Supplemental Material: Base Diagnostics

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Chapter 1

Introduction

This is the supplemental material for experiments with basic diagnostics.

1.1 About our supplemental material

This supplemental material is hosted on GitHub using GitHub pages. The source code and configuration files used to generate this supplemental material can be found in this GitHub repository. We compiled our data analyses and supplemental documentation into this nifty web-accessible book using bookdown.

Our supplemental material includes the following paper figures and statistics:

- Exploitation rate results (Section 2)
- Ordered exploitation results (Section 3)
- Contradictory objectives results (Section 4)
- Multi-path exploration results (Section 5)

1.2 Contributing authors

- Jose Guadalupe Hernandez
- Alexander Lalejini
- Charles Ofria

1.3 Computer Setup

These analyses were conducted in the following computing environment:

print(version)

##

```
## platform
                  x86_64-pc-linux-gnu
                  x86_64
## arch
## os
                  linux-gnu
## system
                  x86_64, linux-gnu
## status
## major
## minor
                  3.1
                  2023
## year
                  06
## month
## day
                  16
## svn rev
                 84548
## language
                 R
## version.string R version 4.3.1 (2023-06-16)
## nickname
                  Beagle Scouts
```

1.4 Experimental setup

Setting up required variables variables.

```
# libraries we are using
library(ggplot2)
library(cowplot)
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(PupillometryR)
## Loading required package: rlang
# data diractory for gh-pages
DATA_DIR = '/opt/ECJ-2023-Suite-Of-Diagnostic-Metrics-For-Characterizing-Selection-School
# data diractory for local testing
{\tt\#\ DATA\_DIR\ =\ '``/Desktop/Repositories/ECJ-2023-Suite-Of-Diagnostic-Metrics-For-Characte}
# graph variables
SHAPE = c(5,3,1,2,6,0,4,20,1)
cb_palette <- c('#332288','#88CCEE','#EE7733','#EE3377','#117733','#882255','#44AA99',
```

```
TSIZE = 20
p_theme <- theme(</pre>
  text = element_text(size = 18),
  plot.title = element_text( face = "bold", size = 20, hjust=0.5),
  panel.border = element_blank(),
  panel.grid.minor = element_blank(),
  legend.title=element_text(size=12),
  legend.text=element_text(size=12),
  axis.title = element_text(size=18),
  axis.text = element_text(size=18),
  legend.position="bottom",
  panel.background = element_rect(fill = "#f1f2f5",
                                  colour = "white",
                                  linewidth = 0.5, linetype = "solid")
)
# colors for streak plots
STK_SHAPE = c(2,6,0,4,20,1)
stk_cb_palette <- c('#EE3377','#117733','#882255','#44AA99','#CCBB44', '#000000')
# default variables
DIMENSIONALITY = 100
GENERATIONS = 50000
# selection scheme related stuff
ACRO = c('tru','tor','lex','gfs','pfs','nds','nov','ran')
NAMES = c('Truncation (tru)', 'Tournament (tor)', 'Lexicase (lex)', 'Genotypic Fitness Sharing (gfs
```

Chapter 2

Exploitation rate results

Here we present the results for **best performances** found by each selection scheme on the exploitation rate diagnostic. 50 replicates are conducted for each scheme explored.

2.1 Data setup

```
DIR = paste(DATA_DIR, 'EXPLOITATION_RATE/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR, 'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

best_df <- read.csv(paste(DIR, 'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

best_df$acro <- factor(best_df$acro, levels = ACRO)

sati_df <- read.csv(paste(DIR, 'sol-fnd.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

sati_df$acro <- factor(sati_df$acro, levels = ACRO)
```

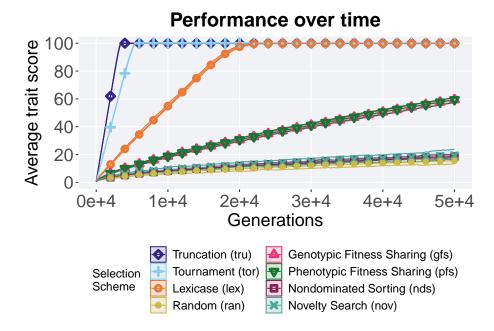
2.2 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
```

```
max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
 ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Performance over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```



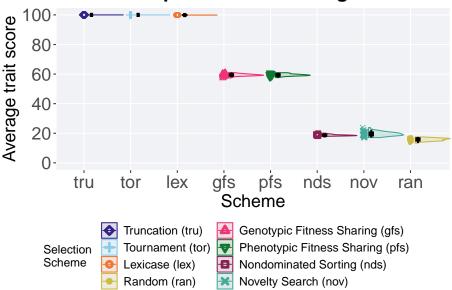
2.3 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100.1),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Best performance throughout



2.3.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('tru','tor','lex','gfs','pfs','sperformance %>%
    group_by(acro) %>%
    dplyr::summarise(
        count = n(),
        na_cnt = sum(is.na(val)),
        min = min(val / DIMENSIONALITY, na.rm = TRUE),
        median = median(val / DIMENSIONALITY, na.rm = TRUE),
        mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
        max = max(val / DIMENSIONALITY, na.rm = TRUE),
        IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
```

<fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <

min median mean

A tibble: 8 x 8

acro count na_cnt

##

IQR

<dbl>

max

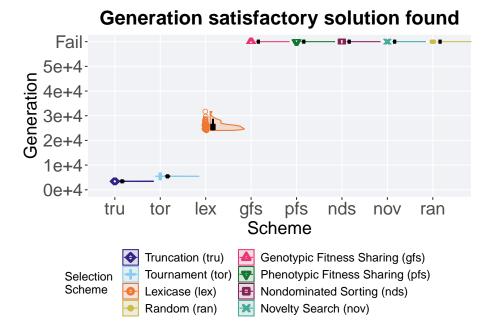
```
## 1 tru
              50
                      0 100
                               100
                                     100
                                           100
                                                 0
## 2 tor
              50
                      0 100
                               100
                                     100
                                           100
## 3 lex
              50
                      0 99.9
                                99.9 99.9 99.9 0.0154
## 4 gfs
              50
                      0 57.3
                                59.3 59.4 61.1 0.984
## 5 pfs
              50
                      0 57.6
                                59.4 59.5
                                            61.0 1.02
## 6 nov
              50
                      0 17.1
                                19.5 19.5
                                            23.9 1.95
## 7 nds
              50
                      0 18.0
                                18.6 18.7
                                            20.1 0.603
## 8 ran
              50
                      0 13.4
                                15.9 15.8 17.5 1.46
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = performance)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 385.26, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: performance$val and performance$acro
##
##
       tru
              tor
                     lex
                            gfs
                                   pfs
                                                 nds
                                          nov
## tor 1.000 -
## lex <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 -
## pfs <2e-16 <2e-16 <2e-16 1.000
## nov <2e-16 <2e-16 <2e-16 <2e-16 -
## nds <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 0.018
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <2e-16
```

2.4 Generation satisfactory solution found

P value adjustment method: bonferroni

First generation a satisfactory solution is found throughout the 50,000 generations.

```
plot = sati_df %>%
  ggplot(., aes(x = acro, y = gen , color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = '
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha
  scale_y_continuous(
    name="Generation",
   limits=c(0, 60001),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000, 60000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4", "Fail")
  scale x discrete(
   name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Generation satisfactory solution found')+
  p_theme
plot_grid(
  plot +
   theme(legend.position="none"),
 legend,
 nrow=2,
 rel_heights = c(3,1)
```



2.4.1 Stats

Summary statistics for the generation a satisfactory solution is found.

```
ssf = filter(sati_df, gen <= GENERATIONS)
ssf$acro = factor(ssf$acro, levels = c('tru','tor','lex'))
ssf %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(gen)),
    min = min(gen, na.rm = TRUE),
    median = median(gen, na.rm = TRUE),
    mean = mean(gen, na.rm = TRUE),
    max = max(gen, na.rm = TRUE),
    IQR = IQR(gen, na.rm = TRUE)
)
```

```
## # A tibble: 3 x 8
     acro count na_cnt
                           min median
                                                        IQR
                                         mean
                                                 max
     <fct> <int>
                   <int> <int>
                                 <dbl>
                                        <dbl> <int>
                                                      <dbl>
## 1 tru
              50
                          3392
                                 3422
                                        3423.
                                                3475
                                                       26
## 2 tor
              50
                                5444.
                       0
                          5390
                                        5447.
                                                5509
                                                       43.2
## 3 lex
                       0 24036 25626. 25883. 31709 1739.
```

Kruskal-Wallis test illustrates evidence of statistical differences.

```
kruskal.test(gen ~ acro, data = ssf)
##
##
   Kruskal-Wallis rank sum test
##
## data: gen by acro
## Kruskal-Wallis chi-squared = 132.46, df = 2, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = ssf$gen, g = ssf$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = 'g')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: ssf$gen and ssf$acro
##
##
       tru
              tor
## tor <2e-16 -
## lex <2e-16 <2e-16
## P value adjustment method: bonferroni
```

Chapter 3

Ordered exploitation results

Here we present the results for **best performances** found by each selection scheme on the ordered exploitation diagnostic. 50 replicates are conducted for each scheme explored.

3.1 Data setup

```
DIR = paste(DATA_DIR,'ORDERED_EXPLOITATION/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

best_df <- read.csv(paste(DIR,'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFact

best_df$acro <- factor(best_df$acro, levels = ACRO)

sati_df <- read.csv(paste(DIR,'sol-fnd.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFact

sati_df$acro <- factor(sati_df$acro, levels = ACRO)
```

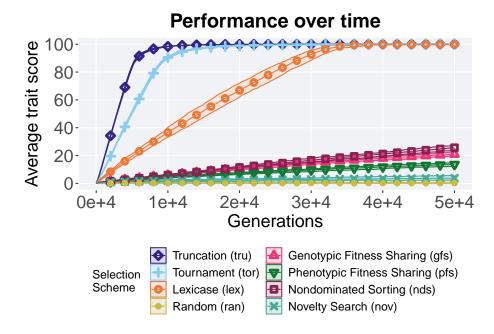
3.2 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
```

```
max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
 ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Performance over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```



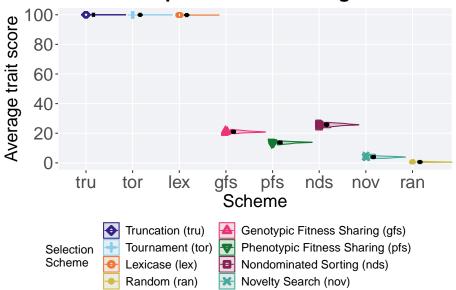
3.3 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Best performance throughout



3.3.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('tru','tor','lex','nds','gfs',')
performance %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val / DIMENSIONALITY, na.rm = TRUE),
    median = median(val / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
    max = max(val / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
```

```
## # A tibble: 8 x 8
##
     acro count na_cnt
                            min median
                                                            IQR
                                           mean
                                                    max
                          <dbl>
                                  <dbl>
                                                          <dbl>
     <fct> <int> <int>
                                           <dbl> <dbl>
## 1 tru
              50
                      0 100.
                                100.
                                         100.
                                                 100.
                                                        0.00168
## 2 tor
              50
                      0 99.9
                                 99.9
                                         99.9
                                                  99.9 0.00650
## 3 lex
              50
                      0 99.7
                                 99.8
                                          99.8
                                                  99.9 0.0247
## 4 nds
              50
                      0 23.7
                                 25.7
                                                  27.3 0.972
                                          25.7
## 5 gfs
              50
                      0 19.7
                                 21.0
                                          21.0
                                                  22.6 0.754
## 6 pfs
              50
                      0 12.2
                                 13.8
                                          13.7
                                                  14.9 0.712
## 7 nov
              50
                          3.00
                                  3.90
                                           4.00
                                                   5.83 0.666
                      0
## 8 ran
              50
                          0.318
                                  0.569
                                           0.605
                                                   1.31 0.279
```

Kruskal–Wallis test illustrates evidence of statistical differences.

kruskal.test(val ~ acro, data = performance)

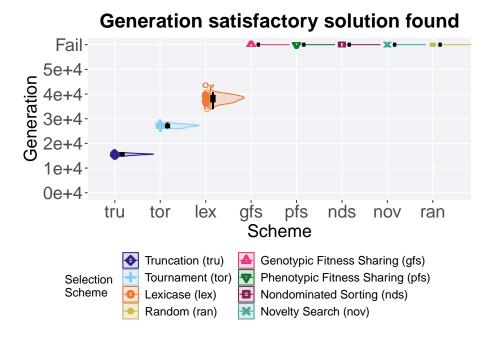
Pairwise comparisons using Wilcoxon rank sum test with continuity correction

```
## data: performance$val and performance$acro
##
##
      tru
             tor
                   lex
                         nds
                                gfs
                                      pfs
                                             nov
## tor <2e-16 -
## lex <2e-16 <2e-16 -
## nds <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 <2e-16 -
## pfs <2e-16 <2e-16 <2e-16 <2e-16 -
## nov <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <2e-16
## P value adjustment method: bonferroni
```

3.4 Generation satisfactory solution found

First generation a satisfactory solution is found throughout the 50,000 generations.

```
plot = sati_df %>%
  ggplot(., aes(x = acro, y = gen , color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = '
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha
  scale_y_continuous(
    name="Generation",
   limits=c(0, 60001),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000, 60000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4", "Fail")
  scale x discrete(
   name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Generation satisfactory solution found')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
 rel_heights = c(3,1)
```



3.4.1 Stats

Summary statistics for the generation a satisfactory solution is found.

```
ssf = filter(sati_df, gen <= GENERATIONS)
ssf$acro = factor(ssf$acro, levels = c('tru','tor','lex'))
ssf %>%
group_by(acro) %>%
dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(gen)),
   min = min(gen, na.rm = TRUE),
   median = median(gen, na.rm = TRUE),
   mean = mean(gen, na.rm = TRUE),
   max = max(gen, na.rm = TRUE),
   IQR = IQR(gen, na.rm = TRUE)
)
```

```
## # A tibble: 3 x 8
     acro count na_cnt
                          min median
                                                     IQR
                                       mean
     <fct> <int>
                  <int> <int>
                               <dbl>
                                      <dbl> <int> <dbl>
## 1 tru
              50
                      0 14776 15585 15570. 16317
## 2 tor
              50
                                     27105. 28495
                      0 25996 27138
                                                    913.
## 3 lex
                      0 33877 38288. 38265. 43565 2215.
```

Kruskal-Wallis test illustrates evidence of statistical differences.

```
kruskal.test(gen ~ acro, data = ssf)
##
##
   Kruskal-Wallis rank sum test
##
## data: gen by acro
## Kruskal-Wallis chi-squared = 132.45, df = 2, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = ssf$gen, g = ssf$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = 'g')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: ssf$gen and ssf$acro
##
##
       tru
              tor
## tor <2e-16 -
## lex <2e-16 <2e-16
## P value adjustment method: bonferroni
```

3.5 Streaks over time

Longest streak of active geens for the best solution found in a population over time. A maximum streak value of 100 and a minimum streak value of 1 is possible. Data points on the graph is the average streak across 50 replicates every 2000 generations. Shading comes from the best and worse streak across 50 replicates.

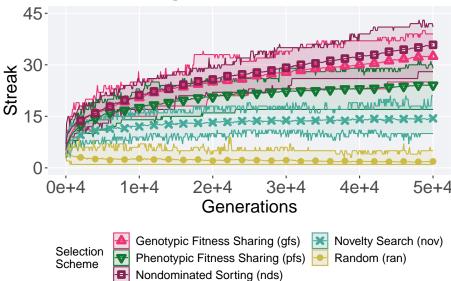
```
lines = filter(over_time_df, acro != 'tor' & acro != 'tru' & acro != 'lex') %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(ele_stk_cnt),
   mean = mean(ele_stk_cnt),
   max = max(ele_stk_cnt))
```

`summarise()` has grouped output by 'scheme'. You can override using the
`.groups` argument.

```
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
```

```
scale_y_continuous(
    name="Streak",
   limits=c(0, 45),
   breaks=seq(0,45, 15)
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
    labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=STK_SHAPE)+
  scale_colour_manual(values = stk_cb_palette) +
  scale_fill_manual(values = stk_cb_palette) +
  ggtitle('Longest streak over time')+
  p_theme +
  guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```

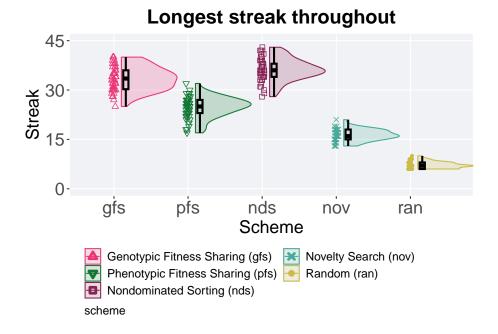
Longest streak over time



3.6 Longest streak throughout

Longest streak of the best solution found in the population throughout 50,000 generations.

```
plot = filter(best_df, var == 'ele_stk_cnt' & acro != 'tor' & acro != 'tru' & acro !=
  ggplot(., aes(x = acro, y = val, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = '
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha
  scale_y_continuous(
    name="Streak",
   limits=c(0, 45),
    breaks=seq(0,45,15)
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=STK_SHAPE)+
  scale_colour_manual(values = stk_cb_palette) +
  scale_fill_manual(values = stk_cb_palette) +
  ggtitle('Longest streak throughout')+
  p_theme + theme(legend.title=element_blank())
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
 nrow=2,
  rel_heights = c(3,1)
```



3.6.1 Stats

2 gfs

3 pfs

4 nov

Summary statistics for the longest streak

50

50

50

0

0

25

17

13

33.5 33.4

24.8

16.3

25

16

```
streak = filter(best_df, var == 'ele_stk_cnt' & acro != 'tor' & acro != 'tru' & acro != 'lex')
streak$acro = factor(streak$acro, levels = c('nds','gfs','pfs','nov','ran'))
streak %>%
  group_by(acro) %>%
  dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(val)),
   min = min(val, na.rm = TRUE),
   median = median(val, na.rm = TRUE),
   mean = mean(val, na.rm = TRUE),
   max = max(val, na.rm = TRUE),
    IQR = IQR(val, na.rm = TRUE)
 )
## # A tibble: 5 x 8
     acro count na_cnt
                                                   IQR
                          min median mean
     <fct> <int> <int> <dbl>
                               <dbl> <dbl> <dbl> <dbl> <
## 1 nds
              50
                      0
                           28
                                36
                                     36.2
                                              43 4
```

40 5.75

32 4

21 3

```
## 5 ran
              50
                             6
                                  7
                                       7.18
                                                10 2
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = streak)
##
##
   Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 226.43, df = 4, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = streak$val, g = streak$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: streak$val and streak$acro
##
##
       nds
                       pfs
               gfs
                                nov
## gfs 0.0017 -
## pfs < 2e-16 2.7e-15 -
## nov < 2e-16 < 2e-16 3.1e-16 -
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16
##
## P value adjustment method: bonferroni
```

Chapter 4

Contradictory objectives results

Here we present the results for activation gene coverage and satisfactory trait coverage found by each selection scheme on the contradictory objectives diagnostic. 50 replicates are conducted for each scheme explored.

4.1 Data setup

```
DIR = paste(DATA_DIR,'CONTRADICTORY_OBJECTIVES/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$cover_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

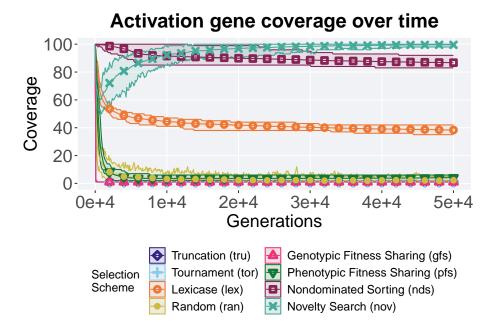
over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)
```

4.2 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(uni_str_pos),
    mean = mean(uni_str_pos),
    max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
 scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale\_shape\_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Activation gene coverage over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
   fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```



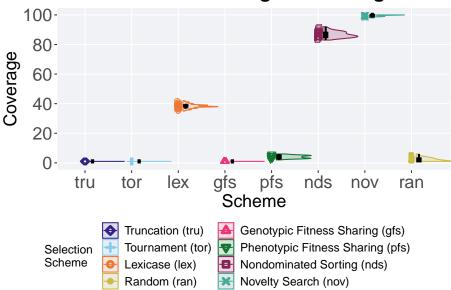
4.3 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100.1),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Final activation gene coverage



4.3.1 Stats

Summary statistics for the coverage found in the final population.

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','nds','lex','pfs','ran'
act_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
    min = min(uni_str_pos, na.rm = TRUE),
    median = median(uni_str_pos, na.rm = TRUE),
    mean = mean(uni_str_pos, na.rm = TRUE),
    max = max(uni_str_pos, na.rm = TRUE),
    IQR = IQR(uni_str_pos, na.rm = TRUE)
```

```
## # A tibble: 8 x 8
##
     acro count na_cnt
                          min median mean
                                                   IQR
                                             max
     <fct> <int> <int> <dbl> <dbl> <int> <dbl>
## 1 nov
              50
                      0
                           98
                                 100 99.6
                                             100
                                                     1
## 2 nds
              50
                      0
                           83
                                  86 86.7
                                              92
                                                     3
## 3 lex
              50
                      0
                           35
                                  38 38.3
                                              42
                                                     1
              50
                            2
                                                     2
## 4 pfs
                      0
                                   4 4.12
                                               6
## 5 ran
              50
                      0
                                   2 2.22
                                               6
                                                     2
                            1
## 6 gfs
              50
                      0
                            1
                                   1
                                     1
                                               1
## 7 tor
              50
                                                     0
                      0
                            1
                                   1 1
                                               1
## 8 tru
              50
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: uni_str_pos by acro
## Kruskal-Wallis chi-squared = 381.66, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bond")
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               nds
                       lex
                               pfs
                                                gfs tor
                                        ran
## nds < 2e-16 -
## lex < 2e-16 < 2e-16 -
## pfs < 2e-16 < 2e-16 < 2e-16 -
## ran < 2e-16 < 2e-16 < 2e-16 7.1e-09 -
## gfs < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 -
## tor < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 1
## tru < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 1
                                                    1
## P value adjustment method: bonferroni
```

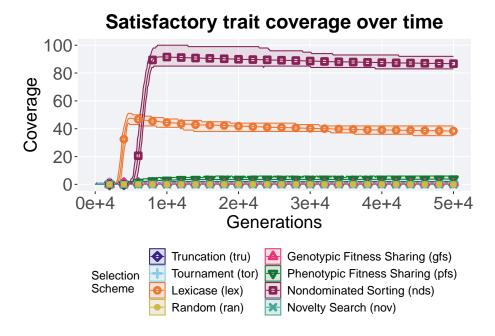
4.4 Satisfactory trait coverage over time

Satisfactory trait coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations.

Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_uni_obj),
    mean = mean(pop_uni_obj),
    max = max(pop_uni_obj)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
 ) +
  scale x continuous(
    name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Satisfactory trait coverage over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```



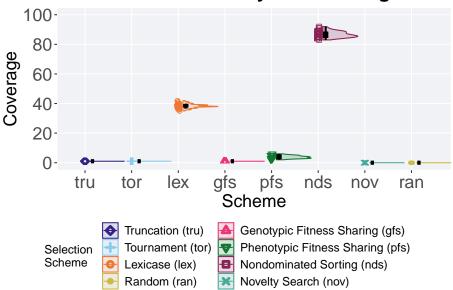
4.5 Final satisfactory trait coverage

Satisfactory trait coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = pop_uni_obj, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(-0.1, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final satisfactory trait coverage')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Final satisfactory trait coverage



4.5.1 Stats

Summary statistics for the coverage found in the final population.

```
sat_coverage = filter(over_time_df, gen == 50000)
sat_coverage$acro = factor(sat_coverage$acro, levels = c('nds','lex','pfs','gfs','tor'
sat_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_uni_obj)),
    min = min(pop_uni_obj, na.rm = TRUE),
    median = median(pop_uni_obj, na.rm = TRUE),
    mean = mean(pop_uni_obj, na.rm = TRUE),
    max = max(pop_uni_obj, na.rm = TRUE),
    IQR = IQR(pop_uni_obj, na.rm = TRUE)
```

```
## # A tibble: 8 x 8
##
    acro count na_cnt
                        min median mean
                                               IQR
                                         max
    <fct> <int> <int> <dbl> <dbl> <int> <dbl>
## 1 nds
            50
                    0
                         83
                               86 86.7
                                          92
## 2 lex
            50
                    0
                         35
                               38 38.3
                                          42
                                                 1
## 3 pfs
            50
                    0
                         2
                                4 3.88
                                           6
                                                 2
## 4 gfs
            50
                                1 1
                    0
                         1
                                           1
## 5 tor
            50
                    0
                         1
                                1 1
                                           1
## 6 tru
            50
                    0
                          1
                                1 1
                                           1
## 7 nov
            50
                    0
                          0
                                0 0
                                           0
                                                 0
## 8 ran
            50
                                0 0
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(pop_uni_obj ~ acro, data = sat_coverage)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: pop_uni_obj by acro
## Kruskal-Wallis chi-squared = 396.63, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = sat_coverage$pop_uni_obj, g = sat_coverage$acro, p.adjust.method = "bond")
                    paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: sat_coverage$pop_uni_obj and sat_coverage$acro
##
##
      nds
             lex
                    pfs
                           gfs
                                  tor
                                         tru
                                                nov
## lex <2e-16 -
## pfs <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 -
## tor <2e-16 <2e-16 1
## tru <2e-16 <2e-16 1
## nov <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 1
##
## P value adjustment method: bonferroni
```

Chapter 5

Multi-path exploration results

Here we present the results for **best performances** and **activation gene coverage** found by each selection scheme on the multi-path exploration diagnostic. 50 replicates are conducted for each scheme explored.

5.1 Data setup

```
DIR = paste(DATA_DIR,'MULTIPATH_EXPLORATION/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$c

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)

best_df <- read.csv(paste(DIR,'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

best_df$acro <- factor(best_df$acro, levels = ACRO)
```

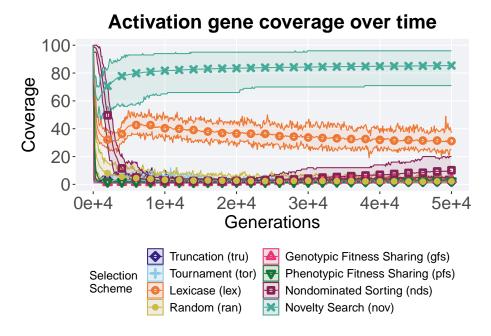
5.2 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(uni_str_pos),
```

```
mean = mean(uni_str_pos),
max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
 ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Activation gene coverage over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```



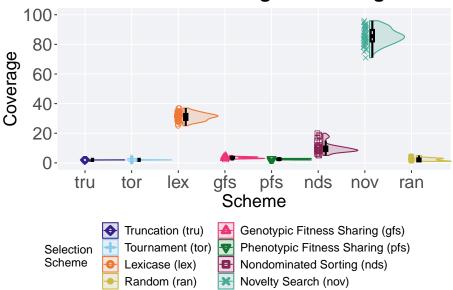
5.3 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Final activation gene coverage



5.3.1 Stats

Summary statistics for the coverage found in the final population.

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','lex','nds','gfs','pfs'
act_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
    min = min(uni_str_pos, na.rm = TRUE),
    median = median(uni_str_pos, na.rm = TRUE),
    mean = mean(uni_str_pos, na.rm = TRUE),
    max = max(uni_str_pos, na.rm = TRUE),
    IQR = IQR(uni_str_pos, na.rm = TRUE)
```

```
## # A tibble: 8 x 8
                          min median mean
##
     acro count na_cnt
                                                   IQR
                                             max
     <fct> <int> <int> <dbl> <dbl> <int> <dbl>
## 1 nov
              50
                      0
                           71
                                85.5 85.4
                                              96 7.75
## 2 lex
              50
                      0
                           25
                                31
                                     31.1
                                              37 4
## 3 nds
              50
                      0
                            5
                                 9
                                     10.2
                                              20
                                                  3
## 4 gfs
                            2
              50
                      0
                                 3
                                      3.48
                                               5 1
## 5 pfs
              50
                      0
                            2
                                 2.5 2.5
                                               3 1
## 6 ran
              50
                      0
                            1
                                 2
                                      2.16
                                               5
                                                  2
## 7 tor
              50
                                 2
                                      2.04
                                               3
                                                  0
                      0
                            1
## 8 tru
              50
                                 2
                                      1.98
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: uni_str_pos by acro
## Kruskal-Wallis chi-squared = 350.25, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bond")
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               lex
                       nds
                                gfs
                                        pfs
                                                ran tor
## lex < 2e-16 -
## nds < 2e-16 < 2e-16 -
## gfs < 2e-16 < 2e-16 < 2e-16 -
## pfs < 2e-16 < 2e-16 < 2e-16 3.6e-10 -
## ran < 2e-16 < 2e-16 < 2e-16 9.4e-08 0.4
## tor < 2e-16 < 2e-16 < 2e-16 < 2e-16 1.2e-05 1.0 -
## tru < 2e-16 < 2e-16 < 2e-16 < 2e-16 1.1e-07 1.0 1.0
## P value adjustment method: bonferroni
```

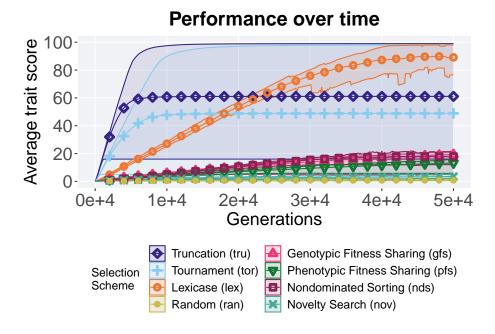
5.4 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes

from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
    max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)',</pre>
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale x continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#1
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117'
  ggtitle('Performance over time')+
 p_theme +
 guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```



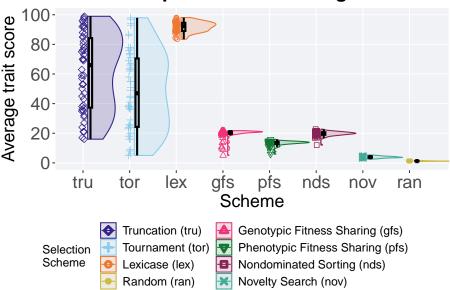
5.5 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Best performance throughout



5.5.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('lex','tru','tor','gfs','nds',')
performance %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val / DIMENSIONALITY, na.rm = TRUE),
    median = median(val / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
    max = max(val / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
```

P value adjustment method: bonferroni

min median mean

92.3 91.9 98.1

<fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>

0 83.4

A tibble: 8 x 8

acro count na_cnt

50

##

1 lex

IQR

5.51

max

```
## 2 tru
              50
                      0 16
                                66.0 61.1 99.0 47.0
## 3 tor
              50
                      0 5
                                47.0 48.9
                                            97.9 46.2
## 4 gfs
             50
                      0 4.99
                                20.7 19.3 21.7
## 5 nds
             50
                      0 12.0
                                19.9 19.7
                                            22.8
                                                   1.72
## 6 pfs
                                13.6 13.2 15.9
             50
                      0 5.87
                                                   1.39
## 7 nov
              50
                      0 2.52
                                 3.83 3.87 5.33 0.793
## 8 ran
              50
                      0 0.865
                                 1.19 1.23 1.72 0.247
Kruskal-Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = performance)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 356.22, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
##
       lex
               tru
                               gfs
                       tor
                                       nds
                                               pfs
                                                       nov
## tru 4.4e-09 -
## tor 1.1e-12 0.33
## gfs < 2e-16 2.3e-13 4.3e-07 -
## nds < 2e-16 1.2e-13 6.8e-07 0.47
## pfs < 2e-16 < 2e-16 5.0e-12 2.3e-11 1.3e-15 -
## nov < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 <
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16
```