

Multilayer networks and the POPNET data

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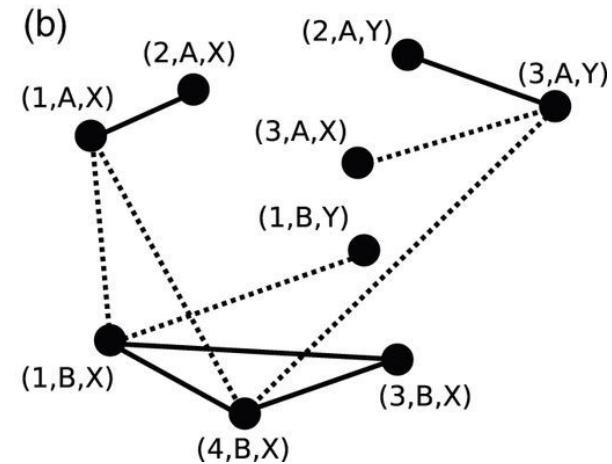
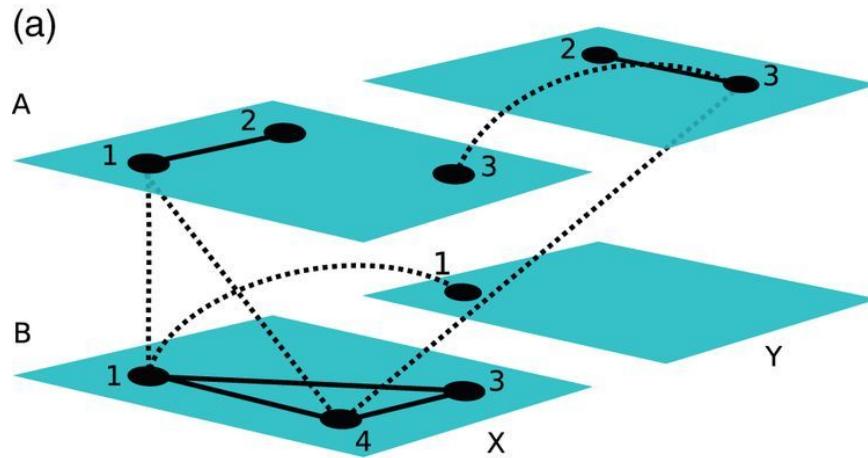


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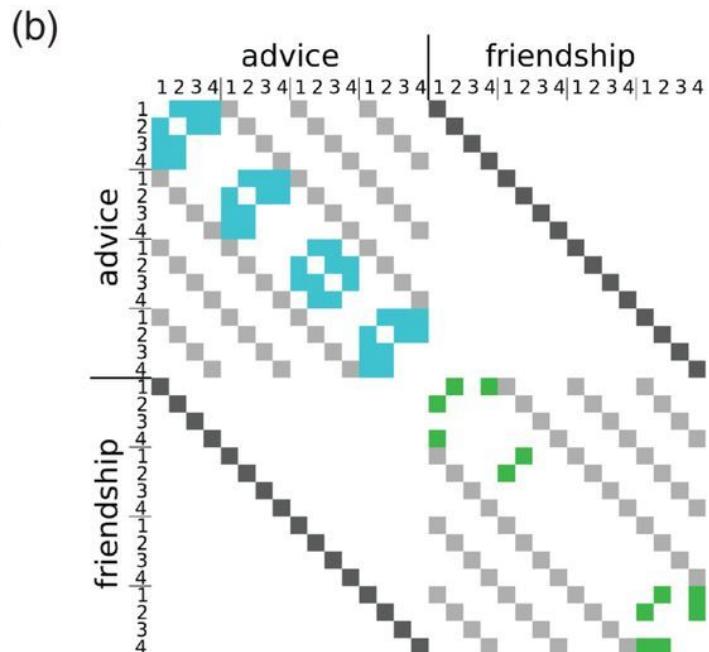
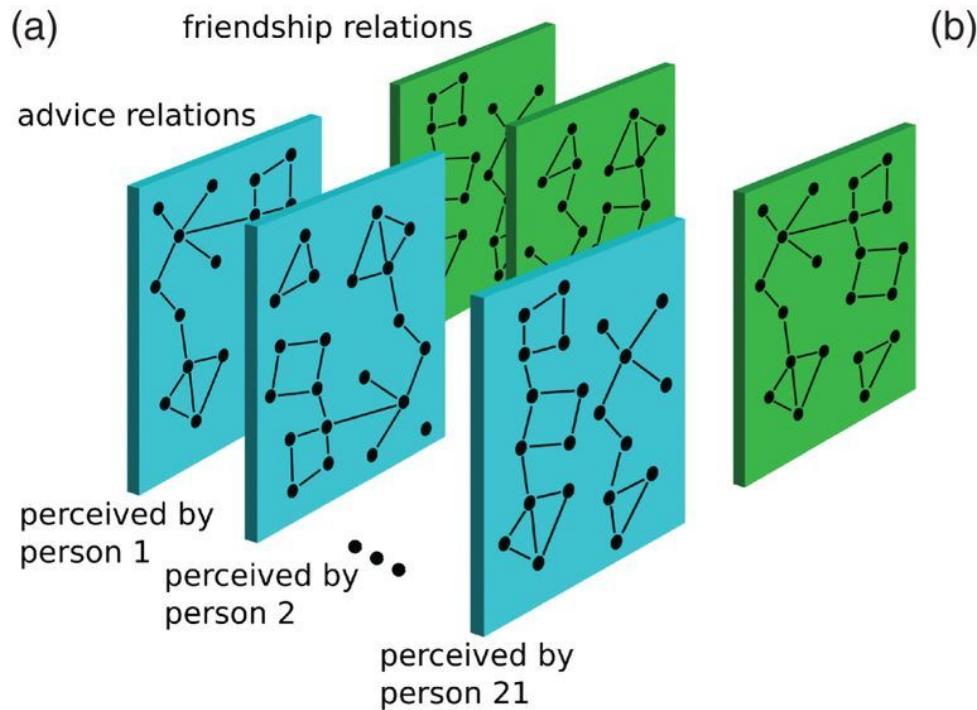


I. Multilayer networks

General problem

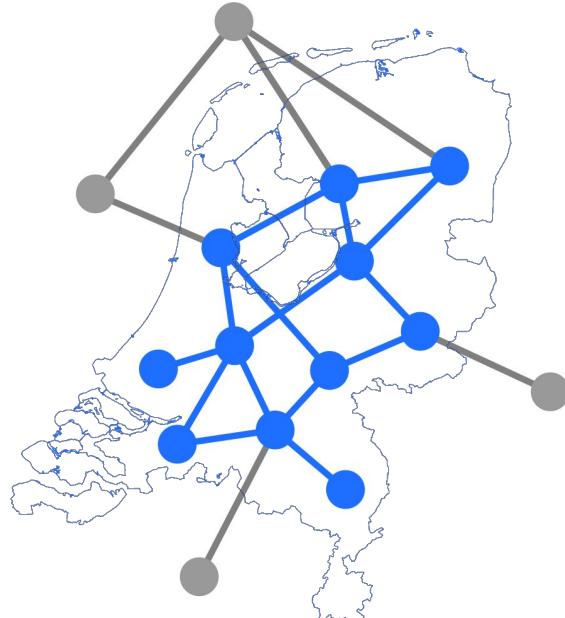


Node alignment and supra-adjacency matrix



I. The **POPNET** data

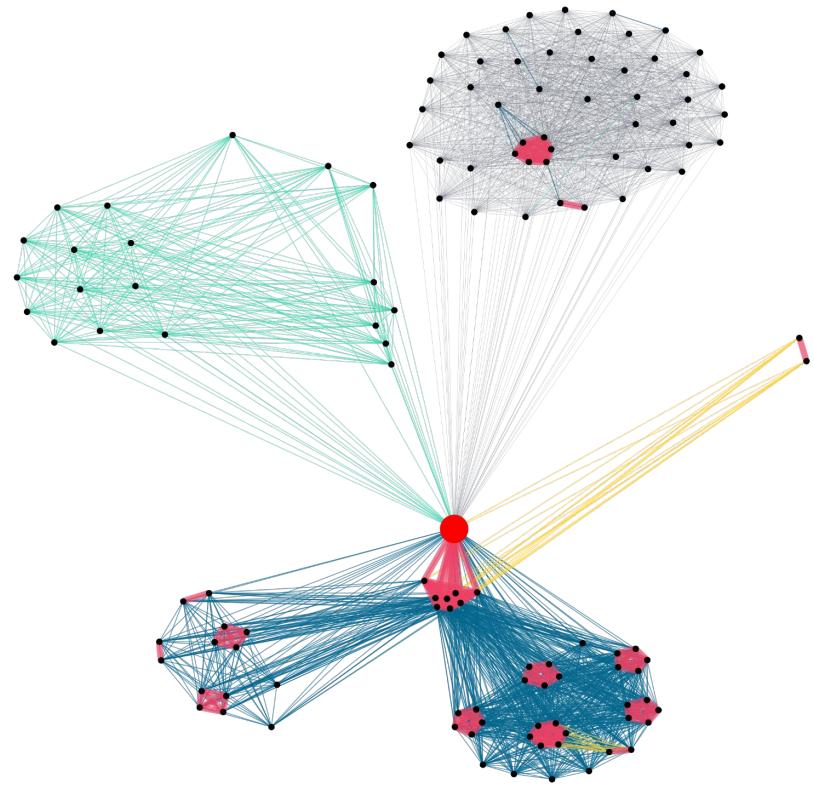
Nodes



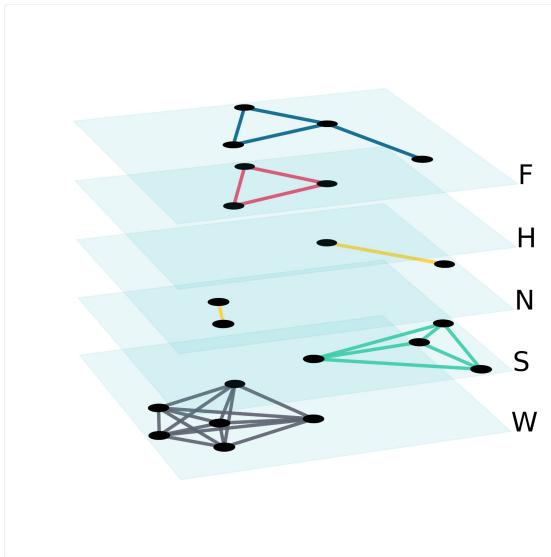
- ~17M people (nodes)
- geography-induced boundary
- various node attributes (age, city / neighborhood, education level, household income, ethnicity, and gender)

Edges

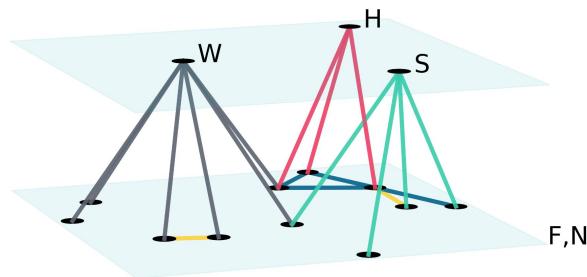
- **Close family and extended family:** directed parent relationships and inferred other family relations
- **Households:** people registered at the same address
- **Next-door neighbors:** links to people in ten closest households
- **Work:** co-workers employed at same organization, large workplaces sampled to the 100 closest colleagues
- **School:** classmates at primary school, high school, special, applied and higher education



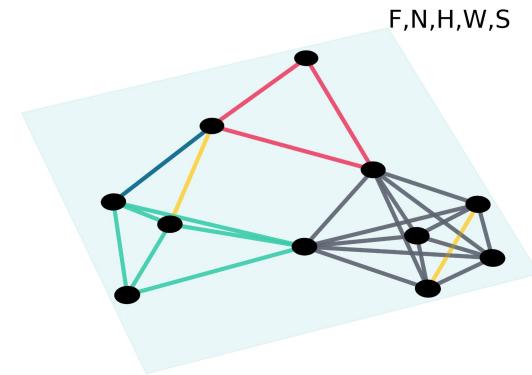
Different viewpoints for the same data



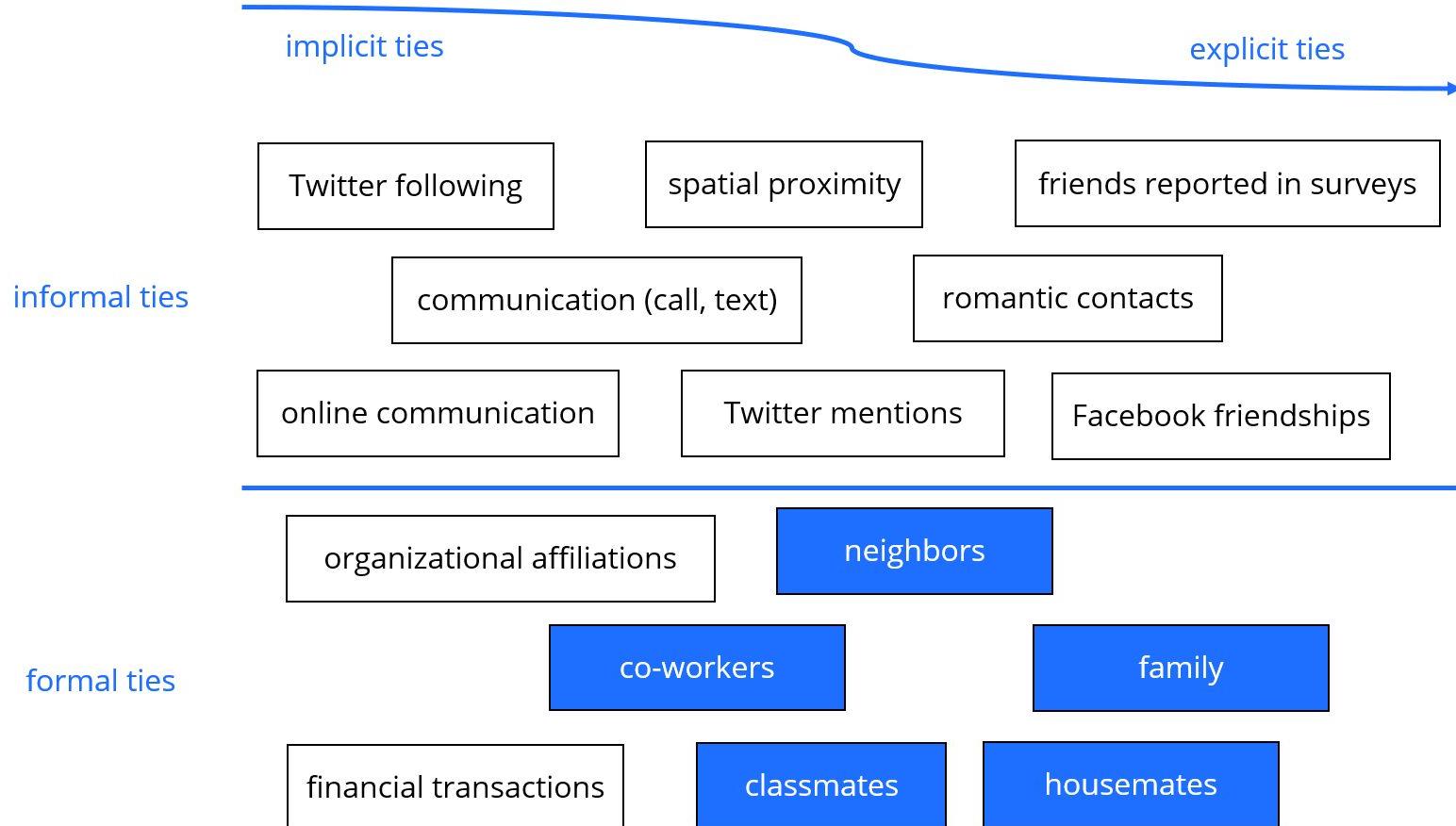
Type 1: node-aligned multilayer network



Type 2: almost bipartite view

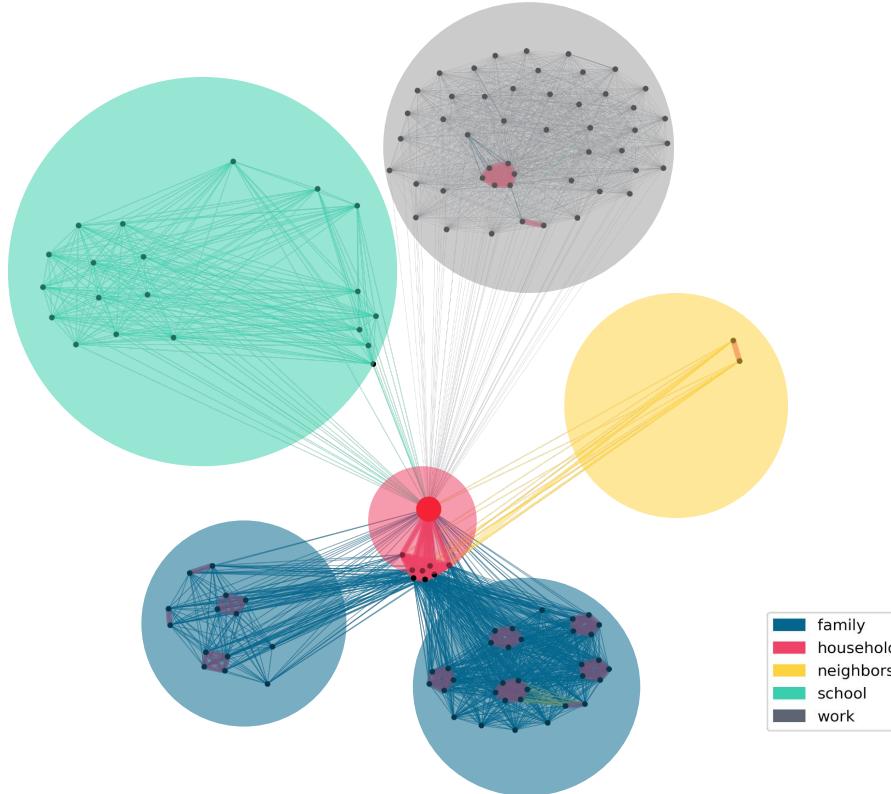


Type 3: projection
“flattened” network



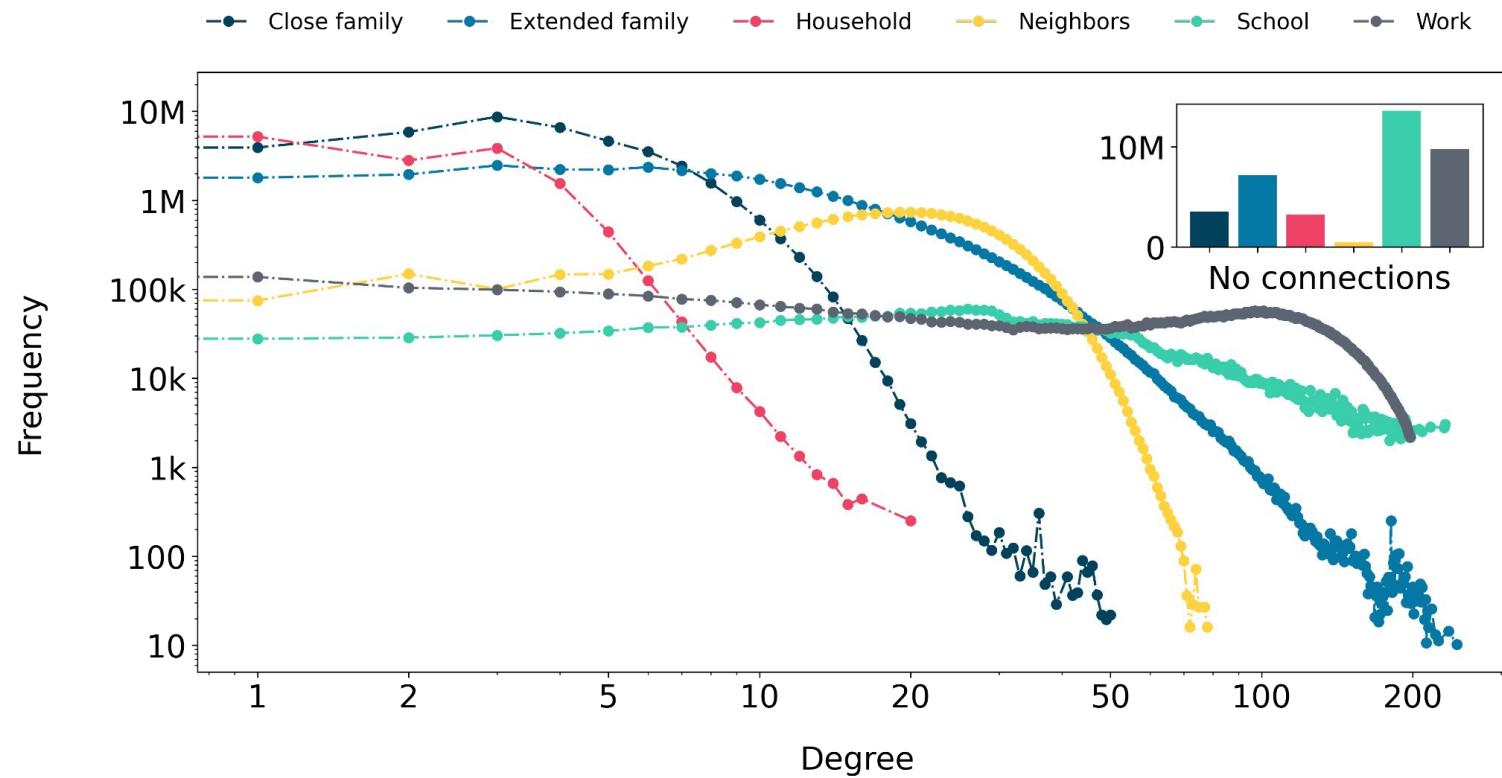
Opportunity structures

a possible interpretation



II. Degree

Degree distribution



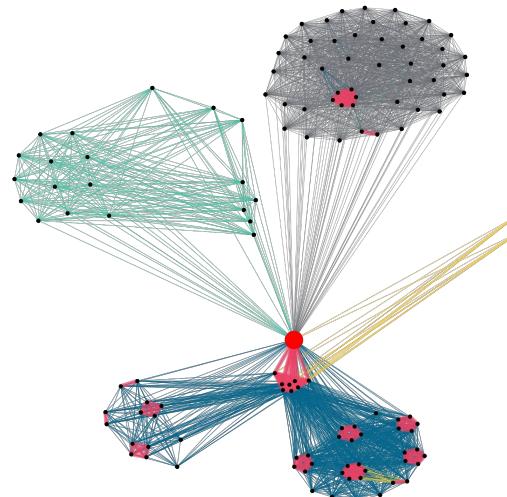
Degree assortativity

	C	E	H	N	S	W
C	1.00	0.53	0.12	0.05	-0.12	0.11
E		1.00	0.07	0.02	-0.02	0.10
H			1.00	0.07	0.10	-0.01
N				1.00	0.04	0.07
S					1.00	-0.04
W						1.00

III. Clustering

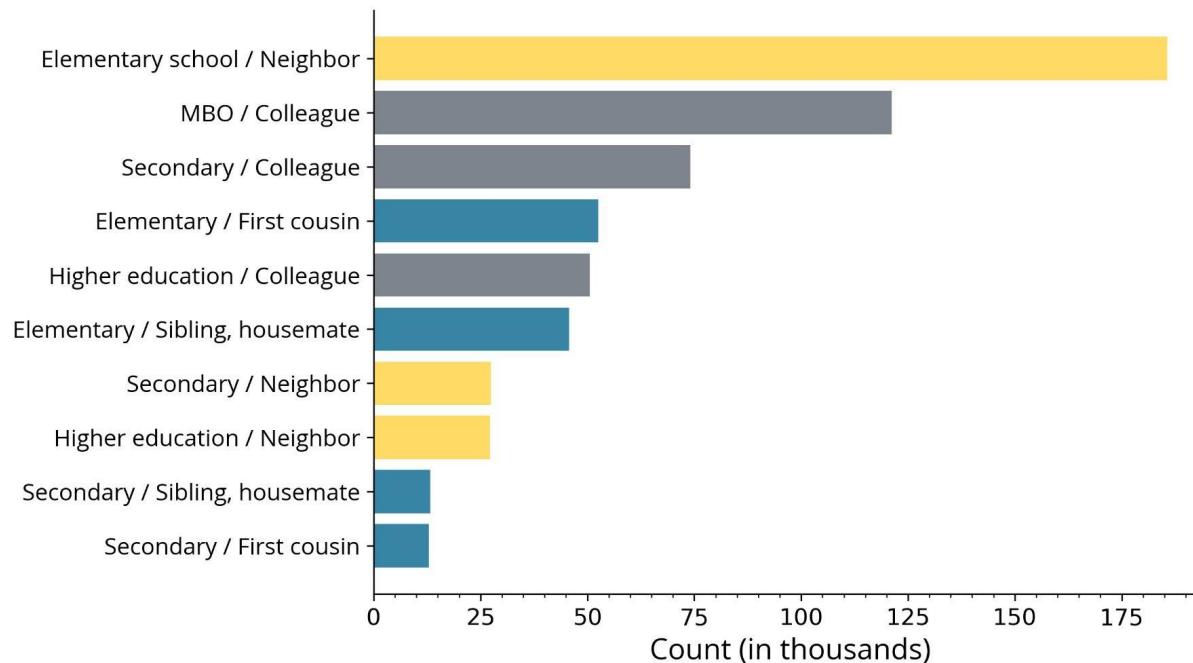
Local clustering coefficient

Network	avg(CC)
Google+	0.048
LiveJournal	0.117
YouTube	0.006
Hyves	0.18
Facebook	0.16
CyWorld	0.16
POPNET	0.40



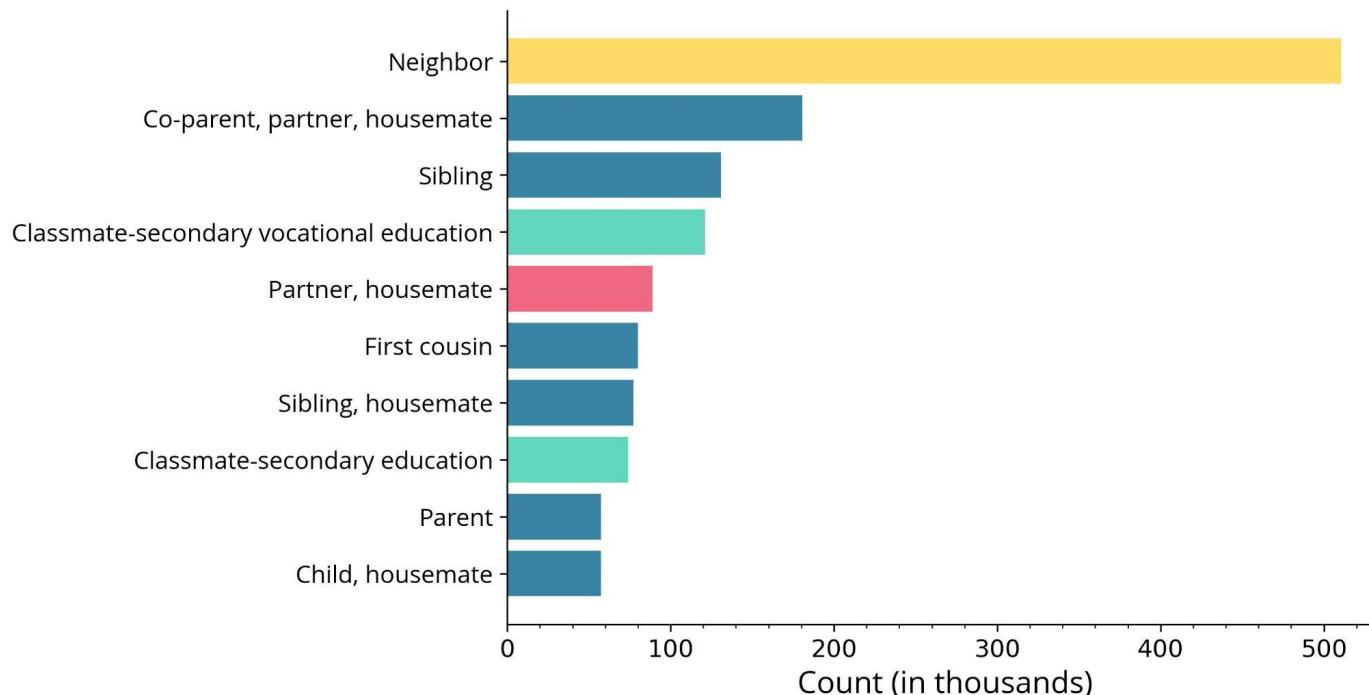
Edges in multiple layers

- Who do people tend to go to **school** with?



Edges in multiple layers

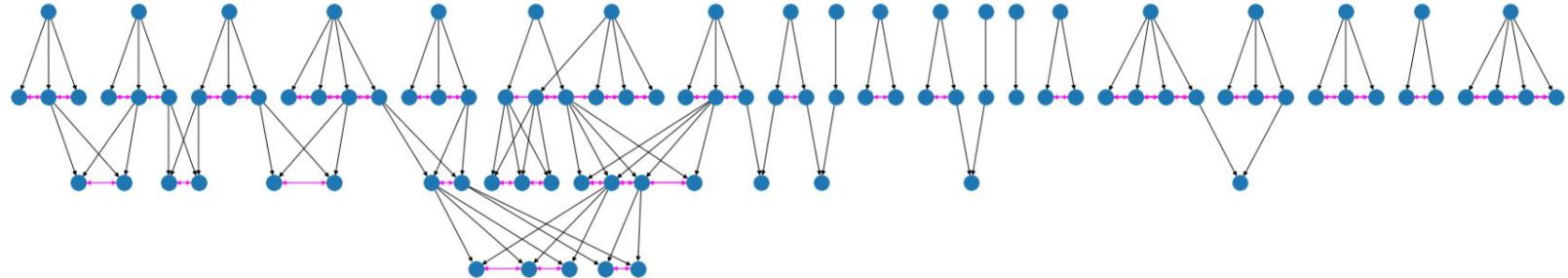
- Who do people tend to **work** with?



IV. Dummy network

Dummy data

1. creating a 4-generation family tree
2. filling it up with different relationships

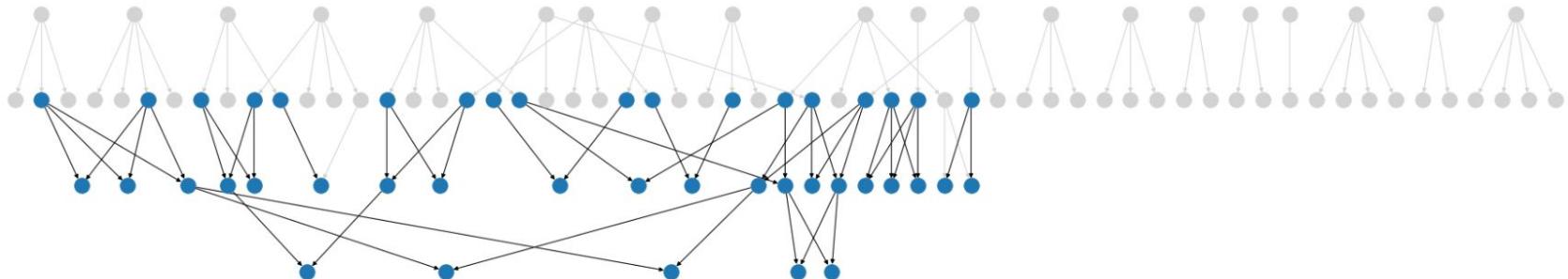


Family structure

- parent
- child
- partner
- grandparent
- grandchild
- sibling
- cousin
- niece / nephew
- aunt / uncle
- cousin

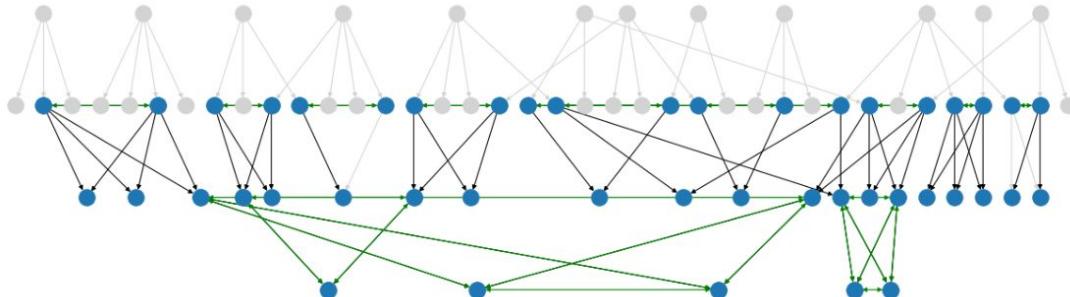
Dummy data

1. creating a 4-generation family tree
2. filling it up with different relationships
3. removing those who “died”

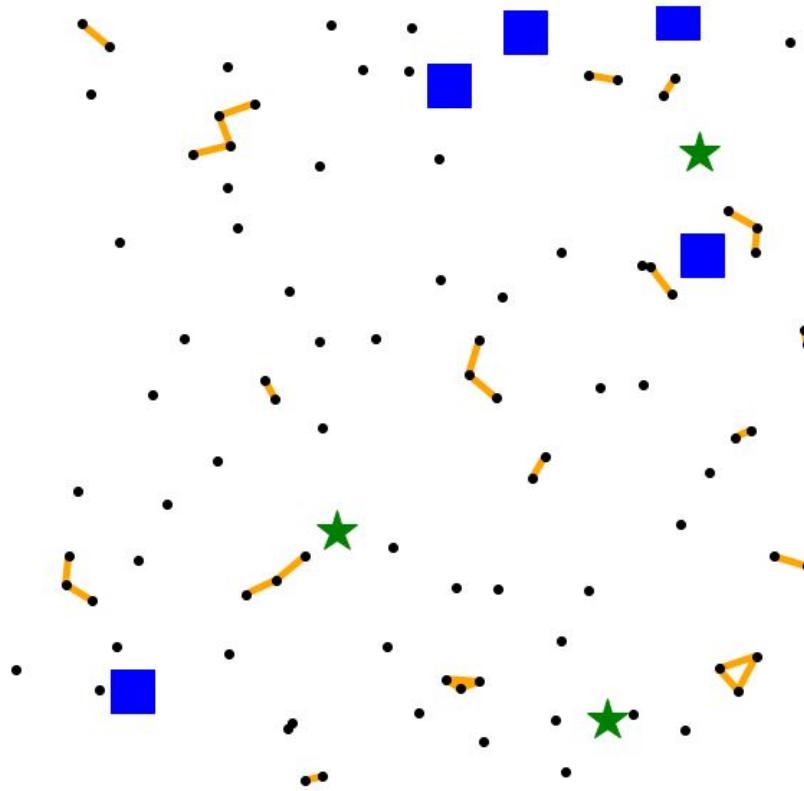


Dummy data

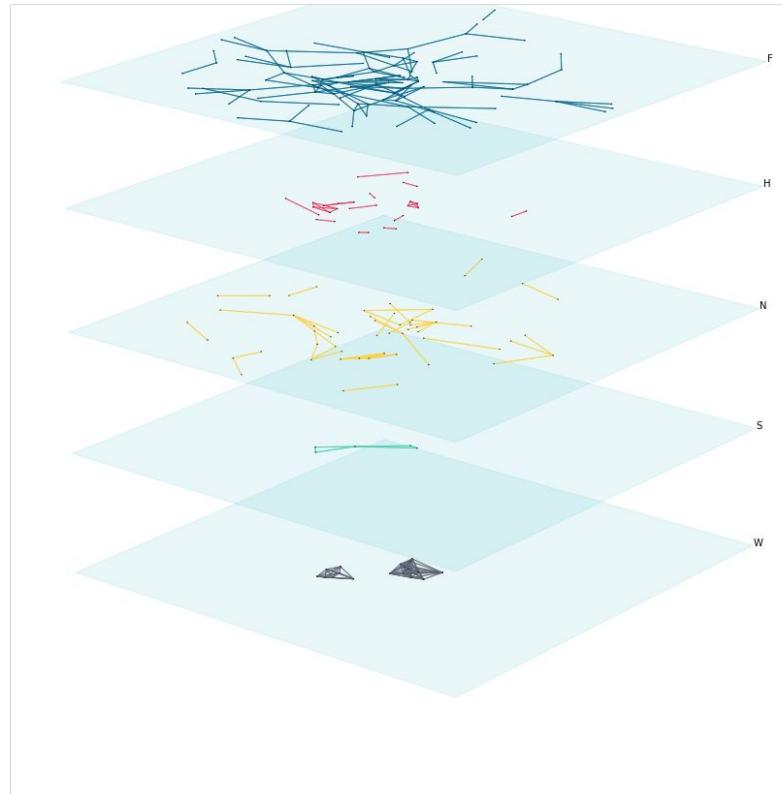
1. creating a 4-generation family tree
2. filling it up with different relationships
3. removing those who “died”
4. arranging households



Neighbor, school, workplace

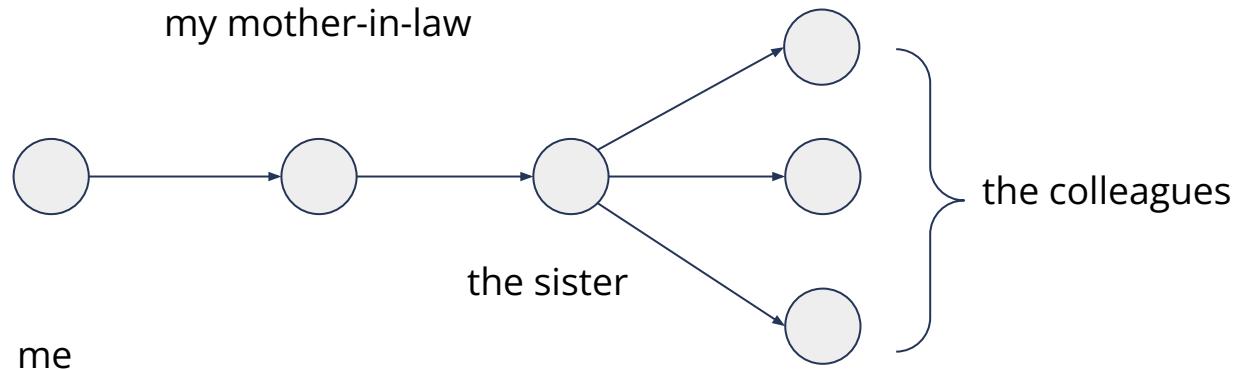


Multilayer network



V. Multilayer walks

A guy I met at my mother-in-law's sister's workplace...



Matrices

$$MiL = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sister = $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$

Colleagues = $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 \end{pmatrix}$

multiplication multiplication

The diagram illustrates the calculation of the mother-in-law of node 0. It shows three matrices: MiL, Sister, and Colleagues. MiL is a 6x6 identity matrix. Sister is a 6x6 matrix where the 5th column contains ones and all other columns are zero. Colleagues is a 6x6 matrix where the 6th column contains ones and all other columns are zero. Arrows labeled 'multiplication' point from MiL to Sister, and from Sister to Colleagues. The result of the first multiplication is highlighted in blue, and the result of the second multiplication is highlighted in yellow.

node 5 is the sister of
the mother-in-law of
node 0!

nodes 1, 3, and 4 are the
colleagues of the sister of the
mother-in-law of node 0!

VI. Bipartite projections

School example

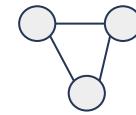
$[(101, 0), (102, 0), (103, 2), (104, 2), (105, 0)]$

↑
node_id of child

school_id

101,102, and 105 and

103 and 104 go to the same school



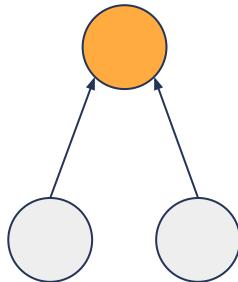
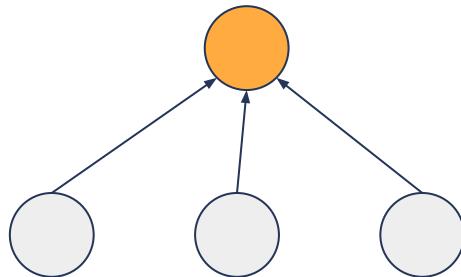
With matrices

$S =$

	School 0	School 1	School 2
Node 101	1	0	0
Node 102	1	0	0
Node 103	0	0	1
Node 104	0	0	1
Node 105	1	0	0

school

child



Length-2 walk

$$S = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

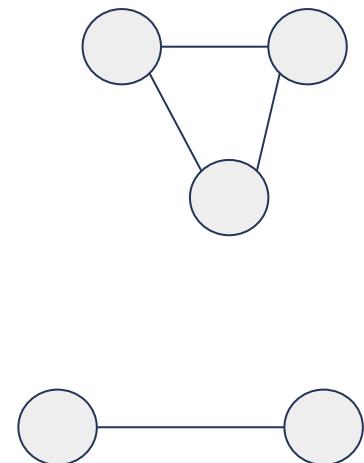
child -> school

$$S^T = \begin{pmatrix} 1 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \end{pmatrix}$$

school -> child

Length-2 walk

$$S \cdot S^T = \begin{pmatrix} \textcolor{blue}{\times} & 1 & 0 & 0 & 1 \\ 1 & \textcolor{blue}{\times} & 0 & 0 & 1 \\ 0 & 0 & \textcolor{blue}{\times} & 1 & 0 \\ 0 & 0 & 1 & \textcolor{blue}{\times} & 0 \\ 1 & 1 & 0 & 0 & \textcolor{blue}{\times} \end{pmatrix} \longrightarrow$$



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POPNET project

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