

La aproximación se expresa como

$$\ln n! \approx n \ln n - n$$

La fórmula de Stirling está dada por:

que se reescribe frecuentemente como:

$$\lim_{n \rightarrow \infty} \frac{n!}{\sqrt{2\pi n} \left(\frac{n}{e}\right)^n} = 1 \qquad n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

$$n! \cong \sqrt{2n} \cdot n^{n+1/2} e^{-n}$$

Una acotación de la fórmula es:


$$\sqrt{2\pi n} \left(\frac{n}{e}\right)^n e^{\frac{1}{12n+1}} < n! < \sqrt{2\pi n} \left(\frac{n}{e}\right)^n e^{\frac{1}{12n}}$$

COMBINATORIA

$$\binom{n}{k} = \binom{n}{n-k}$$

$$\binom{n}{0} + \binom{n}{1} + \cdots + \binom{n}{k} + \cdots + \binom{n}{n} = 2^n$$

$$\binom{n}{0} \binom{n}{n} + \binom{n}{1} \binom{n}{n-1} + \cdots + \binom{n}{n} \binom{n}{0} = \binom{2n}{n}$$


$$\sum_{k=0}^n \binom{n}{k} \binom{n}{n-k} = \binom{2n}{n}$$

$$\sum_{k=0}^{m-1} \binom{m}{k} \binom{n-1}{m-k-1} = \binom{n+m-1}{n}$$

$$\binom{n-1}{k} + \binom{n-2}{k-1} + \cdots + \binom{n-k-1}{0} = \binom{n}{k}$$