

# Lab 1

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1/4/2022

## About me



# Purpose of labs

- ▶ Facilitate learning theoretical concepts covered in lecture
- ▶ Answer questions about homework
- ▶ Review for midterms and the final
- ▶ Implement statistical analyses from lecture in RStudio

# Lab 1 Outline

- ▶ Cover preliminary statistics and probability concepts
- ▶ Intro to R and setup

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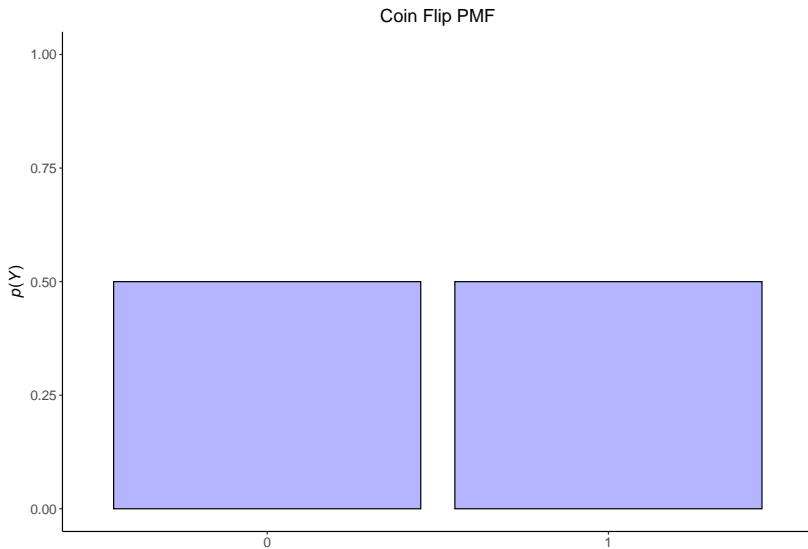
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- ▶ Denote the outcome of a coin flip as  $Y$ 
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  - ▶  $p(Y=1) = 0.5$

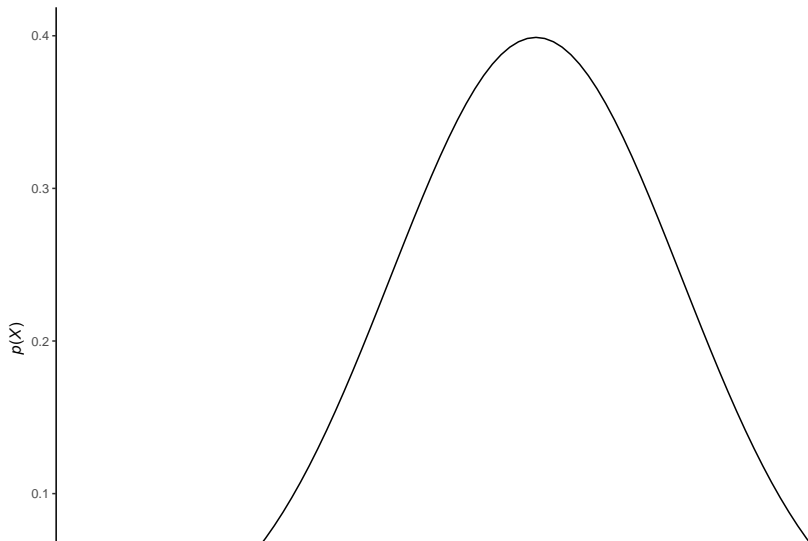
# Probability distribution

- ▶ Probability **mass** function (PMF)
  - ▶ Assigns probabilities to individual values of a *discrete* random variable



## Probability distribution

- ▶ Probability **density** function (PDF)
  - ▶ Similar to a PMF, but instead specifies the probability that a *continuous* variable takes on a range of values.



## Expected value

- ▶ The expected value of a random variable  $Y$  is denoted as  $E(Y)$ .
  - ▶ Probability weighted average of all possible values.

```
y <- c(70,80,85,90,100)
p.y <- c(0.18,0.34,0.35,0.11,0.02)

E.y <- sum(y*p.y)
E.y

## [1] 81.45
```

# Variance

- ▶ A measure of how disperse all possible values of a random variable are from the expected value (i.e. population or sample mean)

```
sum(p.y*y^2) - E.y^2
```

```
## [1] 43.6475
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- ▶ You might notice that this result is different than what the `var()` function outputs, but that is because the function computes an estimator of the population variance (i.e.,  $s^2$ )