

Reviewing R Script of HW7 (Posted on Course Website)

Trend: time index

Seasonalities: add seasonal dummies

Problem 1:

- Make month a categorical predictor
- Plot demand against temperature (looks like it is rising)
- Add time index to account for trend
- Incorporate weekend effects into model

Problem 2:

- Create general linear model fitting model versus all predictors
- Use tables to find error rates according to ratios in assignment
 - False Positive Rate = Number of False Positives / Number of E-mails Not Spam

Reviewing HW 8*Problem 1*

T: Positive test

S: Has disease

Use Bayes Rule

$$P(S|T) = P(S)P(T|S) / P(T)$$

$$P(S) = 1/1000$$

$$P(T|S) = 0.95$$

$$P(T|\sim S) = (1-P)(\sim T|\sim S) = 1 - 0.99 = 0.01$$

$$P(T) = P(T, S) + P(T, \sim S)$$

$$= P(S)P(T|S) + P(\sim S)P(T|\sim S)$$

$$= \dots \text{ (algebra expansion)}$$

$$= 0.01094$$

$$P(S|T) = P(S)P(T|S) / P(T) = 0.001(0.95)/(0.01094) = 8.7\%$$

Costs

$$\$10 * 10 \text{ mil} = \$100 \text{ mil}$$

$$\$50 * 10 \text{ mil} * P(T, \sim S) = \$50 \text{ mil}$$

Benefits

$$10K * 10m * P(T, S) = \$95 \text{ mil}$$

Problem 2

Part A

- a) $E(.5x + .5y) = 0.5E(x) + 0.5E(y) = 15$
 b) $\text{Var}(0.5x + 0.5y)$
 $= 0.5^2 \text{var}(x) + 0.5^2 \text{var}(y) + 2(.5)(.5)\text{cov}(x, y)$
 $= 41.75$

Part B

$$E(x) = 1.03, E(y) = 1.04$$

$$\text{Var}(x) = 6.27 * 10^{-3}; \text{var}(y) = 1.27 * 10^{-2}, \text{cov}(x, y) = -3.17 * 10^{-3}$$

w: initial wealth

p: fraction in x

$$W = wX \text{ if } p=1$$

$$W = wY \text{ if } p=0$$

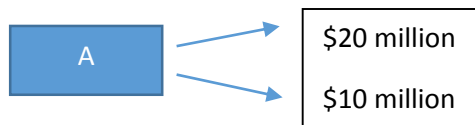
$$\text{Var}(W) = w^2 p^2 \text{var}(x) + w^2 (1-p)^2 \text{var}(y) + w^2 p(1-p) \text{cov}(x, y)$$

So what should be our strategy when choosing a portfolio? Should we:

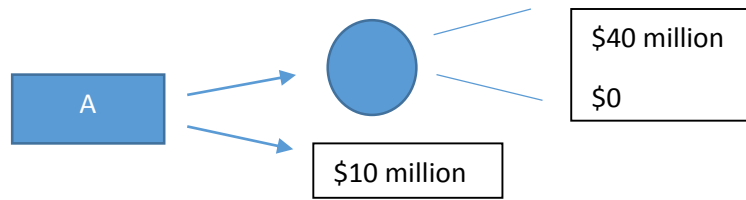
- Maximize expected value? Risky, means you are willing to take swings (more volatile)
- Minimize variance? (aptly dubbed the “Wallflower Strategy” by Dr. Scott) No swings, lower returns

Ideally, we want a mix of both.

Which of these scenarios would you choose?



Above, both are surefire options, so you would definitely choose \$20 million.



Now, there is a 50/50 chance of getting either \$40 million or \$0. Most people would choose the guaranteed \$10 million.

Thus, expected value should not necessarily guide our decisions.

Ex: Flipping Game

You get 2^k once you win a coin toss, or you could get \$10 million guaranteed.

Intuition says you'd pick the \$10 million, but the flipping game's expected value is actually infinity.

- $E(x) = \text{Summation}(x \text{ in all possible outcomes } \lambda) x p(X=x)$