

Algorithm to find minimal media for a metabolic model

Joshua Goldford

Introduction

This is a document describing a mixed-integer linear program to find a minimal media set for metabolic model.

Defs

Let S be an $m \in \mathcal{M}$ by $n \in \mathcal{N}$ stoichiometric matrix, where \mathcal{M} and \mathcal{N} are the sets of metabolites and reactions, respectively. Let v represent the vector of fluxes with some lower bound and upper bound vectors l and u , respectively. For a subset of reactions $\mathcal{U} \in \mathcal{N}$, let \mathcal{U} represent the set of uptake (or exchange reactions), and z_k represent the binary variable, where when $z_k = 1$, uptake reaction $k \in \mathcal{U}$ is required for growth and $z_k = 0$, it is not. For each k , we can enforce this by imposing the following constraint:

$$l_k z_k < v_k < u_k \quad (1)$$

When $z_k = 1$, $v_k \geq lb$, otherwise $v_k \geq 0$, which means there is no uptake flux through reaction k . If we constrain the biomass growth rate to some minimum value μ_{\min} , then the full program is:

$$\begin{aligned} & \underset{v, z}{\text{minimize}} && \sum_k z_k \\ & \text{subject to} && \sum_i s_{ij} v_i = 0, \forall j \in \mathcal{M} \\ & && l_k z_k - v_k \leq 0 \forall k \in \mathcal{U} \\ & && lb_i < v_i < ub_i, \forall i \in \mathcal{N} \\ & && v_{\text{biomass}} > \mu_{\min} \end{aligned}$$