Supplemental Material: Valley Crossing Diagnostics

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Chapter 1

Introduction

This is the supplemental material for experiments with diagnostics and integrated valleys.

1.1 About our supplemental material

This supplemental material is hosted on GitHub using GitHub pages. The source code and configuration files used to generate this supplemental material can be found in this GitHub repository. We compiled our data analyses and supplemental documentation into this nifty web-accessible book using bookdown.

Our supplemental material includes the following paper figures and statistics:

- Exploitation rate results (Section 2)
- Ordered exploitation results (Section 3)
- Contradictory objectives results (Section 4)
- Multi-path exploration results (Section 5)

1.2 Contributing authors

- Jose Guadalupe Hernandez
- Alexander Lalejini
- Charles Ofria

1.3 Computer Setup

These analyses were conducted in the following computing environment:

print(version)

```
##
## platform
                  x86_64-pc-linux-gnu
## arch
                  x86_64
## os
                  linux-gnu
                  x86_64, linux-gnu
## system
## status
## major
                  3.1
## minor
                  2023
## year
## month
                  06
## day
                  16
## svn rev
                  84548
## language
                  R
## version.string R version 4.3.1 (2023-06-16)
## nickname
                  Beagle Scouts
```

1.4 Experimental setup

Setting up required variables variables.

```
# libraries we are using
library(ggplot2)
library(cowplot)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(PupillometryR)
## Loading required package: rlang
# data diractory for gh-pages
DATA_DIR = '/opt/ECJ-2023-Suite-Of-Diagnostic-Metrics-For-Characterizing-Selection-School
# data diractory for local testing
# DATA_DIR = 'C:/Users/jgh9094/Desktop/Research/Projects/SelectionDiagnostics/ECJ-2023
# graph variables
SHAPE = c(5,3,1,2,6,0,4,20,1)
```

```
cb_palette <- c('#332288','#88CCEE','#EE7733','#EE3377','#117733','#882255','#44AA99','#CCBB44',
TSIZE = 26
p_theme <- theme(</pre>
  text = element_text(size = 28),
  plot.title = element_text( face = "bold", size = 22, hjust=0.5),
  panel.border = element_blank(),
  panel.grid.minor = element_blank(),
  legend.title=element_text(size=22),
  legend.text=element_text(size=23),
  axis.title = element_text(size=23),
  axis.text = element_text(size=22),
  legend.position="bottom",
  panel.background = element_rect(fill = "#f1f2f5",
                                  colour = "white",
                                  size = 0.5, linetype = "solid")
## Warning: The `size` argument of `element_rect()` is deprecated as of ggplot2 3.4.0.
## i Please use the `linewidth` argument instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
# default variables
REPLICATES = 50
DIMENSIONALITY = 100
GENERATIONS = 50000
# selection scheme related stuff
ACRO = c('tru','tor','lex','gfs','pfs','nds','nov','ran')
NAMES = c('Truncation (tru)', 'Tournament (tor)', 'Lexicase (lex)', 'Genotypic Fitness Sharing (gfs
# valley crossing comparisons
mvc_{col} = c('#1A85FF', '#D41159')
```

Chapter 2

Exploitation rate results

Here we present the results for **best performances** found by each selection scheme on the exploitation rate diagnostic with valley crossing integrated. 50 replicates are conducted for each scheme explored.

2.1 Analysis dependencies

```
library(ggplot2)
library(cowplot)
library(dplyr)
library(PupillometryR)
```

2.2 Data setup

```
DIR = paste(DATA_DIR, 'EXPLOITATION_RATE/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR, 'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

best_df <- read.csv(paste(DIR, 'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

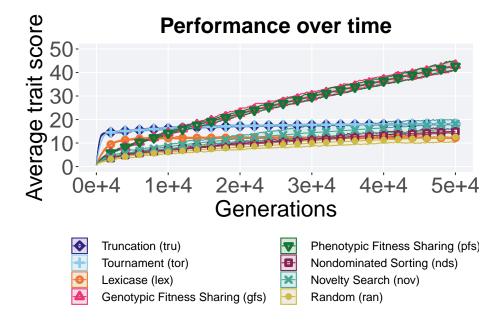
best_df$acro <- factor(best_df$acro, levels = ACRO)
```

2.3 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(pop_fit_max) / DIMENSIONALITY,
   mean = mean(pop_fit_max) / DIMENSIONALITY,
   max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 50),
   breaks=seq(0,50, 10),
   labels=c("0", "10", "20", "30", "40", "50")
 ) +
  scale x continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Performance over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
 guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
over_time_plot
```



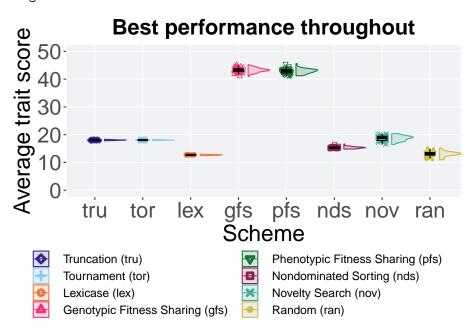
2.4 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .2, y = 0), scale = 'width', alpha = 0.2) +
  geom_point(position = position_jitter(width = .1), size = 1.5, alpha = 1.0) +
  geom_boxplot(color = 'black', width = .2, outlier.shape = NA, alpha = 0.0) +
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 50),
   breaks=seq(0,50,10),
   labels=c("0", "10", "20", "30", "40", "50")
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale colour manual(values = cb palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme + theme(legend.title=element_blank())
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Warning: Using the `size` aesthetic with geom_polygon was deprecated in ggplot2 3.4
i Please use the `linewidth` aesthetic instead.
This warning is displayed once every 8 hours.
Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
generated.



2.4.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('gfs','pfs','tru','tor','nov',':
performance %>%
    group_by(acro) %>%
    dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
```

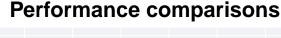
```
min = min(val / DIMENSIONALITY, na.rm = TRUE),
   median = median(val / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
   max = max(val / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
 )
## # A tibble: 8 x 8
     acro count na_cnt
                          min median mean
                                                   IQR
##
     <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                      0 41.0
## 1 gfs
              50
                                43.2 43.2 45.2 0.923
## 2 pfs
              50
                      0 41.2
                                43.0 42.9 45.6 1.17
## 3 tru
              50
                      0 17.8
                                18.1 18.0 18.3 0.140
## 4 tor
                      0 17.9
                                18.1 18.1 18.3 0.150
             50
## 5 nov
             50
                      0 16.4
                                18.8 18.7
                                            20.4 1.51
## 6 nds
              50
                      0 14.8
                                15.3 15.4 16.6 0.418
## 7 ran
              50
                      0 11.0
                                13.2 13.1 15.2 0.900
                                12.7 12.7 13.0 0.154
## 8 lex
              50
                      0 12.5
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = performance)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 367.97, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
              pfs
##
       gfs
                                               nds
                       tru
                               tor
                                       nov
                                                       ran
## pfs 0.4845 -
## tru < 2e-16 < 2e-16 -
## tor < 2e-16 < 2e-16 1.0000
## nov < 2e-16 < 2e-16 1.0000 1.0000
## nds < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 -
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 -
## lex < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 0.0035
##
```

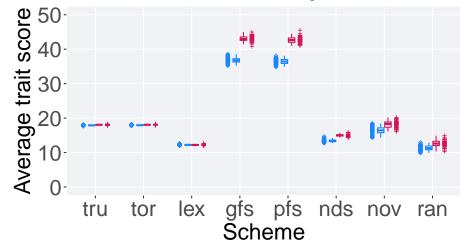
P value adjustment method: bonferroni

2.5 Performance interval comparison

Here we compare the best performance found in the population at generation 40,000 & 50,000 for all selection schemes.

```
interval_df = filter(filter(over_time_df, (gen == 50000 | gen == 40000)))
interval_df$Generation <- factor(interval_df$gen, levels = c(40000,50000))
interval_df$acro <- factor(interval_df$acro, levels = ACRO)</pre>
ggplot(interval_df, aes(x=acro, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation)
 geom_boxplot(width = .3, outlier.shape = NA, alpha = 0.0) +
    geom_point(size = 1.0, alpha = 1.0, position=position_dodge(width=1.0)) +
    scale_y_continuous(
     name="Average trait score",
      limits=c(0, 50),
     breaks=seq(0,50, 10),
     labels=c("0","10", "20", "30", "40", "50")
    ) +
    scale_x_discrete(
     name="Scheme"
    ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
 ggtitle('Performance comparisons')+
 p_theme
```





Generation = 40000 = 50000

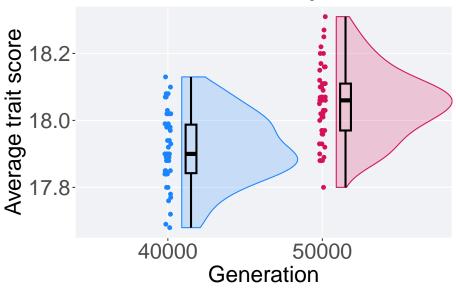
2.5.1 Stats by interval comparisons

Here we present statistical analysis between the performances found at different generation intervals.

2.5.1.1 Truncation

```
filter(interval_df, acro == 'tru') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'tru') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <## 0.145
## 1 40000 50 0 17.7 17.9 17.9 18.1 0.145
## 2 50000 50 0 17.8 18.1 18.0 18.3 0.140</pre>
```

Results for post-hoc Wilcoxon rank-sum test.

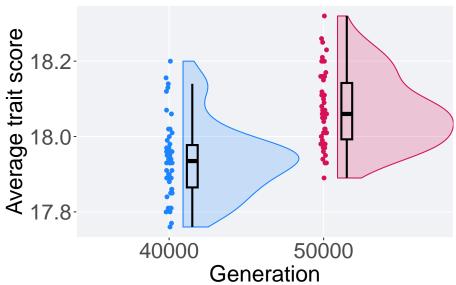
```
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "tru" & Generation == 50000)$pop_fit_max and filter(interval## W = 2013.5, p-value = 7.103e-08
## alternative hypothesis: true location shift is greater than 0
```

2.5.1.2 Tournament

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'tor') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

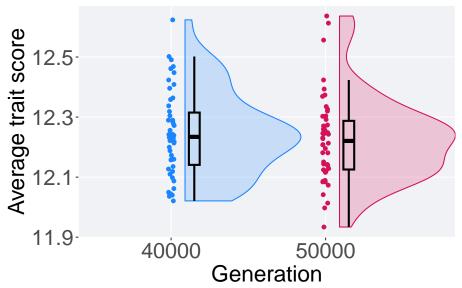
```
filter(interval_df, acro == 'tor') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
 )
## # A tibble: 2 x 8
    Generation count na_cnt
                              min median mean
                                                  max
                                                        IQR
    <fct>
                <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 40000
                   50
                           0 17.8
                                    17.9 17.9 18.2 0.112
## 2 50000
                           0 17.9
                                     18.1 18.1 18.3 0.150
                   50
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'tor' & Generation == 50000)$pop_fit_max,
            y = filter(interval_df, acro == 'tor' & Generation == 40000) pop_fit_max,
            alternative = 'g')
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "tor" & Generation == 50000)$pop_fit_max and fil
## W = 2095.5, p-value = 2.818e-09
## alternative hypothesis: true location shift is greater than 0
```

2.5.1.3 Lexicase

```
filter(interval_df, acro == 'lex') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
  ) +
  scale_x_discrete(
   name="Generation"
  ) +
```

```
scale_shape_manual(values=c(16,16))+
scale_colour_manual(values = mvc_col, ) +
scale_fill_manual(values = mvc_col) +
ggtitle('Performance comparisons')+
p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'lex') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <12.0 12.2 12.2 12.6 0.174
## 2 50000 50 0 11.9 12.2 12.2 12.6 0.162</pre>
```

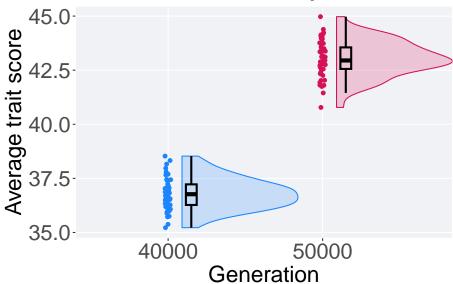
Results for post-hoc Wilcoxon rank-sum test.

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "lex" & Generation == 50000)$pop_fit_max and fil
## W = 1155, p-value = 0.5147
## alternative hypothesis: true location shift is not equal to 0
```

2.5.1.4 Genotypic fitness sharing

```
filter(interval_df, acro == 'gfs') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
     name="Average trait score",
    ) +
    scale_x_discrete(
     name="Generation"
    ) +
  scale_shape_manual(values=c(16,16))+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
 ggtitle('Performance comparisons')+
 p_theme + theme(legend.position="none")
```





Summary statistics for the best performance.

```
filter(interval_df, acro == 'gfs') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

Results for post-hoc Wilcoxon rank-sum test.

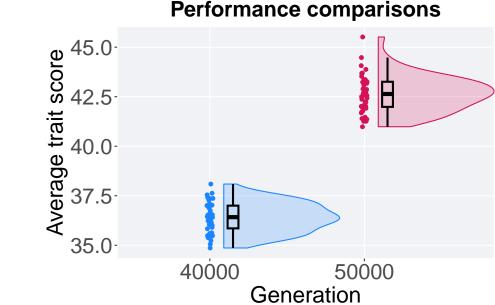
```
##
   Wilcoxon rank sum test with continuity correction
## data: filter(interval_df, acro == "gfs" & Generation == 50000)$pop_fit_max and fil
## W = 2500, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0
```

2.5.1.5 Phenotypic fitness sharing

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'pfs') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
      name="Average trait score",
    ) +
    scale_x_discrete(
      name="Generation"
  scale_shape_manual(values=c(16,16))+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
  ggtitle('Performance comparisons')+
 p_theme + theme(legend.position="none")
```

Performance comparisons



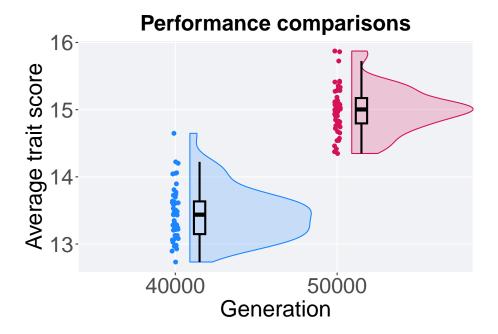
Summary statistics for the best performance.

```
filter(interval_df, acro == 'pfs') %>%
 group_by(Generation) %>%
 dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
## # A tibble: 2 x 8
    Generation count na_cnt
                            min median mean
                                                   IQR
                                            max
##
   <fct>
          <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl><</pre>
## 1 40000
                 50
                       0 34.9
                                 36.4 36.4 38.1 1.15
## 2 50000
                        0 41.0 42.6 42.6 45.5 1.27
                 50
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'pfs' & Generation == 50000)$pop_fit_max,
           y = filter(interval_df, acro == 'pfs' & Generation == 40000) pop_fit_max,
           alternative = 'g')
## Wilcoxon rank sum test with continuity correction
##
## W = 2500, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0
```

2.5.1.6 Nondominated sorting

```
filter(interval_df, acro == 'nds') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=0
geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
scale_y_continuous(
    name="Average trait score",
) +
scale_x_discrete(
    name="Generation") +
```

```
scale_shape_manual(values=c(16,16))+
scale_colour_manual(values = mvc_col, ) +
scale_fill_manual(values = mvc_col) +
ggtitle('Performance comparisons')+
p_theme + theme(legend.position="none")
```



Summary statistics for the best performance.

```
filter(interval_df, acro == 'nds') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <3.487</td>

## 1 40000 50 0 12.7 13.4 13.5 14.6 0.487
## 2 50000 50 0 14.3 15.0 15.0 15.9 0.377
```

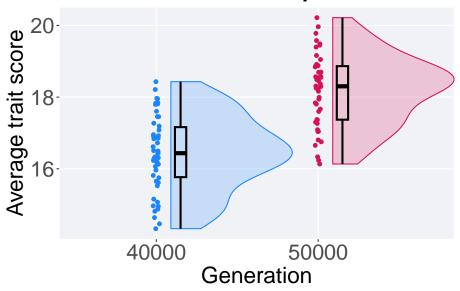
Results for post-hoc Wilcoxon rank-sum test.

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "nds" & Generation == 50000)$pop_fit_max and filter(interval_## W = 2493, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0</pre>
```

2.5.1.7 Novelty search

```
filter(interval_df, acro == 'nov') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'nov') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> 14.3 16.4 16.4 18.4 1.40
## 2 50000 50 0 16.1 18.3 18.2 20.2 1.49
```

Results for post-hoc Wilcoxon rank-sum test.

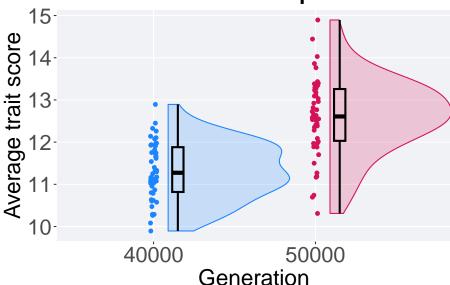
```
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "nov" & Generation == 50000)$pop_fit_max and filter(interval## W = 2209, p-value = 1.951e-11
## alternative hypothesis: true location shift is greater than 0
```

2.5.1.8 Random

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'ran') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'ran') %>%
  group_by(Generation) %>%
 dplyr::summarise(
    count = n(),
   na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
 )
## # A tibble: 2 x 8
    Generation count na_cnt min median mean
                                                 max
                                                       IQR
##
    <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 40000
                  50
                          0 9.89 11.3 11.3 12.9 1.06
## 2 50000
                          0 10.3
                  50
                                  12.6 12.6 14.9 1.23
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'ran' & Generation == 50000)$pop_fit_max,
           y = filter(interval_df, acro == 'ran' & Generation == 40000) pop_fit_max,
           alternative = 'g')
##
##
   Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "ran" & Generation == 50000)$pop_fit_max and fil
## W = 2185, p-value = 5.885e-11
## alternative hypothesis: true location shift is greater than 0
```

Chapter 3

Ordered exploitation results

Here we present the results for **best performances** found by each selection scheme on the ordered exploitation diagnostic with valley crossing integrated. 50 replicates are conducted for each scheme explored.

3.1 Analysis dependencies

```
library(ggplot2)
library(cowplot)
library(dplyr)
library(PupillometryR)
```

3.2 Data setup

```
DIR = paste(DATA_DIR,'ORDERED_EXPLOITATION/', sep = "", collapse = NULL)
over_time_df <- read.csv(paste(DIR,'over-time.csv', sep = "", collapse = NULL), header = TRUE, st
over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

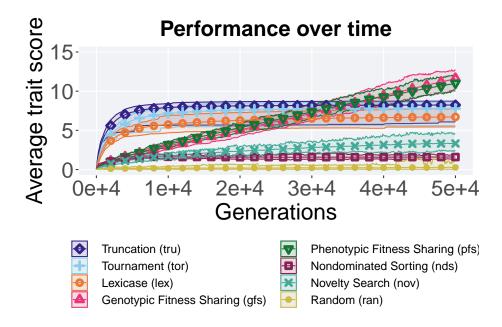
best_df <- read.csv(paste(DIR,'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace
best_df$acro <- factor(best_df$acro, levels = ACRO)</pre>
```

3.3 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
    max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 15),
 ) +
  scale x continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Performance over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
 guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
over_time_plot
```

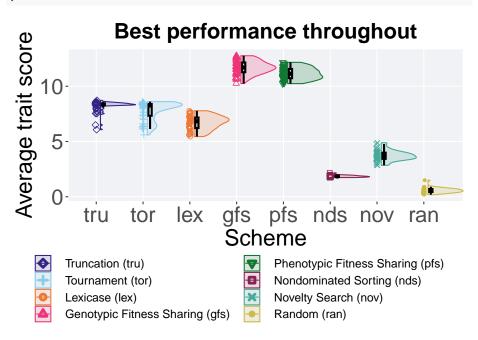


3.4 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score"
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme + theme(legend.title=element_blank())
plot_grid(
  plot +
    theme(legend.position="none"),
```

```
legend,
nrow=2,
rel_heights = c(3,1)
)
```



3.4.1 Stats

Summary statistics for the best performance.

acro count na_cnt

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('gfs','pfs','tru','tor','lex','sperformance %>%
    group_by(acro) %>%
    dplyr::summarise(
        count = n(),
        na_cnt = sum(is.na(val)),
        min = min(val / DIMENSIONALITY, na.rm = TRUE),
        median = median(val / DIMENSIONALITY, na.rm = TRUE),
        mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
        max = max(val / DIMENSIONALITY, na.rm = TRUE),
        IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
)
```

mean

min median

IQR

max

```
<fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 gfs
              50
                     0 10.2
                              11.7
                                     11.7
                                            12.8 0.876
## 2 pfs
              50
                     0 10.2
                                      11.2
                                            12.2 0.840
                               11.1
## 3 tru
              50
                     0 6.07
                               8.35
                                      8.23
                                             8.72 0.166
## 4 tor
             50
                     0 5.60
                               8.26
                                      7.79
                                             8.61 1.07
## 5 lex
              50
                     0 5.44
                               6.83
                                      6.72
                                             7.78 0.949
## 6 nov
              50
                     0 2.84
                               3.70
                                      3.74
                                             4.89 0.555
## 7 nds
              50
                     0 1.74
                               1.84
                                      1.85
                                             2.16 0.114
## 8 ran
              50
                     0 0.192 0.552 0.570 1.50 0.269
```

Kruskal-Wallis test illustrates evidence of statistical differences.

```
kruskal.test(val ~ acro, data = performance)
##
##
            Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 380.24, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                                                                      paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: performance$val and performance$acro
##
##
                       gfs
                                                 pfs
                                                                             tru
                                                                                                       tor
                                                                                                                                  lex
                                                                                                                                                            nov
                                                                                                                                                                                       nds
## pfs 0.00041 -
## tru < 2e-16 < 2e-16 -
## tor < 2e-16 < 2e-16 0.09539 -
## lex < 2e-16 < 2e-16 2.1e-14 2.0e-07 -
## nov < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 -
## nds < 2e-16 < 2e-16
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16 < 2e-16
##
## P value adjustment method: bonferroni
```

3.5 Performance interval comparison

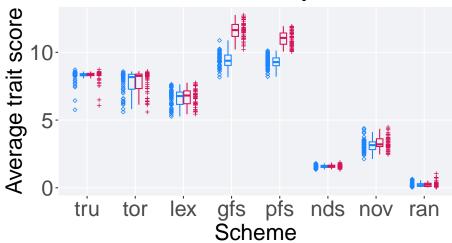
Here we compare the best performance found in the population at generation 40,000~&~50,000 for all selection schemes.

```
interval_df = filter(filter(over_time_df, (gen == 50000 | gen == 40000)))
interval_df$Generation <- factor(interval_df$gen, levels = c(40000,50000))</pre>
```

```
interval_df$acro <- factor(interval_df$acro, levels = ACRO)

ggplot(interval_df, aes(x=acro, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation_boxplot(width = .3, outlier.shape = NA, alpha = 0.0) +
    geom_point(size = 1.0, alpha = 1.0, position=position_dodge(width=1.0)) +
    scale_y_continuous(
        name="Average trait score"
    ) +
    scale_x_discrete(
        name="Scheme"
    ) +
    scale_shape_manual(values=SHAPE)+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme</pre>
```

Performance comparisons



Generation = 40000 = 50000

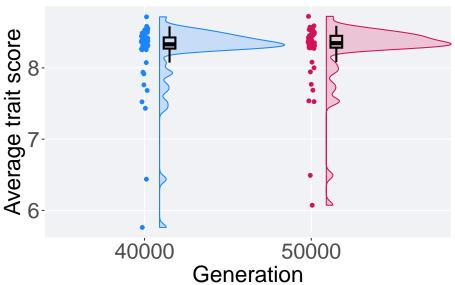
3.5.1 Stats by interval comparisons

Here we present statistical analysis between the performances found at different generation intervals.

3.5.1.1 Truncation

```
filter(interval_df, acro == 'tru') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Color=Generation)
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
      name="Average trait score",
    ) +
    scale_x_discrete(
      name="Generation"
    ) +
  scale shape manual(values=c(16,16))+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
  ggtitle('Performance comparisons')+
  p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

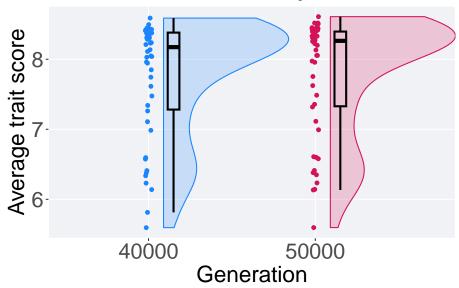
```
filter(interval_df, acro == 'tru') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
```

```
median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
## # A tibble: 2 x 8
    Generation count na cnt
                              min median mean
                                                 max
    <fct>
               <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 40000
                  50
                          0 5.76 8.33 8.21 8.72 0.156
## 2 50000
                                    8.35 8.23 8.72 0.166
                  50
                           0 6.07
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'tru' & Generation == 50000)$pop_fit_max,
           y = filter(interval_df, acro == 'tru' & Generation == 40000) pop_fit_max,
           alternative = 't')
##
##
   Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "tru" & Generation == 50000)$pop_fit_max and fil
## W = 1351, p-value = 0.4884
## alternative hypothesis: true location shift is not equal to 0
```

3.5.1.2 Tournament

```
filter(interval_df, acro == 'tor') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
     name="Average trait score",
    ) +
    scale_x_discrete(
     name="Generation"
    ) +
  scale_shape_manual(values=c(16,16))+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
  ggtitle('Performance comparisons')+
 p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'tor') %>%
group_by(Generation) %>%
dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> 1.07
## 2 50000 50 0 5.60 8.26 7.79 8.61 1.07
```

Results for post-hoc Wilcoxon rank-sum test.

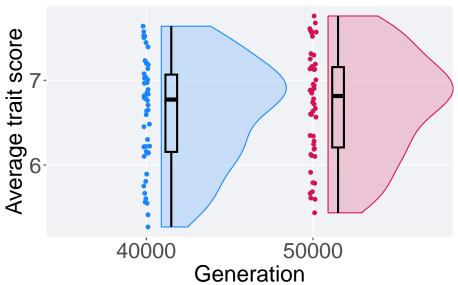
```
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "tor" & Generation == 50000)$pop_fit_max and fil
## W = 1343, p-value = 0.5237
## alternative hypothesis: true location shift is not equal to 0
```

3.5.1.3 Lexicase

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'lex') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
scale_y_continuous(
    name="Average trait score",
) +
scale_x_discrete(
    name="Generation"
) +
scale_shape_manual(values=c(16,16))+
scale_colour_manual(values = mvc_col, ) +
scale_fill_manual(values = mvc_col) +
ggtitle('Performance comparisons')+
p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'lex') %>%
 group_by(Generation) %>%
 dplyr::summarise(
   count = n(),
   na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
## # A tibble: 2 x 8
    Generation count na_cnt
                                                   IQR
                            min median mean
                                             max
              <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 40000
                 50
                        0 5.27
                                 6.77 6.62 7.64 0.912
## 2 50000
                                6.81 6.71 7.76 0.948
                 50
                        0 5.44
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'lex' & Generation == 50000)$pop_fit_max,
           y = filter(interval_df, acro == 'lex' & Generation == 40000) pop_fit_max,
           alternative = 't')
##
## Wilcoxon rank sum test with continuity correction
##
## W = 1346, p-value = 0.5103
## alternative hypothesis: true location shift is not equal to 0
```

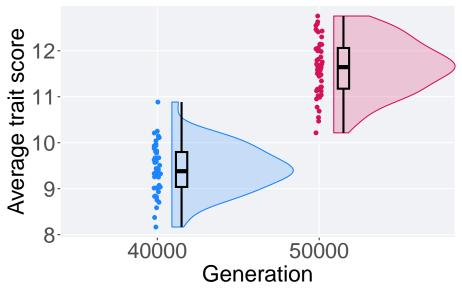
3.5.1.4 Genotypic fitness sharing

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'gfs') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=0
geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
scale_y_continuous(
    name="Average trait score",
) +
scale_x_discrete(
    name="Generation") +
```

```
scale_shape_manual(values=c(16,16))+
scale_colour_manual(values = mvc_col, ) +
scale_fill_manual(values = mvc_col) +
ggtitle('Performance comparisons')+
p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'gfs') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <0.760
## 2 50000 50 0 10.2 11.6 11.6 12.8 0.885</pre>
```

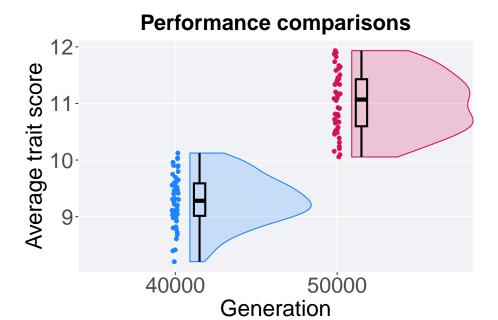
Results for post-hoc Wilcoxon rank-sum test.

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "gfs" & Generation == 50000)$pop_fit_max and filter(interval_## W = 2494, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0</pre>
```

3.5.1.5 Phenotypic fitness sharing

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'pfs') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```



Summary statistics for the best performance.

```
filter(interval_df, acro == 'pfs') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <574
## 2 50000 50 0 10.1 11.1 11.0 11.9 0.831</pre>
```

Results for post-hoc Wilcoxon rank-sum test.

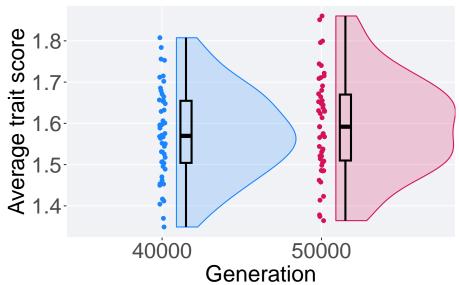
```
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "pfs" & Generation == 50000)$pop_fit_max and filter(interval## W = 2498, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0</pre>
```

3.5.1.6 Nondominated sorting

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'nds') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generation,shape=Geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
        name="Average trait score",
    ) +
    scale_x_discrete(
        name="Generation"
    ) +
    scale_shape_manual(values=c(16,16))+
    scale_colour_manual(values = mvc_col, ) +
    scale_fill_manual(values = mvc_col) +
    ggtitle('Performance comparisons')+
    p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'nds') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
   min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
   max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
 )
## # A tibble: 2 x 8
    Generation count na_cnt
                               min median mean
                                                         IQR
                                                  max
                <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                           0 1.35
## 1 40000
                                     1.57 1.57 1.81 0.150
                   50
## 2 50000
                                     1.59 1.59 1.86 0.160
                   50
                           0 1.36
Results for post-hoc Wilcoxon rank-sum test.
wilcox.test(x = filter(interval_df, acro == 'nds' & Generation == 50000)$pop_fit_max,
            y = filter(interval_df, acro == 'nds' & Generation == 40000) pop_fit_max,
            alternative = 't')
##
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "nds" & Generation == 50000)$pop_fit_max and fil
## W = 1359, p-value = 0.4545
## alternative hypothesis: true location shift is not equal to 0
```

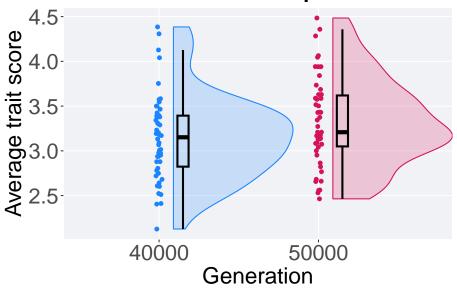
3.5.1.7 Novelty search

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'nov') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
  ) +
  scale_x_discrete(
  name="Generation"
) +
```

```
scale_shape_manual(values=c(16,16))+
scale_colour_manual(values = mvc_col, ) +
scale_fill_manual(values = mvc_col) +
ggtitle('Performance comparisons')+
p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'nov') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <0.570
## 2 50000 50 0 2.46 3.21 3.32 4.48 0.569</pre>
```

Results for post-hoc Wilcoxon rank-sum test.

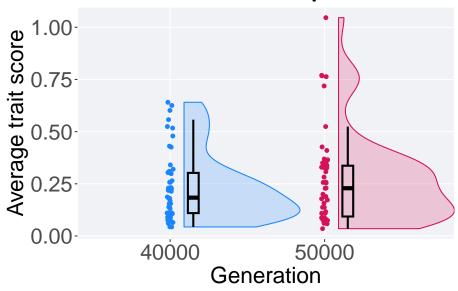
```
##
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "nov" & Generation == 50000)$pop_fit_max and fil
## W = 1506, p-value = 0.07818
## alternative hypothesis: true location shift is not equal to 0
```

3.5.1.8 Random

Plot for comparing performances at interval 40,000 & 50,000.

```
filter(interval_df, acro == 'ran') %>%
ggplot(., aes(x=Generation, y=pop_fit_max/DIMENSIONALITY,fill=Generation,color=Generat
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
    scale_y_continuous(
     name="Average trait score",
    ) +
    scale_x_discrete(
     name="Generation"
    ) +
  scale_shape_manual(values=c(16,16))+
  scale_colour_manual(values = mvc_col, ) +
  scale_fill_manual(values = mvc_col) +
 ggtitle('Performance comparisons')+
 p_theme + theme(legend.position="none")
```

Performance comparisons



Summary statistics for the best performance.

```
filter(interval_df, acro == 'ran') %>%
  group_by(Generation) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_fit_max)),
    min = min(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    median = median(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    mean = mean(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    max = max(pop_fit_max / DIMENSIONALITY, na.rm = TRUE),
    IQR = IQR(pop_fit_max / DIMENSIONALITY, na.rm = TRUE)
)
```

```
## # A tibble: 2 x 8
## Generation count na_cnt min median mean max IQR
## <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> 0.193
## 2 50000 50 0 0.0350 0.229 0.270 1.05 0.243
```

Results for post-hoc Wilcoxon rank-sum test.

```
## Wilcoxon rank sum test with continuity correction
##
## data: filter(interval_df, acro == "ran" & Generation == 50000)$pop_fit_max and fil
## W = 1335, p-value = 0.5602
## alternative hypothesis: true location shift is not equal to 0
```

Chapter 4

Contradictory objectives results

Here we present the results for activation gene coverage and satisfacotory trait coverage found by each selection scheme on the contradictory objectives diagnostic with valley crossing integrated. 50 replicates are conducted for each scheme explored.

4.1 Analysis dependencies

```
library(ggplot2)
library(cowplot)
library(dplyr)
library(PupillometryR)
```

4.2 Data setup

```
DIR = paste(DATA_DIR, 'CONTRADICTORY_OBJECTIVES/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR, 'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$c

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)

best_df <- read.csv(paste(DIR, 'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

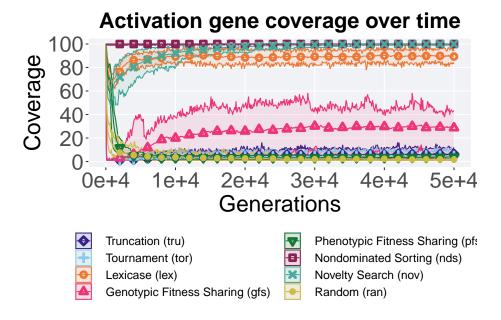
best_df$acro <- factor(best_df$acro, levels = ACRO)
```

4.3 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(uni_str_pos),
   mean = mean(uni_str_pos),
   max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
 ) +
  scale x continuous(
    name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Activation gene coverage over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
  guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
over_time_plot
```



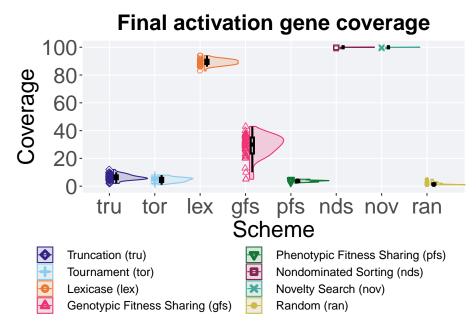
4.4 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.01, height = 0.1), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme + theme(legend.title=element_blank())
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Warning: Removed 46 rows containing missing values (`geom_point()`).



4.4.1 Stats

Summary statistics for the coverage found in the final population.

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','nds','lex','gfs','tor'
act_coverage %>%
group_by(acro) %>%
dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
    min = min(uni_str_pos, na.rm = TRUE),
    median = median(uni_str_pos, na.rm = TRUE),
    mean = mean(uni_str_pos, na.rm = TRUE),
    max = max(uni_str_pos, na.rm = TRUE),
```

IQR = IQR(uni_str_pos, na.rm = TRUE)

```
## # A tibble: 8 x 8
    acro count na_cnt
                                       mean
                                                    IQR
                         min median
                                              max
     <fct> <int> <int> <int> <dbl>
                                      <dbl> <int> <dbl>
## 1 nov
              50
                      0
                           99
                                 100 99.9
                                              100 0
## 2 nds
              50
                      0
                           99
                                 100 100.
                                              100 0
## 3 lex
              50
                      0
                           83
                                  89 89.3
                                               94 3
                                  30 28.7
## 4 gfs
             50
                      0
                            5
                                               43 11.5
## 5 tor
             50
                      0
                            1
                                  5
                                      4.72
                                               8 3
                                               12 2.75
## 6 tru
              50
                      0
                            2
                                     6.28
## 7 pfs
                            2
                                       3.84
                                               5 1
              50
                      0
## 8 ran
              50
                      0
                                       1.72
                                                5 1
Kruskal-Wallis test illustrates evidence of statistical differences.
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
##
## Kruskal-Wallis rank sum test
## data: uni str pos by acro
## Kruskal-Wallis chi-squared = 373.95, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bond")
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               nds
                       lex
                               gfs
                                                       pfs
                                       tor
                                               tru
## nds 1.00
## lex < 2e-16 < 2e-16 -
## gfs < 2e-16 < 2e-16 < 2e-16 -
## tor < 2e-16 < 2e-16 < 2e-16 1.3e-15 -
## tru < 2e-16 < 2e-16 < 2e-16 7.3e-15 1.00
## pfs < 2e-16 < 2e-16 < 2e-16 < 2e-16 0.05
## ran < 2e-16 < 2e-16 < 2e-16 < 2e-16 1.4e-12 1.9e-15 1.8e-12
## P value adjustment method: bonferroni
```

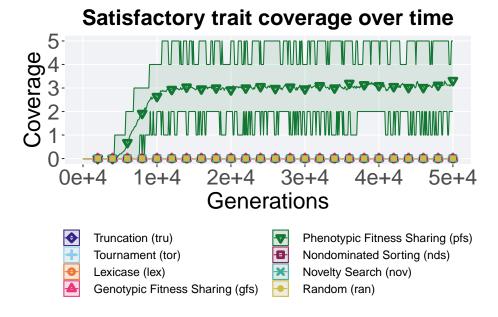
over_time_plot

4.5 Satisfactory trait coverage over time

Satisfactory trait coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(pop_uni_obj),
   mean = mean(pop_uni_obj),
   max = max(pop_uni_obj)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Coverage"
 ) +
  scale x continuous(
    name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
    labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Satisfactory trait coverage over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
  guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
```



4.6 Best satisfactory trait coverage throughout

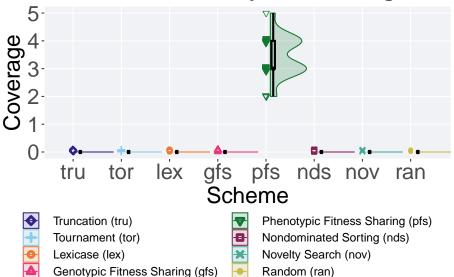
Best satisfactory trait coverage reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_uni_obj') %>%
  ggplot(., aes(x = acro, y = val, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.01, height = 0.1), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 5)
  scale_x_discrete(
   name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best satisfactory trait coverage')+
  p_theme + theme(legend.title=element_blank())
plot_grid(
```

```
plot +
    theme(legend.position="none"),
legend,
nrow=2,
rel_heights = c(3,1)
)
```

Warning: Removed 179 rows containing missing values (`geom_point()`).

Best satisfactory trait coverage



4.6.1 Stats

Summary statistics for the best coverage.

```
sat_coverage = filter(best_df, var == 'pop_uni_obj')
sat_coverage$acro = factor(sat_coverage$acro, levels = c('pfs','nds','lex','gfs','tor'
sat_coverage %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val, na.rm = TRUE),
    median = median(val, na.rm = TRUE),
    mean = mean(val, na.rm = TRUE),
    max = max(val, na.rm = TRUE),
    IQR = IQR(val, na.rm = TRUE)
```

P value adjustment method: bonferroni

```
## # A tibble: 8 x 8
                                                IQR
## acro count na_cnt min median mean
    <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 pfs
           50 0
                         2
                                 3 3.44
                                            5
## 2 nds
            50
                    0
                                 0 0
                          0
                                            0
## 3 lex
                                 0 0
            50
                    0
                          0
                                                  0
                                            0
## 4 gfs
            50
                    0
                          0
                                 0 0
                                            0
## 5 tor
            50
                   0
                          0
                                 0 0
                                            0
## 6 tru
             50
                    0
                          0
                                 0 0
                                            0
                                                 0
## 7 nov
             50
                    0
                          0
                                 0 0
                                            0
                                                 0
## 8 ran
             50
                    0
                                 0 0
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = sat_coverage)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 397.02, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = sat_coverage$val, g = sat_coverage$acro, p.adjust.method = "bonferroni";
                   paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: sat_coverage$val and sat_coverage$acro
##
##
      pfs
            nds lex gfs tor tru nov
## nds <2e-16 -
## lex <2e-16 1
## gfs <2e-16 1
               1
## tor <2e-16 1
                1
                    1
## tru <2e-16 1
                    1
               1
                        1
## nov <2e-16 1 1 1
                        1 1 1
## ran <2e-16 1 1 1
```

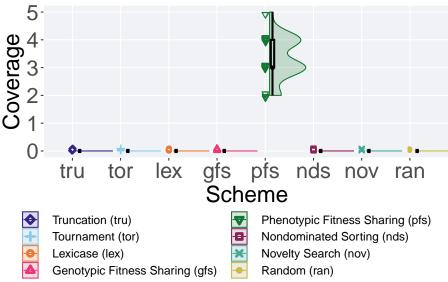
4.7 Final satisfactory trait coverage

Satisfactory trait coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = pop_uni_obj, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = 0.01, height = 0.1), size = 2.0, alpha
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 5)
  ) +
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final satisfactory trait coverage')+
  p_theme + theme(legend.title=element_blank())
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
```

^{##} Warning: Removed 183 rows containing missing values (`geom_point()`).





4.7.1Stats

```
Summary statistics for the coverage found in the final population.
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('pfs','nds','lex','gfs','tor','tru','nov
act_coverage %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(pop_uni_obj)),
    min = min(pop_uni_obj, na.rm = TRUE),
    median = median(pop_uni_obj, na.rm = TRUE),
    mean = mean(pop_uni_obj, na.rm = TRUE),
    max = max(pop_uni_obj, na.rm = TRUE),
    IQR = IQR(pop_uni_obj, na.rm = TRUE)
 )
## # A tibble: 8 x 8
                                                    IQR
     acro count na_cnt
                          min median mean
```

```
<fct> <int> <int> <int>
                              <dbl> <dbl> <int> <dbl>
## 1 pfs
             50
                      0
                            2
                                   3 3.32
## 2 nds
              50
                      0
                            0
                                   0 0
                                               0
                                                     0
                                   0 0
## 3 lex
              50
                                                     0
## 4 gfs
                            0
                                                     0
              50
                      0
```

```
## 5 tor
                50
                         0
                                0
                                        0 0
                                                      0
                                                             0
## 6 tru
                50
                         0
                                0
                                        0
                                           0
                                                      0
                                                             0
                                                             0
## 7 nov
                50
                         0
                                0
                                        0
                                           0
                                                      0
## 8 ran
                50
```

Kruskal–Wallis test illustrates evidence of statistical differences.

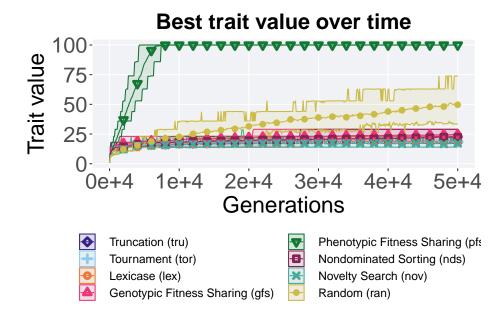
```
kruskal.test(pop_uni_obj ~ acro, data = act_coverage)
##
##
   Kruskal-Wallis rank sum test
##
## data: pop_uni_obj by acro
## Kruskal-Wallis chi-squared = 396.97, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$pop_uni_obj, g = act_coverage$acro, p.adjust.met
                      paired = FALSE, conf.int = FALSE, alternative = '1')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: act_coverage$pop_uni_obj and act_coverage$acro
##
##
              nds lex gfs tor tru nov
       pfs
## nds <2e-16 -
## lex <2e-16 1
## gfs <2e-16 1
                  1
## tor <2e-16 1
                  1
                       1
## tru <2e-16 1
                       1
                           1
                  1
## nov <2e-16 1
                  1
                       1
                           1
                               1
## ran <2e-16 1
                                   1
                  1
                       1
                           1
                               1
##
## P value adjustment method: bonferroni
```

4.8 Best trait value over time

Best trait value in a population over time. Data points on the graph is the average trait value across 50 replicates every 2000 generations. Shading comes from the best and worse trait value across 50 replicates.

```
lines = over_time_df %>%
group_by(scheme, gen) %>%
dplyr::summarise(
   min = min(pop_fit_max),
   mean = mean(pop_fit_max),
   max = max(pop_fit_max)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color = scheme,
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen 1000 == 0 & gen != 0), size = 1.5, stroke = 2.0, alpha =
  scale_y_continuous(
   name="Trait value"
  ) +
  scale_x_continuous(
   name="Generations",
   limits=c(0, 50000),
   breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best trait value over time')+
  p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
  guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
   color=guide_legend(ncol=2, title.position = "bottom"),
   fill=guide_legend(ncol=2, title.position = "bottom")
  )
over_time_plot
```



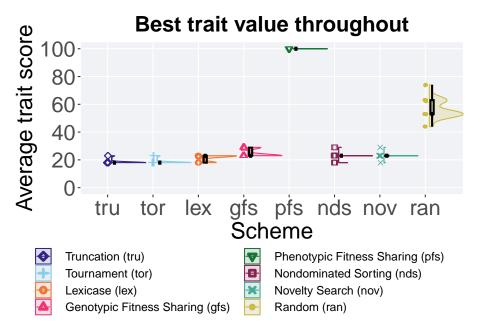
4.9 Best trait value throughout

Best trait value reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha =
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
    name="Average trait score",
    limits=c(0, 100),
    breaks=seq(0,100, 20),
    labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale_x_discrete(
    name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale colour manual(values = cb palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best trait value throughout')+
  p_theme + theme(legend.title=element_blank())
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
)
```

Warning: Removed 18 rows containing missing values (`geom_point()`).



4.9.1 Stats

Summary statistics for the best trait value.

```
trait_val = filter(best_df, var == 'pop_fit_max')
trait_val$acro = factor(trait_val$acro, levels = c('pfs','ran','gfs','nov','nds','lex','tru','ton'
trait_val %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(val)),
    min = min(val, na.rm = TRUE),
    median = median(val, na.rm = TRUE),
    mean = mean(val, na.rm = TRUE),
    max = max(val, na.rm = TRUE),
```

IQR = IQR(val, na.rm = TRUE)

```
## # A tibble: 8 x 8
                                                       IQR
    acro count na_cnt
                          min median mean
                                             max
    <fct> <int> <int> <dbl> <dbl> <dbl> <dbl> <
                                                     <dbl>
                                     100. 100
                      0 100.
                               100
## 1 pfs
              50
                                                 0.000100
## 2 ran
              50
                      0 43.9
                                53.0 56.7 74.0 9.99
## 3 gfs
              50
                      0 23.0
                                23
                                      24.7
                                            29
                                                 5.76
## 4 nov
              50
                      0 18.0
                                23.0 23.0
                                            28.9 0.0528
## 5 nds
              50
                      0 18
                                23
                                      22.4
                                            29 0.00328
## 6 lex
              50
                      0 18
                                22.9 21.5
                                            23
                                                 4.98
## 7 tru
              50
                      0 18.0
                                      18.4 23
                                18
                                                 0
## 8 tor
              50
                      0 18.0
                                18
                                      18.4 23
Kruskal–Wallis test illustrates evidence of statistical differences.
kruskal.test(val ~ acro, data = trait_val)
##
##
  Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 337.68, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = trait_val$val, g = trait_val$acro, p.adjust.method = "bonferro")
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: trait_val$val and trait_val$acro
##
##
                       gfs
       pfs
               ran
                               nov
                                       nds
                                               lex
                                                        tru
## ran < 2e-16 -
                       _
## gfs < 2e-16 < 2e-16 -
## nov < 2e-16 < 2e-16 3.2e-16 -
## nds < 2e-16 < 2e-16 0.00015 1.00000 -
## lex < 2e-16 < 2e-16 3.7e-15 0.00722 1.4e-05 -
## tru < 2e-16 < 2e-16 < 2e-16 4.5e-12 3.0e-11 1.0e-07 -
## tor < 2e-16 < 2e-16 < 2e-16 6.3e-12 7.2e-11 9.4e-08 1.00000
##
## P value adjustment method: bonferroni
```

Chapter 5

Multi-path exploration results

Here we present the results for **best performances** found by each selection scheme on the multi-path exploration diagnostic with valley crossing integrated. 50 replicates are conducted for each scheme explored.

5.1 Analysis dependencies

```
library(ggplot2)
library(cowplot)
library(dplyr)
library(PupillometryR)
```

5.2 Data setup

```
DIR = paste(DATA_DIR, 'MULTIPATH_EXPLORATION/', sep = "", collapse = NULL)

over_time_df <- read.csv(paste(DIR, 'over-time.csv', sep = "", collapse = NULL), header = TRUE, st

over_time_df$uni_str_pos = over_time_df$uni_str_pos + over_time_df$arc_acti_gene - over_time_df$c

over_time_df$scheme <- factor(over_time_df$scheme, levels = NAMES)

over_time_df$acro <- factor(over_time_df$acro, levels = ACRO)

best_df <- read.csv(paste(DIR, 'best.csv', sep = "", collapse = NULL), header = TRUE, stringsAsFace

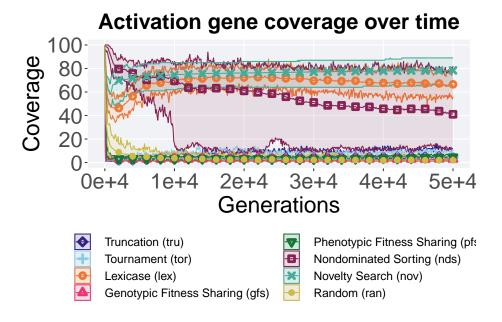
best_df$acro <- factor(best_df$acro, levels = ACRO)
```

5.3 Activation gene coverage over time

Activation gene coverage in a population over time. Data points on the graph is the average activation gene coverage across 50 replicates every 2000 generations. Shading comes from the best and worse coverage across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(uni_str_pos),
    mean = mean(uni_str_pos),
    max = max(uni_str_pos)
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
  geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  ) +
  scale x continuous(
    name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
  ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Activation gene coverage over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
  guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
over_time_plot
```

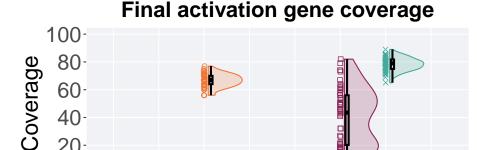


5.4 Final activation gene coverage

Activation gene coverage found in the final population at 50,000 generations.

```
plot = filter(over_time_df, gen == 50000) %>%
  ggplot(., aes(x = acro, y = uni_str_pos, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = 0.01, height = 0.1), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Coverage",
   limits=c(0, 100),
   breaks=seq(0,100, 20),
   labels=c("0", "20", "40", "60", "80", "100")
  scale_x_discrete(
   name="Scheme"
  )+
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Final activation gene coverage')+
  p_theme + theme(legend.title=element_blank())
```

```
plot_grid(
  plot +
    theme(legend.position="none"),
  legend,
  nrow=2,
  rel_heights = c(3,1)
```





5.4.1 Stats

20-

0-

Summary statistics for the coverage found in the final population.

lex

tor

```
act_coverage = filter(over_time_df, gen == 50000)
act_coverage$acro = factor(act_coverage$acro, levels = c('nov','lex','nds','tor','tru'
act_coverage %>%
  group_by(acro) %>%
  dplyr::summarise(
    count = n(),
    na_cnt = sum(is.na(uni_str_pos)),
   min = min(uni_str_pos, na.rm = TRUE),
   median = median(uni_str_pos, na.rm = TRUE),
   mean = mean(uni_str_pos, na.rm = TRUE),
   max = max(uni_str_pos, na.rm = TRUE),
    IQR = IQR(uni_str_pos, na.rm = TRUE)
```

gfs pfs nds nov ran

```
## # A tibble: 8 x 8
                                                     IQR
##
     acro count na_cnt
                           min median mean
                                               max
                                <dbl> <dbl> <int> <dbl>
     <fct> <int> <int> <int>
## 1 nov
              50
                       0
                            65
                                 79
                                       78.4
                                                89 6.75
                                                77 6
## 2 lex
              50
                       0
                            56
                                 67
                                       66.5
## 3 nds
              50
                       0
                            12
                                 43.5 41.0
                                                82 35.8
## 4 tor
              50
                       0
                             1
                                  4
                                        4.4
                                                10 3
                                        4.28
## 5 tru
              50
                       0
                                  4
                                                10 2
                             1
                                        2.88
## 6 gfs
              50
                       0
                             1
                                  3
                                                 5
                                                    1
## 7 pfs
              50
                             2
                                        4.64
                                                 7
                                                    1
                       0
                                  5
## 8 ran
              50
                                  2
                                        1.98
```

Kruskal–Wallis test illustrates evidence of statistical differences.

```
kruskal.test(uni_str_pos ~ acro, data = act_coverage)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: uni_str_pos by acro
## Kruskal-Wallis chi-squared = 333.43, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = act_coverage$uni_str_pos, g = act_coverage$acro, p.adjust.method = "bond")
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
##
   Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: act_coverage$uni_str_pos and act_coverage$acro
##
##
       nov
               lex
                       nds
                                                gfs
                                                        pfs
                               tor
                                        tru
## lex 3.0e-14 -
## nds 1.5e-14 2.0e-09 -
## tor < 2e-16 < 2e-16 < 2e-16 -
## tru < 2e-16 < 2e-16 < 2e-16 1.0000
## gfs < 2e-16 < 2e-16 < 2e-16 0.0032 0.0012
## pfs < 2e-16 < 2e-16 < 2e-16 1.0000 1.0000 1.0000
## ran < 2e-16 < 2e-16 < 2e-16 1.6e-08 1.1e-08 5.8e-05 2.2e-14
## P value adjustment method: bonferroni
```

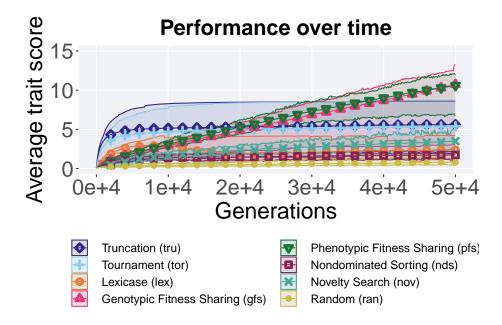
5.5 Performance over time

Best performance in a population over time. Data points on the graph is the average performance across 50 replicates every 2000 generations. Shading comes

from the best and worse performance across 50 replicates.

```
lines = over_time_df %>%
  group_by(scheme, gen) %>%
  dplyr::summarise(
    min = min(pop_fit_max) / DIMENSIONALITY,
    mean = mean(pop_fit_max) / DIMENSIONALITY,
    max = max(pop_fit_max) / DIMENSIONALITY
)
```

```
## `summarise()` has grouped output by 'scheme'. You can override using the
## `.groups` argument.
over_time_plot = ggplot(lines, aes(x=gen, y=mean, group = scheme, fill = scheme, color
  geom_ribbon(aes(ymin = min, ymax = max), alpha = 0.1) +
  geom_line(size = 0.5) +
 geom_point(data = filter(lines, gen %% 2000 == 0 & gen != 0), size = 1.5, stroke = 2
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 15),
 ) +
  scale x continuous(
   name="Generations",
   limits=c(0, 50000),
    breaks=c(0, 10000, 20000, 30000, 40000, 50000),
   labels=c("0e+4", "1e+4", "2e+4", "3e+4", "4e+4", "5e+4")
 ) +
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Performance over time')+
 p_theme + theme(legend.title=element_blank(),legend.text=element_text(size=12)) +
 guides(
    shape=guide_legend(ncol=2, title.position = "bottom"),
    color=guide_legend(ncol=2, title.position = "bottom"),
    fill=guide_legend(ncol=2, title.position = "bottom")
over_time_plot
```

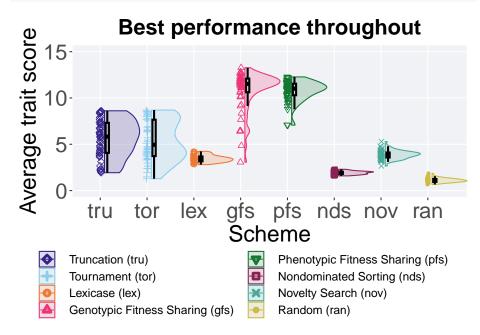


5.6 Best performance throughout

Best performance reached throughout 50,000 generations in a population.

```
plot = filter(best_df, var == 'pop_fit_max') %>%
  ggplot(., aes(x = acro, y = val / DIMENSIONALITY, color = acro, fill = acro, shape = acro)) +
  geom_flat_violin(position = position_nudge(x = .09, y = 0), scale = 'width', alpha = 0.2, width
  geom_boxplot(color = 'black', width = .07, outlier.shape = NA, alpha = 0.0, size = 1.0, position
  geom_point(position = position_jitter(width = .02), size = 2.0, alpha = 1.0) +
  scale_y_continuous(
   name="Average trait score",
   limits=c(0, 15),
  ) +
  scale_x_discrete(
   name="Scheme"
  scale_shape_manual(values=SHAPE)+
  scale_colour_manual(values = cb_palette, ) +
  scale_fill_manual(values = cb_palette) +
  ggtitle('Best performance throughout')+
  p_theme + theme(legend.title=element_blank())
plot_grid(
 plot +
```

```
theme(legend.position="none"),
legend,
nrow=2,
rel_heights = c(3,1)
)
```



5.6.1 Stats

Summary statistics for the best performance.

```
performance = filter(best_df, var == 'pop_fit_max')
performance$acro = factor(performance$acro, levels = c('gfs','pfs','tru','tor','nov',')
performance %>%
    group_by(acro) %>%
    dplyr::summarise(
        count = n(),
        na_cnt = sum(is.na(val)),
        min = min(val / DIMENSIONALITY, na.rm = TRUE),
        median = median(val / DIMENSIONALITY, na.rm = TRUE),
        mean = mean(val / DIMENSIONALITY, na.rm = TRUE),
        max = max(val / DIMENSIONALITY, na.rm = TRUE),
        IQR = IQR(val / DIMENSIONALITY, na.rm = TRUE)
)
```

A tibble: 8 x 8

```
##
    acro count na_cnt
                                                IQR
                        min median mean
                                          max
##
    <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 gfs
             50
                    0 3.07
                             11.5 10.8 13.3 1.48
## 2 pfs
             50
                    0 7.07
                            11.0 10.8 12.3 1.24
## 3 tru
                             5.82 5.61 8.62 3.24
             50
                    0 1.93
## 4 tor
             50
                    0 1.28
                             4.94 5.37 8.69 3.93
## 5 nov
             50
                    0 2.66
                              3.92 3.88 5.29 0.536
## 6 lex
            50
                    0 2.80
                              3.41 3.45 4.23 0.531
## 7 nds
                    0 1.59
                              1.95 1.92 2.30 0.235
            50
## 8 ran
             50
                    0 0.659
                              1.08 1.11 1.86 0.311
```

Kruskal-Wallis test illustrates evidence of statistical differences.

```
kruskal.test(val ~ acro, data = performance)
##
## Kruskal-Wallis rank sum test
##
## data: val by acro
## Kruskal-Wallis chi-squared = 341.54, df = 7, p-value < 2.2e-16
Results for post-hoc Wilcoxon rank-sum test with a Bonferroni correction.
pairwise.wilcox.test(x = performance$val, g = performance$acro, p.adjust.method = "bonferroni",
                     paired = FALSE, conf.int = FALSE, alternative = '1')
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity correction
##
## data: performance$val and performance$acro
##
##
       gfs
               pfs
                       tru
                                tor
                                        nov
                                                lex
                                                        nds
## pfs 0.3635 -
## tru 4.1e-13 5.9e-16 -
## tor 3.2e-13 5.2e-16 1.0000
## nov 1.9e-15 < 2e-16 3.2e-05 0.0055
## lex 1.1e-15 < 2e-16 3.1e-07 1.6e-05 6.3e-05 -
## nds < 2e-16 < 2e-16 2.5e-15 1.2e-13 < 2e-16 < 2e-16 -
## ran < 2e-16 3.5e-16
## P value adjustment method: bonferroni
```