## [Chapter1]

1.4 Using the equations leading to Eq. (1.8) we find

$$V = \frac{\rho I}{2\pi} \left( \frac{1}{s} - \frac{1}{\sqrt{2s}} - \frac{1}{\sqrt{2s}} + \frac{1}{s} \right) = \frac{\rho I}{2\pi} \frac{2 - \sqrt{2}}{s} \Rightarrow \rho = \frac{2\pi s}{2 - \sqrt{2}} \frac{V}{I}$$

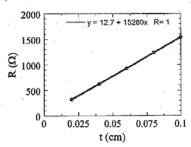


1.5 Using the equations from the notes we find

$$V = \frac{\rho I}{2\pi} \left( \frac{1}{s} - \frac{1}{5s} - \frac{1}{3s} + \frac{1}{3s} \right) = \frac{\rho I}{2\pi} \frac{4}{5s} \Rightarrow \boxed{\rho = 2.5s \frac{V}{I}}$$



1.7 The resistance is given by  $R=\rho t/A + 2\rho_c/A$ . Hence  $\rho=(dR/dt)A$  and  $2\rho_c=R_{intercept}A$ .  $A=7.85\times10^{-5}$  cm<sup>2</sup>. The resistance, plotted as a function of wafer thickness t, is:



From this plot we find

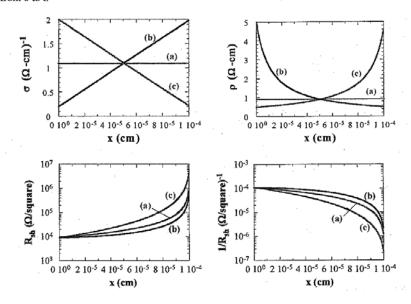
$$\rho = 1.2 \ \Omega \cdot \text{cm}, \ \rho_{\text{c}} = 5 \text{x} 10^{-4} \ \Omega \cdot \text{cm}^2$$

1.15 For an n-type layer on a p-type substrate: (i)  $R_{sh} = \frac{1}{\int_{0}^{t} qn\mu_{n}dx} = \frac{5 \times 10^{15}}{\int_{0}^{t} ndx} = \frac{5 \times 10^{15}}{5.5 \times 10^{15}}$   $R_{sh} = 9.1 \times 10^{3} \Omega / square$ 

(ii) calculate and plot:  $\sigma$  versus x (linear-linear plot),  $\rho$  versus x (linear-linear plot),  $R_{sh}$  versus x (log-linear plot) and  $1/R_{sh}$  versus x (log-linear plot). Use

$$R_{sh} = \frac{1}{\int_{x}^{t} q \mu_{n} n dx} = \frac{1}{\int_{x}^{t} \sigma dx}$$

and let x vary from 0 to t.



$$\rho = \frac{4.532tF(R_{12,34} + R_{23,41})}{2}$$

where F is obtained from the relationship  $\frac{R_r - 1}{R_r + 1} = \frac{F}{\ln(2)} ar \cosh\left(\frac{\exp[\ln(2)/F]}{2}\right)$ 

where  $R_r = R_{12,34}/R_{23,41}$ . For this problem,  $R_r = 74/6 = 12.33$  leading to F = 0.664 and

$$\rho = 6 \Omega \cdot \text{cm}, R_{\text{sh}} = \rho/t = 120 \Omega/\text{square}$$

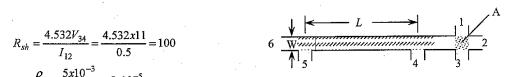
$$R_{sh} = \frac{1}{q\mu_p \int_0^{10^{-4}} 10^{19} e^{-kx} dx} = \frac{6.25 \times 10^{-3} \times 10^5}{1 - e^{-10}} = 625$$

$$V_{34} = \frac{R_{sh}I_{12}}{4.532} = \frac{625 \times 10^{-3}}{4.532} = 0.18; V_{45} = \frac{R_{sh}LI_{16}}{W} = \frac{625 \times 5 \times 10^{-2} \times 10^{-3}}{10^{-3}} = 31.3$$

 $R_{\rm sh} = 625 \ \Omega/{\rm square}, \ V_{34} = 0.18 \ {\rm V}, \ V_{45} = 31.3 \ {\rm V}$ 

1.25 .(a)

$$R_{sh} = \frac{4.532V_{34}}{I_{12}} = \frac{4.532x11}{0.5} = 100$$
$$t = \frac{\rho}{R_{sh}} = \frac{5x10^{-3}}{100} = 5x10^{-5}$$



$$R_{line} = \frac{V_{45}}{I_{26}} = 5x10^4 \Rightarrow W = \frac{R_{sh}L}{R_{line}} = \frac{100x10^{-2}}{5x10^4} = 2x10^{-5}$$

## $R_{\rm sh} = 100 \,\Omega$ /square, $t = 0.5 \,\mu{\rm m}$ , $W = 0.2 \,\mu{\rm m}$

(b) Now we have  $\rho(x) = 0.5x + 0.005$  ohm-cm, with x in cm.

$$R_{ine} = \frac{1}{Wt} \int_{0}^{L} (0.5x + 0.005) dx = 7.5x10^{4}; W_{eff} = \frac{R_{sh}L}{R_{line}} = \frac{100x10^{-2}}{7.5x10^{4}} = 1.33x10^{-5}$$

$$|W_{eff}| = 0.133 \text{ µm}$$

## [Chapter2]

$$\frac{C_{inv}}{C_{ox}} = \frac{1}{1 + \frac{2K_{ox}}{K_s t_{ox}} \sqrt{\frac{K_s \varepsilon_o kT \ln(N_A/n_i)}{qN_A}}}$$

(a) In this problem,  $C_{ox}=C_{ins}$ . With R=0.32,  $K_{ox}=K_{ins}=8$  and  $t_{ox}=t_{ins}=30$  nm, solving the "NA" equation gives:

**(b)** for  $N_A = 10^{16}$  cm<sup>-3</sup>:

 $N_{\rm A} = 1.26 \times 10^{17} \, \rm cm^{-3}$ 

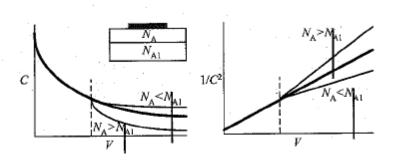
(b) tot 14 to can .

 $C_{\text{inv}}/C_{\text{ins}} = 0.126$ 

(c) Using Eq. (2.19):

 $N_A = 1.41 \times 10^{17} \text{ cm}^{-3}$ 

2.4



2.16 
$$C_p = \frac{C}{(1 + r_s G)^2 + (2\pi f r_s C)^2}; G_p = \frac{G(1 + r_s G) + r_s (2\pi f C)^2}{(1 + r_s G)^2 + (2\pi f r_s C)^2}$$

At high frequencies:  $C_p \approx \frac{C}{(2\pi f r_s C)^2}$ ;  $G_p \approx \frac{1}{r_s} \Rightarrow r_s = 400 \ \Omega$ 

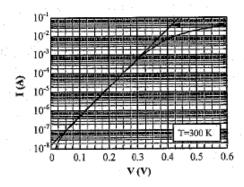
At low frequencies:  $C_p \approx \frac{C}{(1+r_sG)^2}$ ;  $G_p \approx \frac{G}{(1+r_sG)}$ 

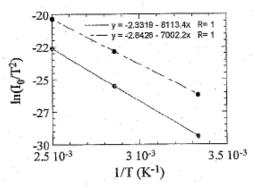
From conductance curve,  $G < 10^{-4} \, S$  at low f, hence,  $r_s G << 1$  and with  $C_p \approx C/(2\pi f r_s C)^2$  at high f. This gives  $C = 125 \, pF$ . From the conductance curve, knowing  $r_s$  and C,  $G = 10^{-5} \, S$ .

$$r_s = 400 \ \Omega$$
,  $C = 125 \ \mathrm{pF}$ ,  $G = 10^{-5} \ \mathrm{S}$ 

## [Chapter3]

3.3 From the I-V curve: Deviation from ideal at I=0.04 A is 0.18 V, leading to  $r_s$ =0.18/0.04=4.5  $\Omega$  Slope=15.2=q/2.3nkT leading to n=1.1.





For low V, we can neglect the "Irs" in the exponent; furthermore, the Io values are obtained by extrapolation to V=0. Hence we have  $I=I_o=AA*T^2\exp(-q\phi_B/kT)\Rightarrow \ln(I/T^2)=\ln(AA*)-q\phi_B/kT$  and a plot of  $\ln(I/T^2)$  vs. 1/T has an intercept of  $\ln(AA*)$  and a slope of  $-q\phi_B/k$ .

For device 1 we have from the intercept  $\ln(AA^*)$ =-2.33 or  $AA^*$ =0.1 leading to  $A^*$ =97 A/cm<sup>2</sup>·K<sup>2</sup>, and from the slope=-8113 we find  $\phi_B$ =-slopek/q giving  $\phi_B$ =0.7 V with q=1.

 $V_{bi} = \phi_B - V_{os} \text{ where } qV_o = E_g/2 - (E_F - E_i). \ E_F - E_i = (kT/q) ln(N_D/n_i) \ giving \ V_o = 0.204 \ V. \ For device 1 \ with \ V = 0, \ V_{bi} = 0.495 \ V \ and \ V_{os} = 0.204 \ V.$ 

 $\Phi_{\rm B1}$ =0.7 V (same as from the I-V data) using the capacitance expression  $C = A \sqrt{\frac{K_s \varepsilon_o q N_D}{2(V_{bi} - V)}}$ 

For 
$$C_2$$
 we have  $C_2 = \frac{A}{2} \left( \sqrt{\frac{K_s \varepsilon_o q N_D}{2(\phi_{B1} - V_o)}} + \sqrt{\frac{K_s \varepsilon_o q N_D}{2(\phi_{B2} - V_o)}} \right) = \frac{C_1}{2} + \frac{A}{2} \sqrt{\frac{K_s \varepsilon_o q N_D}{2(\phi_{B2} - V_o)}}$ 

Substituting numerical values gives Vbi=0.395 V and \$\phi\_{B2}=0.6\$ V.

$$n = 1.1, r_8 = 4.5 \,\Omega, A^* = 97 \,\text{A/cm}^2 \cdot \text{K}^2, \, \phi_{\text{B1}} = 0.7 \,\text{V}, \, \phi_{\text{B2}} = 0.6 \,\text{V}$$

3.13 
$$\ln(I) = \ln(AA * T^2 \exp(-q\phi_B / kT) + \frac{qV}{nkT}; slope = \frac{d \ln(I)}{dV} = \frac{q}{nkT}$$

Since only the slope is affected, it must be caused by a change in diode ideality factor n.

3.17 The TLM test structure below gave the  $R_T$  values in the graph.

(a) Determine R<sub>sh</sub>, R<sub>C</sub>, ρ<sub>C</sub>, and t.

The slope =  $500 = R_{ob}/Z \Rightarrow R_{ob} = 5 \Omega$ /square. The y-intercept is  $2R_c = 0.447 \Rightarrow R_c = 0.224 \Omega$ , the x-intercept is  $2L_T = 8.94 \times 10^{-4}$ 

 $\Rightarrow \rho_c = 10^{-6} \Omega \cdot \text{cm}^2$ . Knowing  $R_{\text{sh}} = 1/q N_D \mu t$  we find  $N_D = 10^{20} \text{ cm}^{-3}$ .

(b) Plot for  $\rho_c = 10^{-7} \Omega \text{-cm}^2$ .

$$R_{\rm sh} = 5 \,\Omega/{\rm square}, R_{\rm c} = 0.224 \,\Omega, \rho_{\rm c} = 10^{-6} \,\Omega{\rm -cm}^2, N_D = 10^{20} \,{\rm cm}^{-3}$$