## **FDTD**

(FDTD)

. Mur

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## **SUMMARY**

We introduce Electromagnetic numerical analysis, FDTD and simulate the electromagnetic field distribution of a microstrip antenna having single patch. We use Mur's absorbing boundary condition, code FDTD and develope a window program simulating the one-patch microstrip antenna.

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1966 K. S. Yee가

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2 FDTD

1) FDTD

FDTD Curl (1)

 $\overrightarrow{\nabla} \times \overrightarrow{E} = \overrightarrow{J_M} - - \frac{\partial \overrightarrow{B}}{\partial t}$ 

 $\overrightarrow{\nabla} \times \overrightarrow{H} = \overrightarrow{J} + \frac{\partial \overrightarrow{D}}{\partial t}$   $\overrightarrow{J}_{M}$ (1)

$$\overrightarrow{D} = \varepsilon \overrightarrow{E}, \ \overrightarrow{B} = \mu \overrightarrow{H}, \ \overrightarrow{J} = \sigma \overrightarrow{E} \qquad \overrightarrow{J}_{M} = \rho' \overrightarrow{H} (\rho' \quad 7)$$

$$(2) \qquad .$$

$$-\frac{\partial \overrightarrow{H}}{\partial t} = -\frac{1}{\mu} \overrightarrow{\nabla} \times \overrightarrow{E} - \rho' \overrightarrow{H}$$

$$-\frac{\partial \overrightarrow{E}}{\partial t} = -\frac{1}{\varepsilon} \overrightarrow{\nabla} \times \overrightarrow{H} - \frac{\sigma}{\varepsilon} \overrightarrow{E} \qquad (2)$$

$$(2) \quad \text{FDTD} \qquad \text{Yee} \qquad \qquad 1 \quad \text{FDTD}$$

Hy
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y

1 Yee

(2)

$$\frac{\partial E_{x}}{\partial t} = -\frac{1}{\varepsilon} \left( \frac{\partial H_{z}}{\partial t} - \frac{\partial H_{y}}{\partial t} \right) - \frac{\sigma}{\varepsilon} E_{x}$$

$$\frac{\partial E_{y}}{\partial t} = -\frac{1}{\varepsilon} \left( \frac{\partial H_{x}}{\partial t} - \frac{\partial H_{z}}{\partial t} \right) - \frac{\sigma}{\varepsilon} E_{y}$$

$$\frac{\partial E_{z}}{\partial t} = -\frac{1}{\varepsilon} \left( \frac{\partial H_{y}}{\partial t} - \frac{\partial H_{x}}{\partial t} \right) - \frac{\sigma}{\varepsilon} E_{z} \tag{3}$$

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$$\frac{\partial H_{x}}{\partial t} = \frac{1}{\mu} \left( \frac{\partial E_{y}}{\partial t} - \frac{\partial E_{z}}{\partial t} \right) - \frac{\rho'}{\mu} H_{x}$$

$$\frac{\partial H_{y}}{\partial t} = \frac{1}{\mu} \left( \frac{\partial E_{z}}{\partial t} - \frac{\partial E_{x}}{\partial t} \right) - \frac{\rho'}{\mu} H_{y}$$

$$\frac{\partial H_{z}}{\partial t} = \frac{1}{\mu} \left( \frac{\partial E_{x}}{\partial t} - \frac{\partial E_{y}}{\partial t} \right) - \frac{\rho'}{\mu} H_{z} \quad (4)$$
(3) (4) FDTD

$$E_{i+\frac{1}{2},j,k}^{n+1} = \frac{\Delta t/\varepsilon}{1+\Delta t\sigma'2\varepsilon} \left[ \frac{1}{\Delta y} \left( H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n+\frac{1}{2}} - H_{i+\frac{1}{2},j-\frac{1}{2},k}^{n+\frac{1}{2}} \right) \right] + \frac{1}{1+\Delta t\sigma'2\varepsilon} E_{i+\frac{1}{2},j,k}^{n}$$

$$- \frac{1}{\Delta z} \left( H_{i+\frac{1}{2},j,k+\frac{1}{2}}^{n+\frac{1}{2}} - H_{i+\frac{1}{2},j,k-\frac{1}{2}}^{n+\frac{1}{2}} \right) + \frac{1}{1+\Delta t\sigma'2\varepsilon} E_{i+\frac{1}{2},j,k}^{n}$$

$$E^{n+1}_{i,j+\frac{1}{2},k} = \frac{\Delta t/\varepsilon}{1+\Delta t} \frac{\varepsilon}{\Delta t} \left[ \frac{1}{\Delta \varepsilon} \left( H^{n+\frac{1}{2}}_{i,j+\frac{1}{2},k+\frac{1}{2}} - H^{n+\frac{1}{2}}_{i+\frac{1}{2},j,k-\frac{1}{2}} \right) \right] - \frac{1}{\Delta t} \left( H^{n+\frac{1}{2}}_{i+\frac{1}{2},j+\frac{1}{2},k} - H^{n+\frac{1}{2}}_{i-\frac{1}{2},j+\frac{1}{2},k} \right) + \frac{1-\Delta t}{\Delta t} \frac{\Delta t}{\Delta t} \frac{\Delta$$

$$E_{i,j,k+\frac{1}{2}}^{n+1} = \frac{\Delta t/\varepsilon}{1+\Delta t} \frac{\varepsilon}{\partial t} \frac{1}{\partial x} \left( H_{i+\frac{1}{2},j,k+\frac{1}{2}}^{n+\frac{1}{2}} - H_{i-\frac{1}{2},j,k+\frac{1}{2}}^{n+\frac{1}{2}} \right) - \frac{1}{\Delta t} \frac{\partial t}{\partial t} \frac{\partial t}{\partial z} \frac{\partial \varepsilon}{\partial z} \left[ H_{i,j+\frac{1}{2},k+\frac{1}{2}}^{n+\frac{1}{2}} - H_{i-\frac{1}{2},j,k+\frac{1}{2}}^{n+\frac{1}{2}} \right] + \frac{1-\Delta t}{1+\Delta t} \frac{\partial t}{\partial t} \frac{\partial \varepsilon}{\partial z} \varepsilon E_{i,j,k+\frac{1}{2}}^{n}$$
 (5)

$$H = \frac{\int \frac{dt}{\mu} \frac{dt}{2}}{1 + \int \frac{dt}{2} \frac{dt}{2} \left[ \frac{1}{\int \frac{dt}{2}} \left( E_{i,j+\frac{1}{2},k+1}^{n} - E_{i,j,k+\frac{1}{2}}^{n} \right) - \frac{1}{\int \frac{dt}{2}} \left( E_{i,j+1,k+\frac{1}{2}}^{n} - E_{i,j,k+\frac{1}{2}}^{n} \right) \right] + \frac{1 - \int \frac{dt}{2} \frac{dt}{$$

$$H_{i+\frac{1}{2},i,k+\frac{1}{2}}^{n+\frac{1}{2}} = \frac{\Delta i / \mu}{1 + \Delta i \rho / 2 \mu} \left[ \frac{1}{\Delta k} (E_{i+1,j,k+\frac{1}{2}}^{n} - E_{i,j,k+\frac{1}{2}}^{n}) \right]$$

$$- \frac{1}{\Delta t} (E_{i+\frac{1}{2},j,k+1}^{n} - E_{i+\frac{1}{2},j,k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i,j+\frac{1}{2},k+\frac{1}{2}}^{n-\frac{1}{2}}$$

$$H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n+\frac{1}{2}} = \frac{\Delta i / \mu}{1 + \Delta i \rho / 2 \mu} \left[ \frac{1}{\Delta t} (E_{i+\frac{1}{2},j+1,k}^{n} - E_{i+\frac{1}{2},j,k}^{n}) - \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) \right] + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) \right] + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) \right] + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) \right] + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) \right] + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i,j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n-\frac{1}{2}}$$

$$- \frac{1}{\Delta t} (E_{i+1,j+\frac{1}{2},k}^{n} - E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}$$

$$- \frac{1}{\Delta t} (E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n} - E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}$$

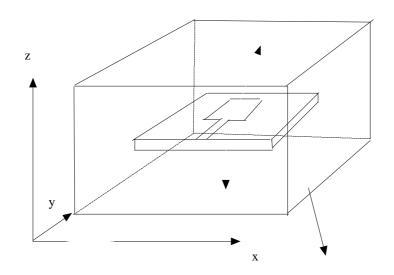
$$- \frac{1}{\Delta t} (E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n} - E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}$$

$$- \frac{1}{\Delta t} (E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n} - E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n}) + \frac{1 - \Delta i \rho / 2 \mu}{1 + \Delta i \rho / 2 \mu} H_{i+\frac{1}{2},k}^{n}$$

$$- \frac{1}{\Delta t} (E_{i+\frac{1}{2},j+\frac{1}{2},k}^{n} - E_{i+\frac{1}$$

 $c\Delta t \leq 1/\sqrt{\frac{1}{(\Delta x)^2} + \frac{1}{(\Delta y)^2} + \frac{1}{(\Delta z)^2}}$ 

FDTD



$$\overrightarrow{\nabla} \cdot \overrightarrow{E} - \frac{1}{c} - \frac{\partial \overrightarrow{E}}{\partial t} \Big|_{boundary} = 0$$
 (8)

(8)

$$\frac{\partial E}{\partial x} - \frac{1}{c} \frac{\partial E}{\partial t} \Big|_{x=0} = 0$$

$$\frac{\partial E}{\partial x} - \frac{1}{c} \frac{\partial E}{\partial t} \Big|_{x=l_x} = 0$$
(9)

(10)

$$E_{0,j,k}^{n+1} = E_{1,j,k}^{n} + \frac{c \Delta t - \Delta x}{c \Delta t + \Delta x} (E_{1,j,k}^{n+1} - E_{0,j,k}^{n})$$

$$E_{l_{x},j,k}^{n+1} = E_{l_{x-1},j,k}^{n} + \frac{c \Delta t - \Delta x}{c \Delta t + \Delta x} (E_{l_{x-1},j,k}^{n+1} - E_{0,j,k}^{n})$$
(10)

y z 7 (11) (12)

$$E_{i,0,k}^{n+1} = E_{i,1,k}^{n} + \frac{c\Delta t - \Delta x}{c\Delta t + \Delta x} (E_{i,1,k}^{n+1} - E_{i,o,k}^{n})$$

$$E_{i,l_{y,k}}^{n+1} = E_{i,l_{y-1},k}^{n} + \frac{c\Delta t - \Delta x}{c\Delta t + \Delta x} (E_{i,l_{y-1},k}^{n+1} - E_{i,l_{y},k}^{n})$$

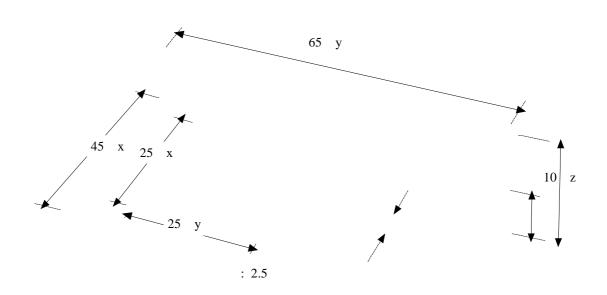
$$E_{i,l_{y,o}}^{n+1} = E_{i,j,1}^{n} + \frac{c\Delta t - \Delta x}{c\Delta t + \Delta x} (E_{i,j,1}^{n+1} - E_{i,j,0}^{n})$$
(11)

 $E_{i,j,l_z}^{n+1} = E_{i,j,l_{z-1}}^{n} + \frac{c\Delta t - \Delta x}{c\Delta t + \Delta x} (E_{i,j,l_{z-1}}^{n+1} - E_{i,j,l_z}^{n})$  (12)

FDTD (5), (6) Mur 1 (10), (11), (12)7

## 3 FDTD

(1)  $3 \qquad . \\ 25 \Delta x \times 25 \Delta y (\text{mm}) \qquad \text{FDTD}$   $45 \Delta x \times 65 \Delta y \times 10 \Delta z \qquad . \\ \varepsilon_r = 2.5 \qquad . \\ 7 \uparrow \qquad \Delta x \times \Delta y \times \Delta z$   $7 \uparrow \qquad \text{mm} \qquad 0.2666 mm \times 0.3188 mm \times 0.1600 mm \qquad .$ 



3:

2)

FDTD 가

가 . (13) 가

가 .

 $g(t, x) = \exp[-(t-t_0-\frac{x-x_0}{v})^2/T^2]$  (13)

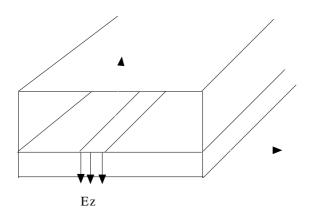
가 가 (14) 가

 $g(t) = \exp[-(t-t_0)^2/T^2]$  (14)

(14)

 $G(f) \propto \exp\left[-\pi^2 T^2 f^2\right]$ 

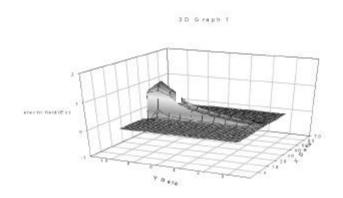
 $\Delta t = 0.341 \times 10^{-12} \text{sec}$   $T = 34 \Delta t$ FDT D



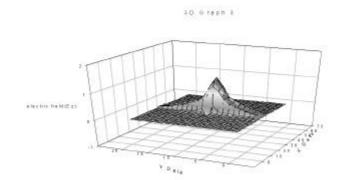
4:

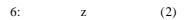
3)  $z \qquad . \qquad 7 + \qquad (5), \ (6), \ (7) \\ 3000 \Delta t = \ 1023 n sec \qquad .$ 

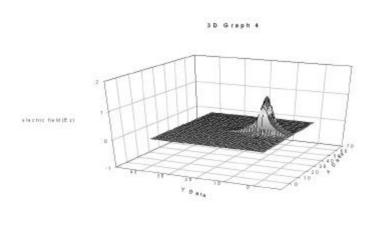
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5: z (1)





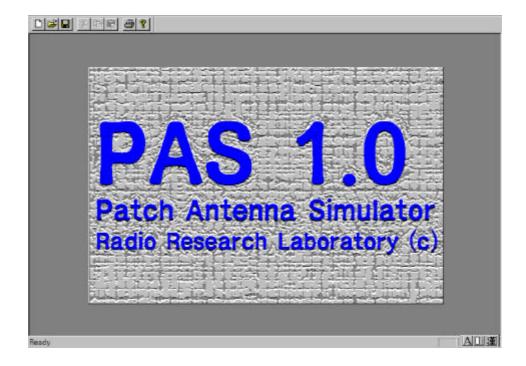


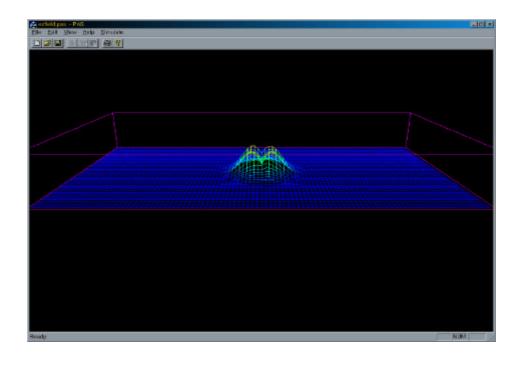
7: z (3)

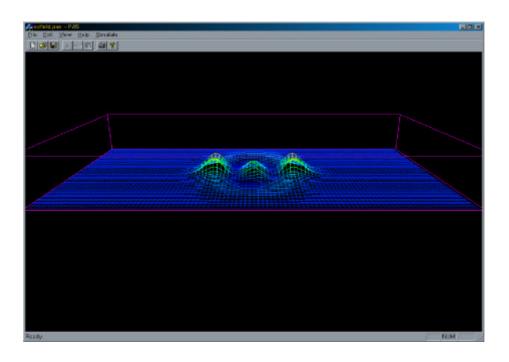
**4**)

가 Visual C++

(8) (9), (10)







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FDTD

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FDTD 가

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- (1) K. S. Yee "Numerical solutions of initial boundary value problems involving Maxwell's equations isotropic media" IEEE Trans. Antennas Propagat. vol. AP-14, pp. 302-307, May 1966.
- (2) Raymond J. Luebbers, Karl S. Kunz, Michael Schneider, Forrest Hunsberger "A finite-difference time domain near zone to far zone transformation" IEEE TRANS. ON ANTENNAS AND PROPAGATION, vol 39, NO.4 pp. 429-433, April 1991
- (3) G. Mur, "Absorbing boundary conditions for the finite difference approximation of the time domain electromagnetic field equation" IEEE Trans. Elec. Comp., vol EMC-32 No. 4. pp.1073-1077 Oct. 1981.
- (4) Kai Fong Lee, Wei Chen "Advance in Microstrip and Printed Antennas" JOHN WIELEY & SONS, INC.
- (5) Karls, Kunz, raymond j. Luebbers "The Finite Difference time Domain Method for Electromagnetics" CRC Press

```
program fdtdmicro
      integer h1,h2,opoint,mt1,wt1,ct1
      parameter(nx=60,ny=100,nz=13)
          parameter(dx=0.389e-3,dy=0.4e-3,dz=0.265e-3)
          parameter(h1=4,h2=7,js=9,opoint=40)
          parameter(mtl=27,wtl=6,ctl=mtl+wtl/2,med=2)
      parameter(ntmax=3000,modmax=100)
          parameter(pie=3.14159265359,c=2.997925e8)
          parameter(e0=8.854185e-12,u0=1.2566371e-6)
          parameter(Rs=50)
      dimension Ex(0:nx,0:ny,0:nz),
     &
                  Ey(0:nx,0:ny,0:nz),
     &
                  Ez(0:nx,0:ny,0:nz),
                 Hx(0:nx,0:ny,0:nz),
     &
                         Hy(0:nx,0:ny,0:nz),
     &
     &
                  Hz(0:nx,0:ny,0:nz),
     &
                  RE(med),ER(med),Vt(ntmax)
                 ! ER : dielectric constant
                      ! med=1 : DIELECTRIC MATERIAL
                     ! med=2 : FREE SPACE
c arrays to store 2 previous time steps on each side
c array format : Xyt(n, ny, nz)
      n = 0 x=0 plane (absorbing boundary)
      n = 1 x=x1 plane
      n = 2 x=Lx-1 plane
      n = 3 x=Lx plane (absorbing boundary)
      t = 0 or 1 to save previous 2 time steps
c Xzt(n, ny, nz) - same but for tangential z component
      dimension Xy0(0:3,0:ny,0:nz)
                ,Xz0(0:3,0:ny,0:nz)
                ,Yx0(0:nx,0:3,0:nz)
                ,Yz0(0:nx,0:3,0:nz)
                Zx0(0:nx,0:ny,0:3)
                ,Zy0(0:nx,0:ny,0:3)
      dimension Xy1(0:3,0:ny,0:nz)
                ,Xz1(0:3,0:ny,0:nz)
     &
     &
                ,Yx1(0:nx,0:3,0:nz)
                ,Yz1(0:nx,0:3,0:nz)
     &
                ,Zx1(0:nx,0:ny,0:3)
     &
                ,Zy1(0:nx,0:ny,0:3)
     &
      data ER/2.5, 1.0/
       dt=c*SQRT(1/dx**2+1/dy**2+1/dz**2)
      dt=0.341e-12
      if(dt.gt.c*SQRT(1/dx**2+1/dy**2+1/dz**2)) \ then \\
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```
print *, 'reset the time'
      endif
      t1=34*dt
      t0=3.*t1
      tg=t0+4.*t1
      rh=dt/u0
      do m=1,med
      RE(m)=dt/(e0*ER(m))
      enddo
c initialization
      do 10 i=0,nx
      do 10 j=0,ny
      do 10 k=0,nz
      Ex(i,j,k)=0.
      Ey(i,j,k)=0.
      Ez(i,j,k)=0.
      Hx(i,j,k)=0.
      Hy(i,j,k)=0.
      Hz(i,j,k)=0.
10
      continue
      do nt=1,ntmax
      Vt(nt)=0.0
      enddo
      print *, 'initialization completed'
      t = 0.0
          open(1,file='ezfild.dat',status='unknown')
      open(0,file='v.dat',status='unknown')
      do 30 nt=1, ntmax ! TIME LOOP
      print *, 'nt=', nt ,Ez(ctl,js,h2-1), Ez(ctl,js+10,h2-1)
c source input
      if(t.le.2*t0) then
          psource=exp(-(t-t0)**2./t1**2.)
      do 332 k=0,nz-1
      do 332 i=0,nx
          if(k.ge.h1.and.k.lt.h2) then
          if(i.ge.mtl.and.i.le.mtl+wtl) then
      Ez(i,js,k)=
c hard source
c include the source resistence
     &+((Hy(i,js,k)-Hy(i-1,js,k))*dy
     & +(Hx(i,js-1,k)-Hx(i,js,k))*dx)*Rs/dz
c soft source
     &+Ez(i,js,k)
```

else

```
Ez(i,js,k)=0.
          endif
          elseif(k.ge.h2) then
          Ez(i,js,k)=0.0
          endif
332 continue
          endif
c Hx step
      do 600 i=0,nx
      do 600 j=0,ny-1
      do 600 k=0,nz-1
      Hx(i,j,k)=Hx(i,j,k)
     &- rh*((Ez(i,j+1,k)-Ez(i,j,k))/dy
     & -(Ey(i,j,k+1)-Ey(i,j,k))/dz)
600 continue
c Hy step
      do 700 i=0,nx-1
      do 700 j=0,ny
      do 700 k=0,nz-1
      Hy(i,j,k)=Hy(i,j,k)
     &- rh*((Ex(i,j,k+1)-Ex(i,j,k))/dz
     & -(Ez(i+1,j,k)-Ez(i,j,k))/dx)
700 continue
c Hz step
      do 800 i=0,nx-1
      do 800 j=0,ny-1
      do 800 k=0,nz
      Hz(i,j,k)=Hz(i,j,k)
     &- rh*((Ey(i+1,j,k)-Ey(i,j,k))/dx
     & -(Ex(i,j+1,k)-Ex(i,j,k))/dy)
800 continue
c Ex step
      do 41 i=1, nx-1
      do 41 j=1, ny-1
      do 41 k=0,h1
      m=2
      Ex(i,j,k)=Ex(i,j,k)
     +RE(m)*((Hz(i,j,k)-Hz(i,j-1,k))/dy
             - (Hy(i,j,k)-Hy(i,j,k-1))/dz)
     continue
      do 42 i=1, nx-1
      do 42 j=1, ny-1
      do 42 k=h1,h2
      m=1
      Ex(i,j,k)=Ex(i,j,k)
     \& + RE(m)*((Hz(i,j,k)-Hz(i,j-1,k))/dy
             - (Hy(i,j,k)-Hy(i,j,k-1))/dz)
     &
     continue
      do 43 i=1, nx-1
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```
do 43 j=1, ny-1
      do 43 k=h2,nz-1
      m=2
      Ex(i,j,k)=Ex(i,j,k)
     +RE(m)*((Hz(i,j,k)-Hz(i,j-1,k))/dy
             -(Hy(i,j,k)-Hy(i,j,k-1))/dz)
43
    continue
c Ey step
      do 51 i=1, nx-1
      do 51 j=1, ny-1
      do 51 k=0,h1
      m=2
      Ey(i,j,k)=Ey(i,j,k)
     +RE(m)*((Hx(i,j,k)-Hx(i,j,k-1))/dz
              - (Hz(i,j,k)- Hz(i- 1,j,k))/dx)
     &
51
     continue
      do 52 i=1, nx-1
      do 52 j=1, ny-1
      do 52 k=h1,h2
      m=1
      Ey(i,j,k)=Ey(i,j,k)
     &+RE(m)*((Hx(i,j,k)- Hx(i,j,k-1))/dz
     &
              - (Hz(i,j,k)-Hz(i-1,j,k))/dx)
52 continue
      do 53 i=1, nx-1
      do 53 j=1, ny-1
      do 53 k=h2,nz-1
      m=2
      {\rm Ey}({\rm i},{\rm j},{\rm k}){=}{\rm Ey}({\rm i},{\rm j},{\rm k})
     +RE(m)*((Hx(i,j,k)-Hx(i,j,k-1))/dz
             - (Hz(i,j,k)-Hz(i-1,j,k))/dx)
53
     continue
c Ez step
      do 61 i=1, nx-1
      do 61 j=1, ny-1
      do 61 k=0,h1
      m=2
      Ez(i,j,k) = Ez(i,j,k)
     \& + RE(m)*((Hy(i,j,k)-Hy(i-1,j,k))/dx\\
              -(Hx(i,j,k)-Hx(i,j-1,k))/dy)
     &
     continue
      do 62 i=1, nx-1
      do 62 j=1, ny-1
      do 62 k=h1,h2
      m=1
      Ez(i,j,k) = Ez(i,j,k)
     +RE(m)*((Hy(i,j,k)-Hy(i-1,j,k))/dx
              -(Hx(i,j,k)-Hx(i,j-1,k))/dy)
62 continue
      do 63 i=1, nx-1
      do 63 j=1, ny-1
```

```
m=2
     Ez(i,j,k)=Ez(i,j,k)
     &+RE(m)*((Hy(i,j,k)-Hy(i-1,j,k))/dx
             -(Hx(i,j,k)-Hx(i,j-1,k))/dy)
63
     continue
c boundary condition for conductors & boundary layer of two medium
     do 73 i=1, nx-1
     do 73 j=1, ny-1
     Ex(i,j,h1)=0.0
     Ey(i,j,h1)=0.0
     if(i.ge.mtl.and.i.lt.mtl+wtl) then
     Ex(i,j,h2)=0.0
     Ey(i,j,h2)=0.0
     elseif (i.lt.mtl.or.i.gt.mtl + wtl) \ then
     Ex(i,j,h2)=Ex(i,j,h2)+2.0*dt/((ER(1)+ER(2))*E0)
     *((Hz(i,j,h2)-Hz(i,j-1,h2))/dy
     & -(Hy(i,j,h2)-Hy(i,j,h2-1))/dz)
     & -(Hy(i,j,h2)-Hy(i-1,j,h2))/dz)
     Ey(i,j,\!h2)\!\!=\!\!Ey(i,\!j,\!h2)\!+\!2.0*dt/((ER(1)\!+\!ER(2))*E0)
     *((Hx(i,j,h2)-Hx(i,j,h2-1))/dz
     &*((Hx(i,j,h2)-Hx(i,j-1,h2))/dz
     & -(Hz(i,j,h2)-Hz(i-1,j,h2))/dx)
         Ey(i,j,h2)=0.0
     endif
73
     continue
CCCCC MUR'S 2ND ORDER ABC CCCCC
c The following need only be done once
     if (nt.eq.1) then
c constants in calculations of surface boundary values
     cx 1=(c*dt-dx)/(c*dt+dx)
     cx 2=(2*dx)/(c*dt+dx)
     cx3=cx2*(c*dt)**2/(4*dy*dy)
     cx4=cx2*(c*dt)**2/(4*dz*dz)
     cy1=(c*dt-dy)/(c*dt+dy)
     cy2=(2*dy)/(c*dt+dy)
     cy3=cy2*(c*dt)**2/(4*dx*dx)
     cy4=cy2*(c*dt)**2/(4*dz*dz)
     cz1=(c*dt-dz)/(c*dt+dz)
     cz2=(2*dz)/(c*dt+dz)
     cz3=cz2*(c*dt)**2/(4*dx*dx)
     cz4=cz2*(c*dt)**2/(4*dy*dy)
         cxy=(c*dt-0.5*sqrt(dx**2+dy**2))
           \&/(c*dt+0.5*sqrt(dx**2+dy**2))
```

do 63 k=h2,nz-1

```
cxz=(c*dt-0.5*sqrt(dx**2+dz**2))
&/(c*dt+0.5*sqrt(dx**2+dz**2))
cyz = (c*dt-0.5*sqrt(dz**2+dy**2))
\&/(c*dt+0.5*sqrt(dz**2+dy**2))
```

## c initialization

do 2 k=0,nz

do 2 j=0,ny

Xy0(0,j,k)=0.

Xy0(1,j,k)=0.

Xy0(2,j,k)=0.

Xy0(3,j,k)=0.

Xy1(0,j,k)=0.

Xy 1(1,j,k)=0.

Xy1(2,j,k)=0.

Xy1(3,j,k)=0.

Xz0(0,j,k)=0.

Xz0(1,j,k)=0.

Xz0(2,j,k)=0.

Xz0(3,j,k)=0.

Xz1(0,j,k)=0.

Xz1(1,j,k)=0.

Xz1(2,j,k)=0.

Xz1(3,j,k)=0.

continue

do 4 k=0,nz

do 4 i=0,nx

Yx0(i,0,k)=0.

Yx0(i,1,k)=0.

Yx0(i,2,k)=0.

Yx0(i,3,k)=0.

Yx1(i,0,k)=0.

Yx1(i,1,k)=0.

Yx1(i,2,k)=0.

Yx1(i,3,k)=0.

Yz0(i,0,k)=0.

Yz0(i,1,k)=0.

Yz0(i,2,k)=0.

Yz0(i,3,k)=0.

Yz1(i,0,k)=0.

Yz1(i,1,k)=0.

Yz1(i,2,k)=0.

Yz1(i,3,k)=0.

continue

do 6 j=0,ny

do 6 i=0,nx

Zx 0(i,j,0)=0.

```
Zx0(i,j,1)=0.
       Zx 0(i,j,2)=0.
       Zx0(i,j,3)=0.
       Zx 1(i,j,0)=0.
       Zx 1(i,j,1)=0.
       Zx 1(i,j,2)=0.
       Zx 1(i,j,3)=0.
       Zy0(i,j,0)=0.
       Zy0(i,j,1)=0.
       Zy0(i,j,2)=0.
       Zy0(i,j,3)=0.
       Zy1(i,j,0)=0.
       Zy1(i,j,1)=0.
       Zy1(i,j,2)=0.
      Zy1(i,j,3)=0.
      continue
       endif
c tangential E fields on the ABS
      do 110 j=1,ny-1
       do 110 k=1,nz-1
c x=0 boundary
      Ey(0,j,k)=-Xy0(1,j,k)
      &+cx1*(Ey(1,j,k)+Xy0(0,j,k))
      x+cx^2(Xy_1(0,j,k)+Xy_1(1,j,k))
      x+cx3*(Xy1(0,j+1,k)-2*Xy1(0,j,k)+Xy1(0,j-1,k)
             + Xy1(1,j+1,k) - 2*Xy1(1,j,k) + Xy1(1,j-1,k)) \\
      -x^4+cx^4+(xy_1(0,j,k+1)-2xy_1(0,j,k)+xy_1(0,j,k-1)
             +Xy1(1,j,k+1)-2*Xy1(1,j,k)+Xy1(1,j,k-1))
      Ez(0,j,k)=-Xz0(1,j,k)
      &+cx1*(Ez(1,j,k)+Xz0(0,j,k))
      \& + cx2*(Xz1(0,j,k) + Xz1(1,j,k))
      \& + cx3*(Xz1(0,j+1,k)-2*Xz1(0,j,k)+Xz1(0,j-1,k)
             +Xz1(1,j+1,k)-2*Xz1(1,j,k)+Xz1(1,j-1,k))
      \& + cx4*(Xz1(0,j,k+1)-2*Xz1(0,j,k)+Xz1(0,j,k-1)
             + Xz1(1,j,k+1) - 2*Xz1(1,j,k) + Xz1(1,j,k-1)) \\
c x=Lx boundary
      Ey(nx,j,k)=-Xy0(2,j,k)
      &+cx1*(Ey(nx-1,j,k)+Xy0(3,j,k))
      \& + cx2*(Xy1(3,j,k) + Xy1(2,j,k))\\
      -x^{2}(Xy_{1}(3,j+1,k)-2Xy_{1}(3,j,k)+Xy_{1}(3,j-1,k)
             +Xy1(2,j+1,k)-2*Xy1(2,j,k)+Xy1(2,j-1,k))
      \& + cx4*(Xy1(3,\!j,\!k\!+\!1) - 2*Xy1(3,\!j,\!k\!) + Xy1(3,\!j,\!k\!-\!1)
             + Xy1(2,j,k+1) - 2*Xy1(2,j,k) + Xy1(2,j,k-1)) \\
      Ez(nx,j,k)=-Xz0(2,j,k)
      &+cx1*(Ez(nx-1,j,k)+Xz0(3,j,k))
      \& + cx2*(Xz1(3,\!j,\!k) + Xz1(2,\!j,\!k))
```

```
&+cx3*(Xz1(3,j+1,k)-2*Xz1(3,j,k)+Xz1(3,j-1,k)
            +Xz1(2,j+1,k)-2*Xz1(2,j,k)+Xz1(2,j-1,k))
     &+cx4*(Xz1(3,j,k+1)-2*Xz1(3,j,k)+Xz1(3,j,k-1)
            +Xz1(2,j,k+1)- 2*Xz1(2,j,k)+Xz1(2,j,k-1))
110 continue
        do 210 i=1.nx-1
        do 210 k=1,nz-1
c y=0 boundary
      Ex(i,0,k) = -Yx0(i,1,k)
     &+cy1*(Ex(i,1,k)+Yx0(i,0,k))
     &+cy2*(Yx1(i,0,k)+Yx1(i,1,k))
     &+cy3*(Yx1(i+1,0,k)-2*Yx1(i,0,k)+Yx1(i-1,0,k)
            +Yx1(i+1,1,k)-2*Yx1(i,1,k)+Yx1(i-1,1,k)
     &+cy4*(Yx1(i,0,k+1)-2*Yx1(i,0,k)+Yx1(i,0,k-1)
            +Yx1(i,1,k+1)-2*Yx1(i,1,k)+Yx1(i,1,k-1)
      Ez(i,0,k)=-Yz0(i,1,k)
     &+cy1*(Ez(i,1,k)+Yz0(i,0,k))
     -x+cy^2(Yz_1(i,0,k)+Yz_1(i,1,k))
     x+cy3*(Yz1(i+1,0,k)-2*Yz1(i,0,k)+Yz1(i-1,0,k)
            +Yz1(i+1,1,k)-2*Yz1(i,1,k)+Yz1(i-1,1,k))
     -x^{+}cy^{4*}(Yz_{1}(i,0,k+1)-2*Yz_{1}(i,0,k)+Yz_{1}(i,0,k-1)
            +Yz1(i,1,k+1)-2*Yz1(i,1,k)+Yz1(i,1,k-1))
c y=Ly boundary
      Ex(i,ny,k) = -Yx0(i,2,k)
     &+cy1*(Ex(i,ny-1,k)+Yx0(i,3,k))
     x+cy2*(Yx1(i,2,k)+Yx1(i,3,k))
     x+cy3*(Yx1(i+1,3,k)-2*Yx1(i,3,k)+Yx1(i-1,3,k)
            +Yx1(i+1,2,k)-2*Yx1(i,2,k)+Yx1(i-1,2,k)
     x+cy4*(Yx1(i,3,k+1)-2*Yx1(i,3,k)+Yx1(i,3,k-1)
           +Yx1(i,2,k+1)-2*Yx1(i,2,k)+Yx1(i,2,k-1)
      Ez(i,ny,k)=-Yz0(i,2,k)
     -x+cy1*(Ez(i,ny-1,k)+Yz0(i,3,k))
     -x+cy^2(Yz_1(i,2,k)+Yz_1(i,3,k))
     x+cy3*(Yz1(i+1,3,k)-2*Yz1(i,3,k)+Yz1(i-1,3,k)
            +Yz1(i+1,2,k)-2*Yz1(i,2,k)+Yz1(i-1,2,k))
     x+cy4*(Yz1(i,3,k+1)-2*Yz1(i,3,k)+Yz1(i,3,k-1)
           +Yz1(i,2,k+1)-2*Yz1(i,2,k)+Yz1(i,2,k-1))
     &
210 continue
      do 310 i=1,nx-1
      do 310 j=1,ny-1
c z=0 boundary
      Ex(i,j,0)=-Zx0(i,j,1)
     -x+cz1*(Ex(i,j,1)+Zx0(i,j,0))
     &+cz2*(Zx1(i,j,0)+Zx1(i,j,1))
     \& + cz3*(Zx1(i+1,j,0)-2*Zx1(i,j,0)+Zx1(i-1,j,0)
           +Zx 1(i+1,j,1)-2*Zx 1(i,j,1)+Zx 1(i-1,j,1))
     x+cz4*(Zx1(i,j+1,0)-2*Zx1(i,j,0)+Zx1(i,j-1,0)
```

```
+Zx 1(i,j+1,1)-2*Zx 1(i,j,1)+Zx 1(i,j-1,1))
       Ey(i,j,0)=-Zy0(i,j,1)
       -x+cz1*(Ey(i,j,1)+Zy0(i,j,0))
       +cz2*(Zy1(i,j,0)+Zy1(i,j,1))
       -x^2+cz^3+(zy_1(i+1,j,0)-z^2+zy_1(i,j,0)+zy_1(i-1,j,0)
               + Zy \, \mathbf{1}(i+1,j,1) \text{--} \, 2*Zy \, \mathbf{1}(i,j,1) + Zy \, \mathbf{1}(i\text{--} \, 1,j,1))
       -x^2+cz^4+(zy_1(i,j+1,0)-z^2+zy_1(i,j,0)+zy_1(i,j-1,0)
               +Zy 1(i,j+1,1)-2*Zy 1(i,j,1)+Zy 1(i,j-1,1))
c z=Lz boundary
       Ex(i,j,nz)=-Zx0(i,j,2)
       &+cz1*(Ex(i,j,nz-1)+Zx0(i,j,3))
       &+cz2*(Zx1(i,j,2)+Zx1(i,j,3))
      &+cz3*(Zx1(i+1,j,3)-2*Zx1(i,j,3)+Zx1(i-1,j,3)
               +Zx 1(i+1,j,2)-2*Zx 1(i,j,2)+Zx 1(i-1,j,2))
      x+cz4*(Zx1(i,j+1,3)-2*Zx1(i,j,3)+Zx1(i,j-1,3)
               + Zx \, \mathbf{1}(i,\!j\!+\!1,\!2) \text{--} \, 2*Zx \, \mathbf{1}(i,\!j,\!2) + Zx \, \mathbf{1}(i,\!j\!-\!1,\!2))
       Ey(i,j,nz){=-}\,Zy0(i,j,2)
      &+cz1*(Ey(i,j,nz-1)+Zy0(i,j,3))
      \& + cz2*(Zy1(i,j,2) + Zy1(i,j,3))
       +Zy 1(i+1,j,2)-2*Zy 1(i,j,2)+Zy 1(i-1,j,2))
       -x+cz4*(Zy1(i,j+1,3)-2*Zy1(i,j,3)+Zy1(i,j-1,3)
               +Zy 1(i,j+1,2)-2*Zy 1(i,j,2)+Zy 1(i,j-1,2))
310 continue
c edges
c parallel to x-axis
       do i=0,nx-1
        Ex(i,0,0)=0.5*(Zx1(i,1,0)+Yx1(i,0,1))
             x+cyz*(0.5*(Ex(i,1,0)+Ex(i,0,1))-Yx1(i,0,0))
       Ex(i,0,nz)=0.5*(Zx1(i,1,3)+Yx1(i,0,nz-1))
             &+cyz*(0.5*(Ex(i,0,nz-1)+Ex(i,1,nz))-Yx1(i,0,nz))
             Ex(i,ny,0)=0.5*(Zx1(i,ny-1,0)+Yx1(i,3,1))
             +cyz*(0.5*(Ex(i,ny-1,0)+Ex(i,ny,1))-Yx1(i,3,0))
             Ex(i,ny,nz)=0.5*(Zx1(i,ny-1,3)+Yx1(i,3,nz-1))
             \& + cyz*(0.5*(Ex(i,\!ny,\!nz\!-1) + Ex(i,\!ny\!-1,\!nz)) - Yx1(i,\!3,\!nz))\\
        enddo
c parallel to y-axis
       do j=0,ny-1
        {\rm Ey}(0,\!j,\!0){=}0.5{*}({\rm Zy1}(1,\!j,\!0){+}{\rm Xy1}(0,\!j,\!1))
             &+cxz^*(0.5^*(Ey(0,j,1)+Ey(1,j,0))-Xy1(0,j,0))
             Ey(0,j,nz)=0.5*(Zy1(1,j,3)+Xy1(0,j,nz-1))
             \& + cxz*(0.5*(Ey(1,j,nz) + Ey(0,j,nz-1)) - Xy1(0,j,nz))
             Ey(nx,j,0)=0.5*(Zy1(nx-1,j,0)+Xy1(3,j,1))
             &+\operatorname{cx} z^*(0.5^*(\operatorname{Ey}(\operatorname{nx-1,j,0})+\operatorname{Ey}(\operatorname{nx,j,1}))-\operatorname{Xy1}(3,j,0))
             Ey(nx.j.,nz) = 0.5*(Zy1(nx-1.j.3) + Xy1(3.j.,nz-1))
             \& + cxz^*(0.5^*(Ey(nx-1,j,nz) + Ey(nx,j,nz-1)) - Xy1(3,j,nz))\\
        enddo
```

```
c parallel to z-axis
      do k=0,nz-1
       Ez(0,0,k)=0.5*(Xz1(0,1,k)+Yz1(1,0,k))
            &+cxy*(0.5*(Ez(0,1,k)+Ez(1,0,k))-Yz1(0,0,k))
            Ez(nx,0,k)=0.5*(Xz1(3,1,k)+Yz1(nx-1,0,k))
            &+cxy*(0.5*(Ez(nx-1,0,k)+Ez(nx,1,k))-Yz1(nx,0,k))
            Ez(0,ny,k)=0.5*(Xz1(0,ny-1,k)+Yz1(1,3,k))
            &+\operatorname{cxy}^*(0.5^*(\operatorname{Ez}(0,\operatorname{ny-1},k)+\operatorname{Ez}(1,\operatorname{ny},k))-\operatorname{Yz}1(0,3,k))
           Ez(nx,ny,k)=0.5*(Xz1(3,ny-1,k)+Yz1(nx-1,3,k))
            \& + cxy*(0.5*(Ez(nx,ny-1,k) + Ez(nx-1,ny,k)) - Yz1(nx,3,k))\\
       end do \\
c Now that we've calulated the n+1 time step value on all surfaces,
c copy these into the arrays that store the previous time steps :
       do 400 j=0,ny
       do 400 k=0,nz
       Xy0(0,j,k)=Xy1(0,j,k)
       Xy0(1,j,k)=Xy1(1,j,k)
       Xy0(2,j,k)=Xy1(2,j,k)
       Xy0(3,j,k)=Xy1(3,j,k)
       Xy1(0,j,k)=Ey(0,j,k)
       Xy1(1,j,k)=Ey(1,j,k)
       Xy1(2,j,k)=Ey(nx-1,j,k)
       Xy1(3,j,k)=Ey(nx,j,k)
       Xz0(0,j,k)=Xz1(0,j,k)
       Xz0(1,j,k)=Xz1(1,j,k)
       Xz0(2,j,k)=Xz1(2,j,k)
       Xz0(3,j,k)=Xz1(3,j,k)
       Xz1(0,j,k)=Ez(0,j,k)
       Xz1(1,j,k)=Ez(1,j,k)
       Xz1(2,j,k)=Ez(nx-1,j,k)
       Xz1(3,j,k)=Ez(nx,j,k)
400 continue
       do 410 i=0.nx
       do 410 k=0,nz
       Yx0(i,0,k)=Yx1(i,0,k)
       Yx0(i,1,k)=Yx1(i,1,k)
       Yx0(i,2,k)=Yx1(i,2,k)
       Yx0(i,3,k)=Yx1(i,3,k)
       Yx1(i,0,k)=Ex(i,0,k)
       Yx1(i,1,k)=Ex(i,1,k)
       Yx1(i,2,k)=Ex(i,ny-1,k)
       Yx1(i,3,k)=Ex(i,ny,k)
       Yz0(i,0,k)=Yz1(i,0,k)
       Yz0(i,1,k)=Yz1(i,1,k)
       Yz0(i,2,k)=Yz1(i,2,k)
```

```
Yz0(i,3,k)=Yz1(i,3,k)
      Yz1(i,0,k)=Ez(i,0,k)
       Yz1(i,1,k)=Ez(i,1,k)
       Yz1(i,2,k)=Ez(i,ny-1,k)
       Yz1(i,3,k)=Ez(i,ny,k)
410
      continue
       do 420 i=0,nx
      do 420 j=0,ny
      Zx 0(i,j,0)=Zx 1(i,j,0)
      Zx0(i,j,1)=Zx1(i,j,1)
      Zx 0(i,j,2)=Zx 1(i,j,2)
      Zx 0(i,j,3)=Zx 1(i,j,3)
      Zx1(i,j,0)=Ex(i,j,0)
      Zx1(i,j,1)=Ex(i,j,1)
      Zx 1(i,j,2)=Ex(i,j,nz-1)
      Zx1(i,j,3)=Ex(i,j,nz)
      Zy0(i,j,0)=Zy1(i,j,0)
      Zy0(i,j,1) \hspace{-0.05cm}=\hspace{-0.05cm} Zy1(i,j,1)
      Zy0(i,j,2)=Zy1(i,j,2)
      Zy0(i,j,3)=Zy1(i,j,3)
      \operatorname{Zy1}(i,j,0) {=} \operatorname{Ey}(i,j,0)
      Zy1(i,j,1)=Ey(i,j,1)
      Zy1(i,j,2)=Ey(i,j,nz-1)
       Zy1(i,j,3)=Ey(i,j,nz)
420
      continue
           !!! TOTAL VOLTAGE Vt(nt) (INPUT+REFLECTION)
      do 99 k=h1+1,h2
       Vt(nt)=Vt(nt)+Ez(ctl,opoint,k)
99
      continue
           write(0,130) nt, Vt(nt)
      do 66 j=0,ny
      do 66 i=0,nx
      if(mod(nt,modmax).eq.0) then
      write(1,150) nt,i, j, Ez(i,j,h2-1)
      endif
66
      continue
      t=t+dt
      continue
                  ! nt (time) LOOP
       ******************
130
      format(i7,f20.10)
      format(4i7,f20.10)
140
150
      format(3i7, f20.10)
130
      format(i7,f20.10)
      close(0)
```

close(1)

stop

end