An FST generates a descendant sequence given an ancestral one. Conditional probability that sequence  $\mathcal{Y}$  evolved from  $\mathcal{X}$ .

 $\chi \xrightarrow{\Delta T} y$  $\mathcal{P}(\mathcal{Y} \mid \mathcal{X})$ Composition operation

 $\mathcal{P}(\mathcal{Z} \mid \mathcal{X}) = \sum_{\mathcal{Y}} \mathcal{P}(\mathcal{Z} \mid \mathcal{Y}) \mathcal{P}(\mathcal{Y} \mid \mathcal{X}) \quad \mathcal{X} \xrightarrow{\Delta T} \forall \mathcal{Y} \xrightarrow{\Delta T} \mathcal{Z}$