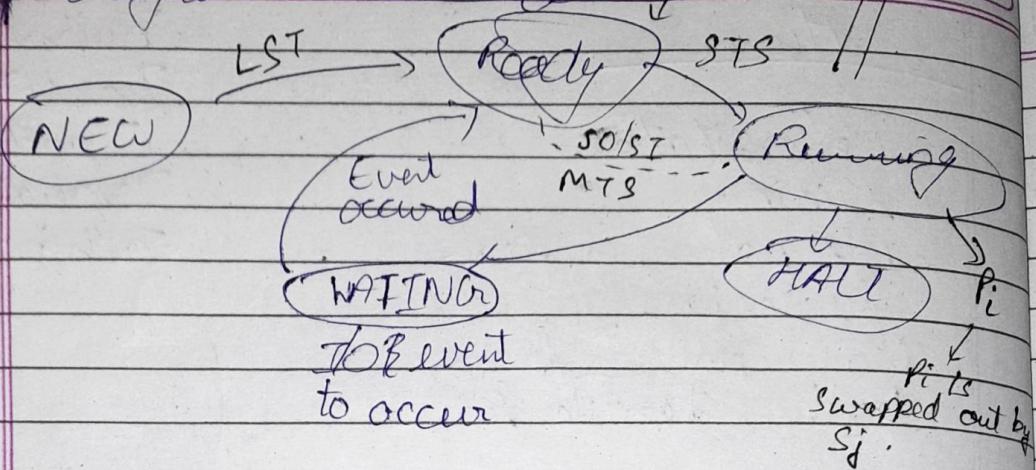


Program execution



New state has a queue of initiated program, so is stored in secondary storage

* Swap out & Swap in:

If some program that was being executed, gets pushed out by a higher priority program; it is said to have been swapped out. and the higher prior prog. is said to have been swapped in.

Scheduling:

Breemptive
Non-Breemptive.

Long term Scheduler

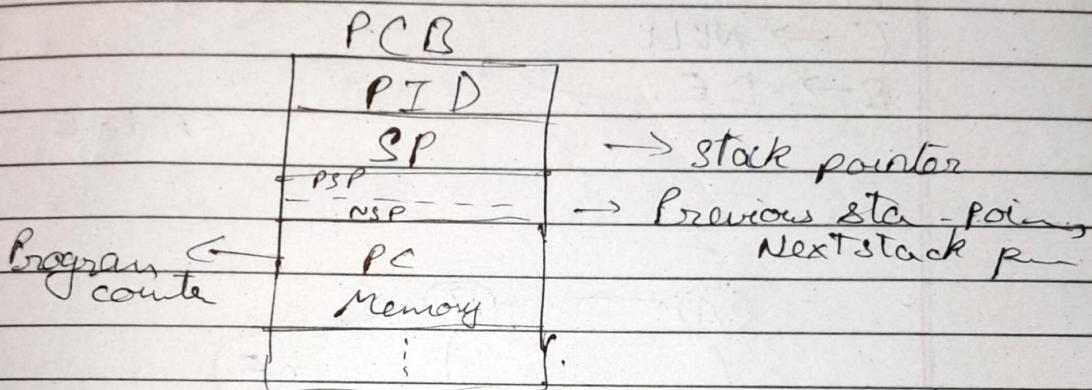
Short term Schedule,

Mid term Scheduler

- * The OS assigns PID (process IDs) to all the processes to uniquely

identify them.

A PCB (Program Control Block) stores the state of execution of the process. It is unique for each process, and has same PTD as the process.



Switching from one process to other is done in the Running state and is called Context Switching.
(swap in & swap out is context switching)

Non-Preemptive: If a process is running, MTS will not stop it in between the exec to push another program

Preemptive: MTS can swap out a running program.

<u>process</u>	<u>Time</u>	<u>Priority</u>
P ₁	10	1
P ₂	20	2
P ₃	15	2
P ₄	5	2
P ₅	10	1

CPU scheduling

FCFS

SJF (SJNF) : (shortest Job first / shortest job next)

Priority scheduling

SRTF : (shortest remaining time first)

Round Robin (RR)

Multilevel Queue Sched. (MLQ)

" Feedback " (MLFQ)

Goals: (of CPU schedule)

- Maximize CPU utilization, Throughput
- Minimize AWAT, WTAT.

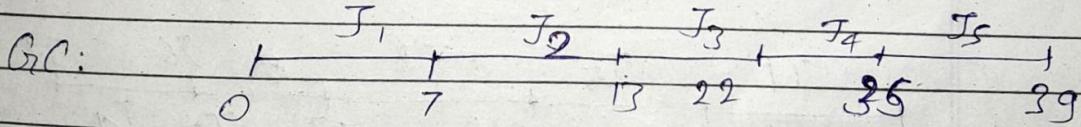
(Average wait time) ^ (turnaround time)

FCFS

Eg: RQ → { J_1, J_2, J_3, J_4, J_5 } → Estimated Execution Time (T_i, P_i)

Arrival time.

	AT	EET
J_1	0	7
J_2	1	6
J_3	1	9
J_4	2	13
J_5	5	4



thus total time taken ⇒

Max (completion time (T_i)),

$$WT(J_i) = 0$$

i.e., 12 - n

J_2 came to RQ at the instance t=1s
and J_1 takes 7 s of execution

so J_2 waited for $7-1=6s$

$$\therefore WT(J_2) = 6$$

so -

$$WT(J_3) = 18-1 = 12$$

$$WT(J_4) = 22-2 = 20$$

$$WT(\cancel{J_5}) = 35-5 = 30$$

$$\therefore AWT = \frac{0+6+12+20+30}{5} = 13.6$$

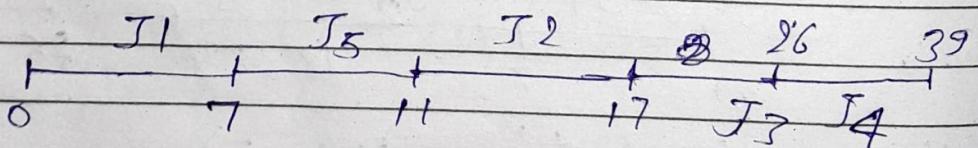
$$ATAT = \sum_{\text{job}} (\text{Time of end} - \text{Time of initiation})$$

$$= (7-0) + (13-1) + (22-8) + \\ (35-2) + (39-5)$$

$$= \underline{\underline{21.9}}$$

② SJF / STN

We need to make sure that the CPU is not idle. So at $t=0$, J_1 is executed.



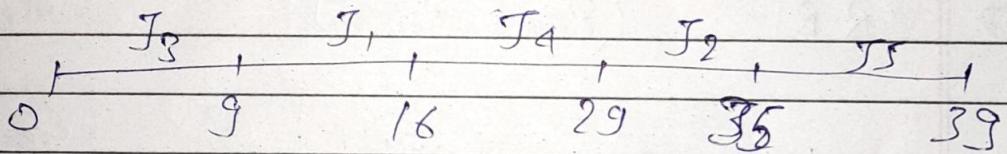
$$AWT: \frac{1}{5} (0 + (7-5) + (11-1) + (17-1) + \\ (26-2)) = 10.4$$

$$ATAT = 18.2$$

Priority Scheduling

	AT	EET	PV
J ₁	0	7	2
J ₂	1	8	3
J ₃	0	8.9	1
J ₄	2	13	2
J ₅	5	4	9

Let's say the scheduler looks at the Ready Queue (RQ) in batches, so, the G-Chart is :



$$AWT = \frac{1}{5} (0 + 9 + (16 - 2) + (29 - 1) + (35 - 5)) \\ = 16.2$$

* Starvation problem : Higher priority process get executed, overlooking the lower priority jobs.

To solve this, after the successful execution of the job, the priority value of each job will be increased by 1.

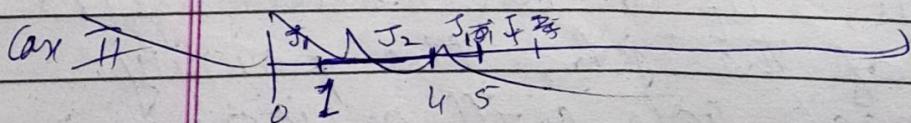
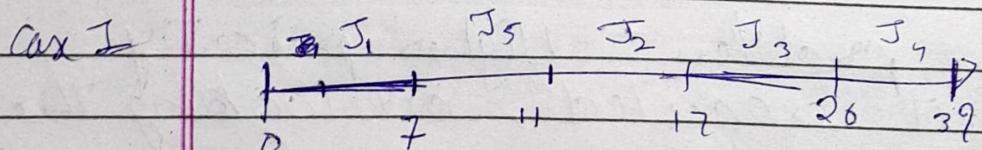
The system only will also set a threshold priority value (say 10 in above case). Once a job reaches this value, it will be given pri of 1 in next job, and will be given the CPU in the next iteration.

This is called ageing.

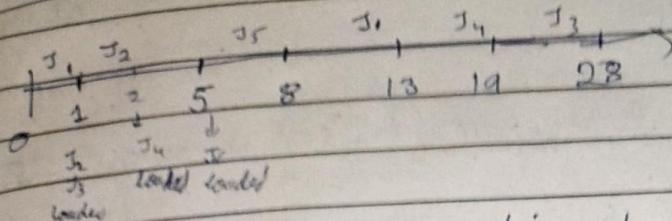
Preemptive Scheduling -

- ① SRTF (Shortest Remaining Task first)
- ② RR (Round Robin)

	AT	EFT	Cox II
J ₁	0	7	→ 6
J ₂	1	6	→ 4 ✓
J ₃	1	9	→ 9
J ₄	2	13	→ 6 ✓
J ₅	5	14	→ 3 ✓



Case II



SRTF → After each time period if a new job is loaded, then the program with lowest time remaining (in execution) will be done.

$$WT(J_1) = 7 \quad \left\{ \begin{array}{l} \text{loaded} = 0 \\ \text{finish} = 13, \text{ running} = 6 \end{array} \right| 13 - 6 = 7 \right\}$$

only 1 context switching → (when one job is stopped for other)

$$WT(J_2) = 0, WT(J_3) = 18$$

$$WT(J_4) = 11, WT(J_5) = 0$$

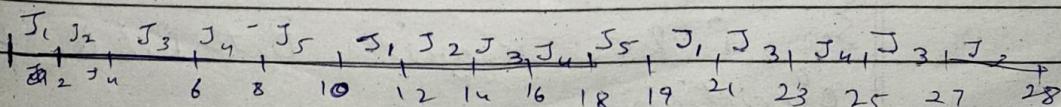
$$\text{WT}_{\text{avg}} = \frac{7+0+18+11+0}{5} = \frac{36}{5} = 7.2$$

② R R

Round Robin.

Time quanta / time slice. → (10 - 100) ms

Same example (Case II) → with time slice = 2.

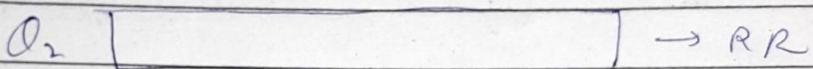


RR \rightarrow removes starvation but too many context switching. Also W/T is a lot

~~W/T is less~~

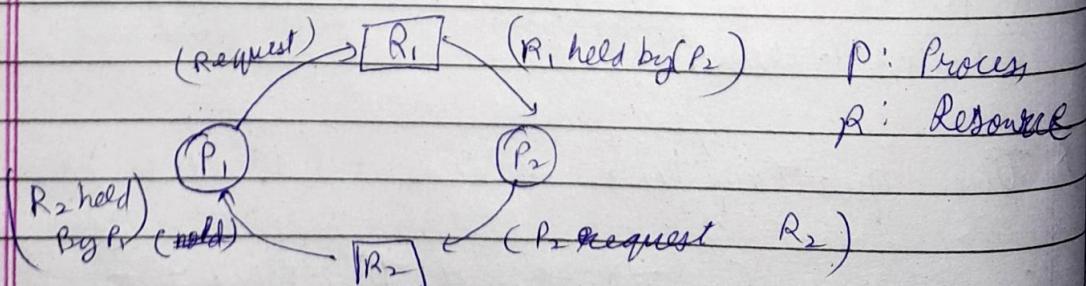
Effective & Useful. (Used in most OS)

MLQ (Multilevel Queue)



{Based on some condⁿ jobs are categorised in diff queues. And diff queues are using diff scheduling techs}

Process Synchronization & Communication



Say, P₁ & P₂ require Both R₁ & R₂ for execution

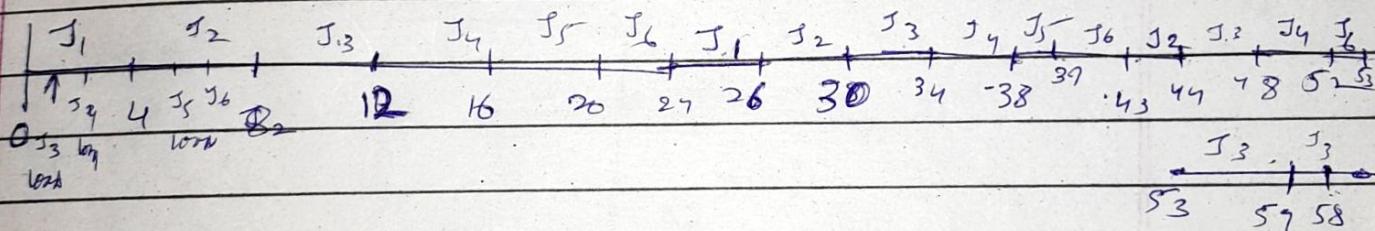


A Programs are in deadlock :-

	AT	CPU	Priority
J ₁	0	6	3
J ₂	0	9	2
J ₃	1	17	4
J ₄	2	12	1
J ₅	5	5	2
J ₆	6	9	5

Implement RR (t=4), Priority, SRTF

RR



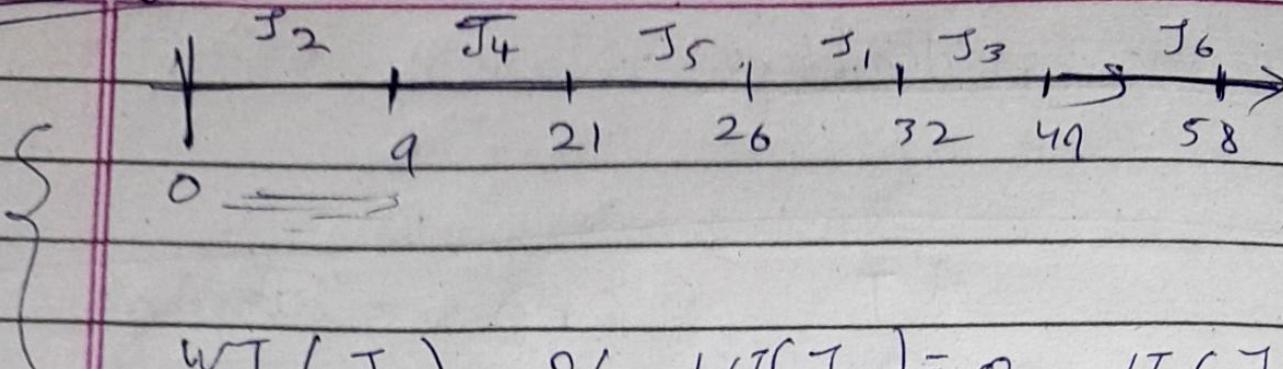
$$WT(J_1) = 20, WT(J_2) = 35, WT(J_3) = 40, WT(J_4) = 38 \\ WT(J_5) = 29, WT(J_6) = 38$$

A. W_{avg} = $\overline{33.3}$ switches = 14

$$TAT(J_1) = 20, TAT(J_2) = 44, TAT(J_3) = 57$$

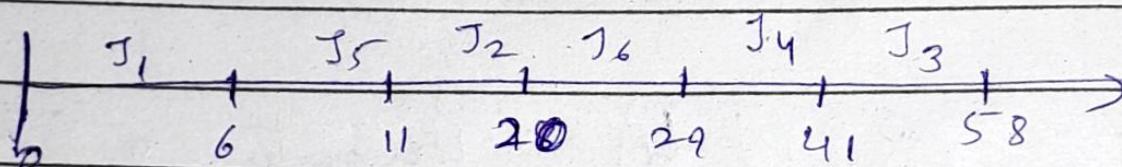
$$TAT(J_4) = 50, TAT(J_5) = 34, TAT(J_6) = \frac{53-6}{4} = 47$$

Priority



$$WT(J_1) = 26, WT(J_2) = 0, WT(J_3) = 3 \\ WT(J_4) = 7, WT(J_5) = 16, WT(J_6) = 43 \\ \text{Avg } WT = 20.5$$

SRTF



$$\text{Avg TAT} = \frac{6+9+20+20+39+57}{6}$$

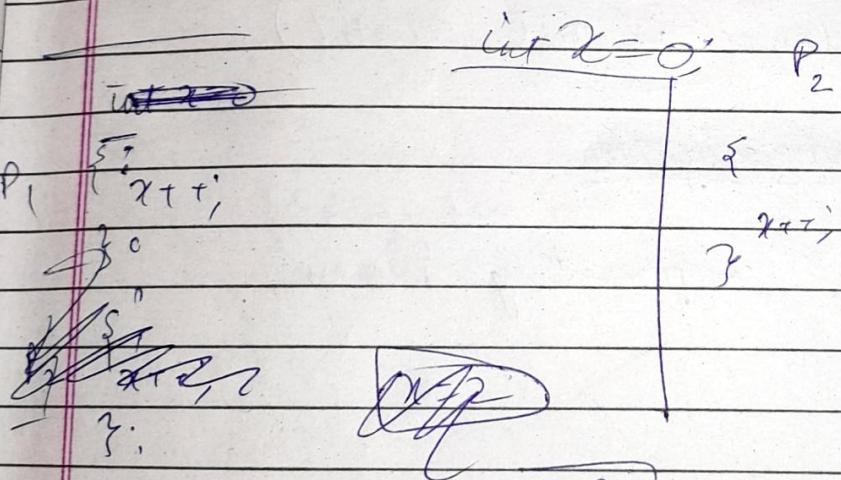
Process Synchronization

- Independent Process
- ~~Dependent~~ Cooperating process
- Race Condition
- Critical Section
 - Mutual Exclusion →
 - Progress
 - Bounded Waiting
- Mutex lock

~~12/12/2021~~

2/11/2021

- Same place
 - Binary
- Semaphore
 - ↳ Binary
 - ↳ continuous



$x++ \Rightarrow$ LW $R_1, x;$
 ADD $R_1, R_1, 1;$
 SW x, R_1

Assume P_1 loads x to R_1 , & then the process finds P_2 must execute first, ~~1/12/2021~~

P₁

P₂

LW R₁, X

* context switch

ADD R₁, R₁, I;
SW X, R₁

x = 1

x = 1

* This is not the right result.
(bank balance is not right)

Lack of synchronization

* P₁ & P₂ are cooperating process

Race condn

No. of process trying to access same section
of code / memory.

Such sections are called critical section

do {
 entry section
 } critical section
 exit section
 remainder section
 } while (true)

give the CS to
 other program
 only when one
 is ~~finished~~ finished
 accessing CS

→ Mutual Exclusion → Programs accessing CS
must be mutually exclusive

→ Bounded Waiting → It should not be the case that
one program is waiting for ∞ time.

mutex lock

access CS → lock flag = 1
 other program ← lock flag = 0 Completion
 can access CS

15/2/24

Deadlock

- Necessary & Sufficient Condⁿ
- Not Mutual exclusion
- Hold & Wait
- No - Preemption
- Circular wait

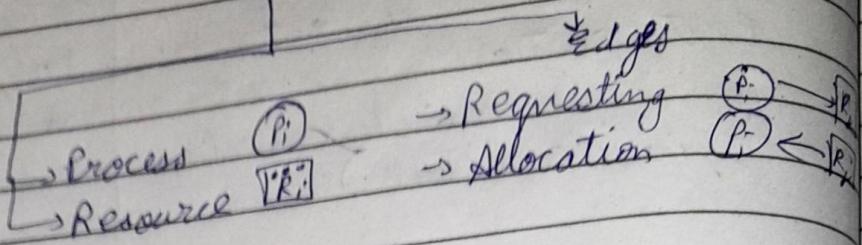
Deadlock Set

- Deadlock Prevention
- .. Avoidance
- .. Detection & Recovery

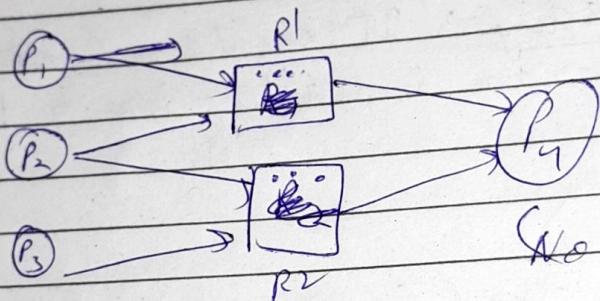
(Until one task if fulfilled the resource must not
 be allocated to other program)

Request
Use
Release

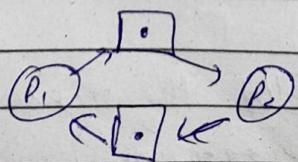
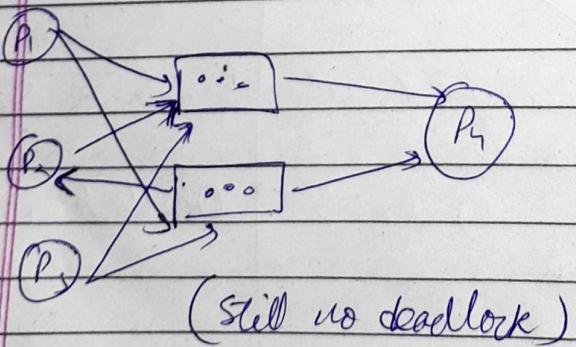
Resource Allocation Graph $G(N, E)$



- diff types of resources
- Each R_i has 'm' no. of identical Resources



... → (...) dots represent no. of identical instances/ resources



This is deadlock

If there is a cycle in graph & all the resources have 1 instance then deadlock will occur

In case of multiple instance → may or may ~~not~~

$$A = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

[min card(S)] if $S \subseteq A$, such that
 $a+b=9$, for some $a, b \in S$.

minimum
cardinality

There exists, $a, b \in S$, such that
 $a+b=9$

So we select all the odd numbers.

$$\therefore S = \{1, 3, 5, 7, 9, \dots\}$$

The last remaining number must be
some even no., which on sum, gives 9

$$\therefore \text{min card} = 5$$

Difference of a polynomial

n^{th} difference of an n^{th} degree
poly is constant and $(n+1)^{\text{th}}$ diff is 0

$$f(x) = a_0 x^n + a_1 x^{n-1} + \dots + a_{n-1} x + a_n$$

$$\Delta f(x) = f(x+h) - f(x)$$

$$= a_0 ((x+h)^n - x^n) + a_1 ((x+h)^{n-1} - x^{n-1}) + \dots + a_n - a_n$$

Deadlock Avoidance

Banker's Algorithm.

n - processes at some time

m - resource types

To handle all the resources, we use a vector.

Available_m : Avail[i] = k

↑

k resources available for ith process

Max^{*}_{nxm} : Max[i, j] = k

k no. of jth resources instances are required for successful execution of ith process.

Allocation_{nxm} : Alloc[i, j] = k

k resources of jth type allocated to P_i

Needed_{nxm} : Need[i, j] = k

k resource instances of jth type are still required by P_i

Request_i : stores the resources required by P_i

The requested amount of resource must be less than equal to Need.

- ① If $\text{Request}_i \leq \text{Need}_i$, then goto step 2
- ② If $\text{Request}_i \leq \text{Available}$ then goto step 3, else wait.
- ③ $\text{Avail} = \text{Avail} - \text{Request}_i$
 $\text{Alloc}_i = \text{Alloc}_i + \text{Request}_i$.
 $\text{Need} = \text{Need} - \text{Request}_i$.
- ④ Check if the new state is safe or not.
 This is done using a safety algorithm.

Safety algo:

- ① $\text{Work} = \text{Available}$;
 $\text{Finish} = \text{False}$;
- ② Find an i such that
 $\text{Finish}[i] = \text{F}$ and $\text{Need}_i \leq \text{Work}_i$;
 if no such i is found goto step 4
- ③ $\text{Work} += \text{Allocated}_i$.
 $\text{Finish}[i] = \text{T}$;
 goto step 2
- ④ $\text{Finish}[i] = \text{True} \forall i$
 Safe state of system

Ans

A B C
10 5 7

(Three resource types)

No. of processes: 5 ; $\{P_0, \dots, P_4\}$

	A	B	C
Allocation	0	1	0
5×3	2	0	0
P_0	3	0	2
P_1	2	1	1
P_2	0	0	2
P_3	0	1	1
P_4	0	0	2

Max_{5x3}:

	A	B	C
P_0	7	5	3
P_1	3	2	2
P_2	9	0	2
P_3	2	2	2
P_4	4	3	3

Available:

A B C
3 3 2

Available = $[10 \ 5 \ 7] - \text{np.sum (Allocation columns)}$

Need_{5x3}:

	A	B	C
P_0	7	4	3
P_1	1	2	2
P_2	6	0	0
P_3	0	1	1
P_4	4	3	1

Need =
Max - Alloc

Now we use safety Algo:

$$\text{Work} : [3 \ 3 \ 2]$$

$$\text{Finish} = [\text{False}] \times 5$$

we find P_i which can be finished with remaining resources. $i=1$ is found.

$$\therefore \text{Finish}[1] = T$$

$$\text{Work}_2 = \text{Work} + \text{Allot}_1$$

$$\Rightarrow [3 \ 3 \ 2] + [2 \ 0 \ 0] \\ = [5 \ 3 \ 2]$$

Next $i=3$

$$P_3 : F[3] = T$$

$$\text{work} + = \text{Allot}_3$$

$$= [7 \ 4 \ 3]$$

$$P_4 : F[4] = T$$

$$\text{work} + = \text{Allot}_4$$

$$= [7 \ 4 \ 5]$$

$$P_5 : F[0] = T$$

$$\text{work} + = \text{Allot}_0$$

$$= [7 \ 5 \ 5]$$

$$P_2 : F[2] = T$$

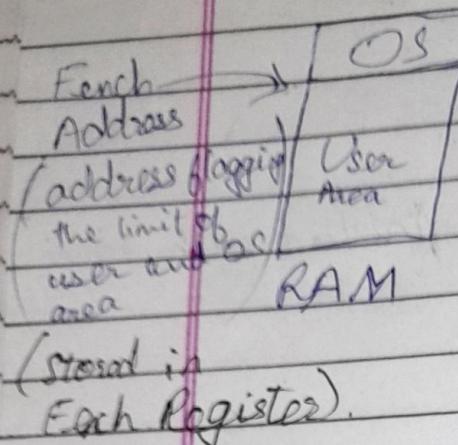
$$\text{work} + = \text{Allot}_2$$

$$= [10 \ 5 \ 7]$$

The safe sequence is: P_1, P_3, P_4, P_0, P_2

22/09/21

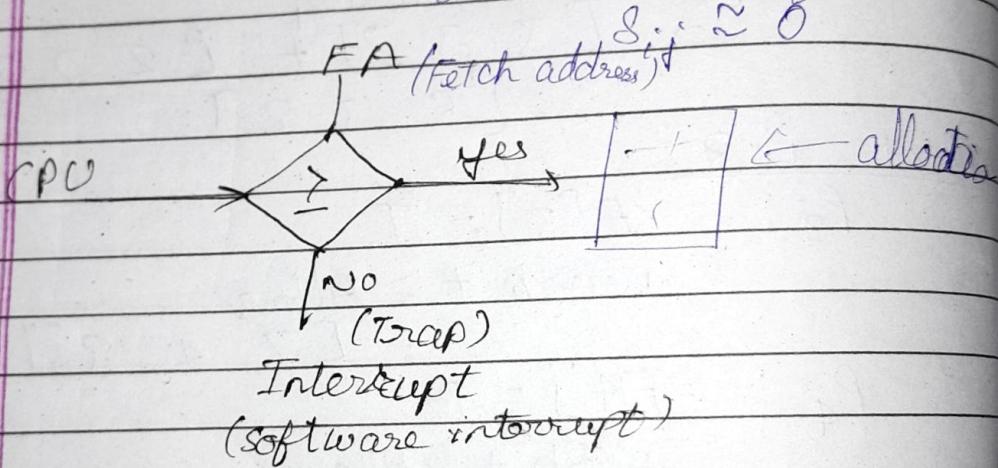
Memory Management



magnetic tape / SSD
 III I III I I I I

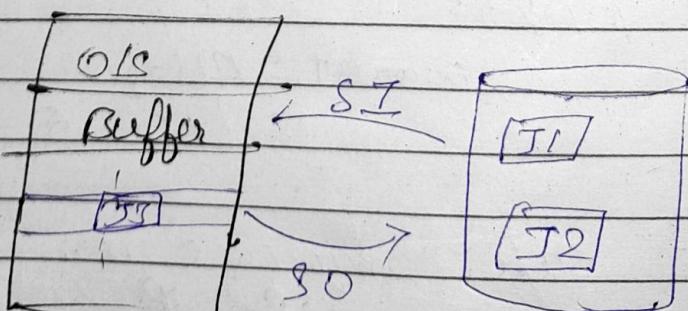
to go from i to j
 memory block in memory
 S_{ij} = No. of blocks (on)

but in case of RAM



(If the requested add is less than
 Fetch address)

Swap in / swap out:

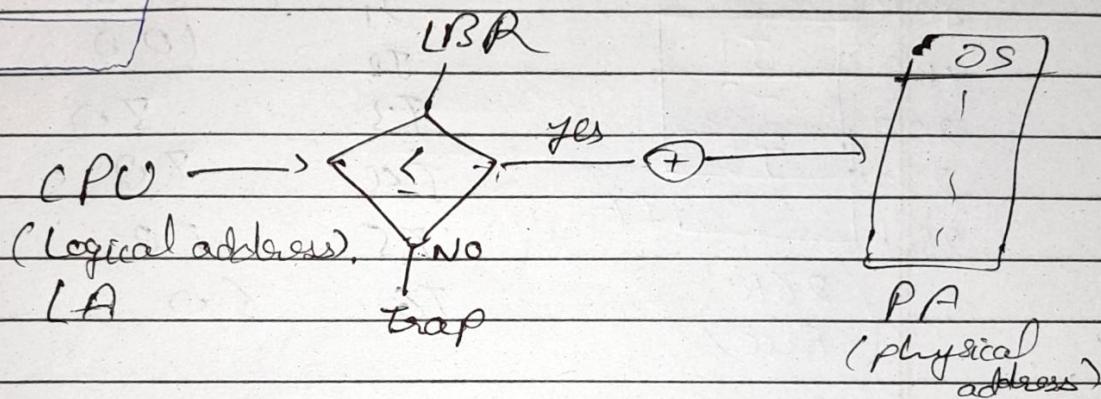
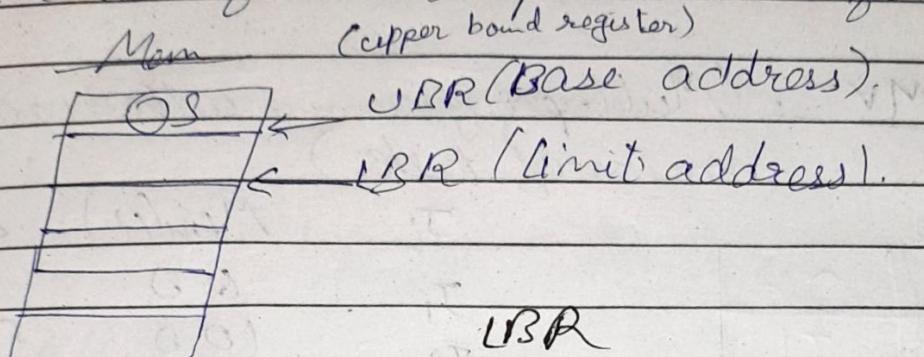


Instead of swapping in/out of the primary memory and secondary storage

The buffer is used in the RAM for this purpose, which is faster.

MFT: (multiprogramming with fixed no of tasks)

The no. of tasks or processes is fixed.



memory allocation can be of three types

- ① First fit: allocate the address whenever space enough is found
- ② Last fit: allocate with least waste
- ③ Worst fit: allocate in the largest block.

Internal fragmentation: empty or wasted space inside the allocated space.

External fragmentation: Fragmented space is available but can't be used as it is not in a single block, so the OS can't allocate it to some other job.

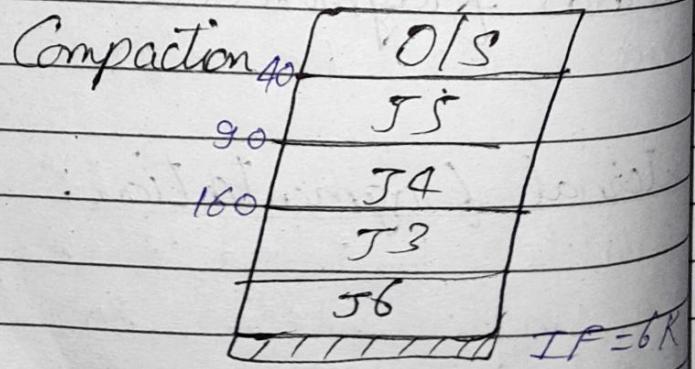
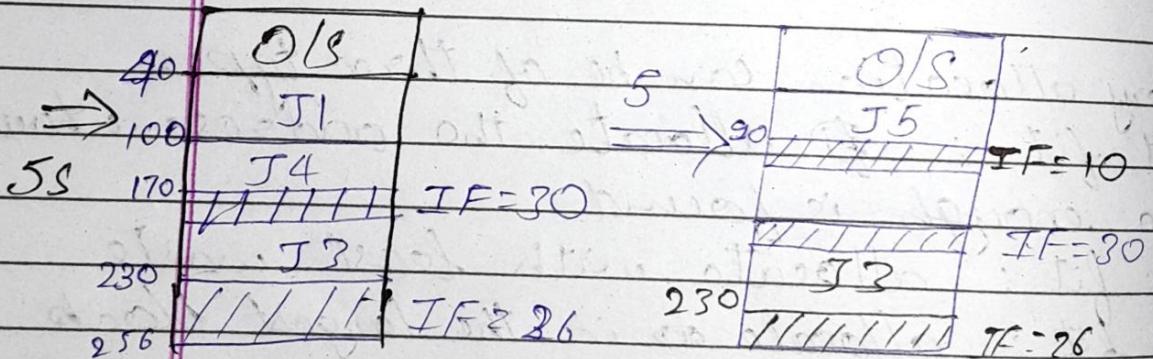
$$\sum_{i=1}^n \text{IF}_i \geq \text{New Job}$$

This unused space can't be allocated
and leads to External fragmentation

(s) MVT: (Multi programming with variable number of tasks)

J_i	Mem(μ)	Stk
J_1	60	10
J_2	100	5
J_3	80	20
J_{40}	70	8
J_5	50	15
J_6	60	9

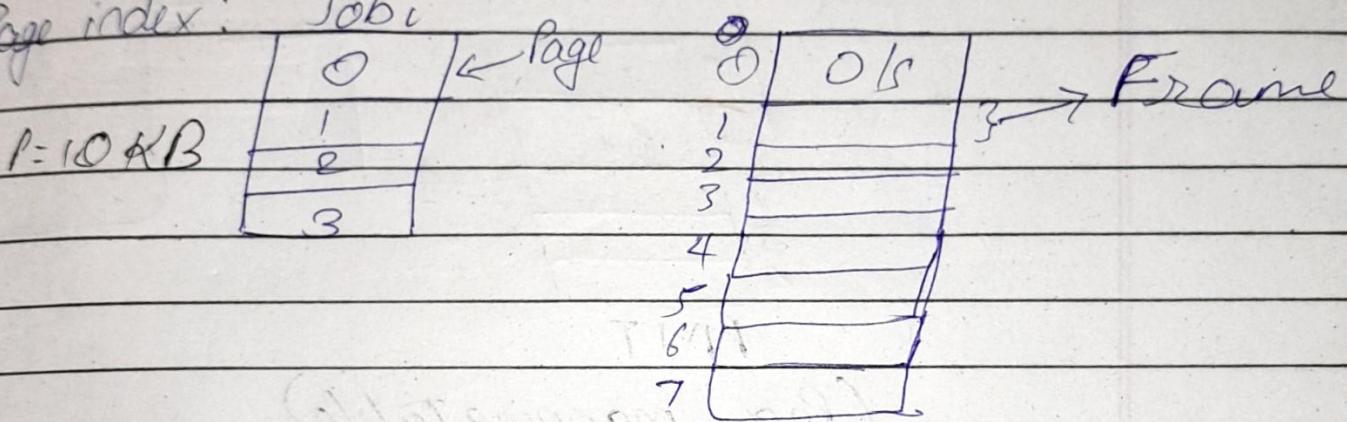
40K O/S 100 J1 200 J2 230 J3 256K IF (26K) Free



MVT results in lots of internal fragmentation. This can be avoided/rectified using a technique called Compaction, where all the unused (fragmented) memory is stored in one block.

Paged Memory management

Page index: Job i



$$\forall i, j, S(P_i) \subseteq S(f_j).$$

also: any $P_i \rightarrow f_j$ iff $f_j = 0$.

P = page size.

$$L = p + d$$

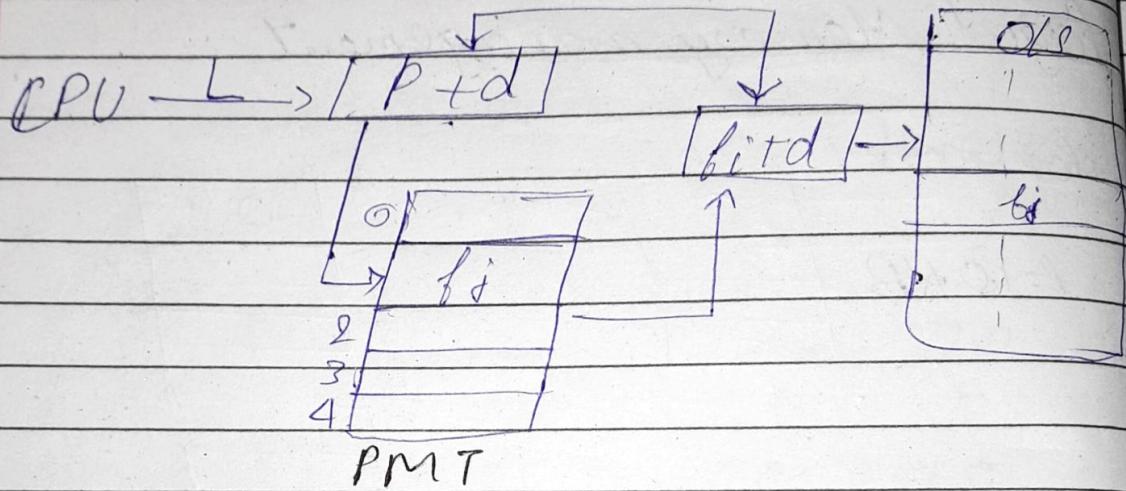
logical address \uparrow offset with the page \downarrow (offset is the space in the page)

page no. \uparrow

page no. $p = L / P$
 $d = L \% P$

- * Any page can be fitted to any frame so we need to find some mapping from pages to frames.

The CPU generates logical address which is given by $P + d$

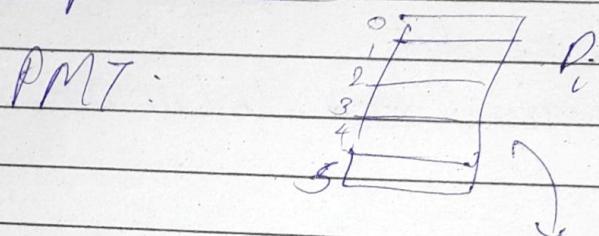


(Page mapping table).

- * (In MFT & MVT the memory was allocated sequentially, but in Paging, it is not necessarily sequential)

- Memory Management
- * MFT (continuous m.)
 - * MVT
 - * Paging Memory management (Non-contiguous memory allocation)
 - * Segmented
 - * Page
 - * Demand/virtual

Page map table



it is mapped to frame given in PMT

0	1	2	3
0	1	2	3
0	1	2	3
0	1	2	3
0	1	2	3

The system calculates the probability of some page being used in near future called V/I locality of reference

V/I: $\rightarrow 0$ implies the page is available in main memory. So if the system needs that page in future, the page is checked for validity.

and then accessed.

We also need to check if the page (say P2) has been updated in main memory. If it has, the change must be reflected in secondary memory.

Say the memory is filled with pages, and the CPU needs a page that is not in RAM. So we need to select a page in the main memory and replace it with the required page.

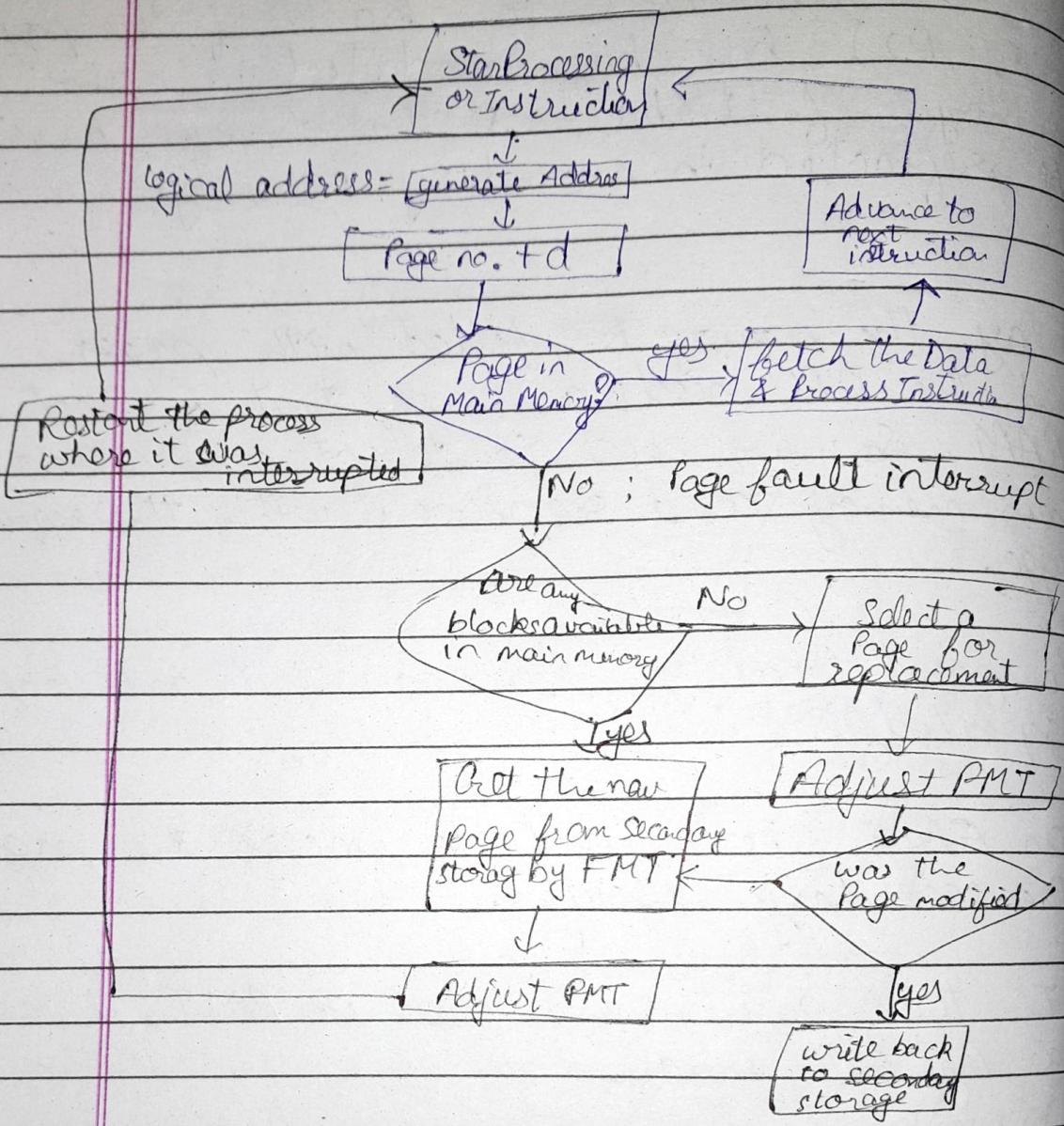
Temporal Locality: for pages that are accessed repeatedly.

an FMT is used to access the page in the secondary storage.

If the page is not listed in PMT, it throws a Page Fault error.

PMT is stored in the CPU cache (11/12)

Master's Flowchart



If a page is updated, the change stays in the main memory with the page. This change is reflected in secondary storage only when it is replaced from main memory.

To select a page we use:

① FIFO

② LRU

③ optimal al.

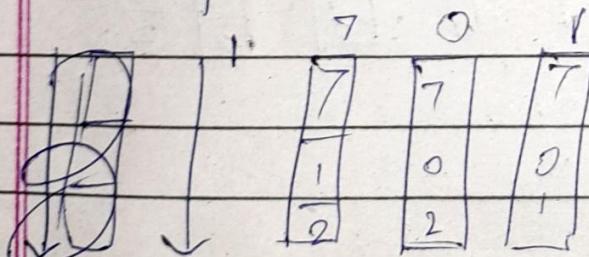
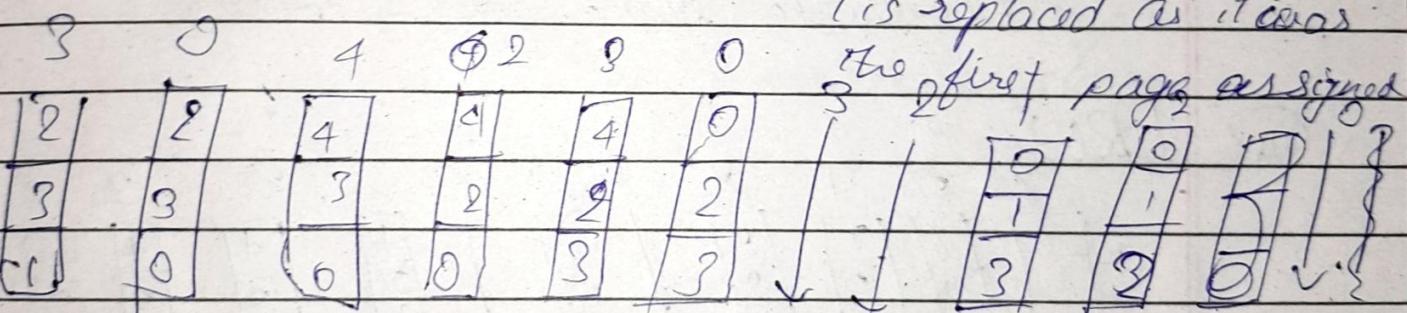
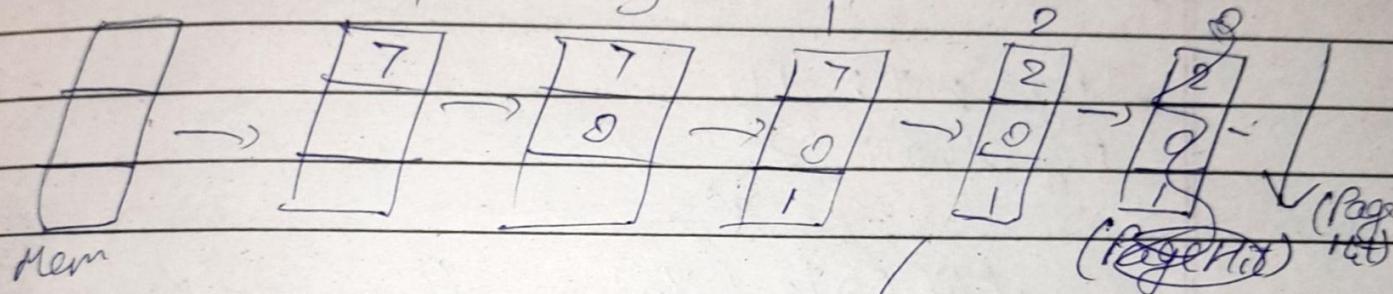
Page Replacement Algorithm

- ① First come First serve
- ② Optimal
- ③ Least Recent Used (LRU)

Ex:

7 0 1 2 0 3 0 4 2 3 0 7 2 1 2 0 1 7 0 1

let's say that our memory has 3 frames.



Page Hits : 5

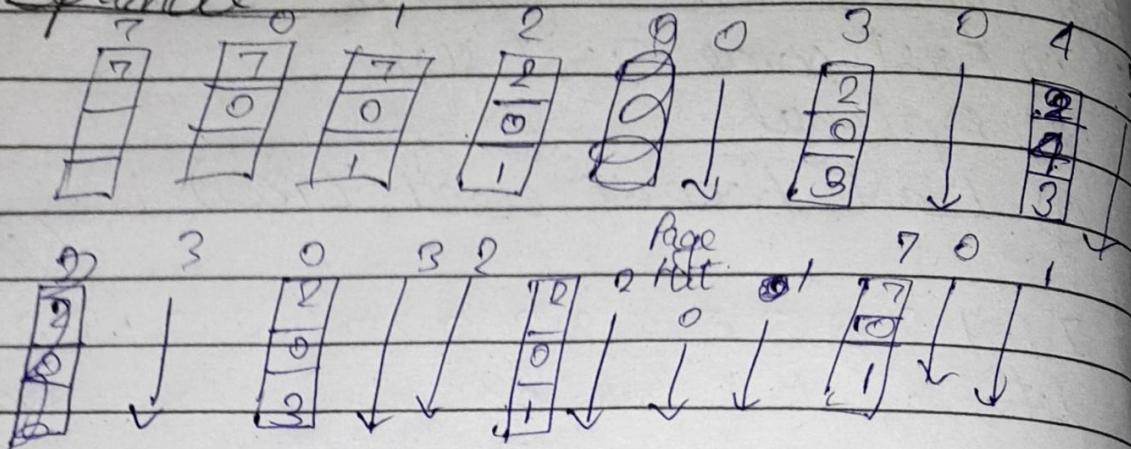
Page Miss: 15

(count after all frames are filled)

Page Hit ratio : $\frac{5}{20} = \frac{H_1}{N}$

Page Miss ratio : $\frac{P_M}{N} = \frac{15}{20}$

ii) Optimal.



Page hit : 11

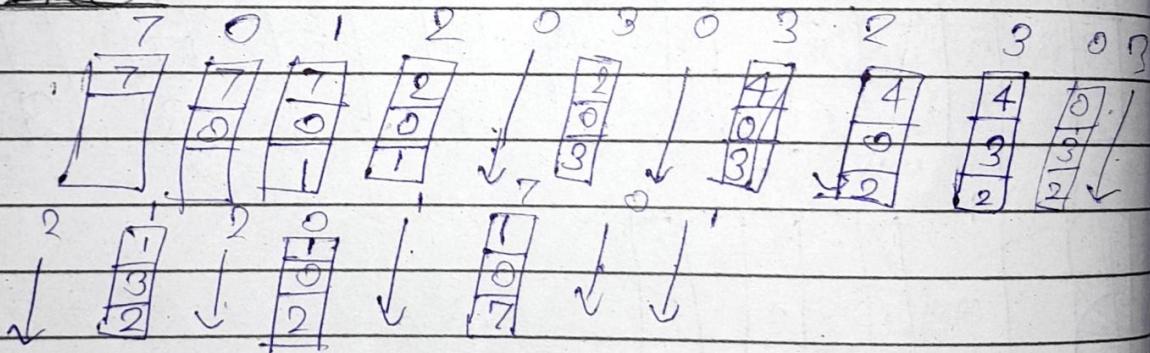
Page Miss : 9

~~Spec~~

$$\text{Hit Rate (HR)} = \frac{11}{20} = 55\%$$

$$\text{Miss rate (MR)} = \frac{9}{20} = 45\%$$

iii) LRU

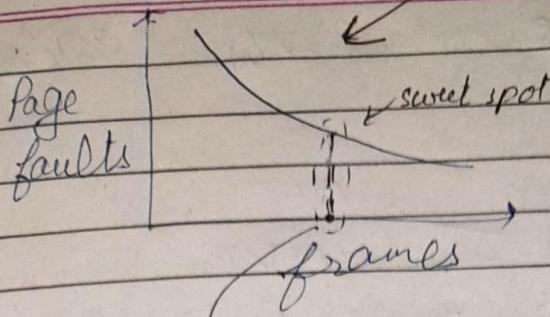


PH. \Rightarrow 8

PM. 12

$$HR = 8/20$$

$$MR = 12/20$$



$\lceil \frac{N}{2} \rceil$ frames = $\lceil \frac{1}{2} \cdot \text{No. of pages} \rceil$.
 (This result is given by an Approximation algorithm).

two parameters play major role in memory management

$t_{a_1} \rightarrow$ Access time in main memory
 $t_{a_2} \rightarrow$ Access time in secondary storage
 $t_{a_1} \ll t_{a_2}$
 ↓ ↓
 associated P P
 with H M

$$\text{then Effective Access Time} = t_{eff} = (H \cdot t_{q_1} + M \cdot t_{q_2})$$

our objective is to minimize T_{eff} .

Ex: (1rc)

9. 76 11 29 5 3 2 11 7 9 5 12 2 10 9 12
11 3 2 16 5 3 2 9 6 7 1

	2	9	5	3	0	11	7	9	5	12	2	9
9	2	92	9	2		2	0	2	5	3	5	1
7	7	9	9	9		11	7	7	7	12	112	
6	6	6	5	5		5	7	7	7	2		
11	11	11	11	3	↓	3	3	9	9	9	9	↓
12	11	3	2	16	5	3	8	9	6	6	7	1
↓	71	7	11	14	15	2	8	8	8	8	8	6
↓	12	12	12	16	16	9	9	9	9	9	9	9
9	2	3	3	3	3	2	3	2	3	2	3	1

$H_k = 5/28$

$H_m = 20/28$

Summary

Memory man.

① Continuous \rightarrow MFT

② Non-Continuous \rightarrow MVT

③ Non-Contiguous \rightarrow Paging

④ Segmented

→ Page-Segmented
Demand page

→ logical address = Page no. + offset

→ physical address \rightarrow Memory in frames.

eff. s(P_i) = s(f_i) // PMT and FMT

→ Master Diagram

→ Write back / write through policy.

(updation in secondary storage)
(of pages)

(simply
replacing
the page)

→ Page Replacement algorithm:

FTFO, Optimal, LRU.

→ Memory access time (t_a)

→ Secondary storage time (t_s)

→ Effective access time

Q In a system, there are three types of resources E, F and G.

Four processes P₁, P₂, P₃ & P₄; The processes have declared their max resource requirement max as Max. Eg:

$\text{Max}(P_2, F)$ is the maximum no. of instances of F that P₂ would require. The Allocation matrix is :

Alloc Max

	E	F	G		E	F	G
P ₁	1	0	1		4	3	1
P ₂	1	1	2		2	1	4
P ₃	1	0	3		1	3	5
P ₄	2	0	0		5	4	1
(S)	5	1	6				

Avail

3 3 0

E F G
8 4 6

Q From the perspective of deadlock avoidance, which of the following is true.

- i System is in safe state
- ii System is not in safe state, but would be, if one more instance of E was available
- iii " " " " "
- iv If one instance of F was available
- v " " " " "
- vi If one instance of G was available

→ P → 07

Need →	P ₁	E	F	G
P ₂	3	3	0	
P ₃	1	0	2	
P ₄	0	3	2	
	3	4	1	

(P1)

$$Av \rightarrow [3 \ 3 \ 0] + [1 \ 0 \ 1]$$
$$[4 \ 3 \ 1].$$

∴ if Av is odd

$$\begin{matrix} & P_2 [4 \ 3 \ 2] \\ \swarrow & \downarrow P_3 [5 \ 2 \ 07] \\ [5 \ 4 \ 4] & \downarrow P_4 \\ & [084 \ 07] \end{matrix}$$

∴ Resource G is required

Qn Exec in Ubuntu / Linux.

```
#include <stdio.h>
int main()
{
    int i;
    for(i=0; i<10; i++)
    {
        if (i%2 == 0)
            fork();
    }
    return 0;
}
```

Ques Consider the processes with arrival time (in ms); and their CPU burst areas follows:

	<u>AT</u>	<u>CT</u>
P ₁	0	3.2
P ₂	1	+ 1
P ₃	3	3
P ₄	4	7

They are executing by SJRTF (Round robin) if the avg waiting time is 1 ms.
 Then value of τ is:

$$BT \leq T.$$

$$\oplus W_1 \rightarrow 0 \quad 3$$

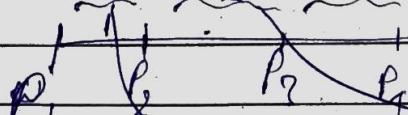
$$W_2 \rightarrow 2 \quad 4$$

$$W_3 \rightarrow 1, \quad 7$$

$$W_4 \rightarrow 3, \quad 7+7$$

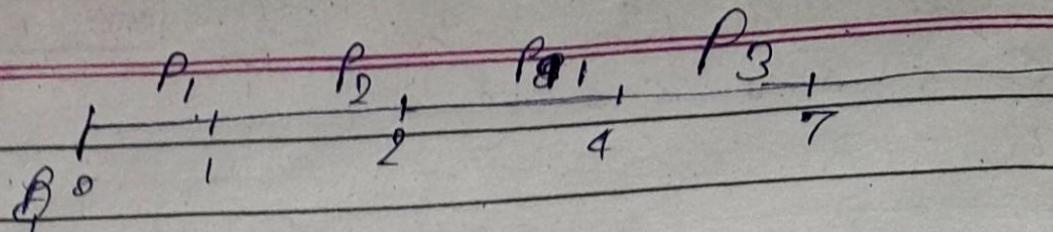
$$(W_1 + W_2 + W_3 + W_4) = 23$$

$$W_1 \rightarrow 0, 2, 1, \dots$$



0 1 3

Case 1



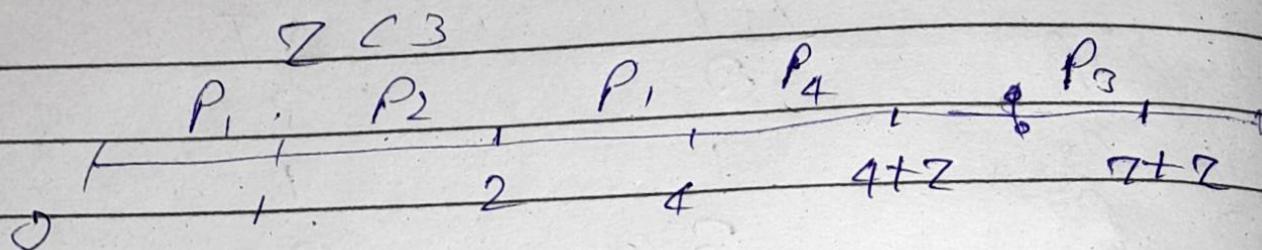
$$w_1 = 1$$

$$w_2 = 0$$

$$w_3 = 1$$

$$w_4 = 3$$

Case 2:



$$w_1 \rightarrow 1$$

$$w_2 = 0$$

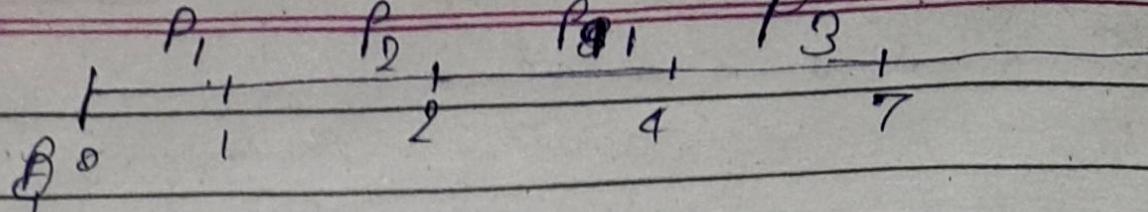
$$w_3 = 1+z$$

$$P_4 = 0$$

$$\frac{9+z}{4} = 1$$

$z = 2$

Case 1



$$z > 3$$

$$\omega_1 = 1$$

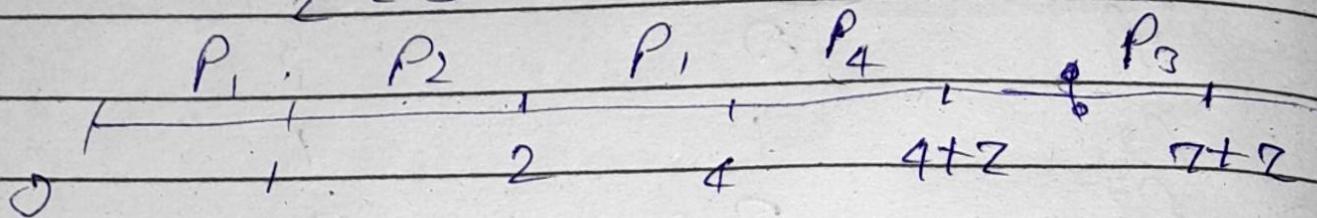
$$\omega_2 = 0$$

$$\omega_3 = 1$$

$$\omega_4 = 3$$

Case 2

$$z < 3$$



$$\omega_1 \rightarrow 1$$

$$\omega_2 = 0$$

$$\omega_3 = 1+z$$

$$\omega_4 = 0$$

$$\frac{1+z}{a} = 1$$

$$z = 2$$

7/3/21

OS

secondary storage:

Storage types -

- RAM (Random Access Memories)
 - serial Access Storage Device (SASD)
 - Direct Access storage Device (DASD)
- divided based
on access time

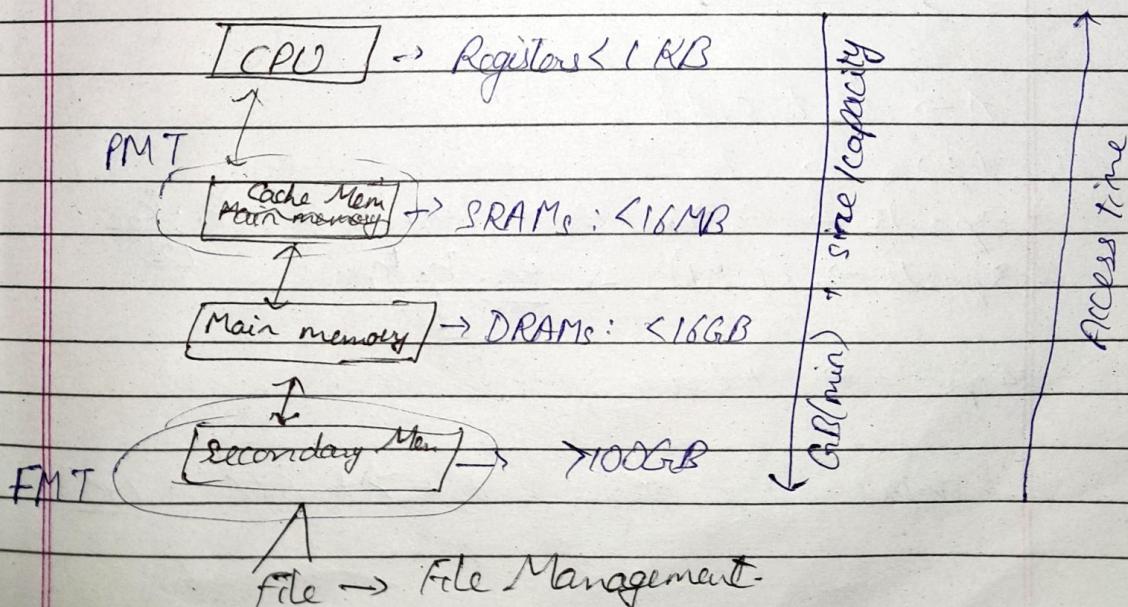
say i is ----- j th (memory block)

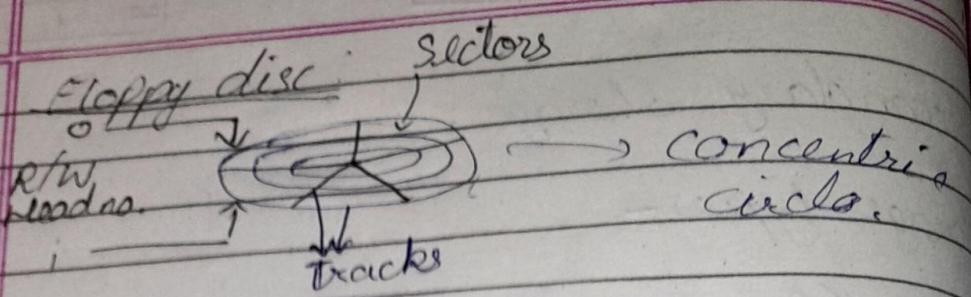
say we need to find T_{ij} . (access time from block i to j).

then if $T_{ij} \approx 0 \rightarrow$ RAM.

for SASD $\rightarrow T_{ij} \rightarrow$ very high (Eg: Magnetic tape)

For DASD $\rightarrow T_{ij} = ?$ 0 - very high?
(Eg: Hard disk; floppy disk)





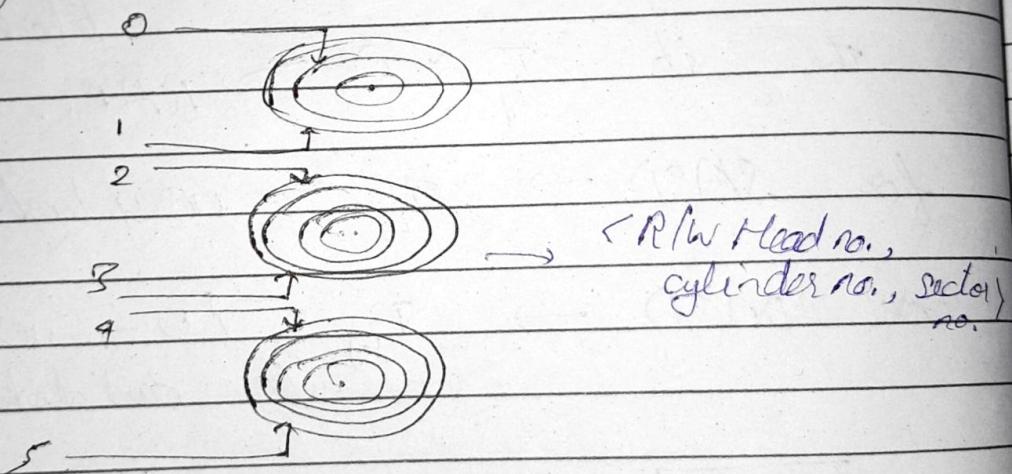
<track no., sector no. >

Block of Memory

if the disc is two sided:

< R/W Head no., track no., sector no. >

if there are multiple discs, then



$A \rightarrow \{a, b, c, d\}$

1 part \rightarrow 1 way

$$2 \text{ parts} \rightarrow (1, 2) \text{ or } (2, 1) \rightarrow \frac{a_1 \cdot b_1}{L^2} + \frac{a_2 \cdot b_2}{L^2}$$

$$3 \text{ parts} \rightarrow (1, 2, 1) \rightarrow \frac{a_1 \cdot b_1 \cdot c_1}{L^2}$$

4 p \rightarrow 1 way ;

$$\therefore \text{total ways of } n : 1 + 2 + 6 + 1 = 10$$