CS 237 Homework 01 Solution -- Data Display in Python

Due Thursday at 11:59 PM in Gradescope (with grace period of 6 hours)

In this first homework, you will become familiar with various methods of displaying the results of probability experiments graphically in Python using Jupyter notebooks and Matplotlib. This will be a fundamental way of understand the results of experiments throughout the course. We will cover:

- Basic introduction to Python and Jupyter Notebook.
- · Basic introduction to Matplotlib and graphing
- Basic introduction to Monte Carlo (probability) simulation.

To submit, Run All before making your PDF version, be careful when you scan it (I recommend, and check to make sure that each page is visible in Gradescope. We will allow you to resubmit to Gradescope if you make mistakes in scanning and uploading for HW 01; thereafter any solutions we can not read or access will be marked wrong.

Anaconda Distribution of Python

- Download from https://www.continuum.io/downloads)
 - Make sure it's Python 3!
 - Be sure to pick the correct Operating System (i.e., Windows, MAC OS, Linux)

Starting Jupyter

- · Open a Terminal Window
 - For MAC OS, open your Applications folder, then open the Utilities folder. Open the Terminal application. (Or, type "terminal" into Spotlight.) You may want to add this to your dock.
 - For Windows, simply search for CMD and run the result
- In the terminal run jupyter notebook
- This will bring you to the home page.
- Click new and then click python3 to create a new lpython3 notebook.
 - Alternatively, use the Anaconda Navigator that will be installed in your Applications folder.

In [1]:

Plotting Points

The scatter(...) function is used to plot points from a list of x values and the associated y values.

```
In [2]:
```

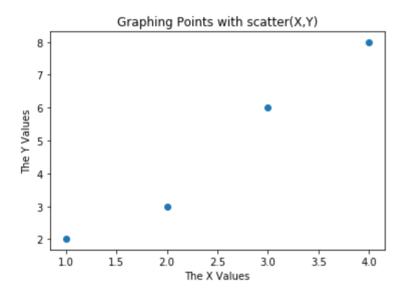
```
# To plot the points (1,2), (2,3), (3,6), (4,8) we would list the x values and t
he corresponding y values:
X = [1,2,3,4]
Y = [2,3,6,8]

print("\nThis is the list of points:",list(zip(X,Y)))
print("They must be input to the function as separate lists:")
print("\tX =",X)
print("\tY =",Y,"\n")
plt.scatter(X,Y)
plt.title('Graphing Points with scatter(X,Y)')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()
```

```
This is the list of points: [(1, 2), (2, 3), (3, 6), (4, 8)]
They must be input to the function as separate lists:

X = [1, 2, 3, 4]

Y = [2, 3, 6, 8]
```



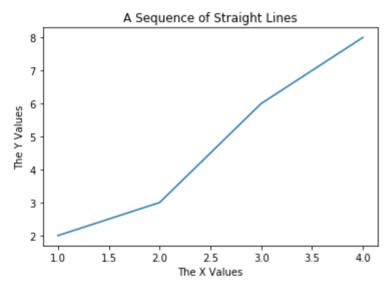
Plotting Lines and Curves

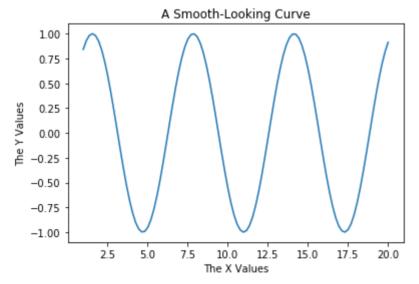
If you call plot(...) instead of scatter(...) you will display a curve created by connecting the points with straight lines. Essentially you can only plot straight lines between points, but if the points are close together, you will not notice, and it will look like a smooth curve.

In [3]:

```
# To plot a curve through the points (1,2), (2,3), (3,6), (4,8) we would use:
plt.plot([1,2,3,4], [2,3,6,8])
plt.title('A Sequence of Straight Lines')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()

X = np.linspace(1,20,100)  # returns a list of 100 equally-spaced valu
es in the range [1..20]
Y = [np.sin(x) for x in X]
plt.plot(X,Y)
plt.title('A Smooth-Looking Curve')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()
```

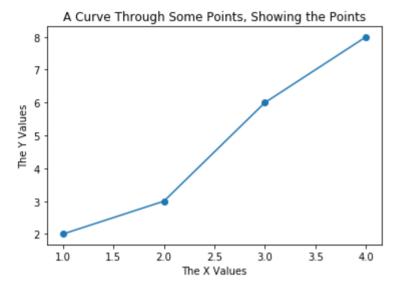




If you want to do both, you can simply call both functions before you call show().

In [4]:

```
plt.scatter([1,2,3,4], [2,3,6,8])
plt.plot([1,2,3,4], [2,3,6,8])
plt.title('A Curve Through Some Points, Showing the Points')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()
```

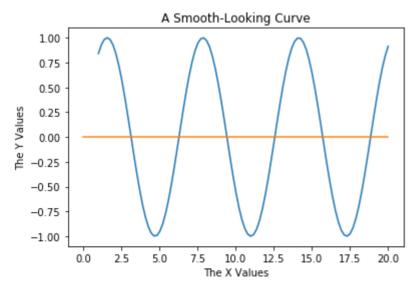


If you want to draw a single line from (x_1, y_1) to (x_2, y_2) you can plot $[x_1, x_2]$ and $[y_1, y_2]$.

Here we have added a zero line to our sin curve:

In [5]:

```
X = np.linspace(1,20,100)  # returns a list of 100 equally-spaced valu
es in the range [1..20]
Y = [np.sin(x) for x in X]
plt.plot(X,Y)
plt.plot([0,20],[0,0])
plt.title('A Smooth-Looking Curve')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()
```



For further details on drawing plots, particularly on color and format, see the Appendix at the end of this document

Problem Zero: Using the Numpy Random Library

We have imported a number of functions from the Numpy Random library, which you can read about https://docs.scipy.org/doc/numpy/user/quickstart.html).

```
In [6]:
# Run this cell several times and and see what happens
random()
Out[6]:
0.7030527670762344
In [7]:
# Run this cell several times and and see what happens
# List comprehensions are your best friend, learn how to use them!!!
size = 10
rands = [ random() for k in range(size) ]
rands
Out[7]:
[0.3403612525607539,
 0.1605122599257076,
 0.4409330858122984,
 0.6211203640421913,
 0.0986457584796181,
 0.9264124599660639,
 0.5633053605133952,
 0.08996236993752804,
 0.03822697862468649,
 0.8957739125111671
In [8]:
# Run this cell several times and and see what happens
# This produces a Numpy 1D vector, which is
# another way to store a sequence.
size = 5
random(size)
Out[8]:
array([ 0.65003909, 0.16738321, 0.9815955 , 0.20359845, 0.039763
82])
```

```
In [9]:
```

```
# In most cases, arrays are interchangeable with lists, but if you need a Python
# list, just do this:
list(random(size))
```

Out[9]:

```
[0.65691157397239996,
0.032023769627935739,
0.40834446594353813,
0.92427090350056929,
0.044537204272105724]
```

In order to make grading easier, we will "seed" the random number generation so that it always produces the same pseudo-random sequence. However, you should generally try running your code several times without the seed, trying it on various random sequences.

Just be sure to include the seed before running your program to submit, so that the graders can see your correct results.

```
In [10]:
```

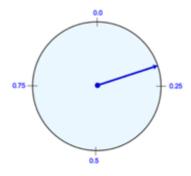
```
# Run this cell several times, and see what happens
# How is it different from the result in cell [210]?
seed(0)
random(5)
Out[10]:
```

```
array([ 0.5488135 , 0.71518937, 0.60276338, 0.54488318, 0.423654 8 ])
```

Problem 1 (Plotting Points)

Part A

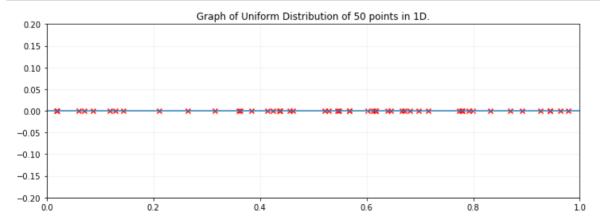
One of our standard examples in lecture will be a "spinner" which can be set in motion to randomly chose a real number in the half-open interval [0..1):



We will simulate this using the Python function random() from the Numpy.random library we imported above.

```
In [11]:
```

```
Use numpy's random() function to build a list of x vals with the following
properties:
#
           - x vals list should have length num trials
#
           - Each value in x vals should be a random float in the range [0..1)
#
      Now plot the points (xi,0) along the x axis in the diagram below
def random line plot(num trials):
   x_vals = [ random() for k in range(num_trials) ] # <--- Your code here</pre>
   y vals = [ 0 for k in range(num trials) ]
                                                         # <--- Your code here
   plt.figure(figsize=(12, 4))
   plt.title('Graph of Uniform Distribution of '+str(num trials)+' points in 1
D.',fontsize=12)
   plt.grid(color='0.95')
   plt.ylim(-0.2, 0.2)
   plt.xlim(-0.0,1.0)
   plt.plot([0,1.0],[0,0])
   plt.scatter(x vals, y vals, marker="x",color="r")
   plt.show()
# TO DO: Complete the lines of code indicated above. Then comment out the <code
>seed(0)</code>
# statement and run this cell several times to see the distribution of points;
# put the seed command back in before you submit!
seed(0)
random line plot(50)
```

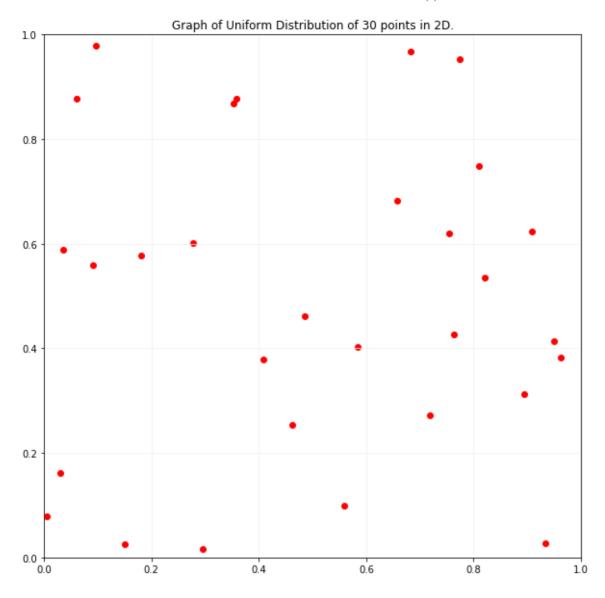


Part B

Now we will simulate the experiment of throwing a dart at a unit square, which will produce a scatter plot of random points in a 2D grid.

In [75]:

```
# TO DO:
         Complete the following function stub which will produce a scatter plot
of
          random points in a unit square.
def random plane plot(num trials):
    """Uses numpy's random function to build a list of x and y values with the f
ollowing properties:
    - x vals should have len num trials
    - y vals should have len num trials
   - Each value in x and y should be between 0 and 1
   HINT: use the same code to build x vals and y vals
   x_vals = [ random() for k in range(num_trials) ]
                                                                   # Your code he
re
                                                                  # Your code he
   y vals = [ random() for k in range(num trials) ]
re
   plt.figure(num=None, figsize=(10, 10))
   plt.title('Graph of Uniform Distribution of '+str(num trials)+' points in 2
D.',fontsize=12)
   plt.grid(color='0.95')
   plt.ylim(0, 1)
   plt.xlim(0,1)
   plt.scatter(x vals, y vals,marker="o",color="r")
   plt.show()
# Comment out the next line and run this cell several times to see the distribut
ion of points;
# put the seed command back in before you submit!
#seed(0)
random plane plot(30)
```



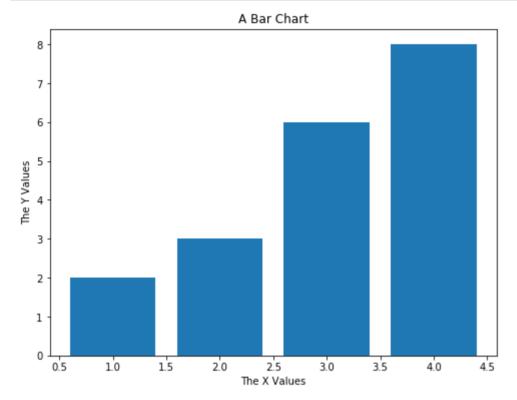
[End of Problem One]

Bar Charts

If we do the exact same thing as we did with a simple plot, but use the function <code>bar(...)</code> we get a bar chart:

In [13]:

```
# To plot the points (1,2), (2,3), (3,6), (4,8) we would list the x values and t
he corresponding y values:
plt.figure(num=None, figsize=(8, 6))
plt.bar([1,2,3,4], [2,3,6,8])
plt.title('A Bar Chart')
plt.xlabel("The X Values")
plt.ylabel("The Y Values")
plt.show()
```

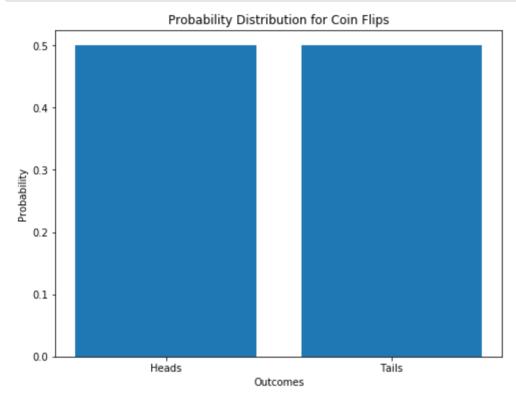


If the Y axis is probabilities (in the range 0 .. 1), we get a distribution of the probabilities among the outcomes of an experiment:

In [14]:

```
# Show the distribution of probabilities for a coin flip:
x = [0,1]
y = [0.5, 0.5]
labels = ['Heads', 'Tails']

plt.figure(num=None, figsize=(8, 6))
plt.xticks(x, labels)
plt.bar(x,y)
plt.bar(x,y)
plt.title('Probability Distribution for Coin Flips')
plt.ylabel("Probability")
plt.xlabel("Outcomes")
plt.show()
```

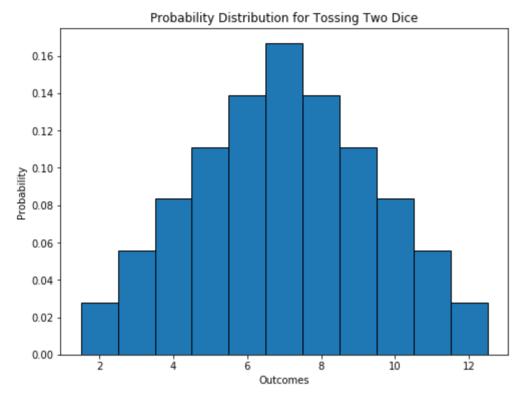


With a few tweaks, you can create an attractive bar chart for arbitrary probability distributions:

In [15]:

```
# Show the distribution of probabilities for flipping two dice
x = [k for k in range(2,13)]
y = [1/36,2/36,3/36,4/36,5/36,6/36,5/36,4/36,3/36,2/36,1/36]

plt.figure(num=None, figsize=(8, 6))
plt.bar(x,y, width=1.0,edgecolor='black')
plt.title('Probability Distribution for Tossing Two Dice')
plt.ylabel("Probability")
plt.xlabel("Outcomes")
plt.show()
```

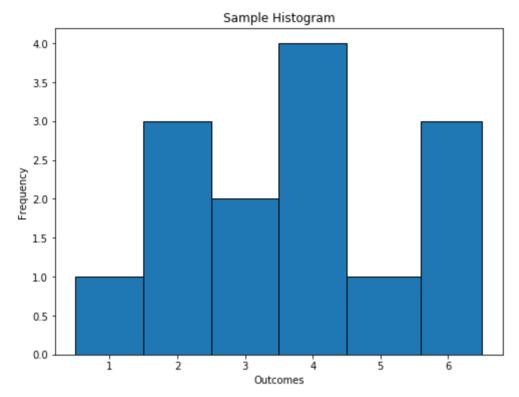


Histograms

- If you give a list of values to hist(...) it will create a histogram counting how many of each value occur; this list can be unordered;
- You will get a cleaner display if you specify where the edges of the bins are, and make sure the edges of the bins are visible, as shown in this example:

In [16]:

```
plt.figure(num=None, figsize=(8, 6))
plt.hist([1,2,4,2,6,2,4,5,6,4,6,3,4,3],bins=[0.5,1.5,2.5,3.5,4.5,5.6,6.5],edgeco
lor='black')
plt.title('Sample Histogram')
plt.xlabel("Outcomes")
plt.ylabel("Frequency")
plt.show()
```



Problem 2

Read and understand the function dieRoll(num_trials) below, which simulates the experiment of rolling a fair, six-sided die num trials times.

- The sample space is {1, 2, 3, 4, 5, 6}.
- The experiment is equi-probable, i.e., the probability of any particular outcome is $\frac{1}{6}$.
- If we record the outcome for a large number of experiments, we would expect the number of outcomes to be "evenly distributed." In other words, for a large number of trials, we would expect the probability of each outcome $k \in \{1, 2, 3, 4, 5, 6\}$ to be

$$\frac{\text{number of times we observed a value } k}{\text{num_trials}} \approx \frac{1}{6}$$

TO DO: For this first problem, simply provide the single line of Python code which would display a histogram of the results of the experiment for 10000 trials with appropriate labels. You should use the Numpy function randint(...), as shown in the next cell.

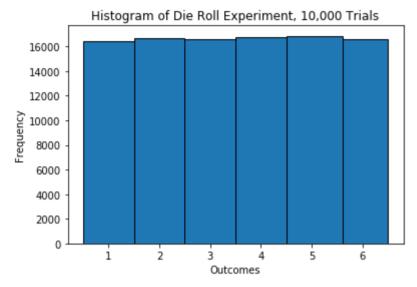
```
In [17]:
```

```
# Demo of randint(lo,hi), which generates a random integer from the sequence
# [lo,lo+1,...,hi-1].
# In other words the upper bound is exclusive, to be consistent with the indices
in lists.
# the Python range function, and so on.
randint(0,4)
Out[17]:
In [18]:
# You can also ask it for an array, since it is a Numpy function:
randint(0,4,10)
Out[18]:
array([3, 3, 3, 2, 2, 1, 0, 3, 0, 2])
In [19]:
# Ok, your turn!
seed(0)
def roll die(num trials = 100000):
    - Simulates rolling a fair die num trials times, i.e., a number is selected
    - (1,2,3,4,5,6) with equal probability num trials times. By default, num tri
als is set to 100000
    - randint(a,b) uniformly and randomly selects an integer x such that a <= x
    - The second argument for randint determines the shape and size of the resul
t array. In this case, we only need
    - a one dimensional array (a list)
    trials and results = randint(1,7,num trials) # this creates a 1D array of le
ngth num_trials of random integers 1..6
    return trials_and_results
example trials = roll die()
```

In [20]:

```
# Solution:

plt.hist(example_trials,bins=[0.5,1.5,2.5,3.5,4.5,5.6,6.5],edgecolor='black')
plt.title('Histogram of Die Roll Experiment, 10,000 Trials')
plt.xlabel("Outcomes")
plt.ylabel("Frequency")
plt.show()
```



Problem 3

Now we will display the same results showing the distribution of probabilities, instead of an explicit histogram.

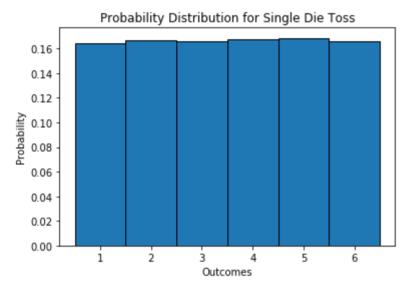
- To calculate the probabilities, you will need to count the number of occurrences of each of the outcomes, you may find the function Counter(...) useful for this (Google "Numpy Counter" to find out how this works);
- Once you have the frequency of each outcome, divide by the total number of trials to get the probability for each.

TO DO: Complete the function stub below which takes the list returned by roll_die(...), or any other experiment returning numerical results, and produces a frequency distribution; this should have the same shape as the histogram, but the Y axis will be probabilities instead of the frequency. Again, create appropriate labels. Demonstrate your function, again, on the list example_trials produced in Problem 1.

```
In [21]:
```

```
seed(0)

# Solution
def show_distribution(outcomes, title='Probability Distribution'):
    num_trials = len(outcomes)
    X = range( int(min(outcomes)), int(max(outcomes))+1 )
    freqs = Counter(outcomes)
    Y = [freqs[i]/num_trials for i in X]
    plt.bar(X,Y,width=1.0,edgecolor='black')
    plt.xlabel("Outcomes")
    plt.ylabel("Probability")
    plt.title(title)
    plt.show()
show_distribution(example_trials,title='Probability Distribution for Single Die Toss')
```



Motivation for Monte Carlo simulation

For the case of a fair die, the distribution is very easily computed. In general, it is very difficult to write down a closed form solution for the distribution of real world events. This is where simulation comes into playinstead of mathematically computing the distribution explicitly, you can use this method of repeating experiments, and recording outcomes to understand the probabilistic rules governing some real world event. When you can come up with an analytical result, this is a nice way of confirming its correctness!

Problem 4

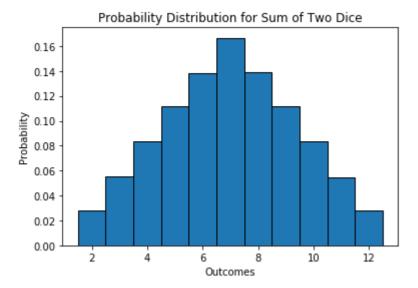
You will now do the same thing you did in the previous problems, but with a new experiment: instead of rolling one die and recording the value, you will simulate rolling n dies and recording their sum. For example, if n=2 and the first die shows up as a 3, and the second die shows up as a 1, the sum (and the value we record) would be 4.

TO DO: Complete the two function stubs below and then demonstrate by providing the single line of code which would print out the probability distribution for rolling 2 dice 100,000 times.

Hint: Not required, but think about how you might do this in one line using Numpy and list comprehensions.

In [22]:

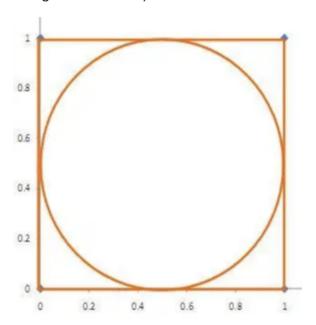
```
seed(0)
# Solution
def roll and add dice(num dice, num trials = 10**5):
    - Perform the trials
   - randint(a,b) uniformly and randomly selects an integer x such that a <= x
 < b
    - The second argument determins the shape of the result. In this case, we on
ly need
   - a one dimensional array (a list)
   trials_and_results = randint(1,7,(num_dice, num_trials))
   acum = np.zeros(num trials)
   for i in range(len(trials and results)):
        acum += trials and results[i]
   return acum
show distribution(roll and add dice(2),title='Probability Distribution for Sum o
f Two Dice')
# Here's another way to do it, showing the power of list comprehensions with num
py!
# A one-line solution!
def roll and add dice(num dice, num trials = 10000):
   return [ sum(randint(1,7,[num dice])) for k in range(num trials) ]
```



Problem 5 (Monte Carlo Calculation of π)

This final problem is also a Monte Carlo simulation, but this time in the continuous domain: we will calculate the value of π using a variation of Problem 1B.

We will leave this one up to you as it the exact details, but you must use the following fact: a circle inscribed in a unit square (i.e., with side of length and area 1.0):



has as radius of 0.5 and an area of $\pi*(0.5^2)=\frac{\pi}{4}$.

Therefore, if you generate num_trials random points in the unit square, as in Problem 1B, and count how many land inside the circle, you can calculate an approximation of π .

For this problem, you must

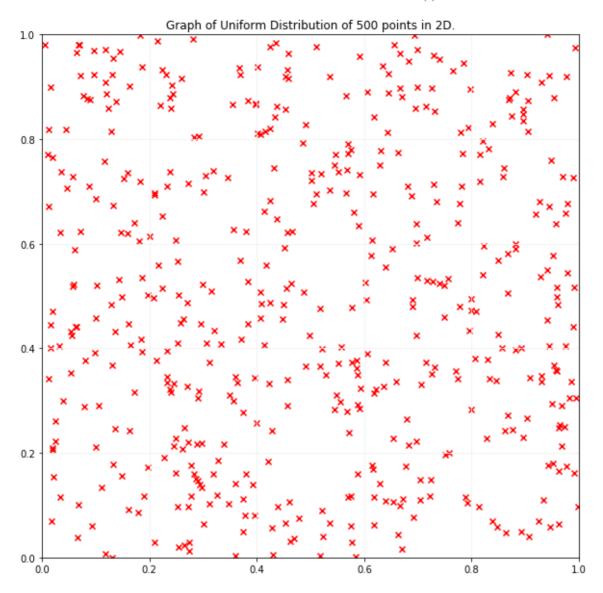
- (A) Draw the diagram of the unit square with inscribed circle and 500 random points, and calculate the value of π .
- (B) With or without drawing the diagram, calculate the value of π you would get from 10^5 trials.
- (C) After completing (B), try to get a more accurate value for π by increasing the number of trials. Your results will depend on your machine, but for comparison, with my new Macbook Pro, I ran it with 10^8 trials while I got a cup of coffee, and it had the answer correct to 3 decimal places. Sometimes I have run big experiments overnight!

</blockquote>

Hint: Start by copying your code from Problem 1B. You might find Mr. Pythagoras's formula useful.

```
In [51]:
```

```
# (A)
def inside(x,y):
    return ((x-0.5)**2+(y-0.5)**2)**0.5 < 0.5
seed(0)
num trials = 500
x vals = [ random() for k in range(num trials) ]
y vals = [ random() for k in range(num trials) ]
plt.figure(num=None, figsize=(10, 10))
plt.title('Graph of Uniform Distribution of '+str(num_trials)+' points in 2D.',f
ontsize=12)
plt.grid(color='0.95')
plt.ylim(0, 1)
plt.xlim(0,1)
plt.scatter(x vals, y vals,marker="x",color="r")
count = 0
for k in range(num trials):
    if inside(x vals[k],y vals[k]):
        count += 1
plt.show()
print("Pi = " + str(4*count/num trials))
```



```
In [24]:
# (B)
#Solution that does not draw the diagram...
            # this will ensure that your results will be consistent with my solu
tion and everyone else's
def find pi(num_trials):
    num inside = 0
    for k in range(num trials):
        x = random()
        y = random()
        if ((x**2 + y**2) ** 0.5 <= 1.0):
            num inside += 1
    return 4.0*num inside / num trials
num trials = 10**5
print("Pi = " + str(find_pi(num_trials)))
Pi = 3.13304
In [25]:
# (C)
num trials = 10**8
print("Pi = " + str(find pi(num trials)))
KeyboardInterrupt
                                           Traceback (most recent cal
l last)
<ipython-input-25-da1629a009f0> in <module>()
      3 num trials = 10**8
----> 4 print("Pi = " + str(find_pi(num_trials)))
<ipython-input-24-265a1f4e1f31> in find pi(num trials)
      7 def find pi(num trials):
      8
            num inside = 0
----> 9
            for k in range(num trials):
                x = random()
     10
     11
                y = random()
```

KeyboardInterrupt:

Appendix: Customizing Your Plots

One thing you have probably noticed is that when you write "bare-bones" code such as we have above, certain defaults are used for the size and layout of the figure and the style of the drawing. One of the most noticable is that when you draw multiple lines, Matplotlib will change the color each time you call the same function (notice that this doesn't happen when calling a different function, e.g., plot followed by scatter).

Using Colors

Matplotlib cycles through a sequence of 10 colors, which is fine if that is what you want. For my taste, they are pretty ugly, and in the next section we will show you how to use the colors you want.

```
In [ ]:
```

```
print("\nThe 10 Matplotlib color sequence, starting at 12 o\'clock and going clo
ckwise:")

plt.figure(figsize=(10,10))
for k in np.arange(0,2*np.pi,np.pi/20):  # arange is like range,
    except it allows you to use floats
        plt.plot([0,np.sin(k)],[0,np.cos(k)],lw=4)

plt.title('Line Colors',fontsize=14)
plt.xlim([-1.2,1.2])
plt.ylim([-1.2,1.2])
plt.show()
```

Here is an example where we simply change the colors of the plot using the appropriate parameter; see a complete list of colors here: https://matplotlib.org/2.0.2/api/colors_api.html) (https://matplotlib.org/2.0.2/api/colors_api.html)

```
In [ ]:
```

```
# EXAMPLE: Plotting a square with lines of different colors
plt.figure(num=None, figsize=(8, 8), dpi=89)
plt.plot([0,1],[0,0],color='red') # Line connecting (0,0) to (1,0)
plt.plot([0,0],[0,1],color='green') # Line connecting (0,0) to (0,1)
plt.plot([0,1],[1,1],color='orange') # Line connecting (0,1) to (1,1)
plt.plot([1,1],[0,1],color='black') # Line connecting (1,0) to (1,1)
```

Changing the Style of Plots

Here is an example showing how to

- · change the size of the whole figure
- · change the color of lines or points
- · change the style of lines or points

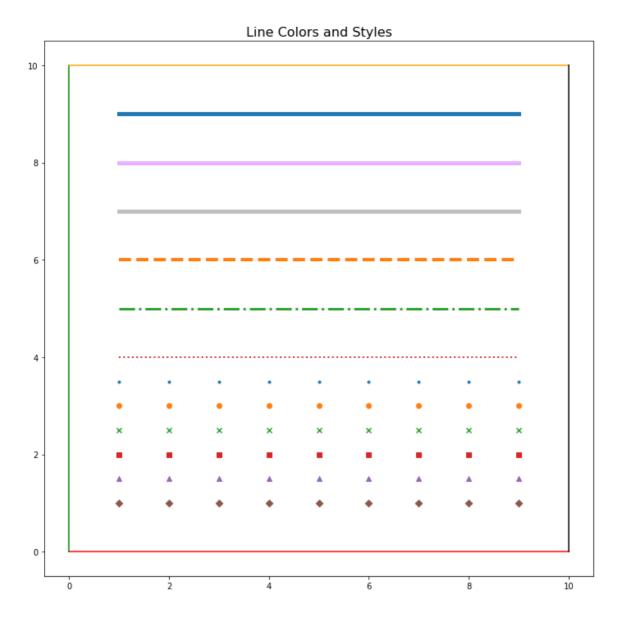
To see a complete list of lines styles see: https://matplotlib.org/2.0.2/api/lines_api.html)
https://matplotlib.org/2.0.2/api/lines_api.html)

To see a complete list of colors see: https://matplotlib.org/2.0.2/api/colors-api.html)
https://matplotlib.org/2.0.2/api/colors-api.html)

To see a complete list of marker (point) styles see: https://matplotlib.org/2.0.2/api/markers api.html#module-matplotlib.markers (https://matplotlib.org/2.0.2/api/markers api.html#module-matplotlib.markers)

In [49]:

```
# EXAMPLE: Plotting a square via lines
plt.figure(figsize=(12, 12))
                                         # the size is (horizontal, vertical)
plt.title("Line Colors and Styles",fontsize=16)
plt.plot([0,10],[0,0], color='red') # Line connecting (0,0) to (1,0)
plt.plot([0,0],[0,10], color='green') # Line connecting (0,0) to (0,1)
plt.plot([0,10],[10,10],color='orange') # Line connecting (0,1) to (1,1)
plt.plot([10,10],[0,10],color='black') # Line connecting (1,0) to (1,1)
plt.plot([1,9],[9,9], linewidth=5)
                                    # give a linewidth in points, default is
 1.0
plt.plot([1,9],[8,8], linewidth=5,color = '#eaafff') # for custom color give
 the RGB value in hex
plt.plot([1,9],[7,7], linewidth=5,color='0.75') # for grey give the percentage o
f white in quotes
plt.plot([1,9],[6,6], lw=4,linestyle='--') # Linestyles
plt.plot([1,9],[5,5], lw=3,linestyle='-.') # Linestyles
plt.plot([1,9],[4,4], lw=2,linestyle=':') # Linestyles
plt.scatter(range(1,10),[3.5]*9,marker='.') # various markers, if you don't spe
cify the colors it will cycle
plt.scatter(range(1,10),[3]*9,marker='o')
                                           # through a bunch of colors, starti
ng with blue, orange, green, etc.
plt.scatter(range(1,10),[2.5]*9,marker='x')
plt.scatter(range(1,10),[2]*9,marker='s')
plt.scatter(range(1,10),[1.5]*9,marker='^')
plt.scatter(range(1,10),[1]*9,marker='D')
print()
```



Et Cetera

Then you can start getting obsessive, adding gridlines, changing the background color, adding legends, text, and so on.

Another nice feature of matplotlib is that you can insert simple Latex commands into titles and text.....

In [1]:

```
• ^'≥÷'# Plotting a smooth curve for the function x^2
x = [i \text{ for } i \text{ in } range(11)]
y = [i**2 for i in x]
plt.figure(figsize=(8, 8))
plt.title('Graph of x = x^2')
plt.xlabel("X")
plt.ylabel("Y")
plt.grid()
plt.plot(x,y)
plt.show()
plt.figure(figsize=(8, 8))
plt.title('Graph of y = x^2')
                            # grid of white lines -- don't use points wit
plt.grid(color='w')
h this, they look funny
plt.gca().set_facecolor('0.95')
                           # background of light grey
plt.plot(x,y,color='b')
plt.xlabel("X")
plt.ylabel("Y")
plt.show()
plt.figure(figsize=(8, 8))
plt.title('Graph of y = x^2')
plt.grid(color='r',alpha=0.1) # alpha sets the transparency, 0 = invisible
and 1 = normal
plt.plot(x,y,color='r',lw=0.5,label='Curve')
plt.scatter(x,y,color='r',marker='o',label='Points')
plt.legend()
plt.xlabel("X")
plt.ylabel("Y")
plt.show()
plt.figure(figsize=(8, 8))
plt.title('Graph of y = x^2', fontsize=16)
plt.xlabel("X", fontsize=14)
plt.ylabel("Y",rotation=0,fontsize=14)
plt.grid(color='0.95')
plt.text(0,90,"The title has been enlarged from default 12 points to 16 points."
)
plt.text(0,80,"Notice that the $y$ axis label is rotated to be upright, \nand th
e x and y labels are also bigger, at 14 points.") # lower left corner of text
string is at point (0,60)
plt.text(0,60,"When drawing points and lines together it looks \nbetter if you m
ake the lines thinner.")
plt.text(0,40,"Honestly I think it is also better to just use\nthe default marke
r (circles) when you draw \nlines, these triangles are kinda fussy\nand they do
n't seem to be centered on \nthe data point.")
plt.plot(x,y,color='b',lw=0.5)
```