Supplemental Material: Base Diagnostics

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Chapter 1

Introduction

This is the supplemental material for experiments with basic diagnostics.

1.1 About our supplemental material

This supplemental material is hosted on GitHub using GitHub pages. The source code and configuration files used to generate this supplemental material can be found in this GitHub repository. We compiled our data analyses and supplemental documentation into this nifty web-accessible book using bookdown.

Our supplemental material includes the following paper figures and statistics:

- Exploitation rate results (Section 2)
- Ordered exploitation results (Section 3)
- Contradictory objectives results (Section 4)
- Multi-path exploration results (Section 5)

1.2 Contributing authors

- Jose Guadalupe Hernandez
- Alexander Lalejini
- Charles Ofria

1.3 Computer Setup

These analyses were conducted in the following computing environment:

print(version)

```
##
                   x86_64-pc-linux-gnu
## platform
                   x86_64
## arch
## os
                   linux-gnu
                   x86_64, linux-gnu
## system
## status
## major
## minor
                   3.1
                   2023
## year
## month
                   06
                   16
## day
```

```
## svn rev 84548
## language R
## version.string R version 4.3.1 (2023-06-16)
## nickname Beagle Scouts
```

1.4 Experimental setup

```
Setting up required variables variables.
# libraries we are using
library(ggplot2)
library(cowplot)
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
                 filter, lag
## The following objects are masked from 'package:base':
##
##
                 intersect, setdiff, setequal, union
library(PupillometryR)
## Loading required package: rlang
# data diractory for qh-pages
DATA_DIR = '/opt/ECJ-2023-Suite-Of-Diagnostic-Metrics-For-Characterizing-Selection-Schemes/DATA/BASE_DI
# data diractory for local testing
\# DATA_DIR = '-\('Desktop\)/Repositories\('ECJ-2023-Suite-Of-Diagnostic-Metrics-For-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Characterizing-Selection-Character
# graph variables
SHAPE = c(5,3,1,2,6,0,4,20,1)
cb_palette <- c('#332288','#88CCEE','#EE7733','#EE3377','#117733','#882255','#44AA99','#CCBB44', '#0000
p_theme <- theme(</pre>
    plot.title = element_text( face = "bold", size = 20, hjust=0.5),
     panel.border = element_blank(),
    panel.grid.minor = element_blank(),
    legend.title=element_text(size=18, hjust = 0.5),
     legend.text=element_text(size=10),
     axis.title = element_text(size=18),
     axis.text = element_text(size=16),
     legend.position="bottom",
     legend.margin = margin(0, 0, 0, 0),
     panel.background = element_rect(fill = "#f1f2f5",
                                                                                   colour = "white",
                                                                                   linewidth = 0.5, linetype = "solid")
)
# colors for streak plots
STK SHAPE = c(2,6,0,4,20,1)
stk_cb_palette <- c('#EE3377','#117733','#882255','#44AA99','#CCBB44', '#000000')
```

```
# default variables
DIMENSIONALITY = 100
GENERATIONS = 50000

# selection scheme related stuff
ACRO = c('tru','tor','lex','gfs','nds','nov','ran')
NAMES = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)', 'Genotypic Fitness Sharing (gfs)','Ph
```

Chapter 2

Exploitation rate results

Here we present the results for **best performances** found by each selection scheme on the exploitation rate diagnostic. 50 replicates are conducted for each scheme explored.

2.1 Data setup

```
DIR = paste(DATA_DIR, 'EXPLOITATION_RATE/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR, 'over-time.csv', sep = "", collapse = NULL), header = TRUE, stringsAs

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

best_df <- read.csv(paste(DIR, 'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFactors =

best_df$acro <- factor(best_df$acro, levels = ACRO)

sati_df <- read.csv(paste(DIR, 'sol-fnd.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFactors

sati_df$acro <- factor(sati_df$acro, levels = ACRO)
```

2.2 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

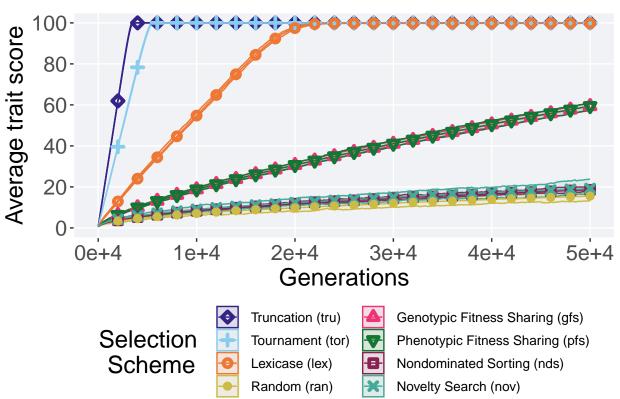
```
lines = over_time_df %%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(pop_fit_max) / DIMENSIONALITY,
   mean = mean(pop_fit_max) / DIMENSIONALITY,
   max = max(pop_fit_max) / DIMENSIONALITY
)

## `summarise()` has grouped output by 'scheme'. You can override using the
```

```
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)',
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape =
geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
geom_line(size = 0.5) +
geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0)</pre>
```

```
scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Performance over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```

Performance over time

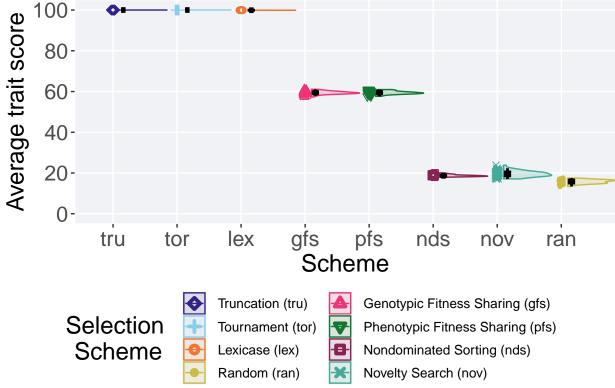


2.3 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Average trait score",
    limits=c(0, 100.1),
    breaks=seq(0,100, 20),
    labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





2.3.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('tru','tor','lex','gfs','pfs','nov','nds','ran')
performance %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val / DIMENSIONALITY, na.rm = TRUE),
    median = median(val / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
    max = max(val / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                         min median mean
                                             max
     <fct> <int> <int> <dbl>
                               <dbl> <dbl> <dbl>
                                                  <dbl>
##
## 1 tru
             50
                      0 100
                               100
                                     100
                                           100
## 2 tor
             50
                      0 100
                               100
                                     100
                                           100
## 3 lex
             50
                     0
                        99.9
                                99.9 99.9 99.9 0.0154
## 4 gfs
             50
                     0 57.3
                                59.3 59.4 61.1 0.984
## 5 pfs
             50
                     0 57.6
                                59.4 59.5 61.0 1.02
## 6 nov
                     0 17.1
                                19.5 19.5 23.9 1.95
             50
```

```
## 7 nds
              50
                      0 18.0
                                18.6 18.7 20.1 0.603
## 8 ran
              50
                        13.4
                                15.9 15.8 17.5 1.46
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = performance)
##
##
   Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 385.26, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
##
              tor
                                   pfs
       tru
                     lex
                            gfs
                                          nov
                                                 nds
## tor 1.000 -
## lex <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 -
## pfs <2e-16 <2e-16 <2e-16 1.000
## nov <2e-16 <2e-16 <2e-16 <2e-16 -
## nds <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 0.018 -
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <2e-16
##
## P value adjustment method: bonferroni
```

2.4 Generation satisfactory solution found

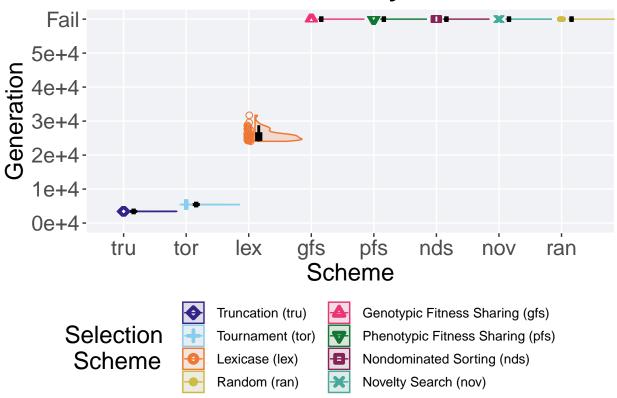
First generation a satisfactory solution is found throughout the 50,000 generations.

```
plot = sati df %>%
  ggplot(., aes(x = acro, y = gen , color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Generation",
   limits=c(0, 60001),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000, 60000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4", "Fail")
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale fill manual(values = cb palette) +
  ggtitle('Generation satisfactory solution found')+
```

```
p_theme

plot_grid(
    plot +
        theme(legend.position="none"),
    legend,
    nrow=2,
    rel_heights = c(3,1)
)
```

Generation satisfactory solution found



2.4.1 Stats

Summary statistics for the generation a satisfactory solution is found.

```
ssf = filter(sati_df, gen <= GENERATIONS)
ssf$acro = factor(ssf$acro, levels = c('tru','tor','lex'))
ssf %>%
group_by(acro) %>%
dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(gen)),
   min = min(gen, na.rm = TRUE),
   median = median(gen, na.rm = TRUE),
   mean = mean(gen, na.rm = TRUE),
   max = max(gen, na.rm = TRUE),
   IQR = IQR(gen, na.rm = TRUE)
```

```
## # A tibble: 3 x 8
                         min median mean
                                                     IQR
    acro count na_cnt
                                              max
     <fct> <int> <int> <dbl> <dbl> <int> <dbl>
                   0 3392 3422 3423. 3475
## 1 tru
            50
                                                    26
                     0 5390 5444. 5447. 5509
## 2 tor
             50
                                                    43.2
## 3 lex
             50
                     0 24036 25626. 25883. 31709 1739.
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(gen ~ acro, data = ssf)
##
## Kruskal-Wallis rank sum test
##
## data: gen by acro
## Kruskal-Wallis chi-squared = 132.46, df = 2, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = ssf$gen, g = ssf$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = 'g')
##
  Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: ssf$gen and ssf$acro
##
##
      tru
             tor
## tor <2e-16 -
## lex <2e-16 <2e-16
## P value adjustment method: bonferroni
```

Chapter 3

Ordered exploitation results

Here we present the results for **best performances** found by each selection scheme on the ordered exploitation diagnostic. 50 replicates are conducted for each scheme explored.

3.1 Data setup

```
DIR = paste(DATA_DIR,'ORDERED_EXPLOITATION/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, stringsAs

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

best_df <- read.csv(paste(DIR,'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFactors =

best_df$acro <- factor(best_df$acro, levels = ACRO)

sati_df <- read.csv(paste(DIR,'sol-fnd.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFactors

sati_df$acro <- factor(sati_df$acro, levels = ACRO)
```

3.2 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

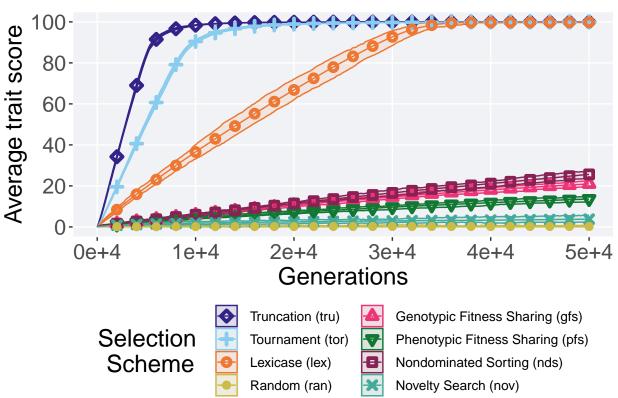
```
lines = over_time_df %%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(pop_fit_max) / DIMENSIONALITY,
   mean = mean(pop_fit_max) / DIMENSIONALITY,
   max = max(pop_fit_max) / DIMENSIONALITY
)

## `summarise()` has grouped output by 'scheme'. You can override using the
```

```
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)',
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape =
    geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
    geom_line(size = 0.5) +
    geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0) </pre>
```

```
scale_y_continuous(
   name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Performance over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```



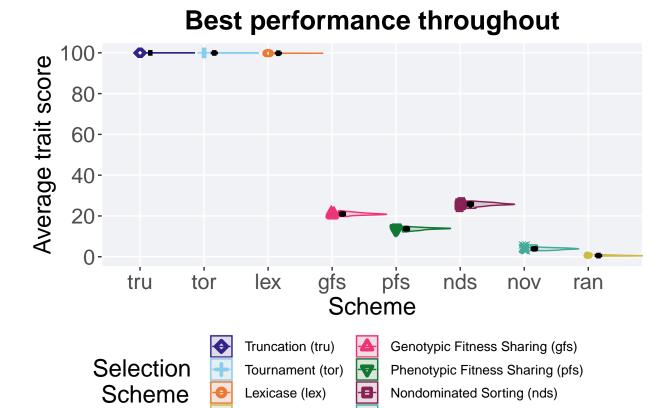


3.3 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Average trait score",
    limits=c(0, 100),
    breaks=seq(0,100, 20),
    labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```

Novelty Search (nov)



Random (ran)

3.3.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('tru','tor','lex','nds','gfs','pfs','nov','ran')
performance %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val / DIMENSIONALITY, na.rm = TRUE),
    median = median(val / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
    max = max(val / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                                  median
                                                             IQR
                             min
                                            mean
                                                     max
                           <dbl>
                                   <dbl>
                                            <dbl>
                                                   <dbl>
                                                            <dbl>
##
     <fct> <int>
                  <int>
              50
                       0 100.
                                 100.
                                          100.
                                                  100.
                                                         0.00168
## 1 tru
                                                   99.9
## 2 tor
              50
                       0
                          99.9
                                  99.9
                                          99.9
                                                        0.00650
## 3 lex
              50
                       0
                          99.7
                                  99.8
                                           99.8
                                                   99.9
                                                         0.0247
## 4 nds
              50
                      0 23.7
                                  25.7
                                           25.7
                                                   27.3 0.972
              50
                        19.7
                                  21.0
                                           21.0
                                                   22.6 0.754
## 5 gfs
## 6 pfs
              50
                      0
                          12.2
                                  13.8
                                           13.7
                                                   14.9 0.712
```

3.00

3.90

4.00

5.83 0.666

0

7 nov

50

```
0.318
## 8 ran
              50
                      0
                                  0.569
                                          0.605
                                                  1.31 0.279
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = performance)
##
##
   Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 392.77, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
                                          pfs
##
              tor
      tru
                     lex
                            nds
                                   gfs
                                                 nov
## tor <2e-16 -
## lex <2e-16 <2e-16 -
## nds <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 <2e-16 -
## pfs <2e-16 <2e-16 <2e-16 <2e-16 -
## nov <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <2e-16
##
## P value adjustment method: bonferroni
```

3.4 Generation satisfactory solution found

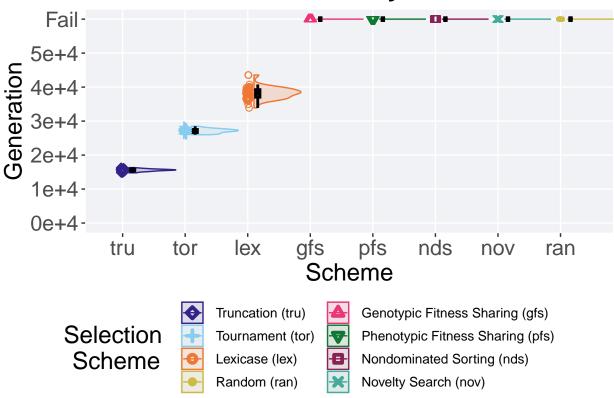
First generation a satisfactory solution is found throughout the 50,000 generations.

```
plot = sati df %>%
  ggplot(., aes(x = acro, y = gen , color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Generation",
   limits=c(0, 60001),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000, 60000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4", "Fail")
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale fill manual(values = cb palette) +
  ggtitle('Generation satisfactory solution found')+
```

```
p_theme

plot_grid(
    plot +
        theme(legend.position="none"),
    legend,
    nrow=2,
    rel_heights = c(3,1)
)
```

Generation satisfactory solution found



3.4.1 Stats

Summary statistics for the generation a satisfactory solution is found.

```
ssf = filter(sati_df, gen <= GENERATIONS)
ssf$acro = factor(ssf$acro, levels = c('tru','tor','lex'))
ssf %>%
group_by(acro) %>%
dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(gen)),
   min = min(gen, na.rm = TRUE),
   median = median(gen, na.rm = TRUE),
   mean = mean(gen, na.rm = TRUE),
   max = max(gen, na.rm = TRUE),
   IQR = IQR(gen, na.rm = TRUE)
```

```
## # A tibble: 3 x 8
##
    acro count na cnt
                          min median
                                                     IQR
                                               max
                                        mean
     <fct> <int> <int> <dbl> <dbl> <int> <dbl>
## 1 tru
                      0 14776 15585 15570. 16317
              50
## 2 tor
              50
                      0 25996 27138 27105. 28495 913.
## 3 lex
              50
                      0 33877 38288. 38265. 43565 2215.
Kruskal-Wallis test illustrates evidence of statistical differences.
kruskal.test(gen ~ acro, data = ssf)
##
##
   Kruskal-Wallis rank sum test
##
## data: gen by acro
## Kruskal-Wallis chi-squared = 132.45, df = 2, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = ssf$gen, g = ssf$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = 'g')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: ssf$gen and ssf$acro
##
##
       tru
              tor
## tor <2e-16 -
## lex <2e-16 <2e-16
## P value adjustment method: bonferroni
```

3.5 Streaks over time

Longest streak of active geens for the best solution found in a population over time. A maximum streak value of 100 and a minimum streak value of 1 is possible. Data points on the graph is the average streak across 50 replicates every 2000 generations. Shading comes from the best and worse streak across 50 replicates.

```
replicates every 2000 generations. Shading comes from the best and worse streak across 50 replicates.

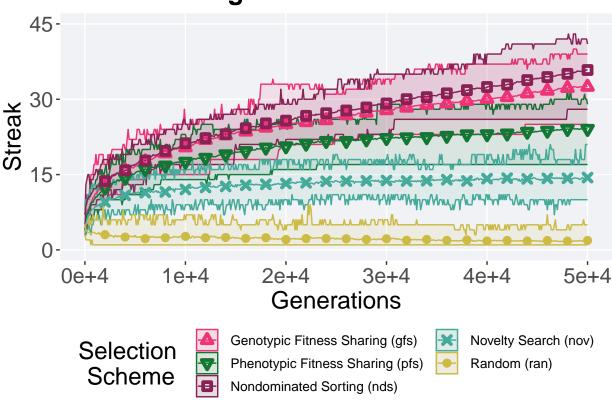
lines = filter(over_time_df, acro != 'tor' & acro != 'tru' & acro != 'lex') %>%
    group_by(scheme, gen) %>%
    dplyr::summarise(
        min = min(ele_stk_cnt),
        mean = mean(ele_stk_cnt),
        max = max(ele_stk_cnt)
)

### `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.

over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape
    geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
    geom_line(size = 0.5) +
    geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0)
    scale_y_continuous(
```

```
name="Streak",
   limits=c(0, 45),
   breaks=seq(0,45,15)
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=STK_SHAPE)+
  scale_colour_manual(values = stk_cb_palette) +
  scale_fill_manual(values = stk_cb_palette) +
  ggtitle('Longest streak over time')+
  p_theme +
  guides(
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```

Longest streak over time

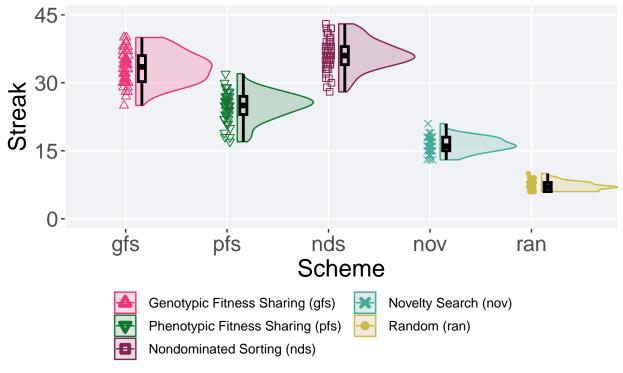


3.6 Longest streak throughout

Longest streak of the best solution found in the population throughout 50,000 generations.

```
plot = filter(best_df, var == 'ele_stk_cnt' & acro != 'tor' & acro != 'tru' & acro != 'lex') %>%
  ggplot(., aes(x = acro, y = val, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Streak",
   limits=c(0, 45),
   breaks=seq(0,45, 15)
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=STK_SHAPE)+
  scale_colour_manual(values = stk_cb_palette) +
  scale_fill_manual(values = stk_cb_palette) +
  ggtitle('Longest streak throughout')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





scheme

3.6.1 Stats

Summary statistics for the longest streak

```
streak = filter(best_df, var == 'ele_stk_cnt' & acro != 'tor' & acro != 'tru' & acro != 'lex')
streak$acro = factor(streak$acro, levels = c('nds','gfs','pfs','nov','ran'))
streak %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val, na.rm = TRUE),
    median = median(val, na.rm = TRUE),
    mean = mean(val, na.rm = TRUE),
    max = max(val, na.rm = TRUE),
    IQR = IQR(val, na.rm = TRUE)
)
```

```
## # A tibble: 5 x 8
                                                    IQR
     acro count na_cnt
                          min median mean
                                              max
                 <int> <dbl>
                               <dbl> <dbl> <dbl> <dbl>
     <fct> <int>
                           28
## 1 nds
              50
                      0
                                36
                                      36.2
                                               43 4
## 2 gfs
              50
                      0
                           25
                                33.5 33.4
                                               40 5.75
                           17
## 3 pfs
              50
                      0
                                25
                                      24.8
                                               32 4
## 4 nov
              50
                           13
                                16
                                      16.3
                                               21 3
                      0
                            6
                                                   2
## 5 ran
              50
                                 7
                                      7.18
                                               10
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(val ~ acro, data = streak)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 226.43, df = 4, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = streak$val, g = streak$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: streak$val and streak$acro
##
               gfs
##
                       pfs
       nds
                               nov
## gfs 0.0017 -
## pfs < 2e-16 2.7e-15 -
## nov < 2e-16 < 2e-16 3.1e-16 -
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16
## P value adjustment method: bonferroni
```

Chapter 4

Contradictory objectives results

Here we present the results for activation gene coverage and satisfactory trait coverage found by each selection scheme on the contradictory objectives diagnostic. 50 replicates are conducted for each scheme explored.

4.1 Data setup

```
DIR = paste(DATA_DIR,'CONTRADICTORY_OBJECTIVES/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, stringsA

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$overlap

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)
```

4.2 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

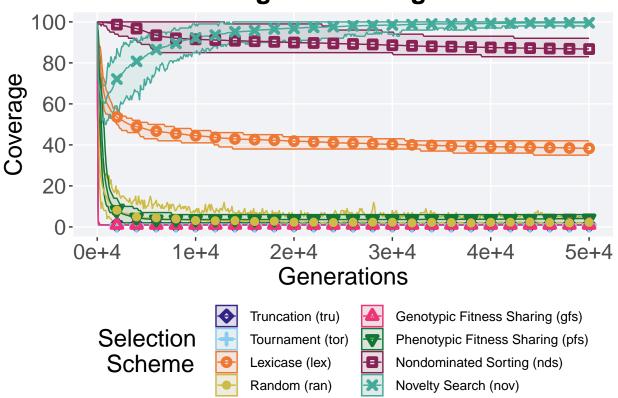
```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(uni_str_pos),
   mean = mean(uni_str_pos),
   max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
```

```
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)', 'Tournament (tor)', 'Lexicase (lex)',
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape
    geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
    geom_line(size = 0.5) +
    geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0)
    scale_y_continuous(
    name="Coverage",</pre>
```

```
limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Activation gene coverage over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```

Activation gene coverage over time

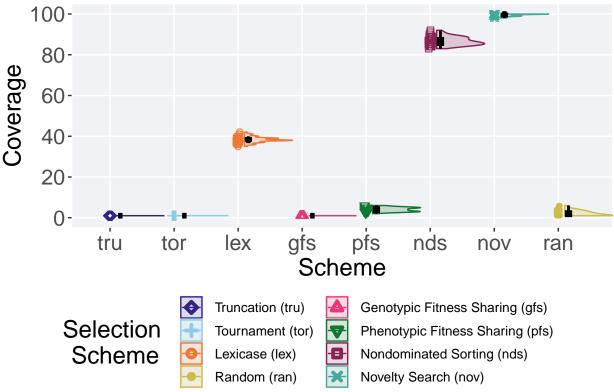


4.3 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Coverage",
    limits=c(0, 100.1),
    breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





4.3.1 Stats

Summary statistics for the coverage found in the final population.

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','nds','lex','pfs','ran','gfs','tor','tru
act_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
    min = min(uni_str_pos, na.rm = TRUE),
    median = median(uni_str_pos, na.rm = TRUE),
    mean = mean(uni_str_pos, na.rm = TRUE),
    max = max(uni_str_pos, na.rm = TRUE),
    IQR = IQR(uni_str_pos, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                          min median mean
                                                     IQR
                                              max
     <fct> <int> <int> <int>
                               <dbl> <dbl> <int> <dbl>
##
## 1 nov
              50
                      0
                            98
                                  100 99.6
                                                       1
## 2 nds
              50
                      0
                            83
                                   86 86.7
                                               92
                                                      3
## 3 lex
              50
                      0
                            35
                                   38 38.3
                                               42
                                                      1
                             2
## 4 pfs
              50
                      0
                                    4 4.12
                                                6
                                                      2
## 5 ran
              50
                             1
                                    2 2.22
                                                      2
                      0
                                                      0
## 6 gfs
              50
                             1
                                                1
```

```
## 7 tor
              50
                                     1 1
## 8 t.ru
              50
                       0
Kruskal-Wallis test illustrates evidence of statistical differences.
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
##
##
   Kruskal-Wallis rank sum test
##
## data: uni_str_pos by acro
## Kruskal-Wallis chi-squared = 381.66, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bonferroni
                      paired = FALSE, conf.int = FALSE, alternative = '1')
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               nds
                        lex
                                                 gfs tor
## nds < 2e-16 -
```

4.4 Satisfactory trait coverage over time

lex < 2e-16 < 2e-16 -

lines = over time df %>%

pfs < 2e-16 < 2e-16 < 2e-16 -

ran < 2e-16 < 2e-16 < 2e-16 7.1e-09 -

P value adjustment method: bonferroni

gfs < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 - ## tor < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 1 ## tru < 2e-16 < 2e-16 < 2e-16 < 2e-16 6.0e-09 1

Satisfactory trait coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
group_by(scheme, gen) %>%
dplyr::summarise(
    min = min(pop_uni_obj),
    mean = mean(pop_uni_obj),
    max = max(pop_uni_obj)
)

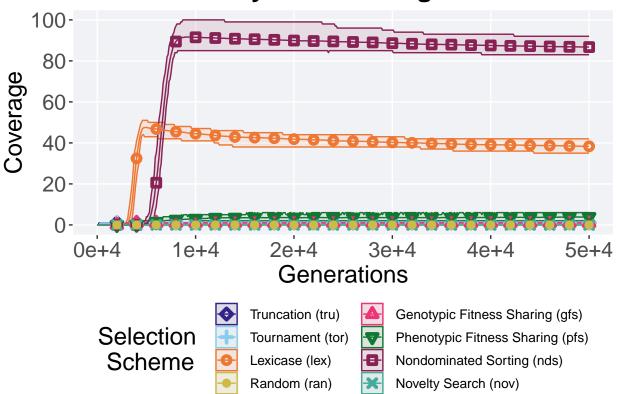
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.

lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)',

over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
    geom_line(size = 0.5) +
    geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0)</pre>
```

```
scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Satisfactory trait coverage over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```

Satisfactory trait coverage over time

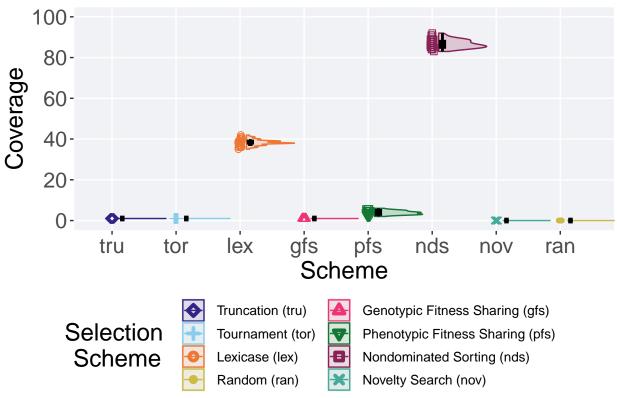


4.5 Final satisfactory trait coverage

Satisfactory trait coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = pop_uni_obj, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Coverage",
    limits=c(-0.1, 100),
    breaks = seq(0,100, 20),
    labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final satisfactory trait coverage')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





4.5.1 Stats

Summary statistics for the coverage found in the final population.

```
sat_coverage = filter(over_time_df, gen == 50000)
sat_coverage$acro = factor(sat_coverage$acro, levels = c('nds','lex','pfs','gfs','tor','tru','nov','ran sat_coverage %>%
    group_by(acro) %>%
    dplyr::summarise(
        count = n(),
        na_cnt = sum(is.na(pop_uni_obj)),
        min = min(pop_uni_obj, na.rm = TRUE),
        median = median(pop_uni_obj, na.rm = TRUE),
        mean = mean(pop_uni_obj, na.rm = TRUE),
        max = max(pop_uni_obj, na.rm = TRUE),
        IQR = IQR(pop_uni_obj, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                          min median mean
                                                     IQR
                                              max
                               <dbl> <dbl> <int> <dbl>
     <fct> <int> <int> <int>
##
## 1 nds
              50
                      0
                            83
                                   86 86.7
                                               92
## 2 lex
              50
                      0
                            35
                                   38 38.3
                                               42
                                                      1
## 3 pfs
              50
                      0
                             2
                                    4 3.88
                                                      2
## 4 gfs
              50
                      0
                             1
                                    1 1
                                                1
                                                      0
              50
                             1
                                                1
                                                      0
## 5 tor
                                    1 1
                      0
                                                      0
## 6 tru
              50
                             1
                                    1
                                                1
```

P value adjustment method: bonferroni

```
## 7 nov
             50
                     0
                            0
                                  0 0
## 8 ran
             50
                      0
                            0
                                  0 0
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(pop_uni_obj ~ acro, data = sat_coverage)
## Kruskal-Wallis rank sum test
##
## data: pop_uni_obj by acro
## Kruskal-Wallis chi-squared = 396.63, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = sat_coverage$pop_uni_obj, g = sat_coverage$acro, p.adjust.method = "bonferroni
                    paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: sat_coverage$pop_uni_obj and sat_coverage$acro
##
                           gfs
##
      nds
             lex
                    pfs
                                  tor
                                        tru
                                               nov
## lex <2e-16 -
## pfs <2e-16 <2e-16 -
## gfs <2e-16 <2e-16 -
## tor <2e-16 <2e-16 1
## tru <2e-16 <2e-16 1
                                  1
## nov <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 <
## ran <2e-16 <2e-16 <2e-16 <2e-16 <2e-16 1
```

Chapter 5

Multi-path exploration results

Here we present the results for **best performances** and **activation gene coverage** found by each selection scheme on the multi-path exploration diagnostic. 50 replicates are conducted for each scheme explored.

5.1 Data setup

```
DIR = paste(DATA_DIR,'MULTIPATH_EXPLORATION/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, stringsA

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$overlap

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)

best_df <- read.csv(paste(DIR,'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFactors = best_df$acro <- factor(best_df$acro, levels = ACRO)
```

5.2 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

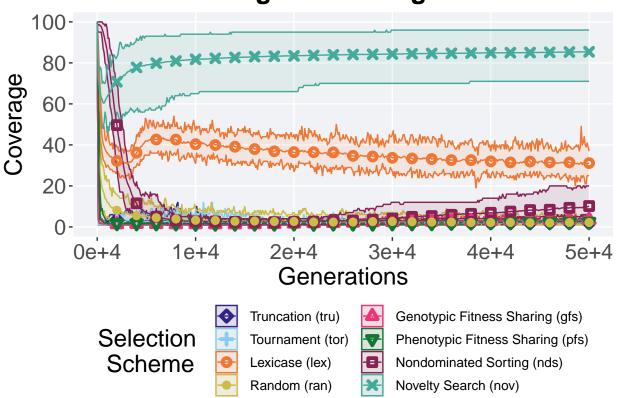
```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(uni_str_pos),
   mean = mean(uni_str_pos),
   max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)',</pre>
```

```
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen % 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0)
```

```
scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale\_shape\_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Activation gene coverage over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
  )
over_time_plot
```

Activation gene coverage over time

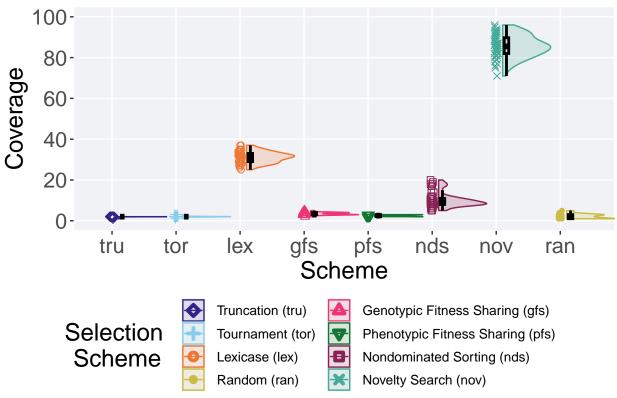


5.3 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Coverage",
    limits=c(0, 100),
    breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





5.3.1 Stats

Summary statistics for the coverage found in the final population.

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','lex','nds','gfs','pfs','ran','tor','tru
act_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
    min = min(uni_str_pos, na.rm = TRUE),
    median = median(uni_str_pos, na.rm = TRUE),
    mean = mean(uni_str_pos, na.rm = TRUE),
    max = max(uni_str_pos, na.rm = TRUE),
    IQR = IQR(uni_str_pos, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                          min median mean
                                                    IQR
                                             max
     <fct> <int> <int> <int>
                               <dbl> <dbl> <int> <dbl>
##
## 1 nov
              50
                      0
                           71
                                85.5 85.4
                                              96 7.75
## 2 lex
                                31
              50
                      0
                           25
                                     31.1
                                              37 4
## 3 nds
              50
                      0
                            5
                                 9
                                     10.2
                                              20 3
                            2
                                 3
## 4 gfs
              50
                      0
                                      3.48
                                               5 1
## 5 pfs
              50
                                 2.5 2.5
## 6 ran
                      0
                                               5
              50
                            1
                                      2.16
```

```
## 7 tor
              50
                       0
                                  2
                                        2.04
                             1
## 8 t.ru
              50
                       0
                             1
                                  2
                                        1.98
                                                 2 0
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
##
##
   Kruskal-Wallis rank sum test
##
## data: uni_str_pos by acro
## Kruskal-Wallis chi-squared = 350.25, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bonferroni
                      paired = FALSE, conf.int = FALSE, alternative = '1')
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               lex
                        nds
                                         pfs
                                                 ran tor
## lex < 2e-16 -
## nds < 2e-16 < 2e-16 -
## gfs < 2e-16 < 2e-16 < 2e-16 -
## pfs < 2e-16 < 2e-16 < 2e-16 3.6e-10 -
## ran < 2e-16 < 2e-16 < 2e-16 9.4e-08 0.4
## tor < 2e-16 < 2e-16 < 2e-16 < 2e-16 1.2e-05 1.0 -
## tru < 2e-16 < 2e-16 < 2e-16 < 2e-16 1.1e-07 1.0 1.0
```

5.4 Performance over time

P value adjustment method: bonferroni

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
    max = max(pop_fit_max) / DIMENSIONALITY
)

## `summarise()` has grouped output by 'scheme'. You can override using the

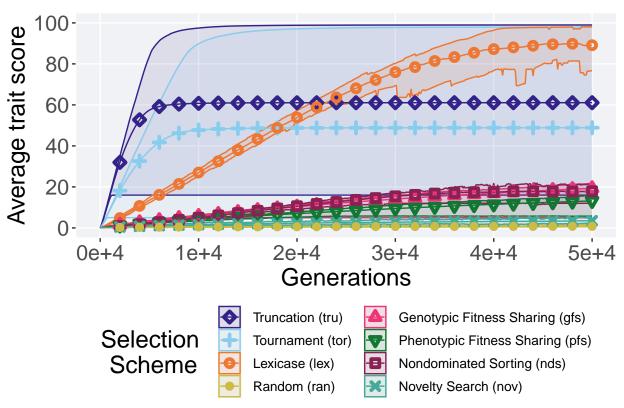
## `.groups` argument.

lines$scheme <- factor(lines$scheme, levels = c('Truncation (tru)','Tournament (tor)','Lexicase (lex)',

over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme, shape geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha = 1.0) scale_y_continuous(</pre>
```

```
name="Average trait score",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=c(5,3,1,20,2,6,0,4))+
  scale_colour_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255',
  scale_fill_manual(values = c('#332288','#88CCEE','#EE7733','#CCBB44','#EE3377','#117733','#882255','#
  ggtitle('Performance over time')+
  p_theme +
  guides (
    shape=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    color=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme'),
    fill=guide_legend(ncol=2, title.position = "left", title = 'Selection \nScheme')
over_time_plot
```

Performance over time

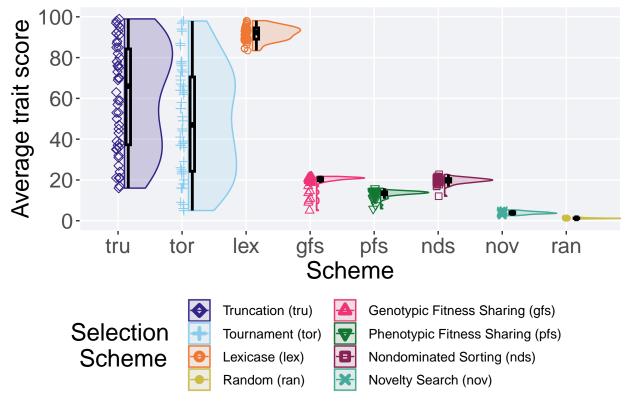


5.5 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .1, y = 0), scale = 'width', alpha = 0.2, width = 1.5)
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position = po
  geom_point(position = position_jitter(width = 0.03, height = 0.02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Average trait score",
    limits=c(0, 100),
    breaks=seq(0,100, 20),
    labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme
plot_grid(
  plot +
    theme(legend.position="none"),
 legend,
 nrow=2,
  rel_heights = c(3,1)
```





5.5.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('lex','tru','tor','gfs','nds','pfs','nov','ran')
performance %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val / DIMENSIONALITY, na.rm = TRUE),
    median = median(val / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
    max = max(val / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 8 x 8
     acro count na_cnt
                          min median mean
                                                    IQR
                                             max
     <fct> <int> <int> <dbl>
                               <dbl> <dbl> <dbl>
                                                  <dbl>
##
## 1 lex
             50
                     0 83.4
                               92.3 91.9
                                           98.1
                                                  5.51
## 2 tru
             50
                     0 16
                               66.0
                                     61.1
                                           99.0
                                                 47.0
## 3 tor
             50
                     0 5
                               47.0 48.9
                                           97.9
                                                 46.2
## 4 gfs
             50
                     0 4.99
                               20.7 19.3 21.7
                                                  1.45
## 5 nds
             50
                     0 12.0
                               19.9 19.7 22.8
                                                  1.72
## 6 pfs
             50
                     0 5.87
                               13.6 13.2 15.9
                                                  1.39
```

```
## 7 nov
            50
                    0 2.52
                              3.83 3.87 5.33 0.793
## 8 ran
            50
                    0 0.865
                              1.19 1.23 1.72 0.247
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(val ~ acro, data = performance)
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 356.22, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = 'l')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
                                               pfs
##
       lex
                               gfs
                                       nds
               tru
                       tor
                                                       nov
## tru 4.4e-09 -
## tor 1.1e-12 0.33
## gfs < 2e-16 2.3e-13 4.3e-07 -
## nds < 2e-16 1.2e-13 6.8e-07 0.47
## pfs < 2e-16 < 2e-16 5.0e-12 2.3e-11 1.3e-15 -
## nov < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 -
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16
## P value adjustment method: bonferroni
```