

Autofocals: Evaluating Gaze-Contingent Eyeglasses for Presbyopes

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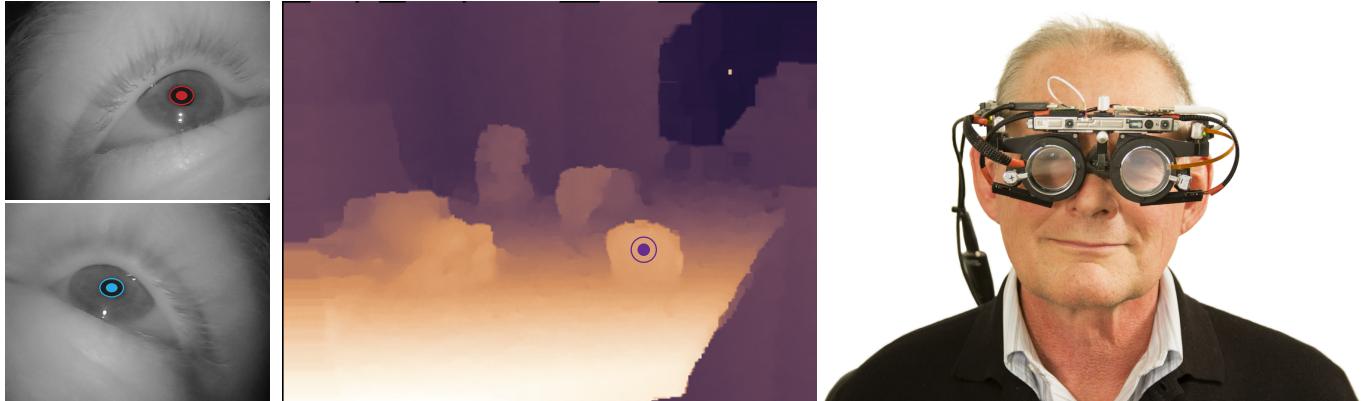


Fig. 1. We present Autofocals, a hardware and software solution for presbyopes (those with an age-related loss of accommodation) that externally mimics the natural accommodation response. With eye trackers and a depth sensor, the system estimates the vergence and gaze direction (left), and scene depth (middle). A sensor fusion algorithm combines these inputs to estimate the fixation distance of the wearer, then brings it into focus using focus-tunable lenses. In contrast to current presbyopia corrections, which either require head movement or reduce visual quality at near distances, our study shows that a user wearing Autofocals (right) can intuitively look to any distance, while maintaining 20/20 acuity.

Presbyopia, the loss of accommodation due to the stiffening of the crystalline lens, affects nearly 20% of the population worldwide. Traditional forms of presbyopia correction use fixed focal elements that inherently trade off field of view or stereo vision for a greater range of distances at which the wearer can see clearly. However, none of these offer the same natural refocusing enjoyed in youth. In this work, we built a new presbyopia correction, dubbed Autofocals, which externally mimics the natural accommodation response by combining data from eye trackers and a depth sensor, and then automatically drives focus-tunable lenses. We evaluated the Autofocals on 24 users (ages 51–81) across a set of visual and task performance metrics: visual acuity, contrast sensitivity, and letter matching. We observed that the Autofocals exhibit significantly better visual acuity at nearer distances when compared to both monovision and progressive lenses, while not sacrificing 20/20 visual acuity at any other distance. No significant difference was observed with respect to contrast sensitivity or task performance. When asked to compare the Autofocals against their own correction in terms of being able to effectively see at all distances, 7 out of 11 participants rated Autofocals higher, with another 2 rating them equivalent.

CCS Concepts: • Human-centered computing → User studies; Accessibility technologies; • Hardware → Sensor applications and deployments;

Additional Key Words and Phrases: presbyopia, computational optometry

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1 INTRODUCTION

Vision is one of the most, if not the most, important senses that humans use to navigate their everyday worlds. Unfortunately, as people age, their ability to accommodate, or refocus the crystalline

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lenses in their eyes to near distances, steadily decreases until most cannot view anything within arms' reach in sharp focus [Duane 1912]. This loss in range of clear vision is known as presbyopia and affects over a billion people worldwide [Holden et al. 2008], with the number guaranteed to grow as the population ages [UN DESA 2017]. People are typically diagnosed with presbyopia by their late 40s. Furthermore, despite impairment, vision gains even more importance in old age, as people rely more on their vision to compensate for degradation of the vestibular or somatosensory system, leading to an increase in falls [Newton 2003].

The problem of presbyopia is understandably not a new one, and people have used various solutions to help them perform tasks at near distances (Figure 2). For example, a simple solution is to carry an extra pair of reading glasses that allow for near vision. In order to avoid the inconvenience of carrying a second set of glasses, many people opt for corrections that can support multiple distances of focus. Bifocals, trifocals, or progressive addition lenses achieve this by assigning different parts of the field of view to different distances. Monovision lenses achieve this by assigning each eye to a different distance. Another option is simultaneous vision lenses, which involve presenting near- and far-corrected visual information superimposed via multifocal lenses. This can be achieved, for example, with concentric or diffractive contact lenses directly over the pupil. Charman [2014] provides a detailed overview of these and other approaches to presbyopia correction.

Despite the variety of vision correction options available to presbyopes, these all fall short of restoring the quality of vision they once enjoyed in their youth. Reading glasses, besides the relative inconvenience, can also be forgotten or misplaced, rendering the wearer incapable of performing near tasks for an extended period. Bifocals, trifocals, and progressives restrict the field of view at any

given desired focal distance and introduce distortions in regions where the refractive power transitions. Lord et al. [2002] showed that these types of glasses impair depth perception and edge-contrast sensitivity, leading to an increased risk when navigating unfamiliar environments or stairs, and recommend using single focal length glasses in such situations – a recommendation which, if followed, negates the convenience of these glasses. As for monovision and the various simultaneous vision approaches, studies consistently show that they too fall short of reading glasses for visual acuity or stereoacuity, with some prospective wearers rejecting them entirely due to poor or unnatural vision [Back et al. 1992; Erickson and Schor 1990; Harris et al. 1992; Sheedy et al. 1991, 1988].

The common thread across these methods is that they use fixed focal elements to approximate vision that was once achieved by varifocal lenses in the wearer’s eyes. A natural response when presented with this fact is to consider using a varifocal element in the corrective eyewear. An early implementation of lenses with tunable power was the Alvarez lens, which required mechanical shifting [Alvarez 1967]. Since then, people have developed prototypes of electronically tunable eyewear using liquid-crystal diffractive lenses or liquid-filled membranes, controllable via either manual input or a depth sensor [Hasan et al. 2017b; Li et al. 2006; Wang et al. 2014]. However, none of these solutions emulate accommodation in a way that matches the behavior that younger people are accustomed to: simply looking around and having focus just work. A system capable of meeting this ideal would require both a depth camera and robust, affordable eye trackers. For example, despite having a depth sensor, Hasan et al. [2017b] omit eye tracking and therefore force the focus to the object directly in the center of the user’s vision, which can be less than ideal. Furthermore, none of these solutions have been evaluated or verified as outperforming traditional fixed-focus methods of correction.

Therefore, we ask the question of whether or not this class of focus-tunable glasses solutions can match or outperform traditional fixed-focus correction along both visual and task-based performance metrics. To test this, we build our own focus-tunable glasses implementation; we incorporate both a wide field of view depth sensor and vergence measurements from eye tracking to estimate the best focal setting for the tunable lenses (Figure 2). With this system, we compare our performance against that of commonly prescribed treatments. Our contributions are therefore that

- we developed a complete hardware and software solution that externally simulates an accurate accommodation response by intelligently driving a focus-tunable optic;
- we developed a sensor fusion algorithm for integrating data from an eye tracker and depth camera and for vergence estimation; and
- we verify that Autofocals are preferred over the traditional methods of treating presbyopia and identify critical areas for technological improvement with a user study.

2 RELATED WORK

2.1 Focus-Tunable Optics

The class of technologies that make true presbyopia correction a tangible possibility is focus-tunable lenses. One of the earlier works



Fig. 2. Typical vision for a presbyope through various methods of correction. Without any correction, near distances are blurry. Progressives and monovision allow focus to both near and far distances by either splitting up the field of view, or using different eyes for each distance, as illustrated. The Autofocals use information from each eye’s gaze to dynamically update the focus to near or far.

in this space was the Alvarez lenses [Alvarez 1967]. These lenses consist of a pair of cubic phase lenses that have complementary correction to one another – when overlapped, they have no refractive power, and shifting one relative to the other can introduce both positive or negative powers. However, this design is not ideal since mechanical components tend to wear down faster, and more extreme powers inherently reduce field of view as the overlapping region of the lenses is reduced.

Since then, there has been much effort made to develop wide field-of-view lenses for use in presbyopic correction. Two main categories that these lenses fall into include liquid-crystal lenses and liquid-filled membrane lenses. In the space of liquid lenses, there have been proposals such as using a liquid lens mounted on a polydimethylsiloxane (PDMS) contact lens [Jiang and Kanhere 2015], but also work put into creating functional larger lenses for eyeglasses-based correction [Hasan et al. 2017a]. Liquid-crystal

229 lenses, on the other hand, may be more flexible in that they can
 230 directly address phase across the field of view, allowing for more
 231 varied corrections with a single element, with much recent work
 232 on making them a more viable option for eyeglasses, improving
 233 focusing time and addressable range [Chen et al. 2014; Lin and Chen
 234 2013; Lin et al. 2014]. Another possible approach involves using a
 235 deformable mirror. Papadatou et al. [2016] for example used one to
 236 create and test simultaneous vision correction.
 237

238 *Focus-Tunable Glasses.* Some have taken these lenses one step
 239 further and incorporated them in eyeglasses. For example, Wang
 240 et al. [2014] developed a set of liquid lenses that they tested on a
 241 single observer. Unfortunately, their system had a response time
 242 on the order of seconds, and was partially table-mounted. Using
 243 a liquid-crystal diffractive lens, Li et al. [2006] created a wearable
 244 prototype that had a response time of under a second. However,
 245 they did not have any method of focus control that depended on the
 246 viewer, making the solution somewhat incomplete. Finally, there is
 247 the prototype from Hasan et al. [2017b] which uses a time-of-flight
 248 sensor pointing directly ahead of the user to close the control loop
 249 and update the liquid lenses. While an important step, this is some-
 250 what limiting and requires the wearer to move their head around to
 251 focus to different distances. Integrating an eye-tracker into the re-
 252 focusing pipeline would remove this requirement. There have been
 253 steps made to address this, but without integration into a system
 254 with focus-tunable lenses [Li and Li 2016]. Finally, it is important to
 255 note that none of these have been evaluated and verified to be more
 256 preferable or to improve task performance relative to traditional
 257 fixed-focus methods of correction.
 258

2.2 Comparison of Presbyopia Treatments

260 When it comes to the traditional forms of correction, each tends to
 261 fall short on some metric. In terms of acuity, the standard to beat is
 262 the correction afforded by simply carrying multiple pairs of single-
 263 vision glasses for each desired viewing distance – which is also
 264 the least convenient solution by far, giving us ample motivation to
 265 improve upon this solution. While bifocals at first glance seem like
 266 a reasonable fix – they are in some sense two stacked single-vision
 267 lenses – they, along with progressives and trifocals, have a decreased
 268 field of view at any given distance. This has been shown to impair
 269 contrast sensitivity and depth perception when walking, increasing
 270 risk of injury [Lord et al. 2002]. Furthermore, progressives have been
 271 shown to perform worse in tasks requiring lateral head movement
 272 than those wearing single-vision lenses [Selenow et al. 2002].
 273

274 Monovision and simultaneous-vision contacts (both diffractive
 275 or concentric lenses) offer both a wider field of view as well as clear
 276 vision over a range of distances without requiring head motion.
 277 While monovision performs better than diffractive and concentric
 278 lenses in terms of visual acuity and contrast and tends to be pre-
 279 ferred by wearers over concentric lenses, it tends to perform worse
 280 on stereoacuity [Harris et al. 1992]. Neither of these corrections,
 281 however, outperform reading glasses, or even bifocals. Studies show
 282 that monovision [Sheedy et al. 1988] and concentric lenses [Sheedy
 283 et al. 1991] are worse than reading glasses for near-distance tasks
 284 and acuity at the reading glasses' correction distance. Also, in terms
 285 of contrast and stereoacuity, reading glasses [Back et al. 1992; Papas

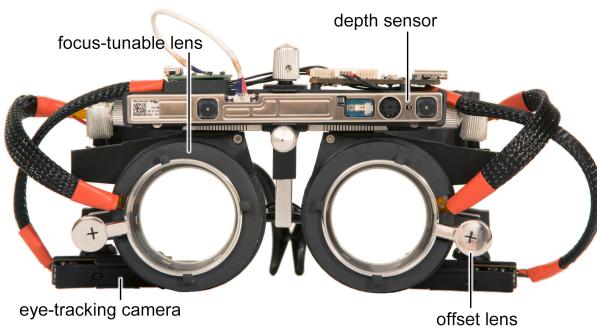


Fig. 3. A photo of the prototype, showing the focus-tunable lenses, depth
 299 sensor, eye-tracking cameras, and offset lenses mounted on a universal
 300 optometrist trial lens frame.
 301

et al. 1990] and bifocals [Erickson and Schor 1990] outperform both
 303 monovision and concentric lenses.
 304

What the Autofocals and other focus-tunable lens solutions aim
 305 to do is provide corrected vision that has comparable field of view
 306 to reading glasses, monovision, and simultaneous vision contacts,
 307 while also providing acuity and task performance that outperforms
 308 them in tasks requiring focus at various distances. The wider field
 309 of view should improve safety outcomes, while providing overall
 310 better vision based on acuity and task performance.
 311

2.3 Vision Correction in Computer Graphics

Over the last few years, a number of interactive techniques related
 313 to vision correction have been discussed in the graphics commu-
 314 nity. For example, Pamplona et al. [2012], Huang et al. [2014], and
 315 Montalto et al. [2015] explore different display technologies that
 316 have the potential to correct the eyesight of myopic, hyperopic, or
 317 presbyopic users when using digital displays. Focus-tunable lenses,
 318 in particular, have also become very popular to address the lack
 319 of focus cues in virtual and augmented reality [Dunn et al. 2017;
 320 Johnson et al. 2016; Konrad et al. 2016; Liu et al. 2008; Love et al.
 321 2009; Padmanaban et al. 2017]. None of these approaches, however,
 322 aim at restoring a users' vision in the real world.
 323

3 AUTOFOCAL EYEGLASSES DESIGN

3.1 Hardware Components

Our prototype (Figure 3) is a tethered system built largely from com-
 329 mercially available components. The frame is built around universal
 330 optometrist trial lens frames, with 3D printed components mounted
 331 on top to accommodate our measurement devices and lenses. The
 332 two measurement devices are used to obtain depth information
 333 about the surrounding, and gaze information from the wearer. A
 334 Realsense R200 (rated for 0.5–3.5 m indoors) supplies depth maps at
 335 a 30 fps, using a pair of infrared stereo cameras with a structured
 336 illumination source. The gaze information is provided by eye track-
 337 ers from Pupil Labs [Kassner et al. 2014]. There is one 120 Hz eye
 338 tracker for each eye, allowing us to also estimate vergence. Finally,
 339 there are the focus-tunable lenses themselves: a pair of Optotune
 340 EL-30-45 liquid lenses, with a 30 mm aperture. Their supported
 341

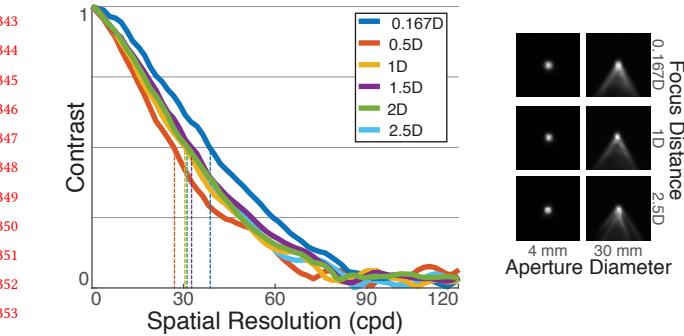


Fig. 4. Optical characteristics of the Optotune EL-30-45 focus-tunable lenses. *Left:* The MTF curves of the lenses, focused at different distances. Dashed lines indicate the MTF50 for each distance. The lenses perform close to 20/20 acuity, with the MTF50 at most distances above 30 cpd. *Right:* Point spread captured through the lenses with different distances and apertures. When the optical axis is horizontal, gravity causes the liquid in the focus-tunable lenses to pool to the bottom, leading to coma using the widest aperture (right column). However, little coma is observed in the Autofocals system where the aperture is constrained by human pupil sizes (left column).

range of focus was measured to be -2.25 to 2 D (diopters, 1/meters), with a 100 ms settling time. To allow the Autofocals to work in the 0 – 4 D range for a wide variety of wearers, we also fit a spherical or cylindrical offset lens for each focus-tunable lens, with the exact lens power chosen based on the wearer’s prescription.

To ensure that the lenses provide enough fidelity for vision correction purposes, we evaluated their optical characteristics. We measured the modulation transfer function (MTF) of the optical system at different distances using the slanted-edge algorithm based on the ISO 12233 standard (Figure 4, left). During measurements, a 4 mm aperture was set 2 cm away from the lens, mimicking the typical pupil size for photopic vision amongst presbyopes [Cardona and López 2016] and distance of the lenses from the eyes. The dashed lines indicate the MTF50 for each of the focusing distances, with the smallest MTF50 of 26.79 cpd occurring at the 0.5 D focusing distance. All other focusing distances had an MTF50 greater than 30 cpd, which corresponds to typical human visual acuity. We do not expect the optical system to be the limiting factor for the visual acuity study in system evaluation.

In addition to MTF measurements we evaluated the the system’s coma. With the optical axis oriented in the horizontal position, gravity causes the lens’ liquid to pool towards the bottom, leading to significant coma when imaging through the full 30 mm aperture (Figure 4, right). However, at any given time, humans only look through a subset of the lens due to their small pupil/aperture and observe minimal coma. In this scenario, the non-uniform distribution of the liquid is instead perceived as a spatially varying focal power across the lens. The measured power of the region 10 mm above the center of the lens adds a +1.5 D shift while the region 10 mm below the center adds a -1.5 D shift. These shifts are consistent across all focusing distances and could theoretically be corrected with a static coma corrector, assuming the glasses will be worn in a predominantly upright position. We did not implement the coma

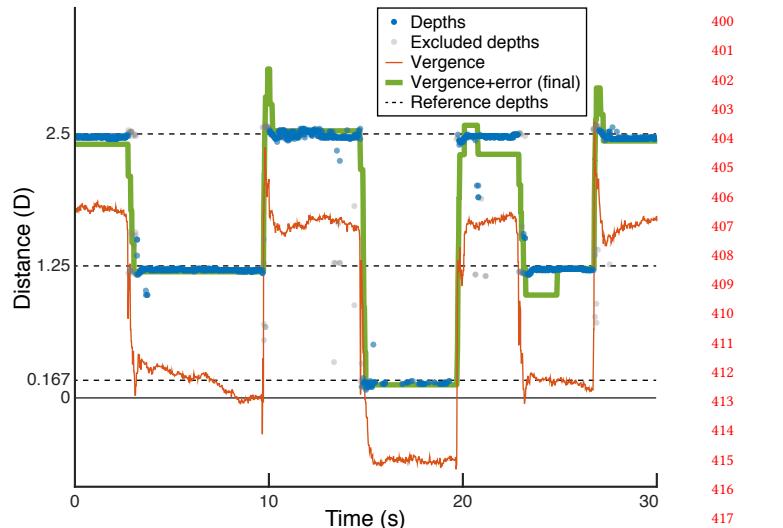


Fig. 5. An example recording of the sensor fusion algorithm. The raw vergence (red) has the right trends, but is noisy and has an offset from the actual fixated depths. Depth values from the R200 (dots) are filtered to valid values (blue). The depth informs an error estimate, which is used to obtain the final lens output powers (green).

corrector, and instead carefully adjusted the Autofocals’ frame so that the eyes were behind the centers of the lenses.

Hardware Limitations. The Pupil Labs eye trackers have an average accuracy of 0.6° per eye, which for a wearer with an inter-pupillary distance of 64 mm, limits the accuracy of accommodation estimates to about 0.25 D in ideal conditions. The accuracy can only get worse as the glasses shift on a wearer’s head. This limits accuracy of vergence measurements.

Our prototype does not currently support more than one offset lens, which limits our ability to correct for both spherical and cylindrical aberrations within the eye. This often means that we left a small amount of astigmatism unaccounted for in the prototype. This can be accounted for simply by adding space for another offset lens that corrects the cylindrical power in a future iteration.

3.2 Fixation Depth Estimation Sensor Fusion

We have four “raw” inputs: the gaze point of the left eye, the gaze point of the right eye, a scene-facing depth camera, and the wearer’s inter-pupillary distance (IPD). We then process these into a vergence estimate and a single depth estimate, which are the inputs to the sensor fusion algorithm.

The gazes are given as (x, y) coordinates normalized to a range of 0 to 1 relative to the field of view of the R200 – this is done via Pupil Labs’ calibration software. Since the geometry of the calibration scene relative to the wearer is set ahead of time, the wearer’s IPD and the separation distance of two gaze points is sufficient to determine the wearer’s vergence distance. Though not necessary, this estimate can then be refined by calibrating the vergence at two known distances and scaling the geometric estimate accordingly.

457 Furthermore, we discard any values outside the -1 to 4 D range.
 458 These limits are based on the depth extremes in our study setup.

459 For the depth estimate, we first inpaint the depth map using a
 460 Navier-Stokes algorithm [Bertalmio et al. 2001]. Then, we use the
 461 left eye's gaze coordinate to index into a 5×5 neighborhood of
 462 depth map, from which we take the median depth. We use the left
 463 eye because it is approximately aligned with the camera of the R200;
 464 if the left eye is not available, we fall back to the right eye.

465 Given these processed values, the high level operation of the
 466 sensor fusion algorithm can be described as vergence plus an error
 467 term (estimated as the difference between the vergence and depth).
 468 We choose this approach since vergence updates much faster and
 469 is not affected by depth discontinuities at edges. However, it is
 470 sensitive to inaccuracies in calibration, which manifests itself as a
 471 nearly constant offset in the range of operation (Figure 5). Since
 472 the depth map itself is accurate, this offset is corrected for with the
 473 gaze-indexed depth estimate.

474 The details of this algorithm are in Algorithm 1. Since the ver-
 475 gence estimate, v , is noisy (Figure 5, red), it is first smoothed with
 476 an exponential average to obtain v_{filt} (line 5). Then, to correct for
 477 the offset in vergence, we check for a new filtered depth estimate,
 478 d_{filt} (Figure 5, blue). These two values are used to update the error
 479 estimate, v_{err} , with an exponential average, but such that fluctua-
 480 tions from depth discontinuities are not considered (line 8). We also
 481 allow error updates at either extreme of the depth range to control
 482 for initial conditions with large vergence error. Finally, the lens
 483 focal power (Figure 5, green) is set to the new error-compensated
 484 vergence estimate (line 13), with a minimum step size of 0.25 D to
 485 prevent jitter caused by limits of the eye tracking accuracy (Sec-
 486 tion 3.1).

487 The value for d_{filt} , used in Algorithm 1, is calculated as seen in
 488 Algorithm 2. The raw depth estimate, d , exhibited a tendency to drop
 489 by nearly a diopter for some frames (Figure 5, gray). We consider a
 490 drop of more than 0.5 D to potentially be an artifact. However, some
 491 drops are clearly the users looking to a new distance. Therefore, we
 492 reject depth estimates until an exponential filter starting from the
 493 last valid depth (line 11) "catches up."

495 4 USER STUDY DESIGN

496 In order to evaluate the Autofocals and focus-tunable technology
 497 in general, we conducted a user study consisting of 26 participants
 498 (ages 51–81, mean age 63.6, 9 male, 17 female). All users had far
 499 vision corrected to 20/20. Two progressive wearers were excluded
 500 due to inability to simultaneously correct spherical and cylindrical
 501 aberrations using our prototype. Due to possible improvements in
 502 proficiency using presbyopic correction as a function of length of
 503 use, we only compare the Autofocals against the correction the
 504 users wear on a regular basis. This splits our study population into
 505 6 people that typically wear monovision and 18 with progressives.
 506 All procedures were approved by the institutional review board of
 507 the home institution.

508 Our user study consisted of four phases, repeated once with their
 509 correction and once with the Autofocals (correction order alternated
 510 between participants): first, we measure their required prescription
 511 using the Grand Seiko WAM-5500 autorefractor; second, we evaluate

ALGORITHM 1: Sensor fusion: vergence + error

```

1  $v_{\text{filt}} = v_{\text{err}} = 0; \alpha_v = 0.2; \alpha_e = 0.2;$ 
2 while running do
3   if checkNewValidEyeTrackerVergence() then
4      $v \leftarrow \text{getNewValidEyeTrackerVergence}();$ 
5      $v_{\text{filt}} \leftarrow \alpha_v v + (1 - \alpha_v)v_{\text{filt}};$ 
6     if checkDepthUpdated() then
7        $d_{\text{filt}} \leftarrow \text{getLatestDepth}();$ 
8       if  $|d_{\text{filt}} - (v_{\text{filt}} + v_{\text{err}})| < 0.5$  or  $v_{\text{filt}} < 0.75$  or
9          $v_{\text{filt}}, d_{\text{filt}} > 2.0$  then
10         $v_{\text{err}} \leftarrow \alpha_e(d_{\text{filt}} - v_{\text{filt}}) + (1 - \alpha_e)v_{\text{err}};$ 
11      end
12    end
13    if  $|\text{getLensPower}() - (v_{\text{filt}} + v_{\text{err}})| > 0.25$  then
14       $\text{setLensPower}(v_{\text{filt}} + v_{\text{err}});$ 
15    end
16  end

```

ALGORITHM 2: Depth denoiser

```

1  $d_{\text{denoiser}} = 0; \alpha_d = 0.2;$ 
2 while running do
3   setDepthUpdated(False);
4   if checkNewR200DepthMeasurement() then
5      $d \leftarrow \text{getNewR200DepthMeasurement}();$ 
6     if  $d_{\text{denoiser}} - d < 0.5$  then
7        $d_{\text{denoiser}} \leftarrow d;$ 
8       setLatestDepth( $d$ );
9       setDepthUpdated(True);
10    else
11       $d_{\text{denoiser}} \leftarrow \alpha_d d + (1 - \alpha_d)d_{\text{denoiser}};$ 
12    end
13  end
14 end

```

their visual performance using acuity and contrast eye charts; then
 551 we evaluate their performance on a task requiring changing focus
 552 distance; finally, we let them freely observe a natural scene with
 553 several objects on and beyond a table. All eye charts were displayed
 554 using monitors with approximately 190 cd/m^2 of output when white,
 555 and with high enough resolution to support at least 20/10 vision
 556 at their chosen distance (at 2.5 D and 1.25 D, a 5.98" display with
 557 a 1440p resolution, and at 0.167 D a 24" display at 1080p). The
 558 monitors were all calibrated with measurements of light output at
 559 all gray levels with the SpectraScan PR670, a spectroradiometer. All
 560 eye charts used the Sloan font [Pelli et al. 1988]. For the eye chart
 561 and task performance tests the users were asked to rest their chin
 562 on a chin rest to fix their distance to the monitors.

563 It should be noted that for most of the tasks, we make a slight
 564 modification to the operation of the lenses. While for the natural
 565 scene evaluation, we use the sensor fusion algorithm as described in
 566 subsection 3.2, the other tasks instead use a version that is set to the
 567 known distances of the displays. Acuity and contrast are set to the
 568 distance of the currently visible eye chart, and the task performance

571 is set to the display distance nearest to the user’s current vergence.
 572 The rationale for the decision to use these alternative modes of
 573 operation is twofold: first, our purpose is to evaluate the acuity and
 574 contrast at specific working distances as compared to traditional
 575 corrections, and second, we wished to reduce the latency and jitter
 576 as much as possible when distances are known. These both stem
 577 from a desire to evaluate the underlying technology, which is in its
 578 infancy, as opposed to limiting ourselves to our current prototype.
 579

580 4.1 Acuity

581 The acuity tests were administered using a logMAR (minimum angle
 582 of resolution) chart based on the ETDRS chart [Ferris et al. 1982]
 583 at 99% contrast. One line of five random letters (from the 10 Sloan
 584 letters) was shown at a time, with each subsequent line smaller by
 585 0.1 logMAR. This continued until the user identified three or more
 586 letters incorrectly within the same line. The final reported acuity
 587 was the acuity of that line, minus 0.02 logMAR per letter answered
 588 incorrectly during that trial. Acuity corresponding to 20/20 vision is
 589 defined as 0.0 logMAR. The acuity tests were conducted at distances
 590 of 0.167, 1.25, and 2.5 D (6 m, 80 cm, and 40 cm), with three repeats
 591 at each distance, and with the order randomized across all trials.
 592

594 4.2 Contrast Sensitivity

595 For the contrast test, we construct a chart based on the Pelli-Robinson
 596 contrast chart [Pelli et al. 1988], using Sloan letters at a size corre-
 597 sponding to 20/120 acuity. Again, one line was displayed at a time,
 598 but with 3 Sloan letters in each line. Starting with 0.05 logCS (We-
 599 ber contrast sensitivity) for the first line, each subsequent line had
 600 contrast reduced by 0.15 logCS until the user incorrectly identified
 601 two letters in a single line, or until the user got to 1.7 logCS, which
 602 was the limit of the display. The final contrast sensitivity was the
 603 contrast of the last line with a majority of letters identified correctly.
 604 The contrast test was conducted only at the intermediate distance of
 605 1.25 D, a distance supported by all forms of correction considered.
 606

607 4.3 Task Performance

609 Next, for the task performance test, we place in front of the user two
 610 displays, one at 0.167 D, and the other at 2.5 D (image in Supple-
 611 mental Material). We display a single letter on each monitor, with 50%
 612 probability of them being the same letter. In this case, we use the
 613 full extended Sloan alphabet (with the exception of the letters ‘G’
 614 and ‘W’ which had unusual shapes compared to typical fonts), and
 615 at a size corresponding to 20/40 acuity. The task is then to indicate
 616 whether or not the letters match, using a keyboard. The user would
 617 perform this task for two minutes, at the end of which we calculate
 618 their accuracy and speed. Users were prompted to focus on accu-
 619 racy while maintaining speed with the following prompt, “We are
 620 recording both speed and accuracy, so try to get as many correct
 621 as you can while still going quickly.” Users were given a training
 622 period of 20 pairs ahead of the timed portion to get accustomed to
 623 the controls. When wearing the Autofocals for this task, the user
 624 was asked to move their head as little as possible to avoid losing eye
 625 tracker calibration. One monovision wearer and three progressive
 626 lens wearers were excluded from the task performance data due
 627

628 to inability to calibrate the eye trackers after repeated attempts
 629 (leaving 5 monovision, 15 progressives).
 630

631 4.4 Natural Scene Preference

632 Finally, we allow the users to freely view a natural scene (image
 633 in Supplemental Material) for roughly a minute each with their
 634 correction and with the Autofocals. We also add a second mode
 635 of operation to the Autofocals that uses only the depth from the
 636 center of the R200’s field of view to evaluate the benefits afforded
 637 by incorporating eye trackers. This center-depth mode is made to
 638 imitate Hasan et al.’s system [2017a] and is only used during the
 639 natural scene evaluation. After the users evaluate the scene, we
 640 have them rank the three conditions on physical comfort and “how
 641 effectively they allowed [them] to see to all distances,” allowing ties,
 642 as well as recording any general feedback that they gave. A rank of
 643 1 indicated that a correction was the best, and 3 the worst.
 644

645 The first 10 users consistently noted jitter in the focus state as
 646 unacceptable when ranking the corrections. Since the natural scene
 647 viewing is the only portion that implemented the sensor fusion
 648 algorithm, we treated these first users as a pilot to refine the sensor
 649 fusion algorithm. In particular, we traded off some precision and
 650 latency in exchange for reducing the amount of refocusing jitter –
 651 for example, by increasing the smoothing on vergence, and only
 652 updating the lens power for changes in distance of 0.25 D or more
 653 (as described in Section 3.2).
 654

655 Three progressive lens wearers were excluded from the task per-
 656 formance data due to inability to calibrate the eye trackers after
 657 repeated attempts (leaving 1 monovision, 10 progressives).
 658

659 5 RESULTS

660 5.1 Acuity

661 The average acuity using each correction at each of the three dis-
 662 tances can be seen in Figure 6. From the figure, it is clear that while
 663 the Autofocals maintain at least 20/20 vision at all distances, the
 664 tradeoffs involved in having higher near add powers (positive correc-
 665 tion added for near vision) in traditional correction result in reduced
 666 acuity at the closest distance. The two groups of users (monovision
 667 and progressives) were analyzed separately with a 2×3 two-way re-
 668 peated measures ANOVA, with independent variables of correction
 669 (their correction vs. Autofocals) and distance. Greenhouse-Geisser
 670 sphericity correction was applied. Post-hoc tests were conducted as
 671 pairwise *t*-tests only between the corrections at each distance (due
 672 to lack of interpretability of other comparisons), with Bonferroni
 673 correction applied to the *p*-values.

674 For monovision, the ANOVA shows significant main effects of
 675 correction ($F(1, 5) = 7.26, p < 0.05$) and distance ($F(1.72, 8.61) =$
 676 7.24, $p < 0.05$). There is also a significant interaction of correction
 677 and distance ($F(1.24, 6.21) = 22.7, p < 0.01$). Since the interaction
 678 is significant, we conduct followup *t*-tests for the post-hoc analysis.
 679 The Autofocals show a significant improvement over monovision at
 680 a distance of 2.5 D ($p < 0.01$), with monovision faring worse than
 681 20/20 acuity on average at this distance (0.117 logMAR).
 682

683 For progressive lenses, the ANOVA shows a significant main ef-
 684 fect of distance ($F(1.69, 28.65) = 16.0, p < 0.001$). There is also a
 685 significant interaction of correction and distance ($F(1.34, 22.81) =$
 686

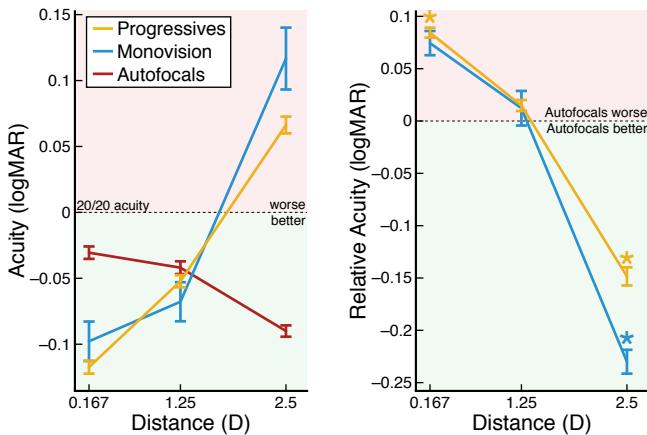


Fig. 6. Left: The average acuities for each correction and distance. The Autofocals are on average better than 20/20 at all distances, unlike the other corrections at the nearest distance. Right: Average acuity of the Autofocals relative to each user's correction (paired differences). Stars indicate that the Autofocals performed significantly better or worse for the given distance and correction ($p < 0.01$). Error bars represent standard error.

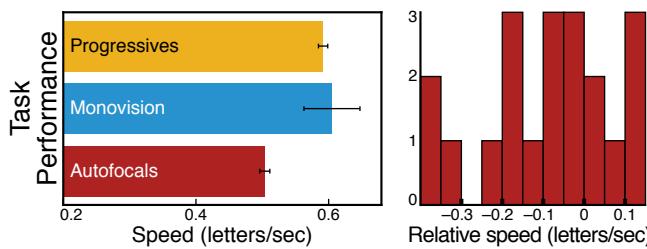


Fig. 7. Left: The average speeds of the users during the letter matching task. Error bars represent standard error. Autofocals perform the slowest on average. Right: However, a histogram of the speed of a wearer using Autofocals relative to their own correction shows that nearly a third of users were faster in Autofocals. This indicates that miscalibration, not latency, may have affected the speed for a subset of users.

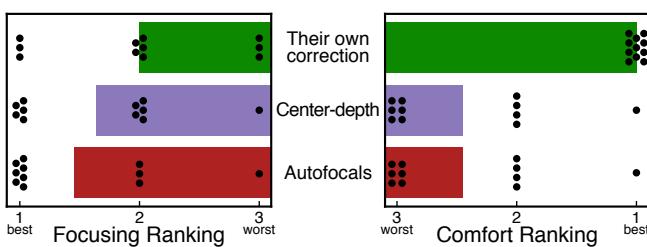


Fig. 8. Left: The average rankings for how effectively users were able to see to all distances (1 is the best rank). Individual rankings are shown as black circles. The trend favors the Autofocals over center-depth, and both modes over their own correction. This indicates that eye-tracked systems may be preferable despite their drawbacks in comfort, need for calibration, and familiarity. Right: Average comfort rankings show a clear and expected result in favor of their own correction. Users that ranked either mode of the prototype as tied for 1 cited not having to crane their necks back to look at near things higher in their visual field.

32.87, $p < 0.001$), and so we conduct followup t -tests. At a distance 742
of 0.167 D, progressive lenses significantly outperform Autofocals 743
($p < 0.01$), whereas Autofocals significantly outperforms progressive 744
lenses at 2.5 D ($p < 0.01$). It should be noted that progressive 745
lenses were worse than 20/20 on average at the near distance (0.0663 746
logMAR). On the other hand, the Autofocals still supported at least 747
20/20 vision at the far distance (-0.033 logMAR), even though they 748
performed worse than progressives. 749

In summary, the Autofocals performed significantly worse than 750
progressives at the far distance, but significantly better, and by a 751
wider margin, than both monovision and progressives at the near 752
distance. Furthermore, only the Autofocals performed better than 753
20/20 acuity on average at every distance. 754

5.2 Contrast Sensitivity

The average contrast sensitivities are as follows: 1.56 logCS for 755
Autofocals with monovision wearers, 1.62 for monovision, 1.62 for 756
Autofocals with progressives wearers, and 1.66 for progressives. 757
Several users were able to consistently read the lowest contrast line 758
supported by the monitor (1.7 logCS): 3 using monovision, 12 using 759
progressives, and 14 with the Autofocals (3 and 11 from the monovision 760
and progressives groups, respectively). Since this clipping of values 761
violates assumptions of normality, we run a Wilcoxon 762
signed-rank test for each correction, which shows no statistically 763
significant differences at the 0.05 level. 764

5.3 Task Performance

The speed of the users in each correction can be found in Figure 7. 765
The mean accuracy in each correction is: 92.0% for Autofocals with 766
monovision wearers, 92.1% for monovision, 95.7% for Autofocals 767
with progressives wearers, and 93.9% for progressives. This indicates 768
that users generally went slower to maintain accuracy, as desired. 769
The speed is calculated only based on correctly identified matches. 770
Comparing the speeds with paired t -tests for each correction shows 771
no statistically significant differences at the 0.05 level. 772

5.4 Natural Scene Preference

The average rankings for physical comfort of the Autofocals using 773
our sensor fusion and in center-depth mode were 2.45 for both. 774
Their own correction on the other hand had a universal ranking 775
of 1, which is understandably better (Figure 8). When looking at 776
their rankings for effectiveness of vision at all distances, we see that 777
on average our sensor fusion performed slightly better than center-depth, 778
which was in turn slightly better than their own correction. 779
A Friedman test of the rankings shows no statistically different 780
differences in these rankings. 781

6 DISCUSSION

6.1 Acuity and Contrast Sensitivity

Traditional forms of correction, as expected, performed well for the 792
intermediate and far distances (1.25 D and 0.167 D) and showed 793
slight improvements in terms of visual acuity when compared to 794
the Autofocals. While progressives show a statistically significant 795
improvement at the far distance over the Autofocals, *only* users 796
using the Autofocals were capable of reaching at least 20/20 acuity 797

799 on average at each of the tested distances (2.5 D, 1.25 D, and 0.167 D).
 800 Observing acuity at the nearest distance, users wearing the Autofocals
 801 significantly outperformed both monovision and progressive
 802 wearers and were able to see better than 20/20 when previously,
 803 they could not with their correction. This is despite the spatially
 804 varying focal power across the lenses (Section 3.1). Therefore, these
 805 results can only improve with reduced aberration, such as a coma
 806 corrector. Each of the tested correction methods exhibited very sim-
 807 ilar contrast sensitivity results, at least within the range of contrasts
 808 tested.

809 An interesting trend is the improvement in visual acuity for users
 810 wearing the Autofocals at nearer distances. This can be attributed
 811 to the near triad, which is the oculomotor response when viewing
 812 a near target resulting in binocular convergence, increased accom-
 813 modation, pupil miosis (i.e. constriction, images in Supplemental
 814 Material). When the users look to a far distance, their pupils nat-
 815 urally dilate, resulting in an effectively larger aperture through the
 816 focus-tunable optic. In Section 3.1 we show that a larger aperture
 817 leads to increased aberrations, which could explain the slight re-
 818 duction in visual acuity at far distances. With better focus-tunable
 819 optics, visual acuity should remain similar to the near acuity at
 820 farther distances.

821 It should also be noted that there is a fundamental tradeoff in the
 822 near add power for progressive and monovision corrections. For
 823 monovision, higher add powers may decrease comfort and stereoacu-
 824 ity; many monovision wearers that entered our study reported also
 825 wearing reading glasses for near vision. Though powers for progres-
 826 sive lenses can get much higher, this requires more precise head
 827 movements. The Autofocals system has no physiological tradeoff
 828 on the nearest focusing distance.

831 6.2 Task Performance

832 We see that people on average perform slower using Autofocals
 833 in the task performance study. This seems to imply that the lag in
 834 the lenses and processing pipeline makes a measurable impact on
 835 refocusing speed. However, the data (Figure 7) shows that 6 users
 836 actually performed faster using the Autofocals than their correc-
 837 tion. In fact, the second-fastest trial across all participants with a
 838 speed of 0.8 letters/sec was using the Autofocals, as compared to
 839 0.76 letters/sec in their progressives (the fastest trial was a differ-
 840 ent participant wearing monovision). This implies that rather than
 841 inherent latency, other factors were involved. Observation of the
 842 gaze estimates during trials showed that they sometimes become
 843 less accurate as the users moved their heads – the slower perfor-
 844 mance is therefore likely due to miscalibration from movement of
 845 the Autofocals relative to the users’ eyes. Another confounding
 846 factor is that traditional presbyopia corrections sometimes do not
 847 require any refocusing at all: multiple participants did not move
 848 their heads while wearing progressive lenses, and one stated that
 849 they placed their focus between the two distances when performing
 850 the task, allowing both displays to be slightly blurry but still legible;
 851 this method is one not possible with Autofocals or non-presbyopic
 852 vision, since that would require vergence to not be at either display
 853 distance.

854 6.3 Preference Rankings

855 Finally, our preference ranking after the natural viewing study
 856 points gives us at least one obvious conclusion: comfort is important,
 857 and the Autofocals are heavy; every user consistently rated their
 858 usual correction as more comfortable. Much of the weight is in the
 859 lenses themselves, which means that focus-tunable lens technology
 860 targeting presbyopia correction has to focus on reducing its weight,
 861 especially since these devices will be worn all day. On the other
 862 hand, most users felt that they were able to see more effectively to
 863 all distances with the Autofocals. This shows that the technology
 864 itself has distinct advantages to user experience over fixed focus
 865 methods. Furthermore, some that chose their own correction said
 866 that they liked their own best because it was what they were used
 867 to now. Others pointed to the fact that the Autofocals were great
 868 when they worked – such as during the task performance, when
 869 it was clamped to two distances and they were instructed to move
 870 their heads as little as possible – but they felt unpredictable at times
 871 during the natural viewing.

872 This brings us to the most important point outside of form factor:
 873 predictability. The key with adapting to traditional corrections such
 874 as progressives or monovision is that the fixed focus lenses provide
 875 predictability. The wearer does not have to guess if the glasses will
 876 work or not. In this respect, the center-depth mode, made to imitate
 877 a system like that of Hasan et al. [2017a] works quite well; a single
 878 depth sensor pointing straight ahead of the wearer is a lot more pre-
 879 dictable than an eye-tracked system that is dependent on calibration.
 880 However, that many still preferred having the eye trackers means
 881 that a depth sensor-only system is not the best possible correction,
 882 just one that performs well with the current state of technology.
 883 The limiting factor in current technology, based on our reading of
 884 user accounts, is the eye tracking, specifically for vergence tracking.
 885 An ideal system using focus tunable lenses need only know the
 886 vergence state of the wearer, since that alone gives the intended
 887 focus distance, but it also needs to be able to accurately track and
 888 self-calibrate the vergence regardless of removal or adjustment of
 889 the eyewear. Though there have been great strides in making robust
 890 and affordable eye tracking systems for head-mounted displays in
 891 virtual and augmented reality [Stengel et al. 2015], the problem
 892 presbyopic corrections face is inherently more difficult due to the
 893 aforementioned issues, and the relatively higher cost of failure.

894 6.4 General Observations

895 A potential benefit that we explored relates to the potential for *ex-
 896 ceeding* visual performance of younger people. Accommodation has
 897 a response time of around 370 ms [Campbell and Westheimer 1960]
 898 for externally modulated stimuli. Our system on the other hand the-
 899 oretically responds within around 125 ms (average processing time
 900 per update plus lens settling time), which should allow for faster
 901 performance than natural accommodation. A pilot study indicated
 902 that the limiting factor in task performance between younger and
 903 older users was likely not accommodation speed.

904 Another thing to note is that nobody complained about the field of
 905 view of the focus-tunable lenses – interestingly, one user remarked
 906 that they enjoyed having “full field vision.” This may be because
 907 many of them were used to small field of view on their progressive

lenses, but the 30 mm aperture is also comparable in vertical extent to typical corrective eyewear. This is important since larger focus-tunable lenses often come with hard tradeoffs in response time or quality. It seems that retaining the current size and instead looking to improve speed may be sufficient for most people.

Finally, some users claimed their corrections could be out of date. An added benefit of having a focus-tunable correction is that it can be updated on-the-fly in software, removing the need for constantly buying new glasses as prescriptions change.

7 CONCLUSION

Presbyopia, despite being a nearly universal problem in old age, still does not have an ideal commercially-available solution. Focus-tunable lens technology shows promise and may enable technologies closer to the ideal of youthful vision. We built a prototype system, Autofocals, for evaluating the utility and current state of focus-tunable lens technology for correcting presbyopia. Even with this early prototype, the Autofocals are often comparable to and sometimes even exceeds traditional forms of correction. This also has important ramifications for real-world tasks; one user even remarked, “I haven’t seen my hand this clearly in decades!” Despite never having worn the Autofocals previously, people preferred them to their own daily correction. This is a promising result for continued pursuit of focus-tunable presbyopia corrections.

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