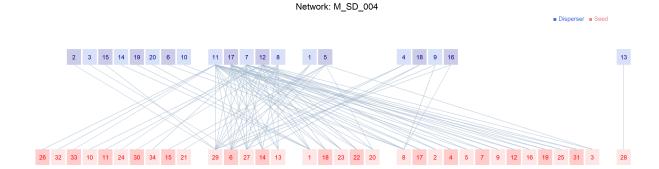


Figure 11: kcoreorder bipartite graph.

Now, it is easy to spot the different k-shells, with species of 4-shell being the most interconnected. On their left, we find 1-shell, on their right, 3-shell, 2-shell and finally, species disconnected of the giant component. The only difference between the two styles is the order of the species, but

information is still concentrated in two lines of nodes.

What if we could keep the whole idea of bipartite plot but spreading part of the visual information in two dimensions? That is the idea behind the third style, the *chillopod* plot. The name refers to the resemblance of this plot with a centipede. Nodes of 1-shell that we call *tails* in the ziggurat plot are mived away from the guild lines, and appear as short appendices. We apply the same grouping idea that in ziggurat's fat tails, nodes that has just one link and are tied to the same species of a higher shell, are plotted together.

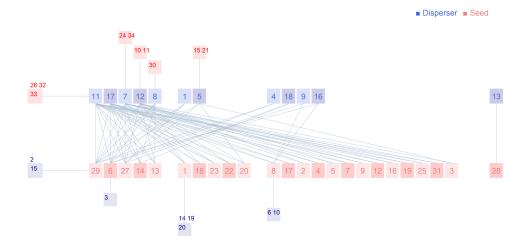


Figure 12: Chilopod bipartite graph.

The default function call is:

```
lsize_kcoremax = 3, lsize_legend = 4, lsize_core_box = 3.0,
labels_color = c(),
hide_plot_border = TRUE,
label_strguilda = "",
label_strguildb = "", landscape_plot = TRUE,
backg_color = "white", show_title = TRUE, show_legend = 'TOP',
file_name_append = "", svg_scale_factor= 10, weighted_links = "none",
progress=NULL)
```

This is the meaning of the input parameters:

- datadir: name of the file of the interaction matrix.
- filename: file with the interaction matrix.
- sep: field separator character.
- species inheader: TRUE if species names are stored as row and column names inside the network data file.
- print_to_file: if set to FALSE the plot is displayed in the R session window.
- plotsdir: the directory where the plot is stored.
- orderkcoremaxby: sets the order of kcoremax to kradius or kdegree
- style: bipartite representation style: legacy, kcoreorder, chilopod
- paintlinks: if set to FALSE links will be hidden. It is useful to test the plot appearance when the network is huge.
- flip_results: displays the graph in portrait configuration.
- alpha_level: transparency for ziggurats' filling.
- color_guild_a: default filling for nodes of guild_a.
- color_guild_b: default filling for nodes of guild_b.
- color_link default: link color.
- alpha_link: link transparency.
- size_link: width of links.
- lsize_kcoremax: nodes in main lines label size.
- lsize_legend: legend label size.
- labels_color: default label colors.
- hide_plot_border: hide border around the plot.
- label_strguilda: string labels of guild a.
- label_strguildb: string labels of guild b.
- landscape_plot: paper landscape configuration
- backg_color: plot background color.
- show_title: show plot title.
- show_legend: show plot legend position: "TOP", "BOTTOM", "NONE".
- file_name_append: a label that the user may append to the plot file name for convenience.
- svg_scale_factor: only for interactive apps, do not modify.
- weighted_links: weight function to display links, ("none","log10","ln","sqrt")
- progress: only for interactive apps, do not modify.

The function returns its own environment called **bpp** where configuration parameters and results are stored. If you are developing an application, you can retrieve among other values:

- bpp\$plot: the bipartite plot.
- bpp\$svg: the bipartite plot as an SVG object.
- bpp\$bipartite_argg: function call parameter values.
- bpp\$g: the internal graph object.

6 Matrix Plot

The Matrix Plot is another traditional way of plotting bipartite networks. It is just the depiction of the interaction matrix, with species of guild A as columns and species of guild B as rows. For binary matrixes, the cell i, j is filled with solid color if there is a link between species i of guild A and species j of guild B. For weighted networks, the interaction strength is usually encoded as a color gradient. Nodes are sorted by their degree in descending order. This kind of plot is simple, and is useful to spot spatial properties as nestedness, but it is pretty hard to discover chains of specialists.

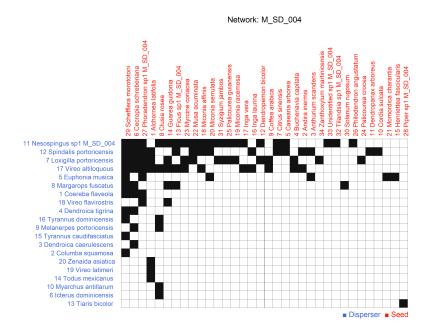


Figure 13: Matrix graph of an avian frugivore community SD_004

The function allows to flip the matrix to show it in landscape layout for convenience, as in this example. Besides the traditional order by degree, *kcorebip* offers order by kradius and kdegree. Species names can be removed, and this feature is of special interest when the network is big.

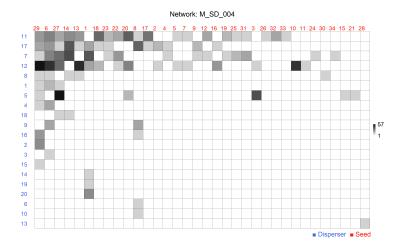


Figure 14: Matrix graph of the same avian frugivore community, with nodes sorted by kradius

The default function call is:

This is the meaning of the input parameters:

- datadir: name of the file of the interaction matrix.
- filename: file with the interaction matrix.
- sep: field separator character.
- speciesinheader: TRUE if species names are stored as row and column names inside the network data file
- style: "matrix", do not change. tem orderby: sort species of the same guild by degree, kradius or kdegree in descending order.
- label_strguilda: string labels of guild a.
- label_strguildb: string labels of guild b.
- label_size: species label size.
- color_guild_a: default filling for nodes of guild_a.
- color_guild_b: default filling for nodes of guild_b.
- flip_matrix: transpose interaction matrix.
- color_linkst: link color.
- links_weight: for weighted networks, fill interactions with gradient color
- show_species_name: include species names in node labels
- show_title: show plot title.
- show_legend: show plot legend position: "TOP", "BOTTOM", "NONE".
- print_to_file: if set to FALSE the plot is displayed in the R session window.
- plotsdir: the directory where the plot is stored.
- plot_size: size of printed plot in inches..
- ppi: printer dots per inch.
- progress: only for interactive apps, do not modify.

The function returns its own environment called mat where configuration parameters and results are stored. If you are developing an application, you can retrieve among other values:

- mat\$plot: the matrix plot.
- mat\$mat_argg: a list with the result of the network analysis. See analyze_network for details.
- mat\$result_analysis: the internal graph object.

7 The Polar Plot

The *Polar Plot* shows nodes (species) centrality and provides an overview of network distribution. It was inspired by the *fingerprint-like* graph, developed by Alvarez-Hamelin *et al.* [AH+05] to plot very large *k-decomposed* networks.

Nodes are depicted with their centers located at k_{radius} . Angles are assigned at random by the visualization algorithm and each guild lies inside one of the half planes. The size of each node is proportional to its k_{degree} and the color represents the k_{shell} . This visualization does not include links. The user may choose adding the histograms of k-magnitudes, a handy option because they convey a wealth of structural information.

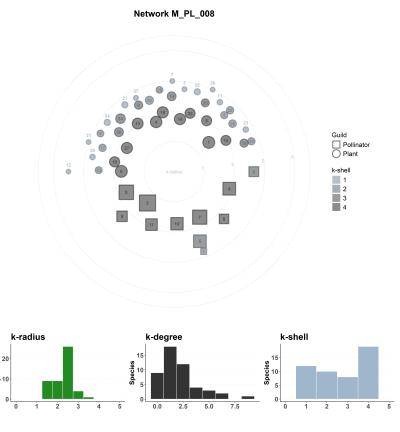
The function call is:

The parameters red, directorystr and plotsdir are the name of the interaction matrix, the directory where it is stored and the name of the plotting directory. If print_to_file is set to FALSE the polar plot will be displayed in the current R session. The name of the output file is that of the input file plus _polar.png. Paths are relative to the current working path in R but you may also specify absolute paths.

File plots have a resolution of 600 dots per inch, and a size of 12×12 inches. If the user wants to display the result in the current R session, label sizes may appear different depending on the 3.0d fonts and size of the plotting window.

The following command creates the file M_PL_008_polar.png in the directory graphresults/

pgr <- polar_graph("../data/","M_PL_008.csv",plotsdir="grafresults/", print_to_file = TRUE)

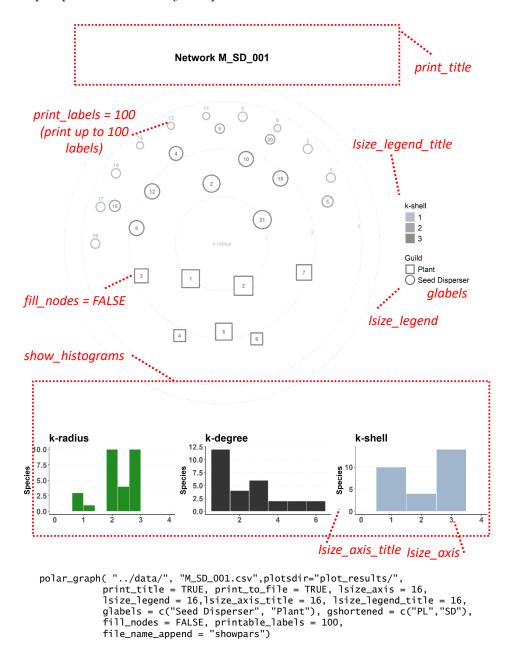


By default, nodes are unlabeled. You may choose to print some of them with the parameter printable_labels, but have in mind that the diagram may become messy. Guild labels are also

configurable. The function will set automatically "Plant, Pollinator" and "Plant, Disperser" if the file follows the naming convention of the web of life site; you may choose any other pair of values with the input parameter glabels.

Three histrogams are displayed under the main plot, with the distributions of k_{radius} , k_{degree} and k_{shell} .

The configuration of a polar graph is quite simple. The following picture shows how and where the different input parameters modify the plot.



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