



Social network analysis

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Contents

+ Social networks

+ Relational Event History Data (**REH**)

+ Relational Event Model (**REM**)



+ Exponentioal Random Graph Model (**ERGM**)

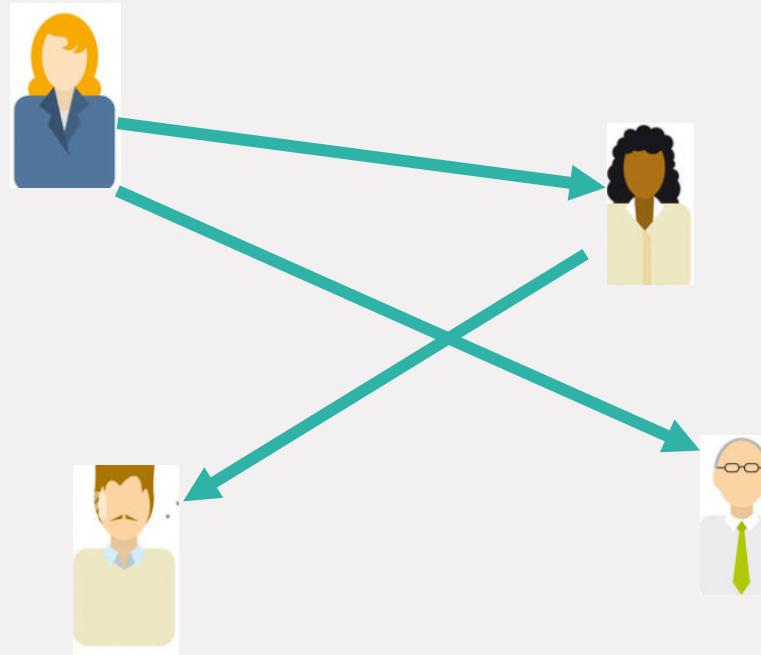
+ Stochastic Actor Oriented Model (**SAOM**)

+ Longitudinal network analysis: ERGMs - SOAM, TERGMs -
REMs

Network

+ Representations of **relational data**.

+ **Nodes** (actors/vertices) represent **entities** while the **links** (edges/ties) connecting them represent any form of **interaction** or **connection** between the entities.



Social networks

+ A **Relation** defined on a collection of **individuals (actors)**.

For example

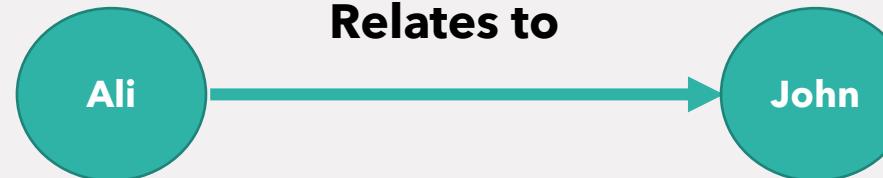
Ali goes to John for **advice**...

Ali considers John as a **friend**...

Ali sends an **email** to John...

Ali **calls** John...

...



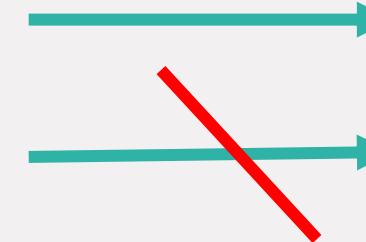
Social networks

+ A **Relation** defined on a collection of **individuals**.



Tie present: On

Tie absent: Off

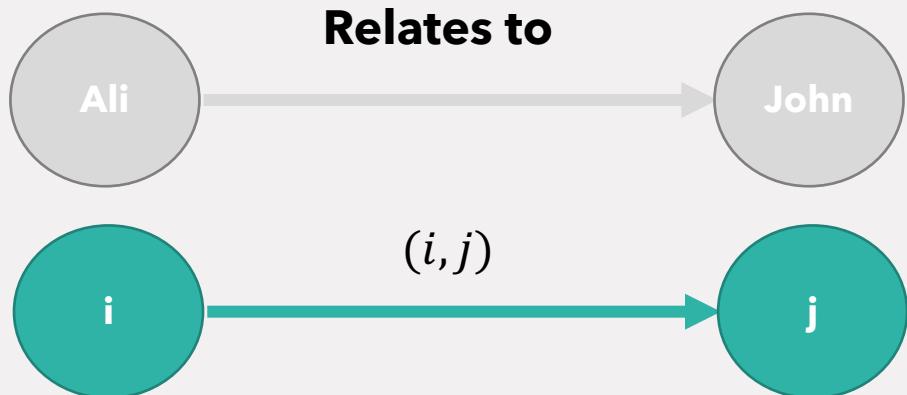


Social networks

A network is a **Graph**: $G(V, E)$, on

Individuals / actors: $V = \{1, 2, \dots, n\}$

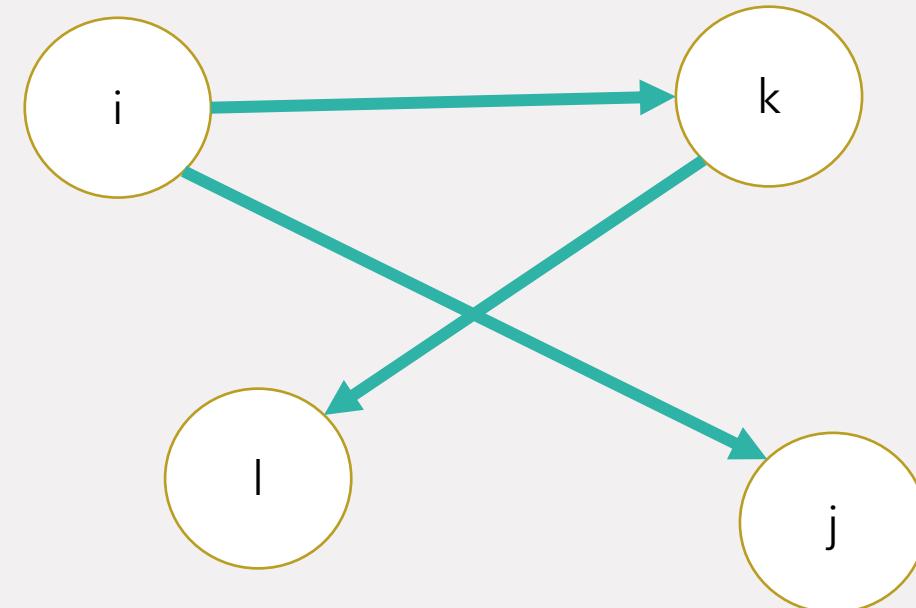
Relation / edges: $E \subseteq \{(i, j) : i, j \in V\}$



Tie present: On



Tie absent: Off



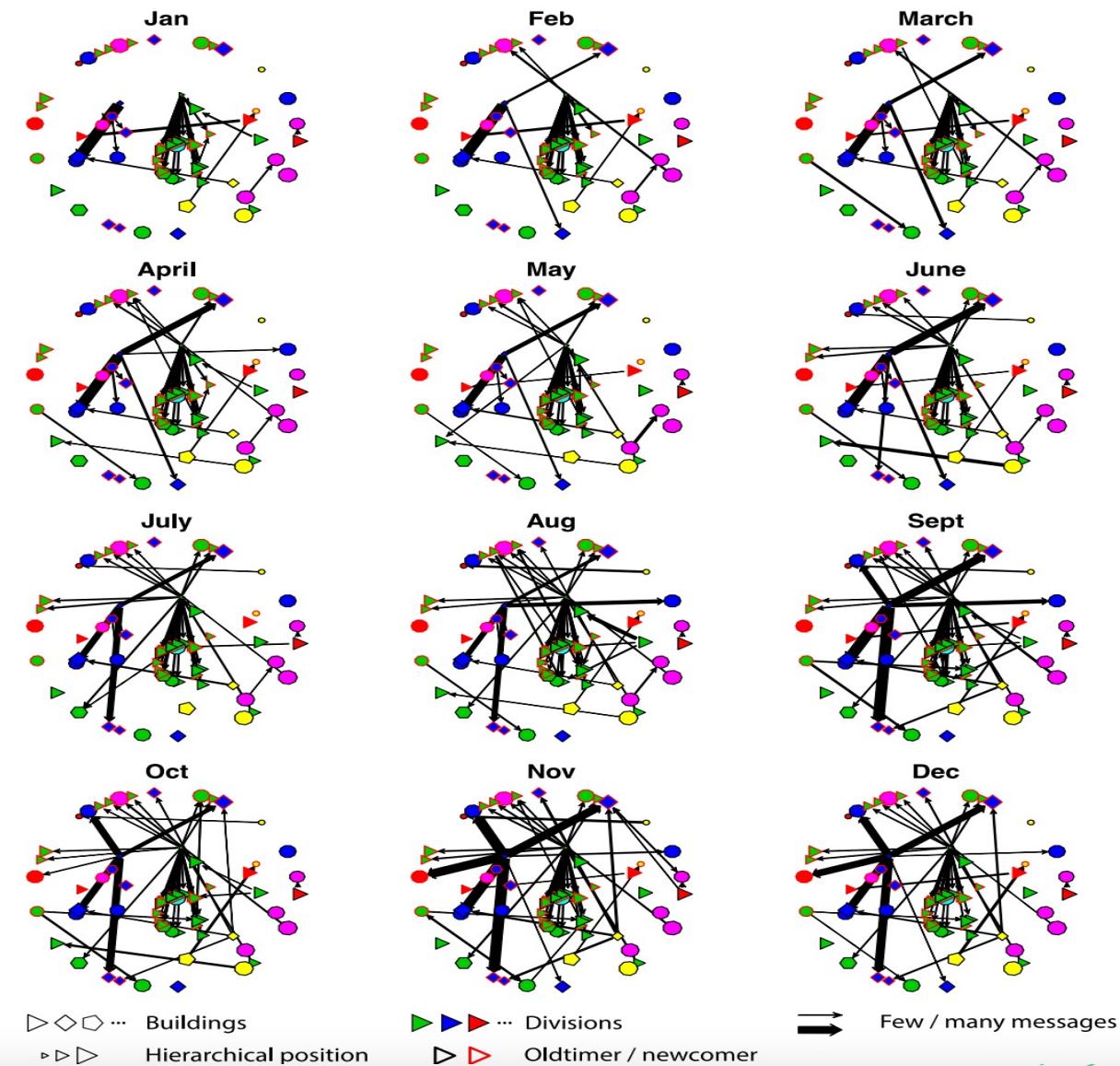
Apollo 13, Communication Network

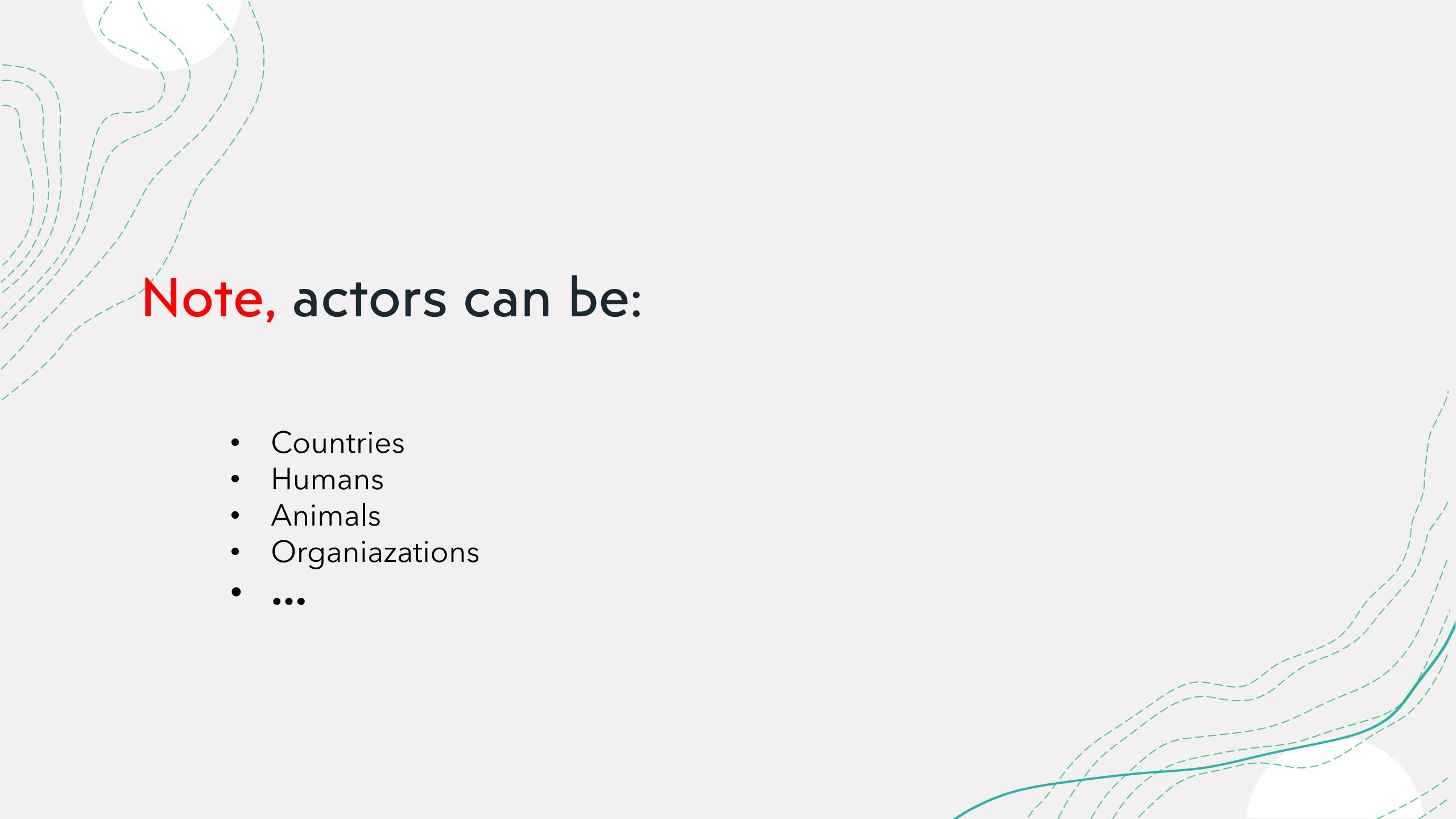


Email Network

Mulder J., Leenders R., 2019

Aggregated networks over different months.





Note, actors can be:

- Countries
- Humans
- Animals
- Organizations
- ...

Relational Event History Data (REH data)

Relational Event History Data (**REH** data)

- + REH is a type of network data.
- + REH data contain detailed information **what** happened (message, email, etc.), **when** it happened (time), and **who** were involved (sender, receiver).
- + They are time-stamped interactions.
- + REH data contains at least **receiver** (target), **sender** (source), and **time/order**.
- + A **relational event**: “a **discrete event** generated by a social actor (the ‘sender’) and directed toward one or more targets (the ‘receivers’), ... **at a certain point in time**” (Butts, 2008, p. 159).
- + Event = (sender, receiver, time, ...)

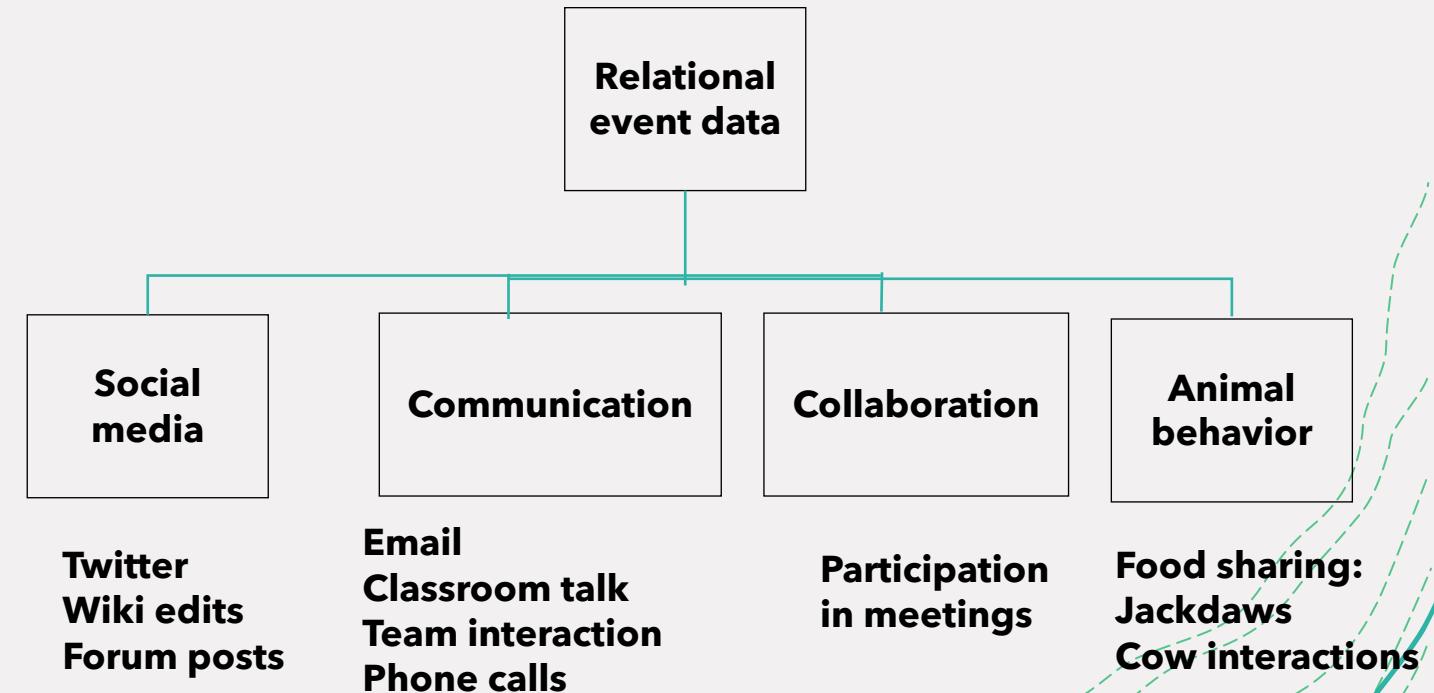
Why study relational events?

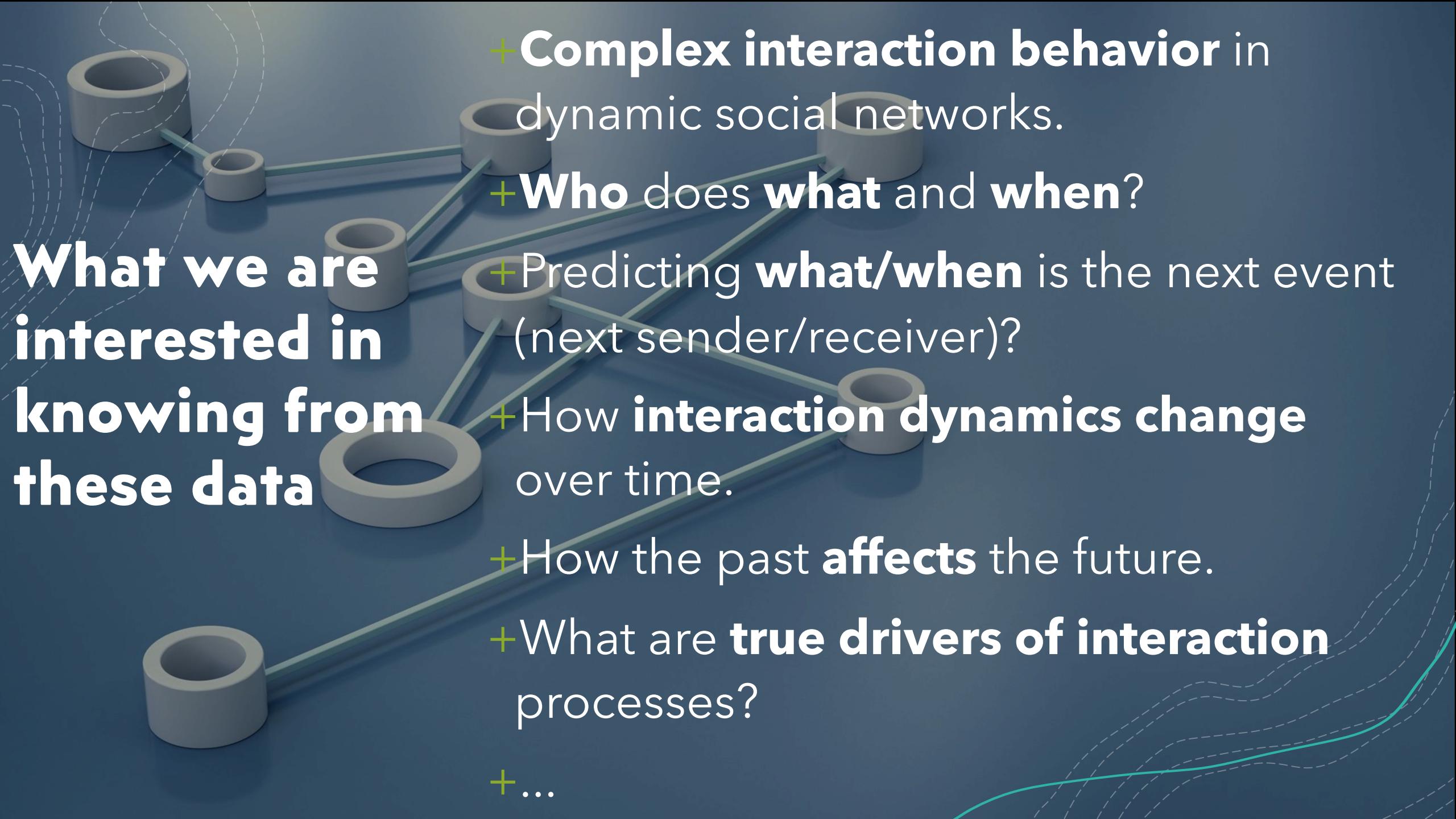
+ Relational events are everywhere, and **increasingly available** due to the development of technology.

+ Often in the form of Big Data

e.g.

+ Sociometric badges, digital communication (email), video monitoring, etc.





What we are interested in knowing from these data

- + **Complex interaction behavior** in dynamic social networks.
- + **Who** does **what** and **when**?
- + Predicting **what/when** is the next event (next sender/receiver)?
- + How **interaction dynamics change** over time.
- + How the past **affects** the future.
- + What are **true drivers of interaction** processes?
- + ...

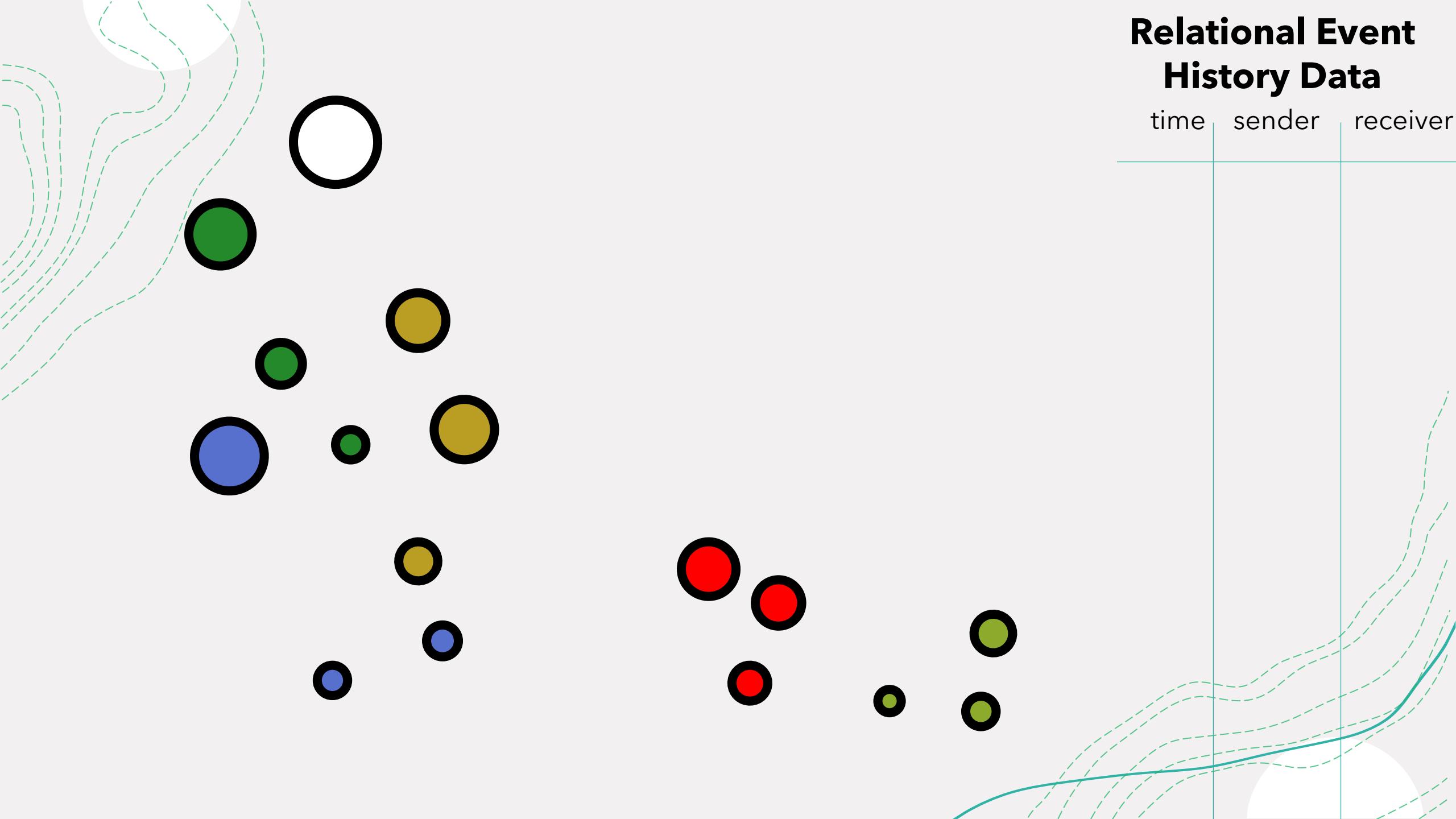
Example



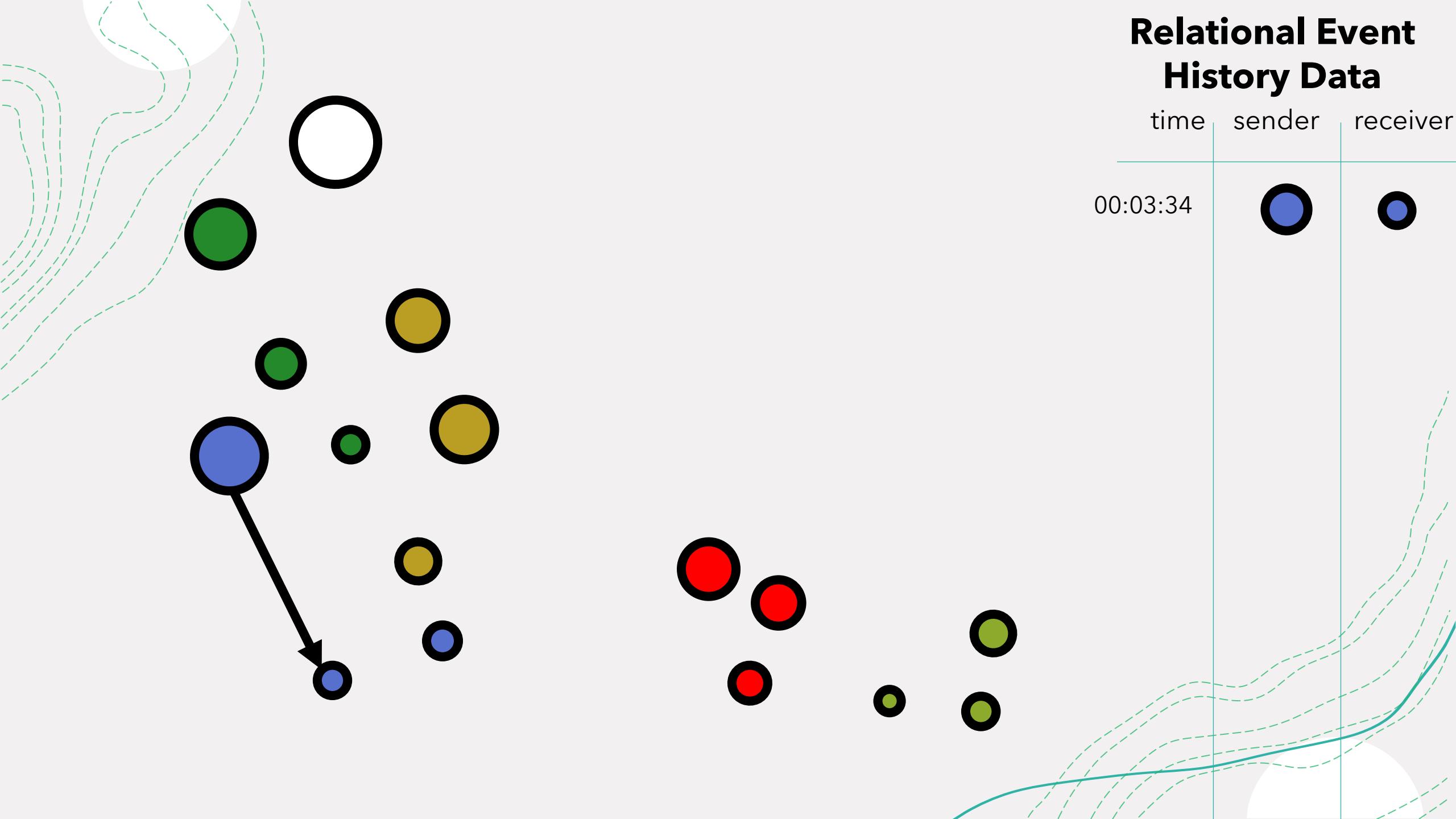
Employees in organizations share information with each other via email.

How (**fast**) do employees share information with coworkers?

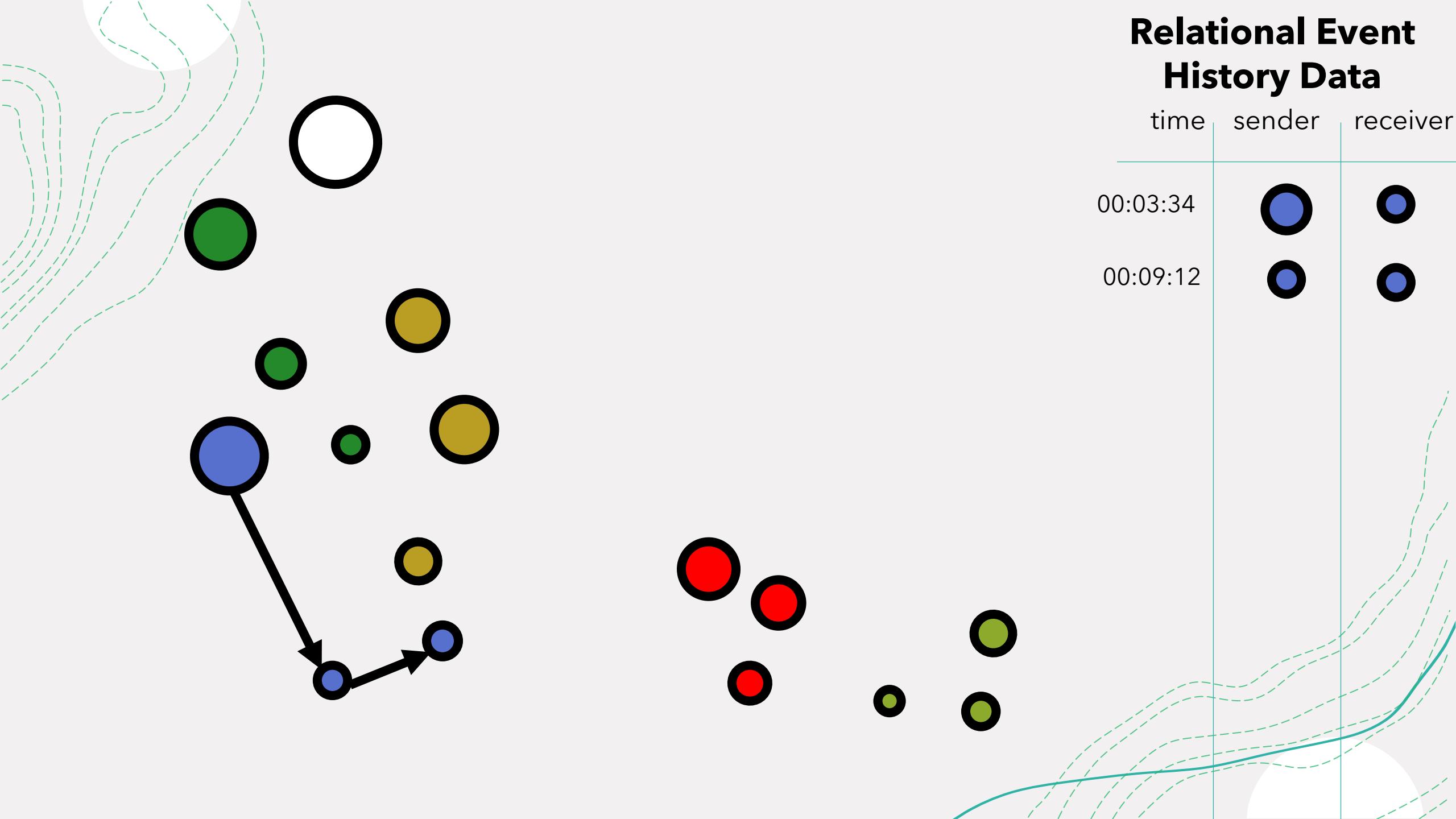
Relational Event History Data



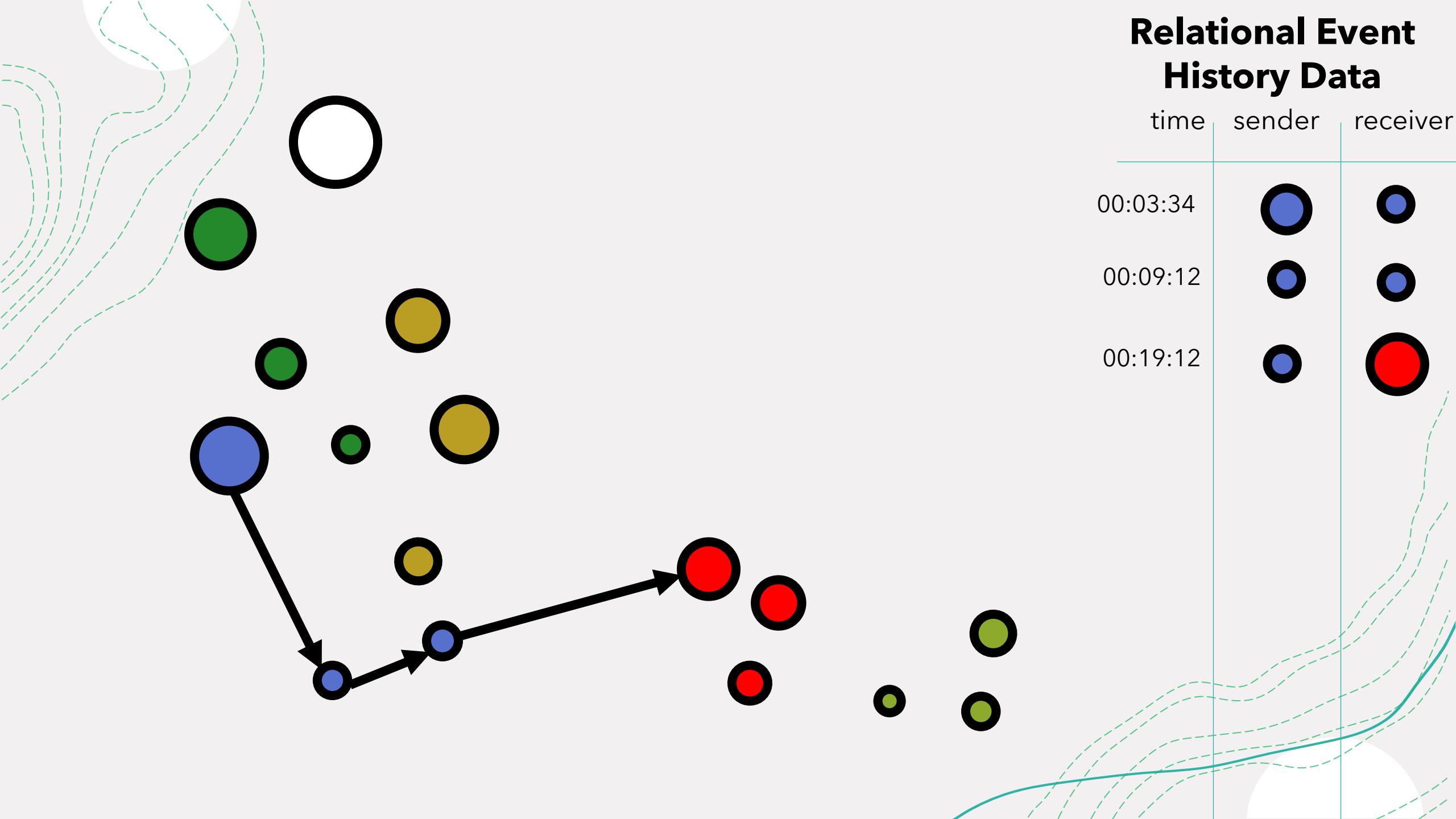
Relational Event History Data



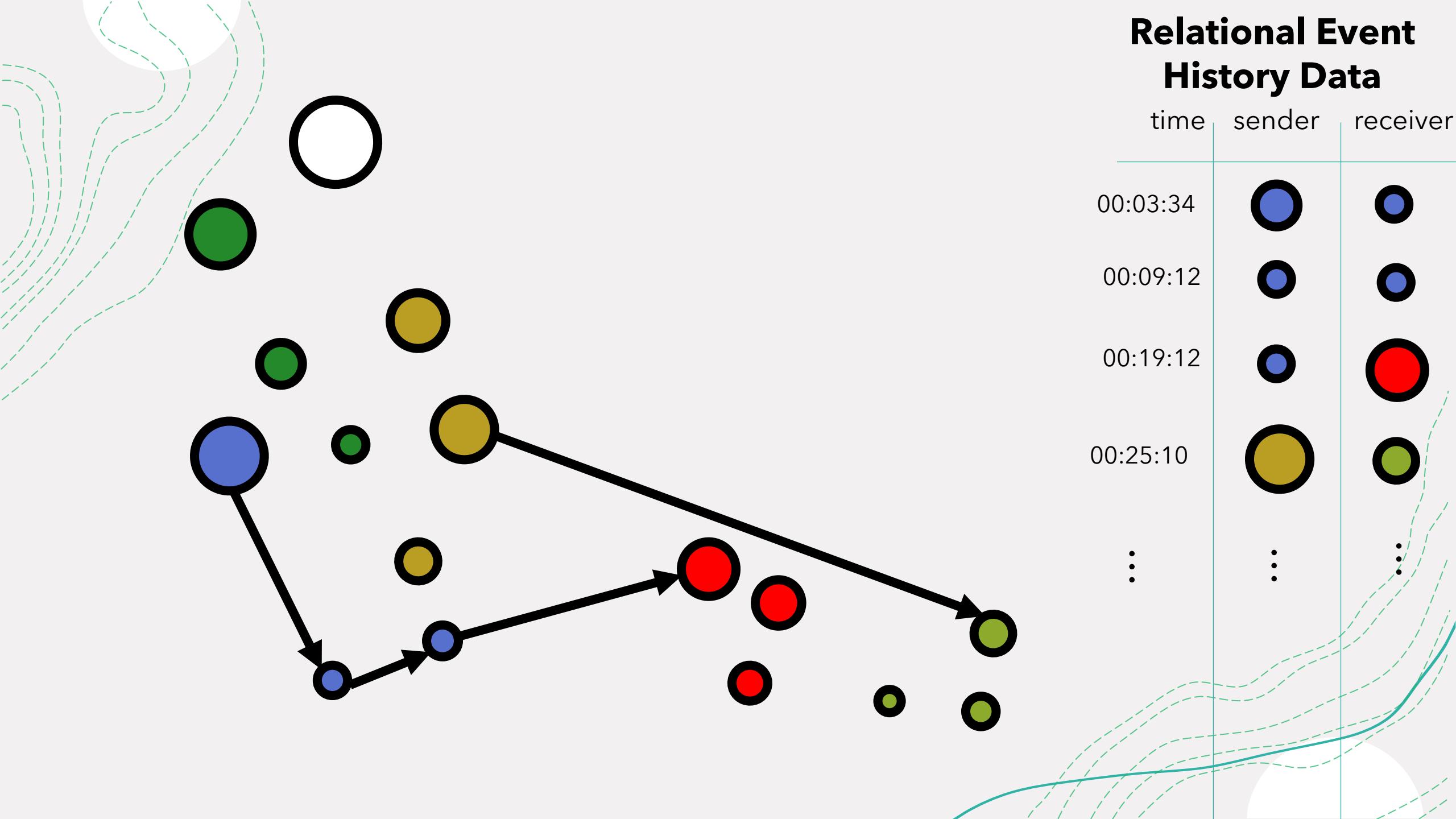
Relational Event History Data

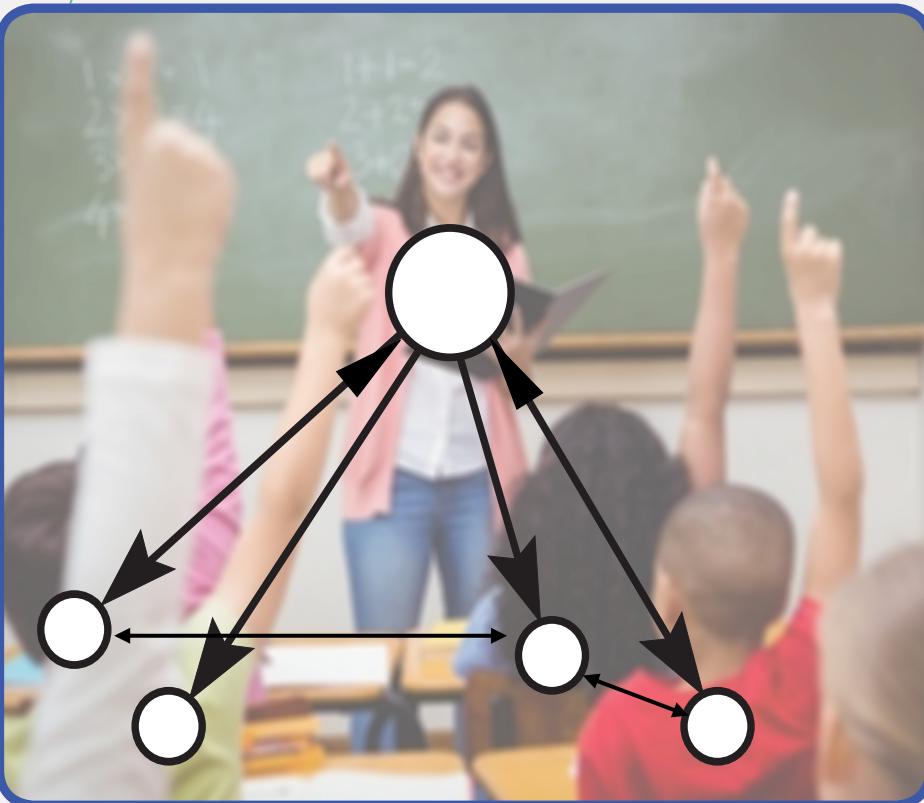


Relational Event History Data



Relational Event History Data





Teachers and students interact with each other in classrooms

How do the teachers and students interact?

Can we predict **when** defiant behavior will occur?

Some other interesting questions

- + Why do nation states declare war on one another?
- + What explains the structure of communication networks in organizational settings?

Some important points:

- + Events occurs at **sharp discrete moments** in time (well-defined duration).
- + Ties are **existing in these short temporal moments** in continues time
- + We have good information on the sequencing (order) and duration of ties changes.
- + It seems we can examine the frequency and time to activation among relational events



Remark

+ Note that **relational event data** is distinct from network **panel data** in that ties are short lasting and occur in exact moments in time.

Network Panel Data



Coarse tie measurements

Measuring the same network at different points in time where the gap between measurements is usually large

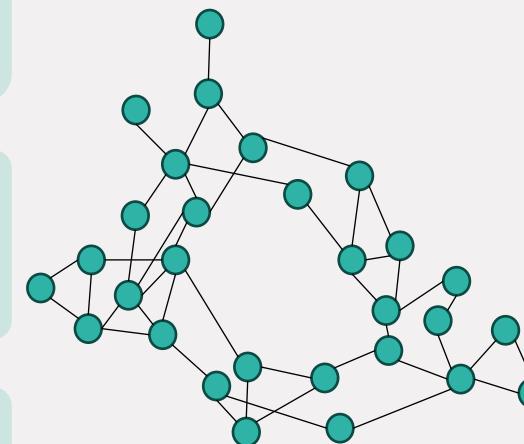


Typically, ties are assumed to be long lasting
E.g., friendships, business relationships.

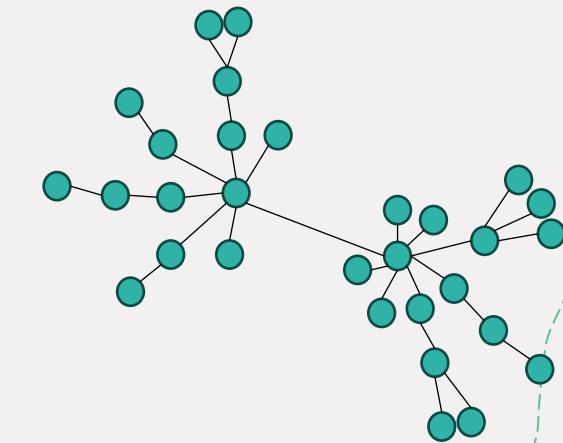


We know the network changed between panels,
but we don't know the order of those changes

t=1



t=2

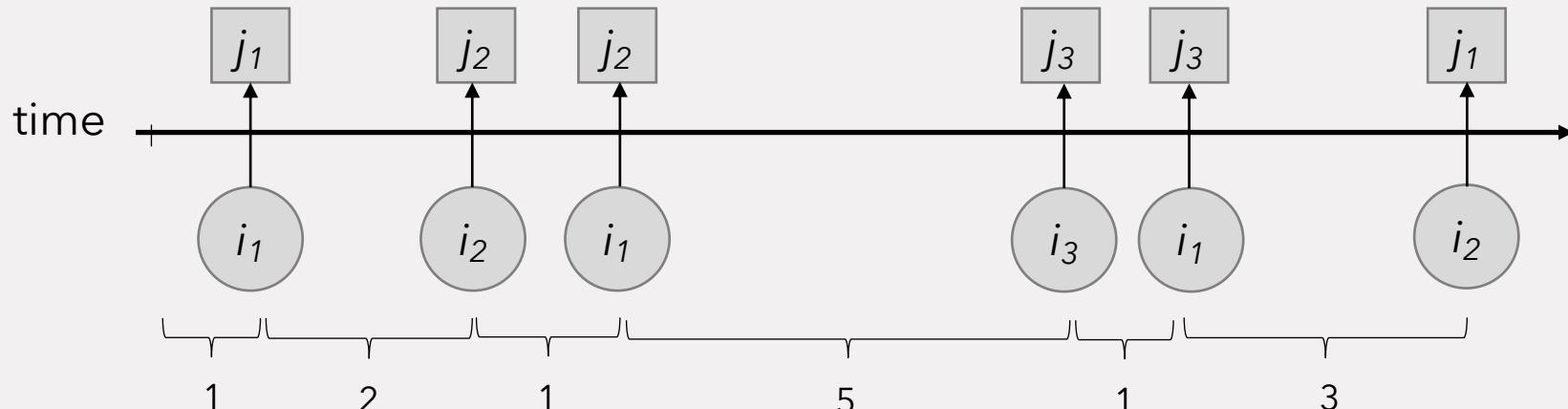


Relational event data- Network panel data

+ Relational event data is *distinct* from network panel data in several ways

Criterion	Network Panel Data	Relational Event Data
Data on timing	Coarse	Exact (or near exact)
Unobserved tie changes?	Yes	No
Nature of relationship	Long-lasting	Ephemeral

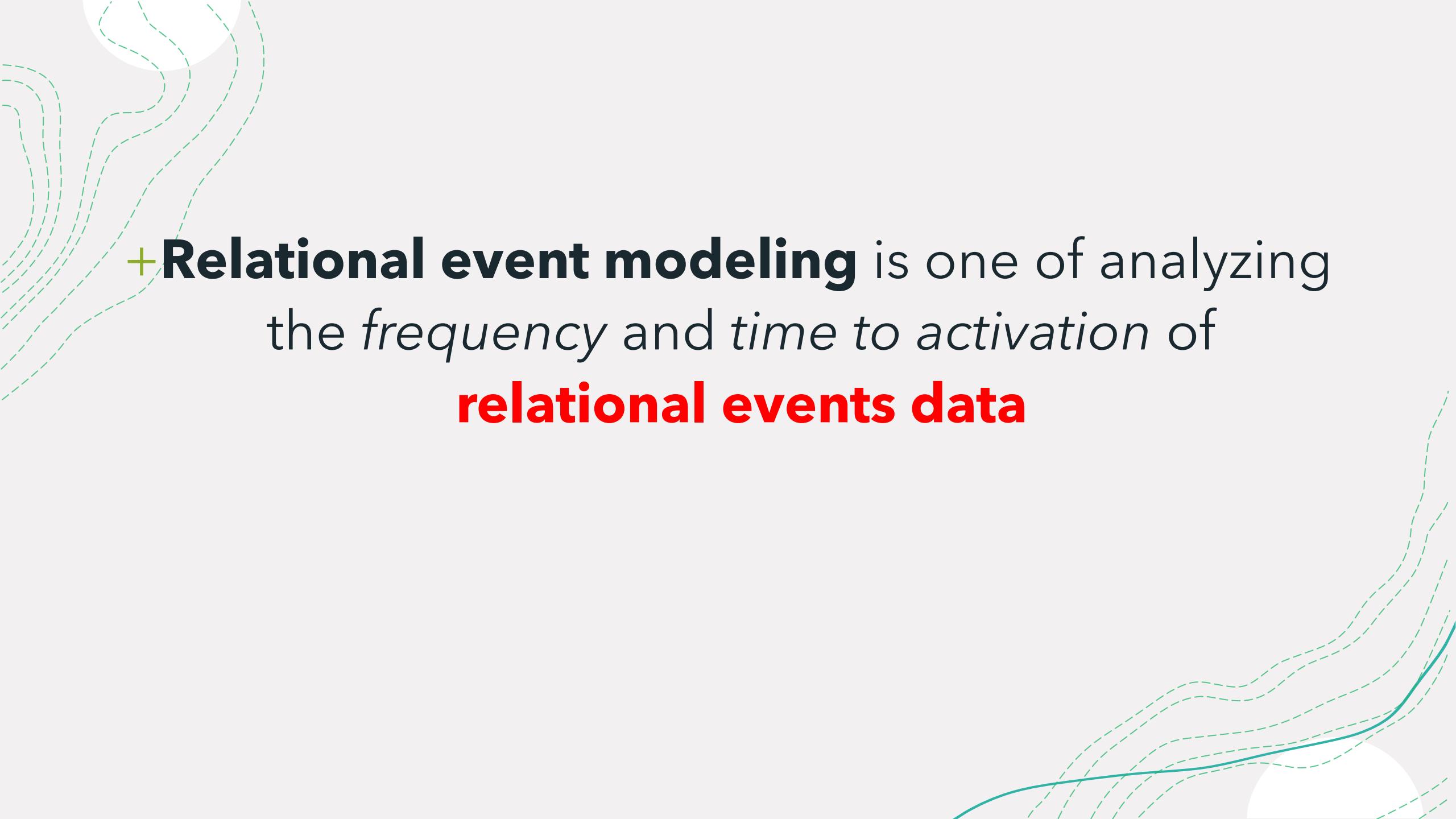
REH Data



Event sequence translated into a data frame: edgelist

time	sender/source	receiver/ target
0	i_1	j_1
3	i_2	j_2
4	i_1	j_2
9	i_3	j_3
10	i_1	j_3
13	i_2	j_1

Edgelist reduced demands on computer memory



+ **Relational event modeling** is one of analyzing
the *frequency* and *time to activation* of
relational events data

Model to analyze REH data:

Relational Event Models (REMs)

R packages:

relevent

survival

remstats

remify

remulate

•

•

Soon



Relational Event Models (REMs)

- + First introduced by Butts (2008), modelling the time between events
- + Combination of **event history analysis** and **network analysis**.
- + Relational event models (REM) are a **statistical model** for *relational* event data.

Relational event modeling

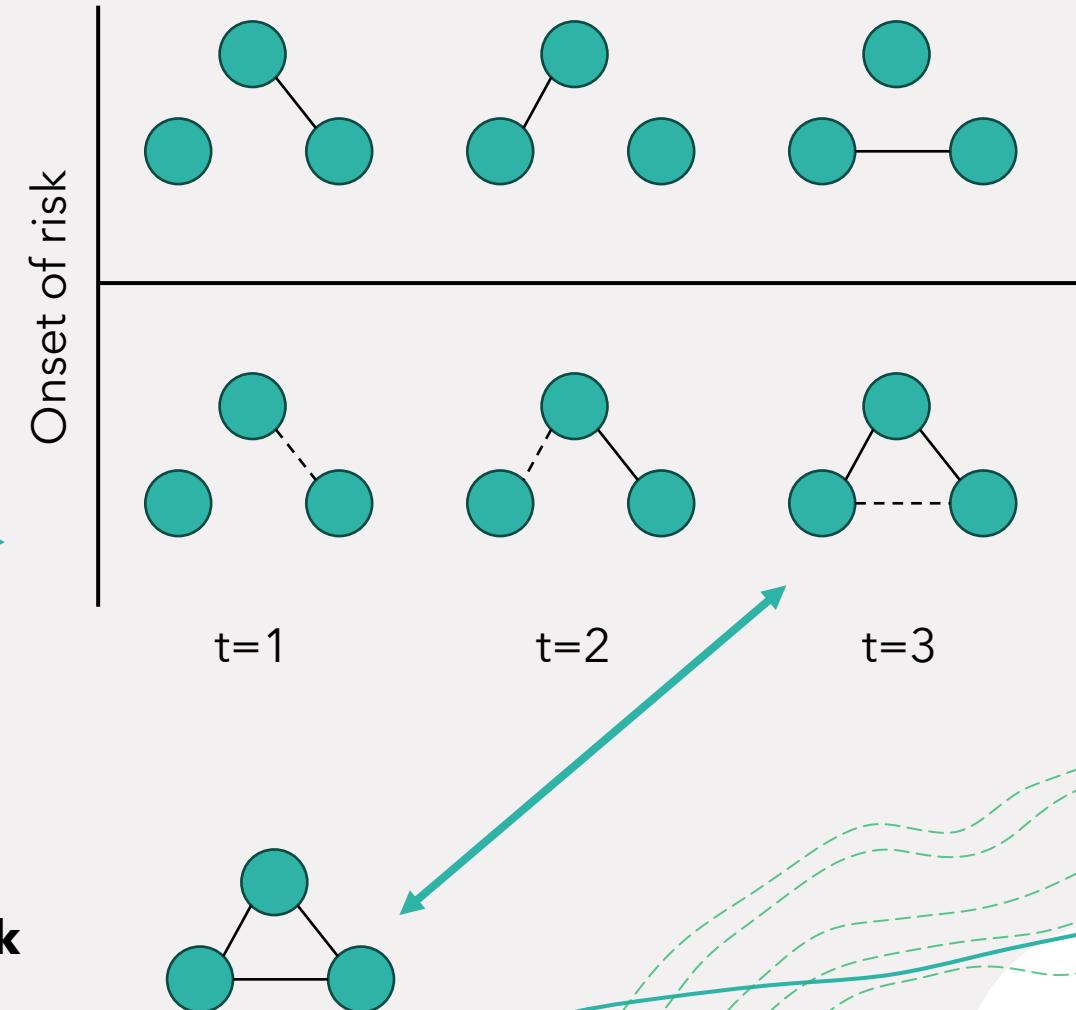
+ A model that allows ties to **form** and **dissipate** in their natural time frame



+ We also need to account for the *endogenous network structures* that accrue from histories of prior events



Aggregated network

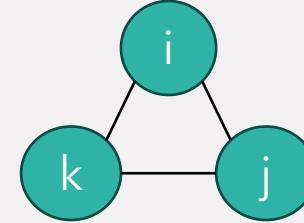


Relational event models (REM)

- + In REM we model the ***hazard rate*** of relational event activity
- + The model can handle continuous time or ordinal time and can include **endogenous and exogenous** network statistics
- + We'll focus on the dyadic case that treats **the dyad as the unit of analysis.**

Relational event models (REM): The technical side

- + We treat the **dyad** as the **unit of analysis**
- + Let (i,j) be a relational event connecting nodes i and j at time t
- + We assume a **nonhomogeneous Poisson process** for the count of ties at each observation
- + **Or** we assume exponential distribution for modeling the time between events



Nonhomogeneous Poisson process for the count of ties at each observation

A nonhomogeneous Poisson process implies that the **rate at which ties occur may vary over time** or across different dyads.

This assumption allows for flexibility in modelling the data.

Relational event models (REM): The technical side

+ A Poisson probability model for the frequency of events at each time period:

$$\Pr(n_{ij}(t)) = \frac{\lambda_{ij}(t)^{n_{ij}(t)} \cdot \exp(-\lambda_{ij}(t))}{n_{ij}(t)!}$$

n is the number of events per time period t that could have occurred

λ is our *hazard rate*.

Higher values of λ indicate higher event frequencies at a given time period; lower values indicate lower event frequencies.

Delving into the Hazard λ

- + The propensity of an event to occur is defined via its hazard (rate).
- **Indicate dependent variable:** **what** will happen next, **when** will it happen, and **who** will be involved.
- For each **dyad** (actor i , actor j) at time t there is a **rate parameter λ** which is a **loglinear function** of predictors.
- + Each event that is possible at a given moment has a **non-zero hazard**.
- + Larger hazards correspond to higher propensities (**the concept of risk set!**)

Relational event models (REM): The technical side

In practice, we are often interested in interpreting the coefficients that *increase or decrease* the hazard rate

We model the hazard rate using a generalized linear model:

$$\lambda_{ij}(t) = \exp(\lambda_0 + \boldsymbol{\theta}^T z(x, A))$$

Or

$$\log \lambda_{ij}(t) = \lambda_0 + \boldsymbol{\theta}^T z(x, A)$$

A is the *event sequence*, or history of prior relational events

x contains our exogenous node, edge, and time period level variables

$Z()$ is a mapping function that calculates sufficient statistics

θ contains our coefficients for interpretation

λ_0 is the baseline hazard rate (the intercept for our model). It tells us how likely an ij event is to occur by random chance, conditional on other variables

Rate function

$$\log \lambda_{ij}(t) = \lambda_0 + \boldsymbol{\theta}^T z(x, A)$$

- ✓ The **statistics** calculated by $z(x, A)$ translate the observed relationships into independent variables
- ✓ Coefficients, θ , represent the increase/decrease in the log-hazard ratio of event occurrence.
- ✓ Exponentiating θ gives us the increase/decrease in the hazard ratio per one unit change in $z(x, A)$.
- ✓ λ_0 is the **baseline hazard rate** (the intercept for our model: how likely an event is to occur by random chance, conditional on other variables)

Interpretation of θ

$$\log \lambda_{ij}(t) = \lambda_0 + \boldsymbol{\theta}^T z(x, A)$$

Because of REM's flexibility, we can interpret θ in three ways:

- As **the frequency of relational events at a given time periods**. Higher values indicate that (i,j) ties are more common at a given time period.
- As **the probability of an event occurring at a given time period**. Higher values indicate that a focal (i,j) connection is more likely at a given time period.
- As **the timing to event occurrence**. Positive values indicate *shorter* times to event occurrence; lower values indicate *longer* time to event occurrence

Relational Event Models (REMs): Model overview

- **The dependent variable:** **what** will happen next, **when** will it happen, and **who** will be involved.

$$\log \lambda(i,j,t) = \lambda_0 + \theta_1 \mathbf{x}_1(i,j,t) + \theta_2 \mathbf{x}_2(i,j,t) + \theta_3 \mathbf{x}_3(i,j,t) + \dots$$

$$\log \lambda_{ij}(t) = \lambda_0 + \boldsymbol{\theta}^T z(x, A)$$

Relational Event Models (REMs)

- **The predictor variables:**

- + **Actor characteristics** (tenure of employees x_1 , hierarchy, gender,...)
- + **The past** (volume of past interactions x_2 , ...)
- + **External factors** (epidemic situation x_3 ,...)

$$\log \lambda(i,j,t) = \lambda_0 + \theta_1 x_1(i,j,t) + \theta_2 x_2(i,j,t) + \theta_3 x_3(i,j,t) + \dots$$

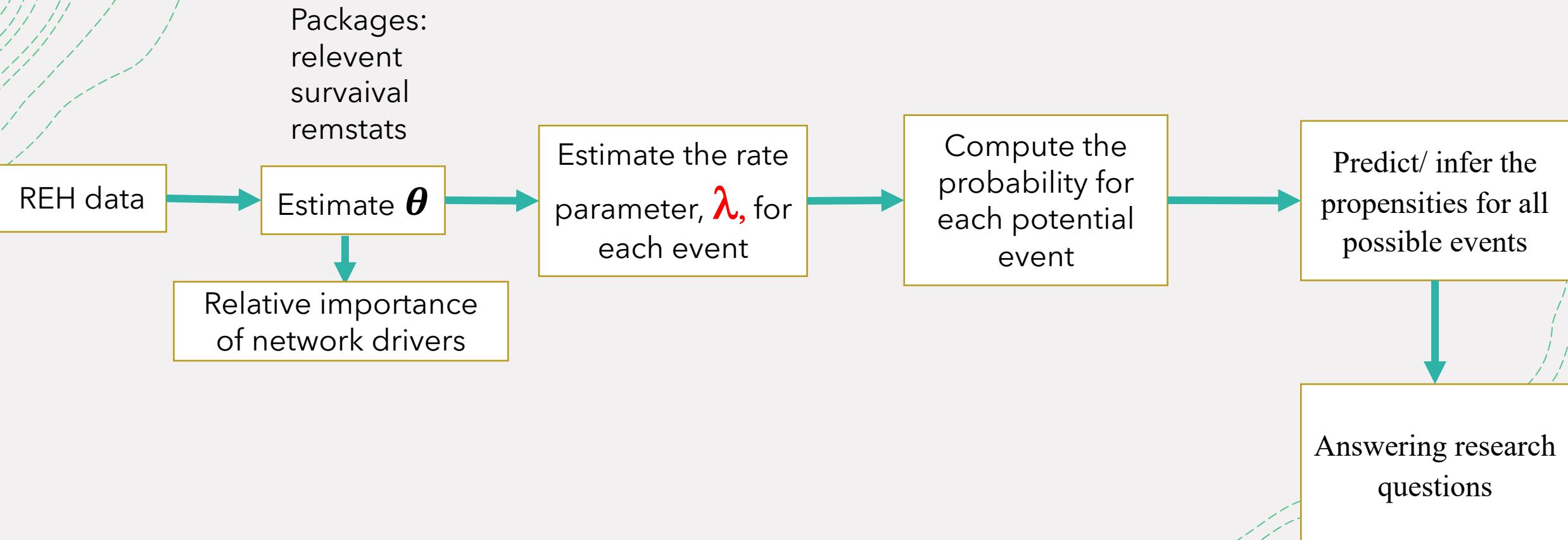
Fitting a REM

- + Requires the **estimation** of the $\lambda(i,j,t)$.
- + Or requires the **estimation** of the **probability** that a particular sequence of events transpired as a function of exogenous and endogenous factors.
- + The **rate** for each dyad is a **function of statistics** such as **inertia, reciprocity, gender** of actors as well as **parameters** that represent the **sign** and **strength** of the statistics' effects.

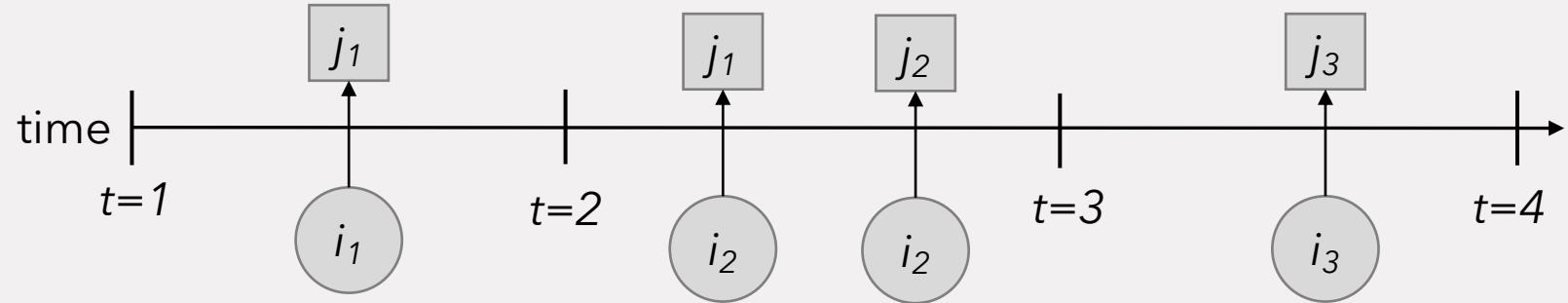
$$\log \lambda(i,j,t) = \lambda_0 + \theta_1 x_1(i,j,t) + \theta_2 x_2(i,j,t) + \theta_3 x_3(i,j,t) + \dots$$

β that represents the magnitude of a particular effect (Stadtfeld et al., 2018).

Relational Event Models (REMs)



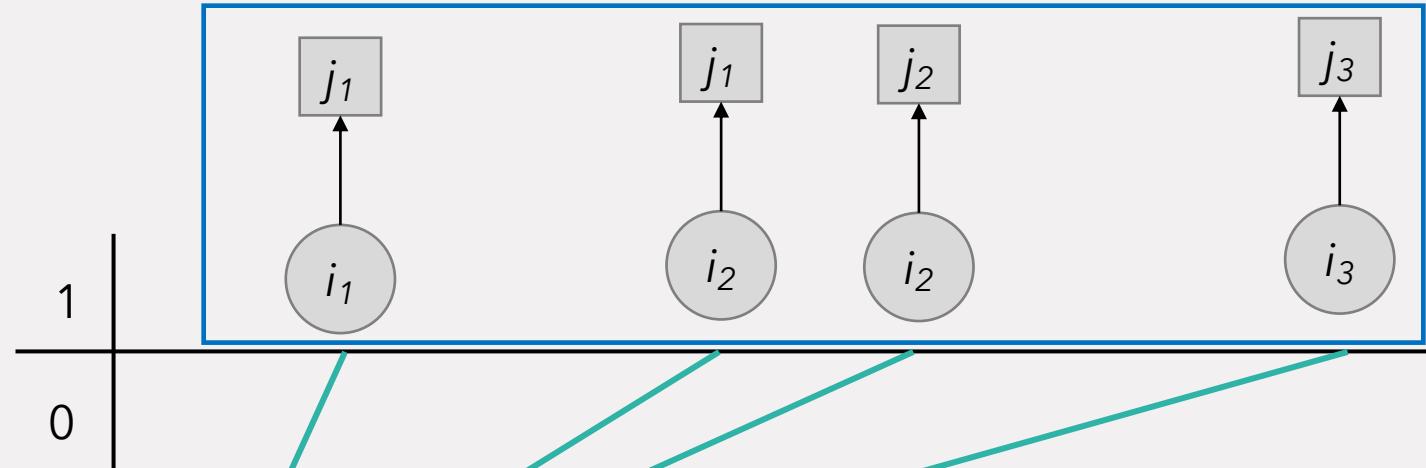
Risk set



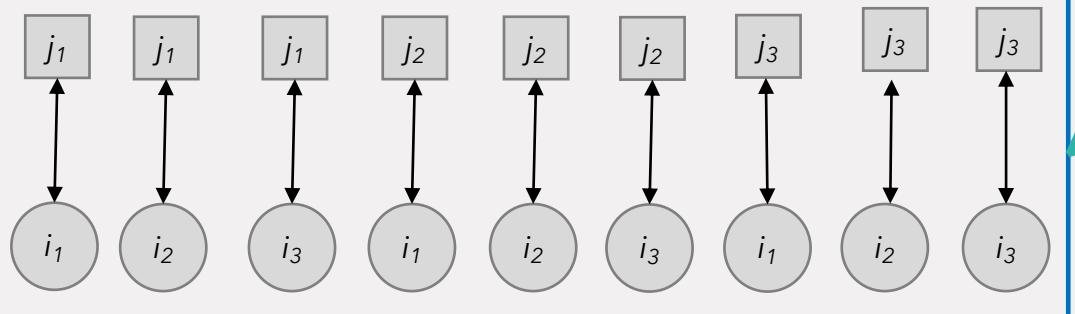
risk set

All events that have or could have occurred at one point in time

true events



risk set



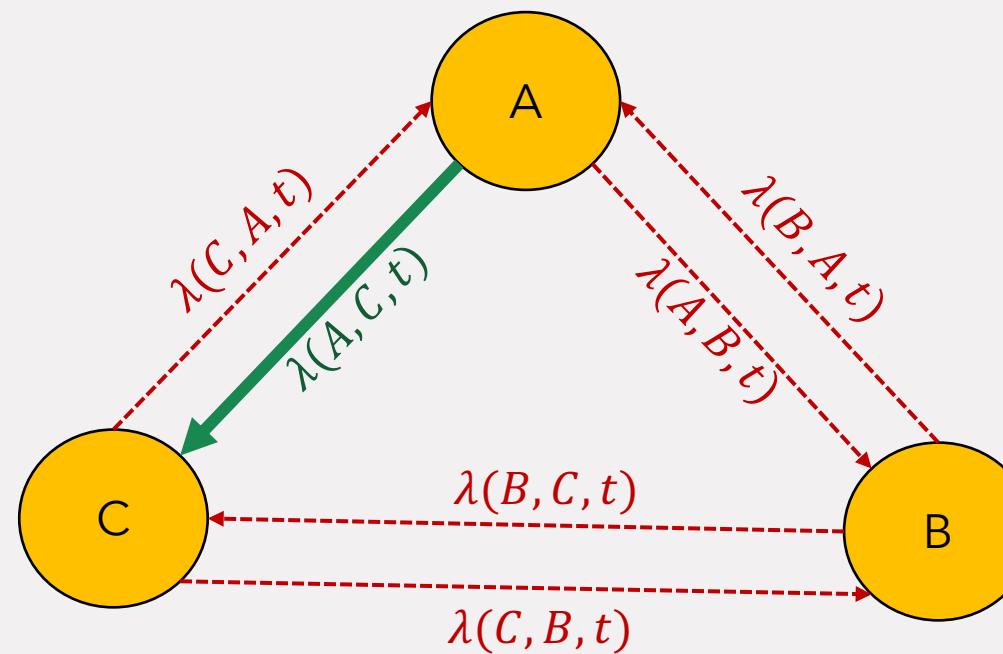
Example: Relational Event History data (REH)

Sender (i)	Receiver (j)	Time (t)
A	C	2
C	A	2.4
B	A	3

Sender	Receiver	Time (h)	$\hat{\beta}_1$ <u>Inertia</u>	$\hat{\beta}_2$ <u>Reciprocity</u>	$\hat{\beta}_3$ <u>Gender</u>	λ <u>Rate</u>	Prob of event
A A B B C C	B C A C A B	2 2 2 2 2 2	0 0 0 0 0 0	0 0 0 0 0 0	1 1 0 0 0 0	λ_{AB} λ_{AC} λ_{BA} λ_{BC} . .	$\lambda_{AB}/\sum \lambda$ $\lambda_{AC}/\sum \lambda$ $\lambda_{BA}/\sum \lambda$ $\lambda_{BC}/\sum \lambda$
A A B B C C	B C A C A B	2.4 2.4 2.4 2.4 2.4 2.4	0 1 0 0 0 0	0 0 0 0 0 0	1 1 0 0 0 0	. .	
C C .	A B .	2.4 2.4 .	0 0 .	1 0 .	0 0 .		

Probability that a particular sequence of events transpired

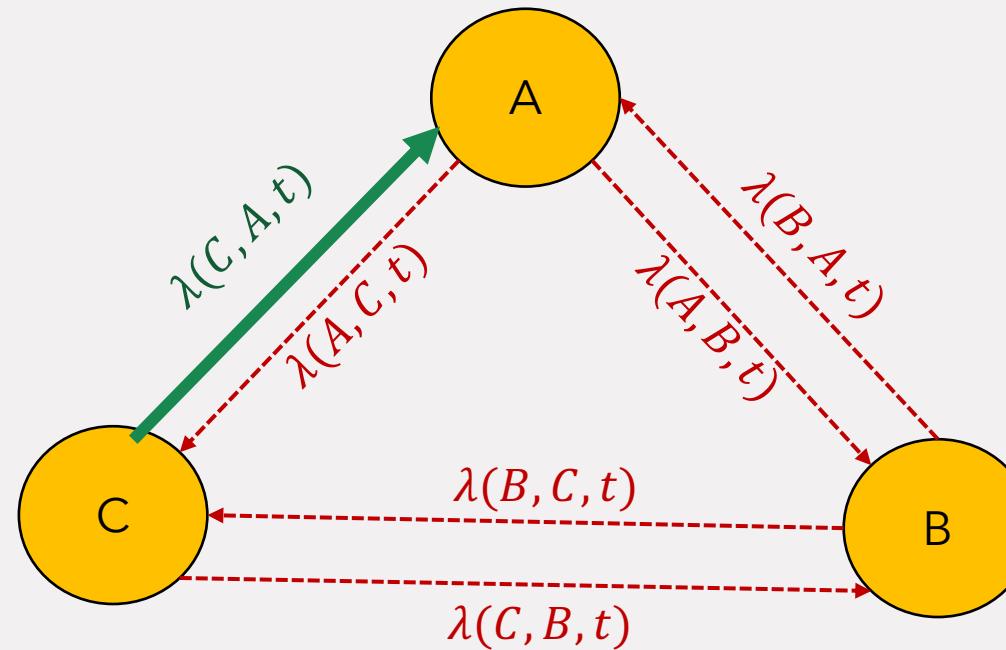
$t=2$



- + Time till the next event: $t_m - t_{m-1} \sim \text{Exp}(\sum \lambda(s', r', t))$, $(s', r') \in R_t$
- + Which relational event: $P(s, r) = \frac{\lambda(s, r, t)}{\sum \lambda(s', r', t)}$
- + REM captures the probability of the full sequence by **tuning the rate parameters** and **maximizing the likelihood of each observed event**.

Probability that a particular sequence of events transpired

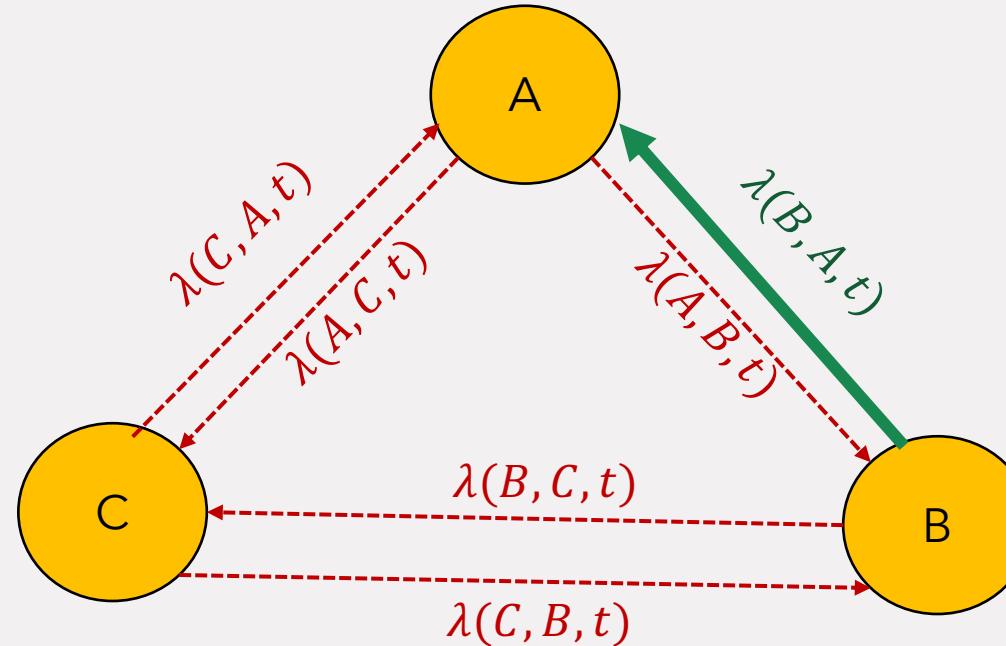
t=2.4



- + Time till the next event: $t_m - t_{m-1} \sim \text{Exp}(\sum \lambda(s', r', t))$, $(s', r') \in R_t$
- + Which relational event: $P(s, r) = \frac{\lambda(s, r, t)}{\sum \lambda(s', r', t)}$
- + REM captures the probability of the full sequence by **tuning the rate parameters** and **maximizing the likelihood of each observed event**.

Probability that a particular sequence of events transpired

$t=3$



- + Time till the next event: $t_m - t_{m-1} \sim \text{Exp}(\sum \lambda(s', r', t))$, $(s', r') \in R_t$
- + Which relational event: $P(s, r) = \frac{\lambda(s, r, t)}{\sum \lambda(s', r', t)}$
- + REM captures the probability of the full sequence by **tuning the rate parameters** and **maximizing the likelihood of each observed event**.

R packages for implementing REM

For estimating the parameters:

- + relevant -----(**rem.dyad()**, **rem()**)
- + survival -----(**coxph()**)

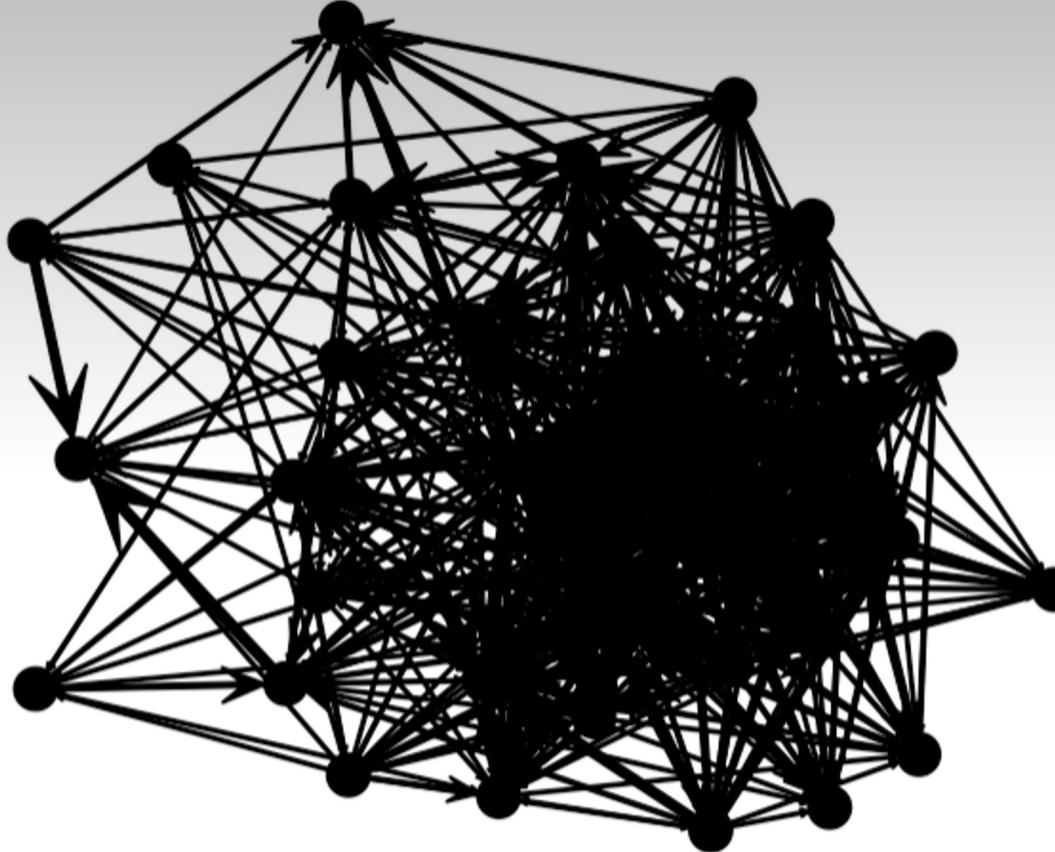
Estimation of the parameters

- + For computing statistics
- + remstats, remify, remulate,...

Computing statistics and fit the model

- + **Note:** For **relevant::rem()**, and **survival::coxph()** you need to compute the statistics first.

Twitter



```
Twitter1 <- rem.dyad(Twitter_data_rem3,n=39, effects = c("PSAB-BA", "PSAB-BY"), ordinal =  
FALSE, hessian = TRUE)  
  
summary(twitter1)
```

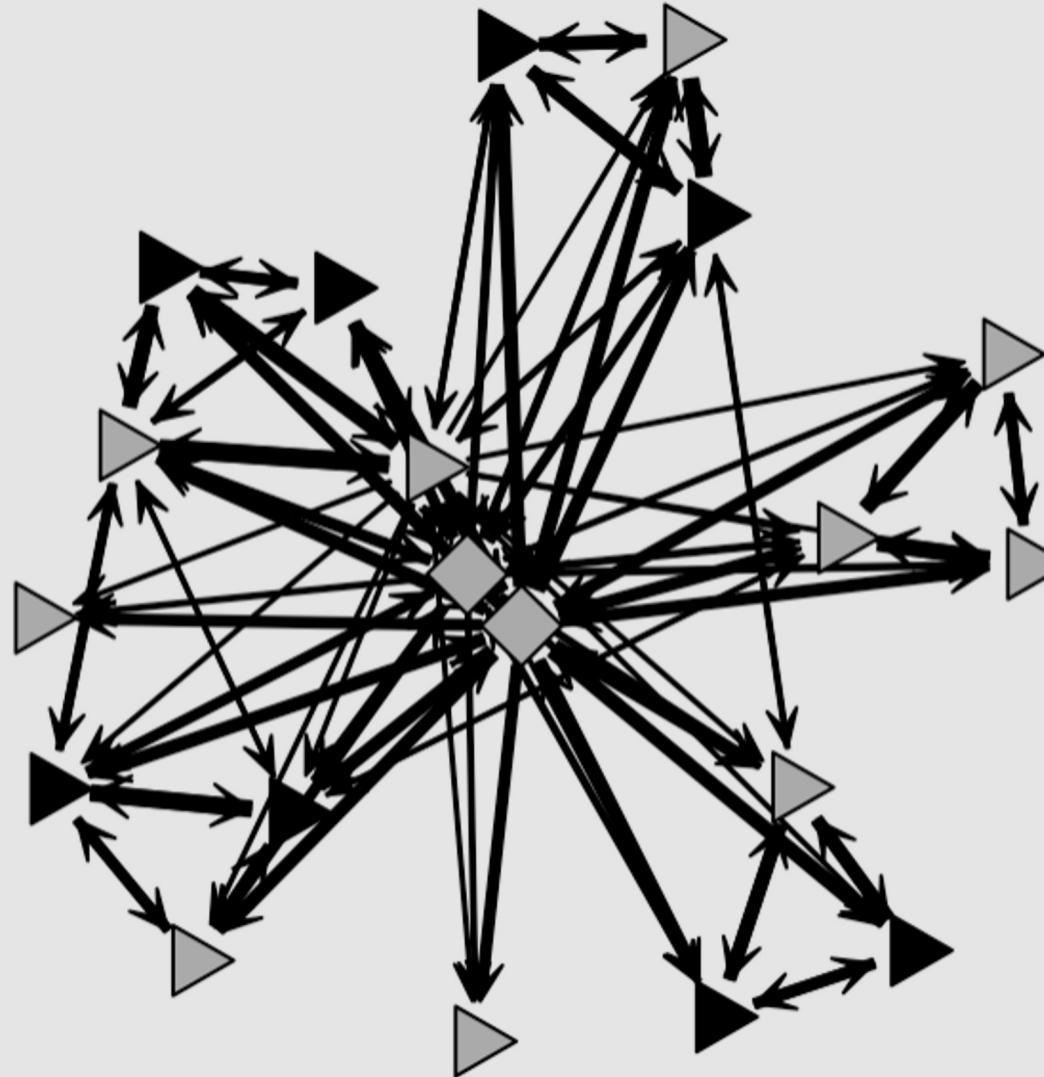
Relational Event Model (Temporal Likelihood)

	Estimate	Std.Err	Z value	Pr(> z)
PSAB-BA	-6.757	0.5777.	-11.697	< 2.2e-16 ***
PSAB-BY	-8.285.	0.2040.	-40.611	< 2.2e-16 ***

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 '' 1

Class



```
classfit5<-rem.dyad(Class,n=20, effects=c("CovSnd","CovRec","RRecSnd","RSndSnd",
"PSAB-BA","PSAB-AY","PSAB-BY"), covar=
list(CovSnd=cbind(ClassIntercept,ClassIsTeacher),
CovRec= cbind(ClassIsTeacher,ClassIsFemale))
summary(classfit5)
```

	Estimate	Std.Err	Z value	Pr(> z)
+ RRecSnd	2.429210	0.155367	15.6353	< 2.2e-16 ***
+ RSndSnd	-0.986720	0.144668	-6.8206	9.068e-12 ***
+ CovSnd.1	-5.003468	0.090610	-55.2197	< 2.2e-16 ***
+ CovRec.1	-0.722667	0.141950	-5.0910	3.562e-07 ***
+ PSAB-BA	4.622159	0.137602	33.5908	< 2.2e-16 ***
+ PSAB-BY	1.677639	0.164930	10.1718	< 2.2e-16 ***
+ PSAB-AY	2.869985	0.103114	27.8330	< 2.2e-16 ***

The predictor variables:

(X_1, X_2, X_3, \dots)

- + Inertia...
- + Reciprocity
- + Transitivity
- + In(out) degree sender/receiver
- + ...
- + Age
- + Hierarchy
- + Same location
- + ... whatever you believe is important

Inertia

The **tendency** of person i to continue to initiate events towards person j , as a function of the **volume of past events** from i to j .



Example-- Inertia

- + A teacher exhibits a tendency to ask students they have been frequently asked questions in the past.
- + Then the true effect value $\beta_{INERTIA}$ of inertia statistics is positive, and the REM should find a positive and significant estimate.

$$\log \lambda(i,j,t) = \lambda_0 + \beta_{INERTIA} * \text{Inertia}(i,j,t) + \theta_2 x_2(i,j,t) + \theta_3 x_3(i,j,t) + \dots$$

Reciprocity

The tendency of person i to initiate events towards person j , as a function of the volume of past events i received from j .



$$\log \lambda(i,j,t) = \lambda_0 + \beta_{INERTIA} * \mathbf{Inertia}(i,j,t) + \beta_{recipro} * \mathbf{Recipro}(i,j,t) + \theta_3 x_3(i,j,t) + \dots$$

Example-- Reciprocity

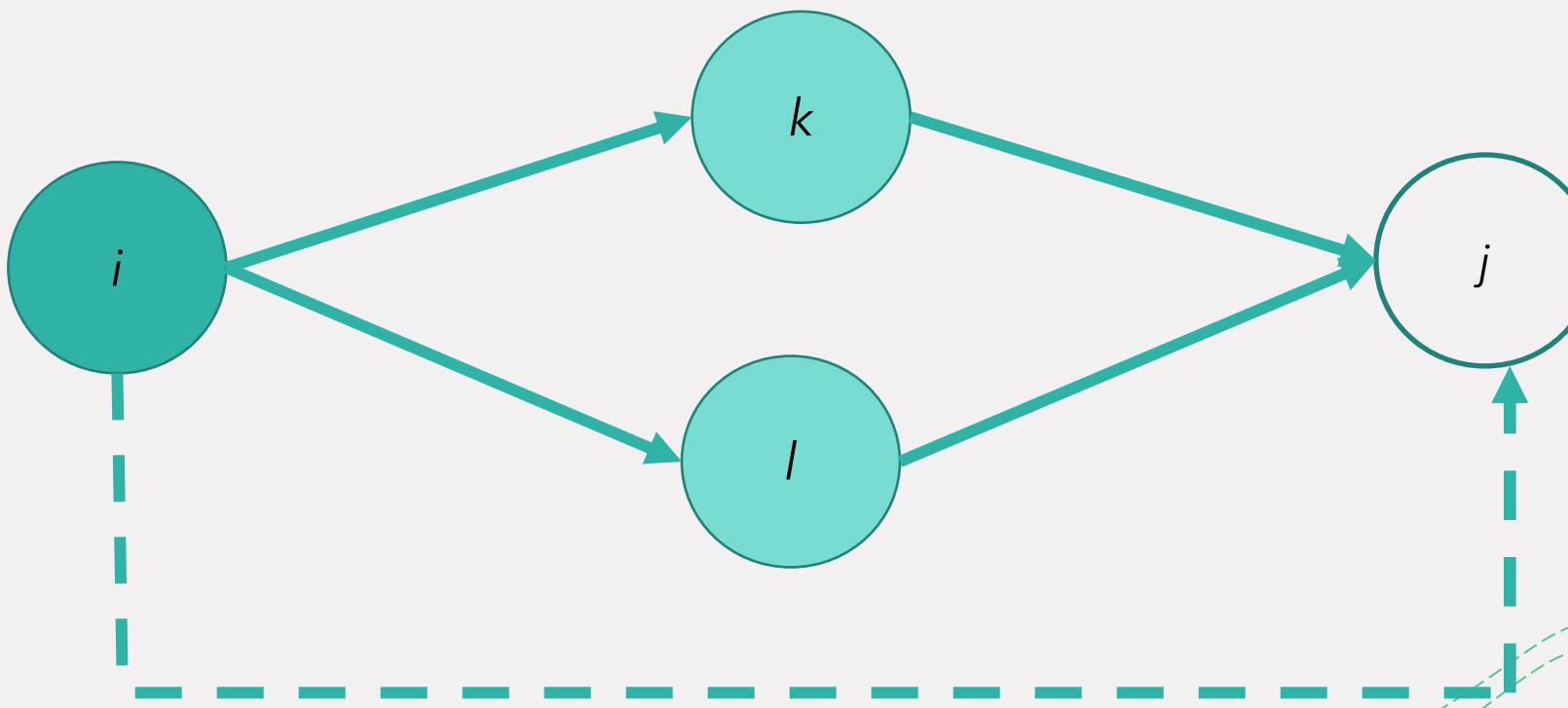
- + Teachers and students do reciprocate over time in ways that are not influenced by reciprocating in the past. This can be understood as a teacher who does not show the tendency to ask the same student who has already asked a question more often.
- + When this is the case, the effect of the reciprocity statistic should be small.
- + The results would not show a tendency for reciprocating (i.e., connecting through a chain of questions and answers).
- + $\log \lambda(i,j,t) = \lambda_0 + \beta_{INERTIA} * \text{Inertia}(i,j,t) + \beta_{recipro} * \text{Recipro}(i,j,t) + \theta_3 x_3(i,j,t) + \dots$

Example of Kitts et al. (2017)

- + **Research question:** Do hospitals engage in the social norm of reciprocity when exchanging patients, instead of sending them to the hospital that can offer the best service for the patient?
- + Using REM, they examined reciprocity in over 4,000 patient exchanges between 21 hospitals in a region of Italy, spanning 5 years.
- + **Result:** hospitals do reciprocate patient exchanges over time in ways that are not explained by the availability of beds, the quality of service, or the specialization of hospitals.

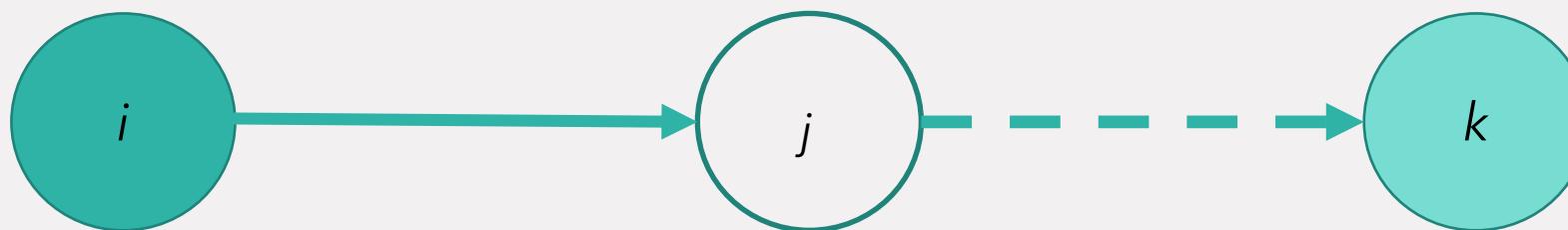
Transitivity

The tendency of person i to initiate events towards person j , as a function of the volume of past events j received from others to whom i had sent events.



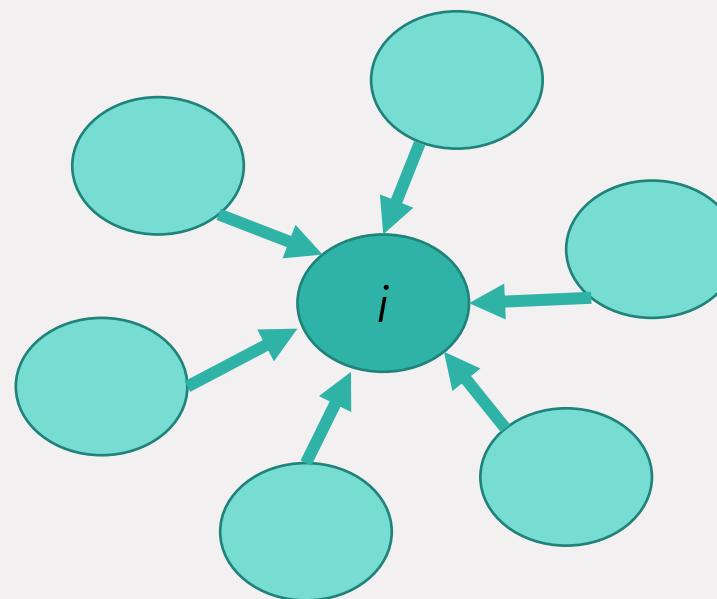
Participation shift AB-BY (“turn receiving”)

The tendency of an initial receiver j of an event to, **in turn**, direct the next event to another person k .



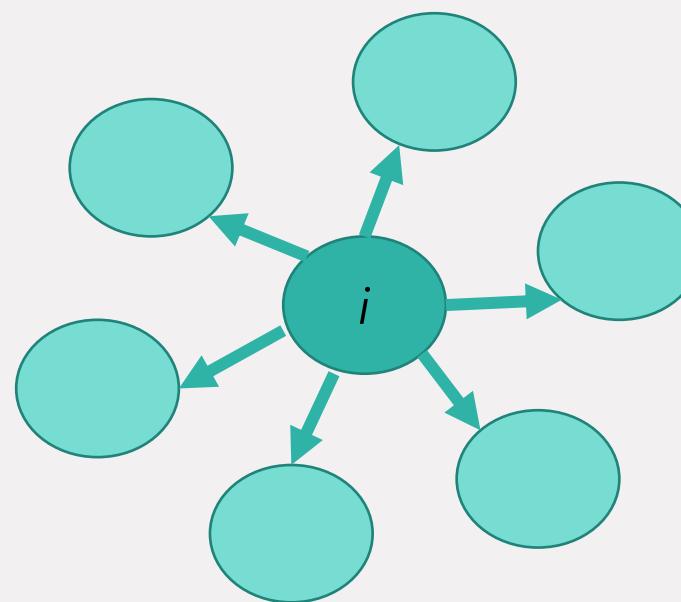
In-degree

In-degree is the number of connections that point inward at a vertex. Actors with high in-degree are impacted by multiple other actors.



Outdegree

Out-degree is the number of connections that originate at a vertex and point outward to other vertices.



In a nutshell, REM is suitable for

- + **Estimating** the relative important of *network driver effects* β .
- + **Testing** *temporal social theories* via competing statistical models.
- + **Predicting** future events, *what* will happen next, *when* it will happen, and *who* will be involved. REMs predict the occurrence of the next event in a temporally distributed sequence of events (Marcum & Butts, 2015)
- + This means that, in REM, the dependent variable can be the occurrence of the next event in a sequence, which is modelled as a function of the sequence of past events.
- + **Understanding** how interaction behavior *changes in continuous time*.
- + Why did some node tie to another at this point in time and not previously?

Longitudinal network analysis: ERGMs - TERGMs – SAOMS and REMs

- + The **choice** of network inference model depends on how time is recorded.

Four main network inference models:

- + Exponential Random Graph Models
- + Temporal Exponential Random Graph Models and
- + Stochastic Actor Oriented Model (SAOM)
- + **Relational Event Models**

Exponential Random Graph Model (ERGM)

R package: [ergm](#)

ERGM: Exponential Random Graph Model

- + Goal: “to **describe parsimoniously the local selection forces that shape the global structure of a network**” (Hunter et al. 2008). (the processes that influence link creation).
- + Why do we observe this particular network structure as oppose to some other possible network configuration?
- + ERGMs are tie-based statistical models for understanding **how and why social network ties arise**.
- + **Cross sectional model** for network structure. (single measurement of the network)

ERGM

- Let say G is a graph.
- **Summary measures $z(G)$:** or “network statistics,”
- Network statistics such as the **number of edges** in G , and so on.
- Network structural characteristics (triangles, two stars etc), exogenous actor and dyad characteristics (race, sex, homophily)
- The ERGM assigns probability to graphs according to these statistics:
$$P_{\theta}(G) = ce^{\theta_1 z_1(G) + \theta_2 z_2(G) + \dots + \theta_p z_p(G)}$$
 c is a normalizing constant.

This is the probability of a given network.

The parameters inform us of the **importance** of each configuration.

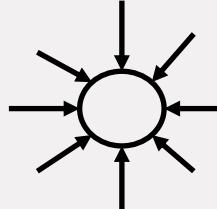
Remark:

- **Random Sample assumption:** the observed network is a random sample from a larger population of possible networks.
- Ties between nodes in real social networks are not independent; for example, as we've seen, reciprocity and transitivity are common features of human social networks.
- This non-independence violates the most basic assumption of regression!
- Through simulation, ERGMs allow dyadic and higher-order dependencies to be modelled.

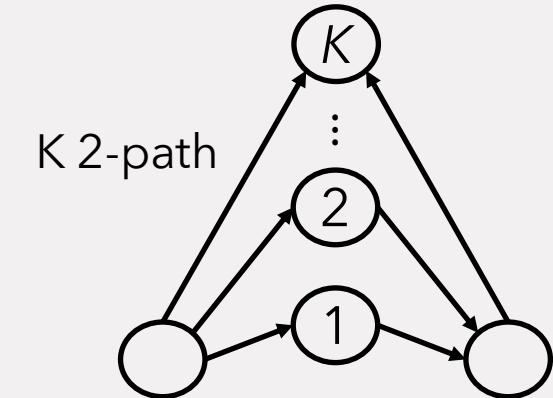
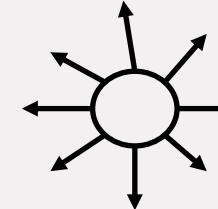
Different considered network statistics. More detailed explanations can be found in [Lusher et al. \(2013\)](#)



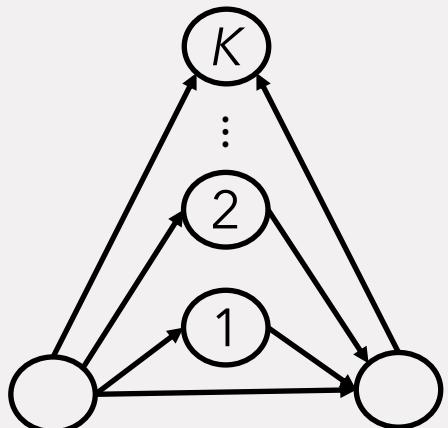
Popularity (K in-stars)



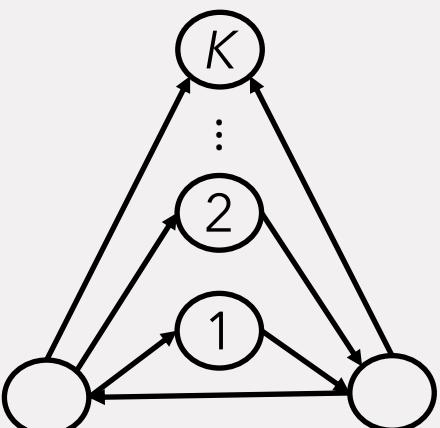
Activity (K out-stars)



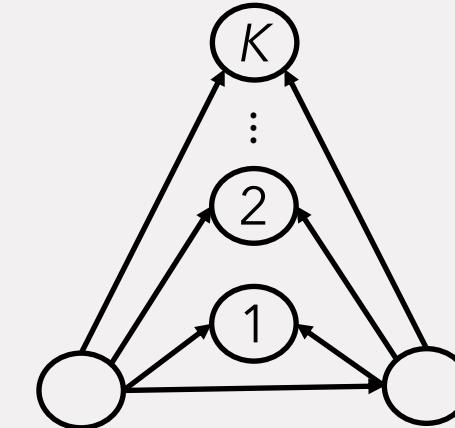
Path closure AT-T



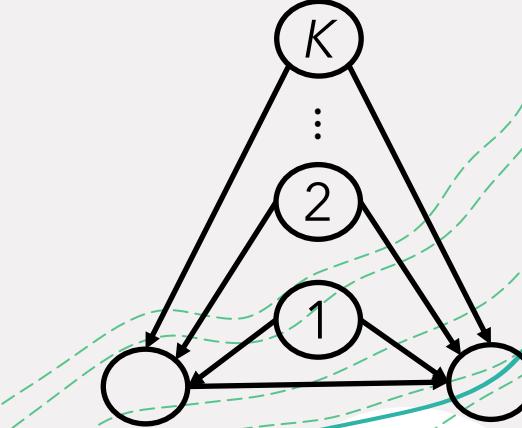
Cyclic closure AT-C



Activity closure AT-U



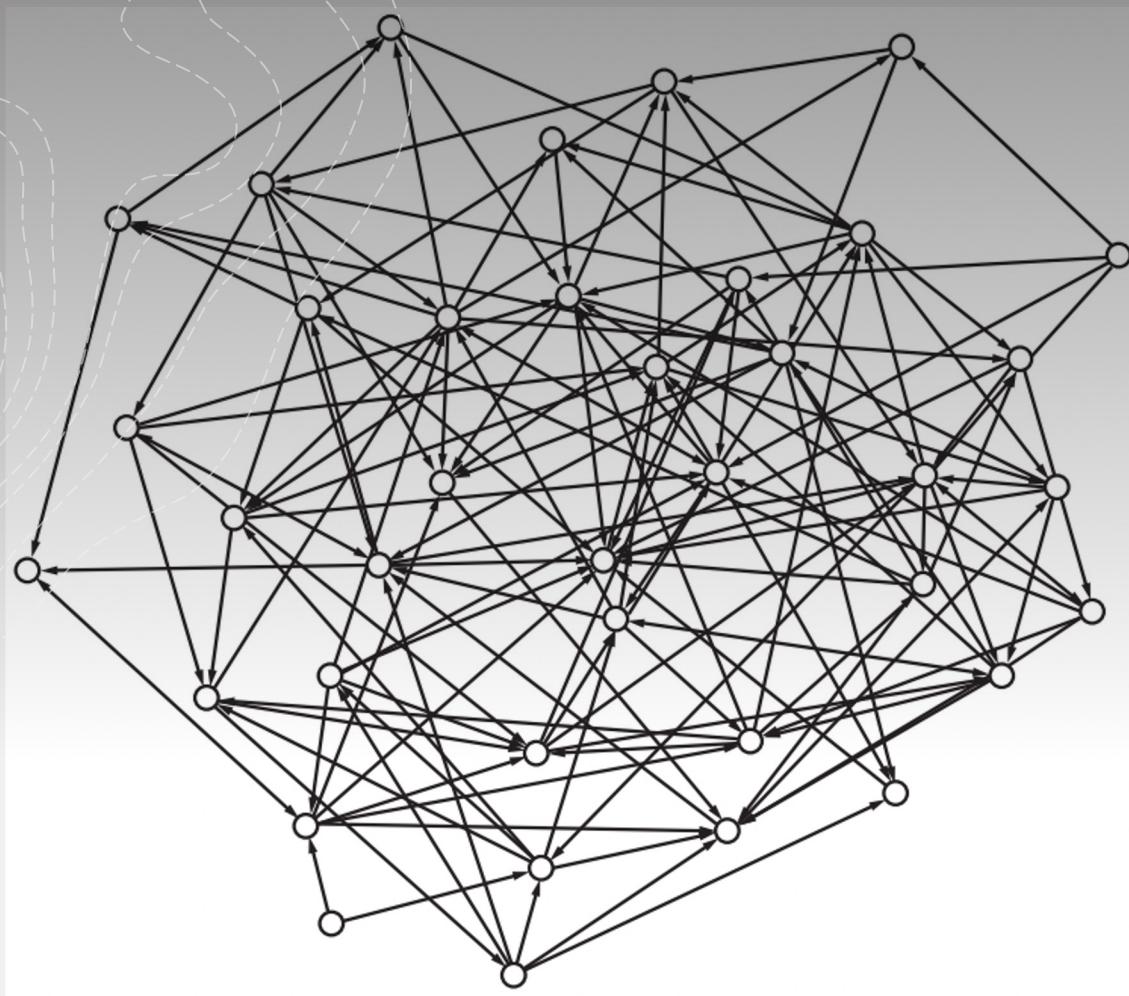
Popularity closure AT-D



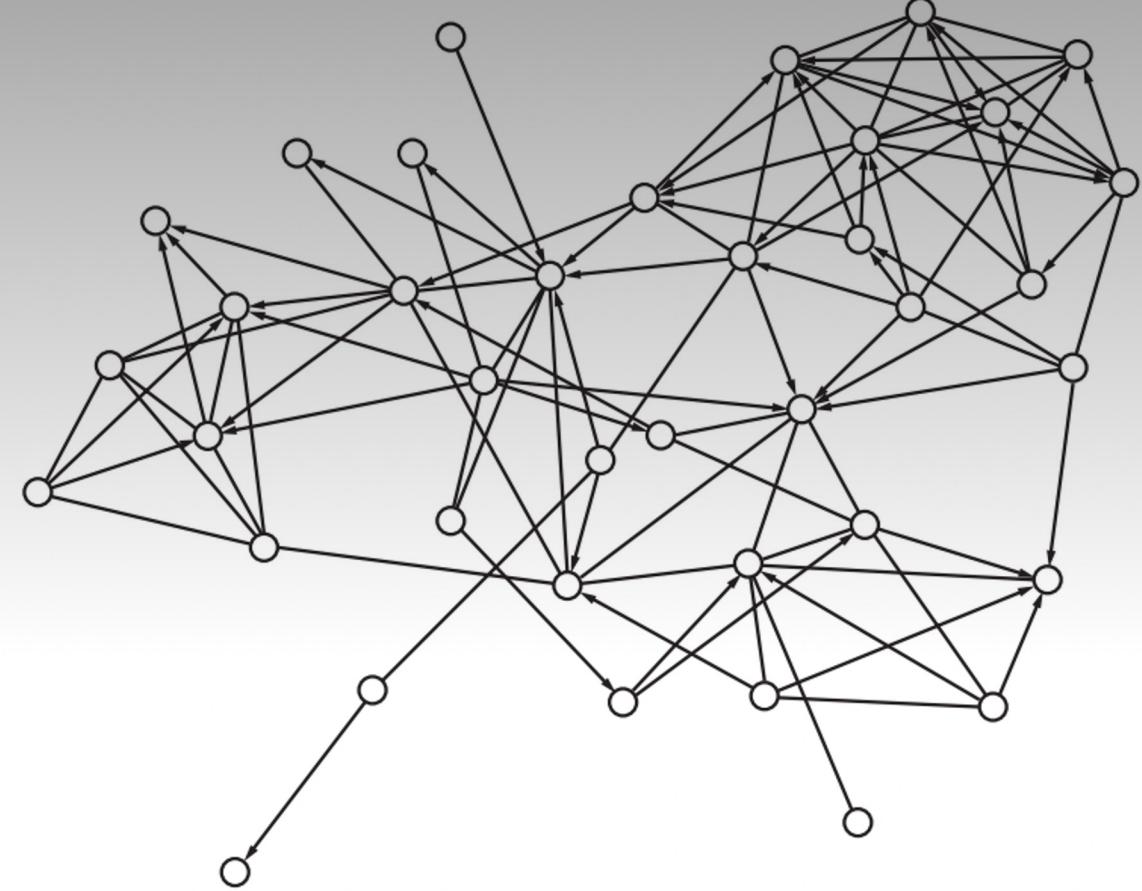
In nutshell:

- Include variables in the model that are hypothesised to explain the observed network.
- The ERGM will provide information relative to the statistical significance of the included variable.

- **Choose** a set of configurations of theoretical interest.
-
- ```
graph TD; A["• Choose a set of configurations of theoretical interest."] --> B["• Estimate the parameters by applying ERGM"]; B --> C["• Do inferences about the configurations - the network patterns - in the data."]; C --> D["• Do inferences about the type of social processes that are important in creating and sustaining the network"]
```
- **Estimate** the parameters by applying ERGM
  - Do **inferences about the configurations** - the network patterns - in the data.
  - Do **inferences about the type of social processes** that are important in creating and sustaining the network



(a)



(b)

Figure 4.1. (a) Simple random network and (b) empirical communication network.

[Lusher et al. \(2013\)](#)

*Table 4.1. Selected network statistics for networks in Figure 4.1*

|                   | Random network | Communication network |
|-------------------|----------------|-----------------------|
| Actors            | 38             | 38                    |
| Arcs              | 146            | 146                   |
| Reciprocated arcs | 6              | 44                    |
| Transitive triads | 53             | 212                   |
| In-2-stars        | 292            | 313                   |
| Out-2-stars       | 254            | 283                   |

# Examples

+ **The presence of reciprocity** : There is a process that generates a significant number of **reciprocated structure** that **is not** the result of **random link creation** e.g., a tendency to create a link between common friends.

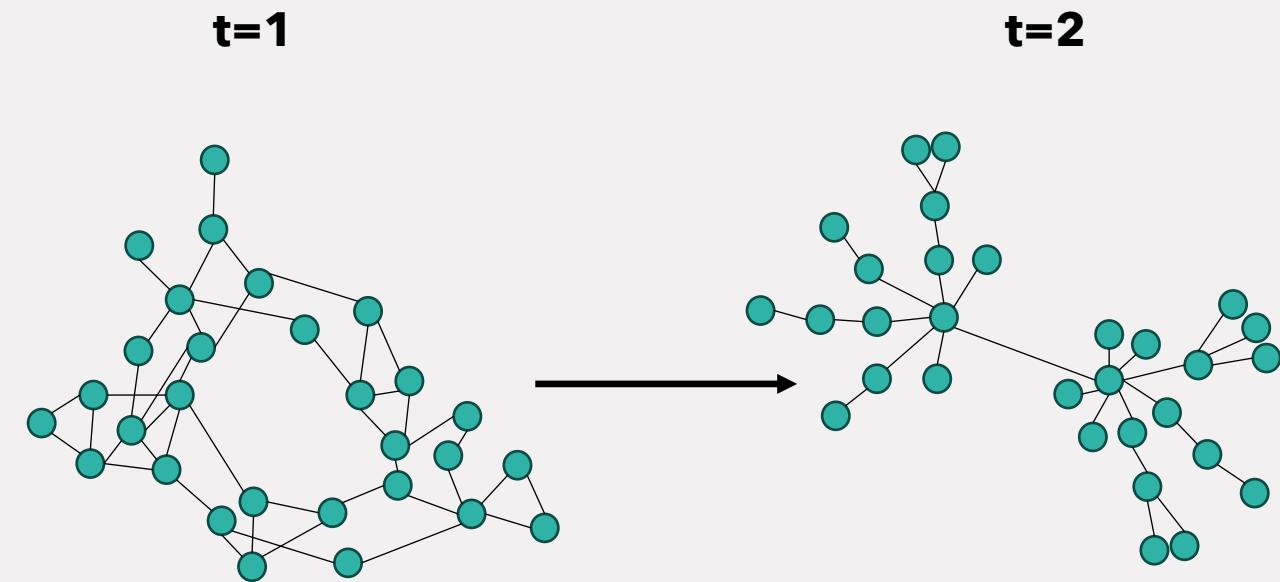
## Reciprocity



# TERGM is the temporal version of ERGM

+ Network Panels

+ Only the changes between Network panels



# **Stochastic Actor Oriented Models (SAOMs)**

(Snijders, 1996; Snijders et al., 2010)

R package: [RSiena](#)

# SAOMs

- Models for network **dynamics** and network **panel data**

**Network dynamic** through simulations.

**Network panel** data are common for representing relations like **friendship, advice, collaboration, exchange** which can be regarded as *states* rather than *events*.

# Application of SAOMs

a wide variety of domains:

- Study of selection patterns in school classrooms ,
- The evolution of communication networks in high-risk social-ecological systems,
- The role of teen drinking behaviour in friendship selection,
- ...

# SAOMs

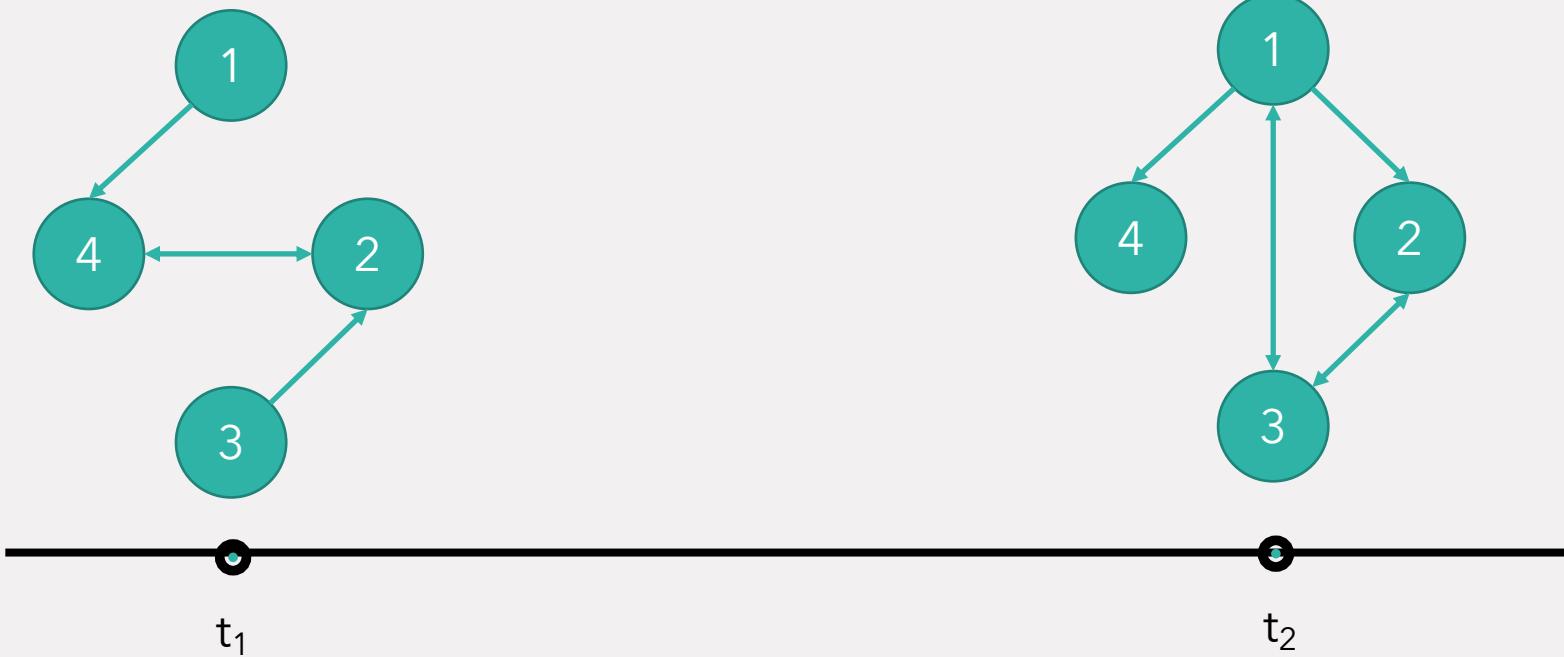
- developed for the analysis of **longitudinal social network** data, collected by taking two or more "snapshots" ("**panels**" or "**waves**") of a network as it evolves over time.
- **agent-based ('actor-oriented')** : They model changes from the perspective of the actors (**creating, maintaining or terminating ties** to other actors (a series of "**choices**" )) within a (potentially) changing network.

# SAOM as a model of the network evolution

- All network changes are decomposed into very small steps, so-called **ministeps**, in which one actor creates or terminates one outgoing tie.
- These **ministeps** are **probabilistic** and made sequentially.
- The **transition** from the observation at **one wave** to the **next** is done by means of normally a large number of ministeps. These **changes** are not individually observed, but they are **simulated**.
- This simulation model implements the statistical model for the **network dynamics**.

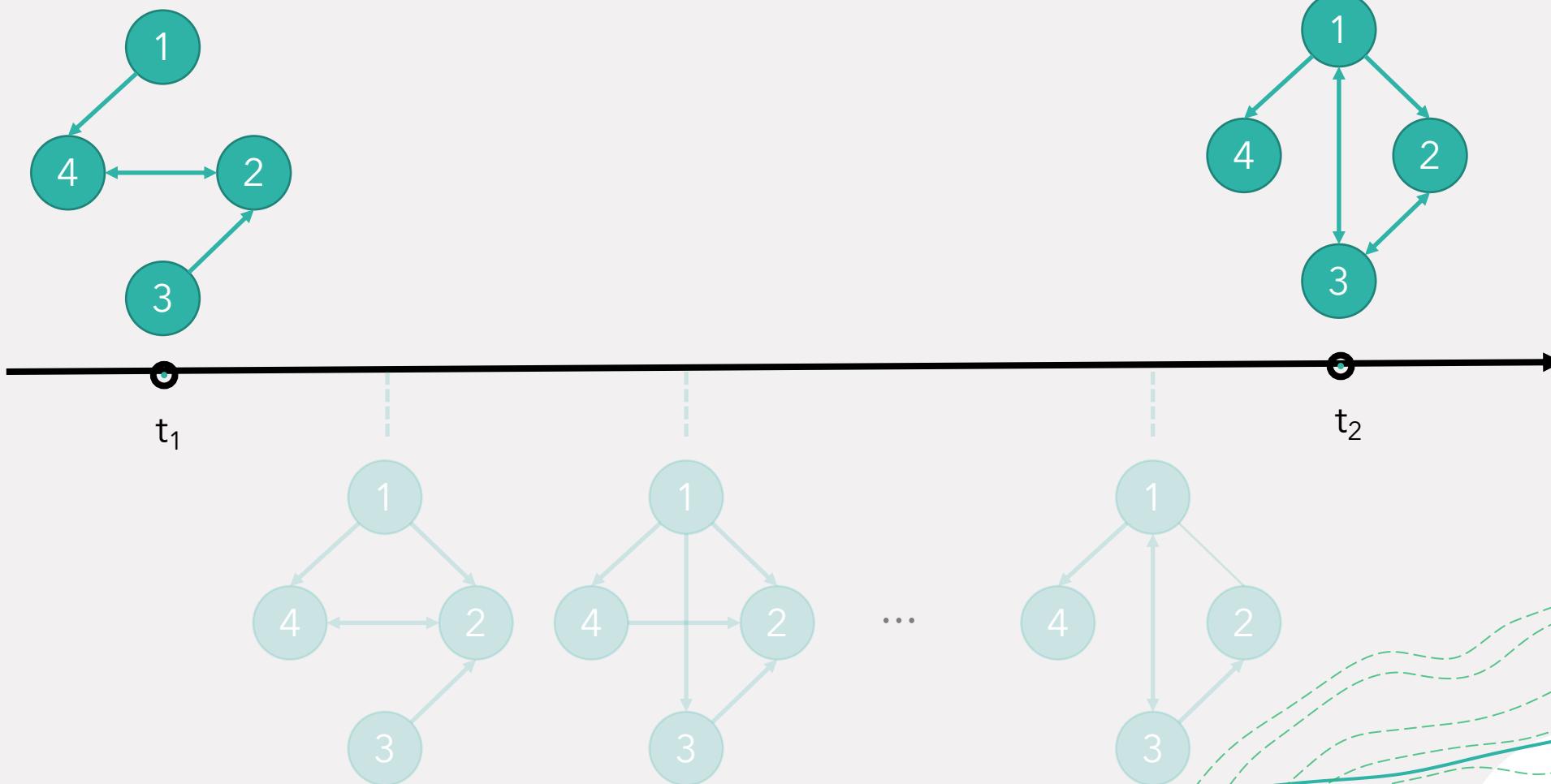
# SAOMs

Model assumptions: consequences



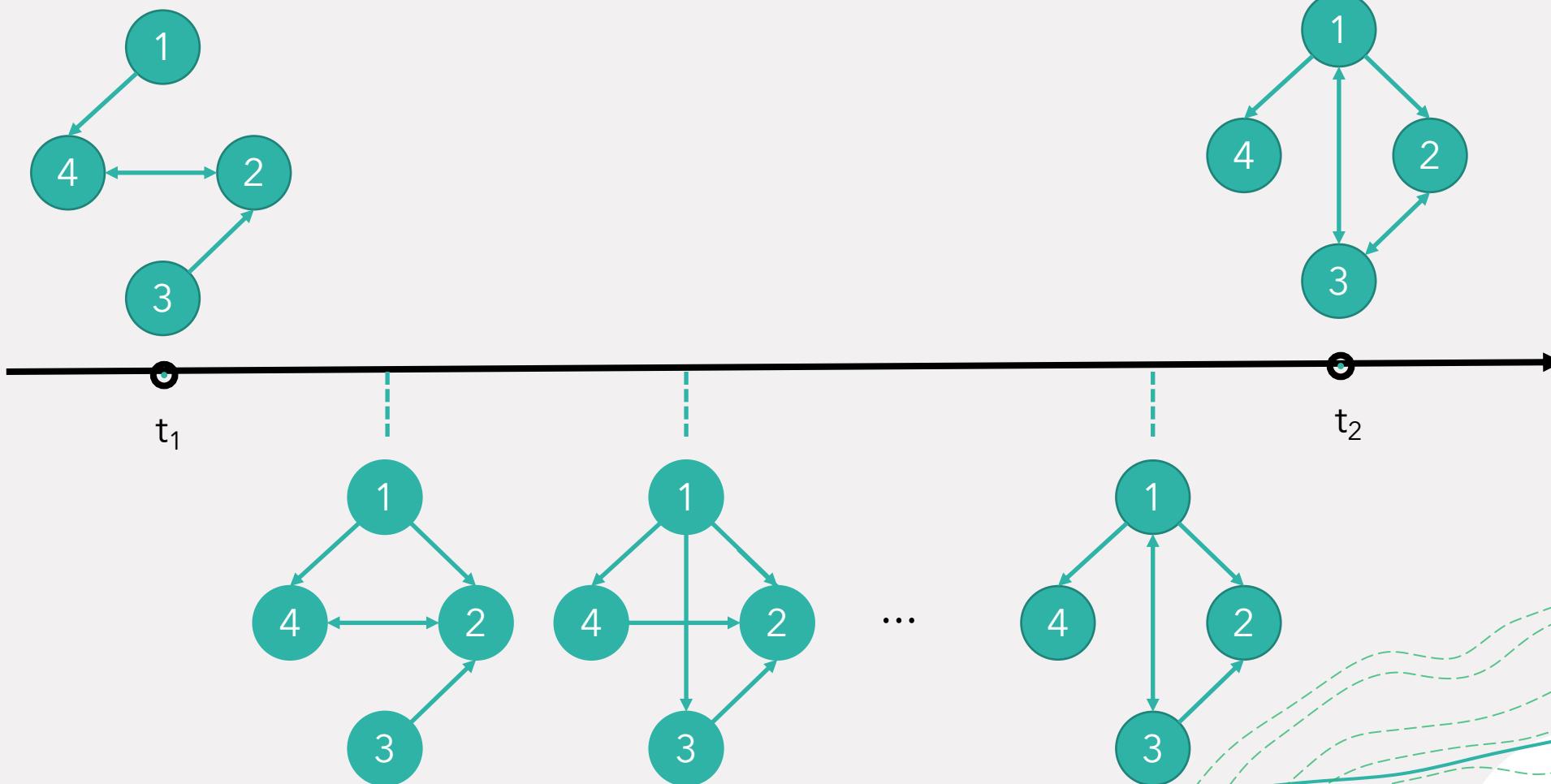
# SAOMs

## Model assumptions : illustration



# SAOMs

## Model assumptions: illustration



# Modeling tie changes

**Who gets the opportunity for a tie change and when?**

A **person** from the network is chosen to make a change according to **the rate function**.

For actor  $i$ , the waiting time until the next opportunity for change is exponentially distributed with rate parameter

$$\lambda_i(x, v) = \exp(\sum_k \alpha_k r_{i,k}(x, v))$$

**To whom?**

Next, we model **which tie change** is made. This is modelled in the objective function:

$$f(\beta, x, v, w) = \exp(\sum_k \beta_k s_{i,k}(x, v, w))$$

At each time step, the actors move in a direction that **maximizes their particular objective function**

# REM, ERGMs, TERGMs and SAOMs

- + For **ERGMs, TERGMs or SAOMs** the issue of **dependence between observations** is critical (Kalish, 2020; Lusher et al., 2013).
- + In REM, each event is considered to be **conditionally independent** of all other events in the sequence.
- + REM assumes temporal dependence.



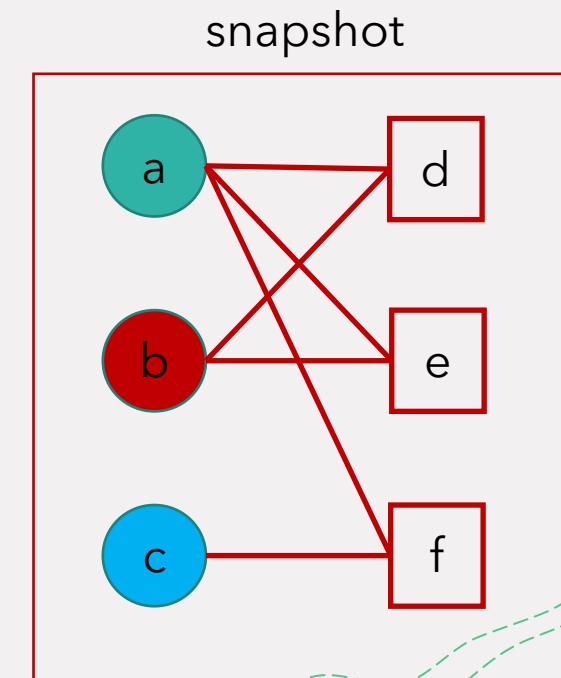
# Which model should we use?

# Longitudinal network analysis: ERGMs – SOAM, TERGMs – REMs

- + If you have 1 snapshot of your network → run an ERGM
- + ERGM = exponential random graph model

## Research question

Which factors affect the structure of the network?



$t = 1$

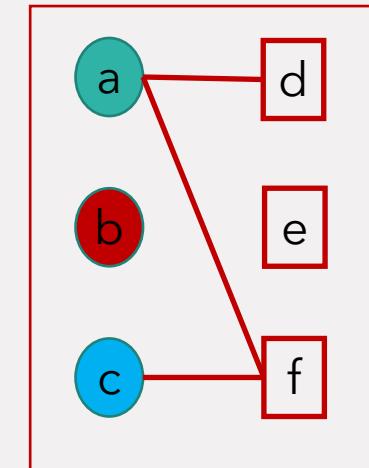
# Longitudinal network analysis: ERGMs – SOAM, TERGMs – REMs

- + If you have multiple snapshots of your network → run an tERGM or SAOM
- + tERGM = temporal exponential random graph model

## Research question

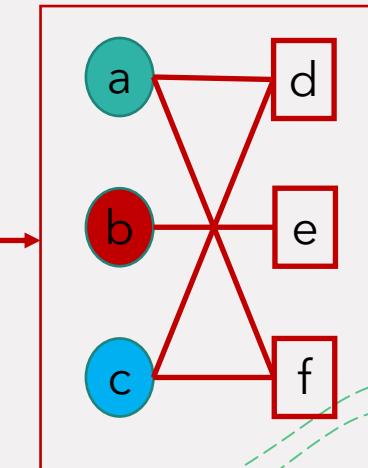
Which factors affect the structure of the networks and how do networks change over time?

snapshot1



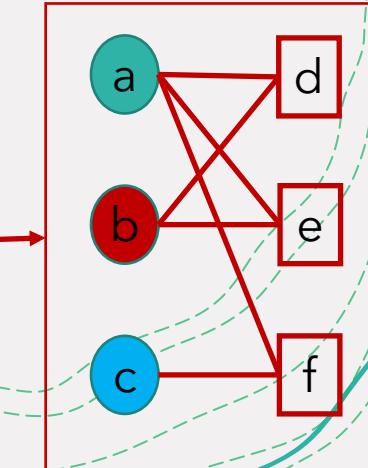
$t = 1$

snapshot2



$t = 2$

snapshot3

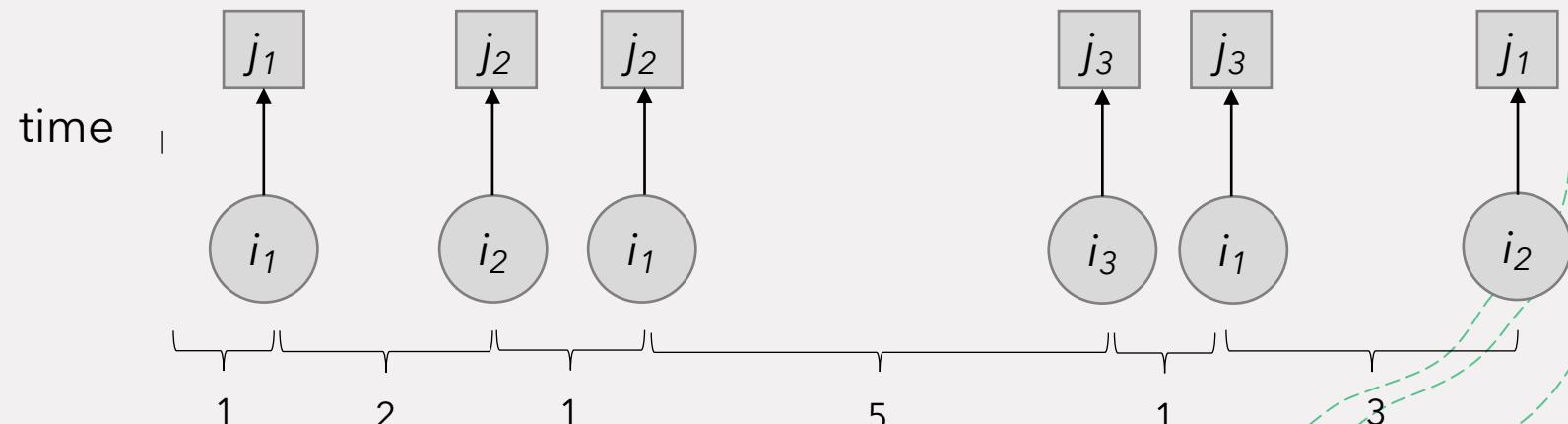


$t = 3$

# Longitudinal network analysis: ERGMs – SOAM, TERGMs – REMs

- + If you know the **time/order** each tie is created in a network → run a REM
- + ... recorded in exact time or ordered

**Research question**  
Which factors affect  
the probability of an  
edge forming at time  
point  $t$ ?



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