

# ALY6050 Introduction to Enterprise Analytics

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Module 3

Time Series Analysis

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# Introduction

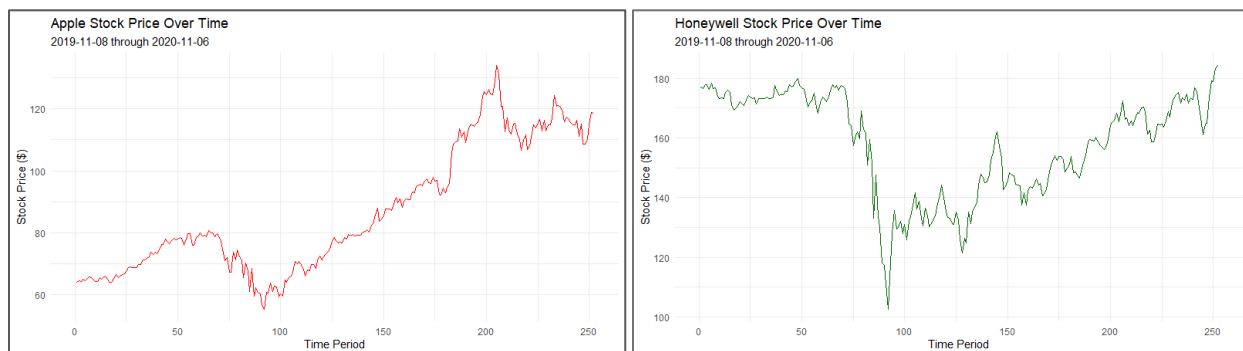
Predicting stock performance is crucial for investors and financial analysts. This study will center around historical stock prices for Apple Inc (AAPL) and Honeywell International Inc (HON). Using data provided for the study, short and long-term forecasting methods will be deployed to predict future performance of both stocks. Statistical tests will be performed on each forecast to ensure appropriate use of techniques and to determine the optimal variable values to maximize the effectiveness of the models.

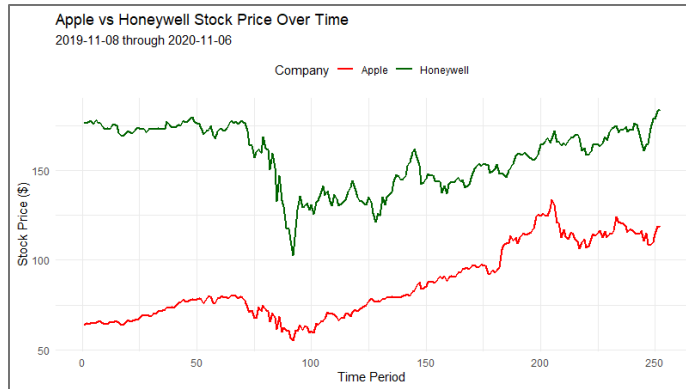
The dataset provided for this project contained the closing stock price and total volume for each company from November 8<sup>th</sup>, 2019, through November 11<sup>th</sup>, 2020. Each observation represents one trading day and is represented both by the date and a numerical period value which ranged from 1 to 252. The first steps of the project involved loading the data into R Studio, along with necessary packages for analysis. The data was also split into unique datasets for each company.

## Part 1: Short-Term Forecasting

### i. Plotting the data

To begin the analysis, plots were created to show movement of each company's stock price over the study period. The first plots were of the companies separately, and then a combined plot





In these plots, the effect of the Covid-19 pandemic is clear as both stock prices plunge in March of 2020. In the case of Honeywell, it takes nearly the entire study period to recover back to the late 2019 values. With Apple, by period 125 (May 8<sup>th</sup>, 2020) March losses are recovered, and a long positive trend is observed going forward.

## ii. Exponential Smoothing

To produce forecasted values for the next period in the study, period 253, an exponential smoothing function will be used. Successive values for alpha will be deployed (0.15, 0.35, 0.55, and 0.75) and each result will be evaluated based on the resulting MAPE (Mean Absolute Percentage Error).

First, the exponential smoothing function is defined, utilizing the Holt-Winters

```
exp_smoothing <- function(data, alpha) {
  model <- Holtwinters(data, alpha = alpha, beta = FALSE, gamma = FALSE)
  forecast <- forecast(model, h = 1)
```

This function will also calculate the MAPE of each resulting function.

```
mape <- mean(abs((data - forecast$fitted) / data), na.rm = TRUE) * 100
return(list(forecast = forecast, mape = mape))
```

With the function defined, the list of alpha values can be passed through the function and applied to each company's dataset.

```
appl_exsmo <- lapply(c(0.15, 0.35, 0.55, 0.75), function(alpha) exp_smoothing(appl, alpha))
hon_exsmo <- lapply(c(0.15, 0.35, 0.55, 0.75), function(alpha) exp_smoothing(hon, alpha))

sapply(appl_exsmo, function(x) x$mape)
sapply(hon_exsmo, function(x) x$mape)
```

With the calculations completed, the MAPE values for each can be evaluated.

```
> hon_mapes
[1] 3.061768 2.349148 2.032281 1.895824
> appl_mapes
[1] 3.874227 2.468633 2.082012 1.969072
~ |
```

For both companies, the best performance came from the fourth alpha value considered, which was 0.75. In both examples, an alpha of 0.75 resulted in the smallest MAPE value, indicating the smallest deviation from observed values.

### iii. Adjusted Exponential Smoothing

To increase the predictive capabilities of the model, the next step is to introduce adjusted exponential smoothing techniques. For this, alpha will be set at 0.55 and the trend (or beta) will be tested at values of 0.15, 0.25, 0.45, and 0.85. This technique is best deployed when trends are evident in the data and the initial plots do indicate a trend, particularly in the Apple prices.

As with the simple exponential smoothing, a function will be designed to implement the adjusted exponential smoothing calculation along with the MAPE values.

```
adj_exp_smoothing <- function(data, alpha, beta) {
  model <- Holtwinters(data, alpha = alpha, beta = beta, gamma = FALSE)
  forecast <- forecast(model, h = 1)
  mape <- mean(abs((data - forecast$fitted) / data), na.rm = TRUE) * 100
  return(list(forecast = forecast, mape = mape))
}
```

Then, the dataset for each company will be passed through the function for each of the desired beta values.

```
appl_adj_exsmo <- lapply(c(0.15, 0.25, 0.45, 0.85), function(beta) adj_exp_smoothing(appl, 0.55, beta))
hon_adj_exsmo <- lapply(c(0.15, 0.25, 0.45, 0.85), function(beta) adj_exp_smoothing(hon, 0.55, beta))
```

```
> sapply(appl_adj_exsmo, function(x) x$mape)
[1] 2.026042 2.048863 2.170707 2.303869
> sapply(hon_adj_exsmo, function(x) x$mape)
[1] 2.063393 2.084121 2.167818 2.276372
```

With these calculations complete, the final forecasts for period 253 can be compared.

	Exponential Smoothing ( $\alpha=0.75$ )	Adj. Exponential Smoothing ( $\beta=0.15$ )
Apple	118.39	118.08
Honeywell	183.72	185.14

## Part 2: Long-Term Forecasting

### i. 3-Period Weighted Average

For the next stage of the analysis, a 3-period weighted average will be used to forecast values for the first 100 periods. Then weights will be added for each period at 0.5 for the most recent, 0.3 for the next most recent, and 0.2 for two periods ago. Then, the observed value from period 100 be used as the base for a linear trend which will be used to predict values for period 101-257.

To start, a function is defined to perform the 3-period weighted average

```
weighted_moving_average <- function(data, weights) {
  n <- length(data)
  forecast <- rep(NA, n) # Initialize with NA
  weights <- weights / sum(weights) # Normalize weights to sum to 1

  if (length(weights) != 3) {
    stop("Weights vector must have exactly 3 elements.")
  }

  for (i in 3:n) {
    forecast[i] <- sum(data[(i-2):i] * weights)
  }
  return(forecast)
}
```

Next, the weights are defined, and the function is applied to each company's dataset for the first 100 periods.

```
# Define weights
weights <- c(0.2, 0.3, 0.5)

# Apply 3-period weighted moving average for AAPL and HON data (first 100 periods)
appl_wma <- weighted_moving_average(appl[1:100], weights)
hon_wma <- weighted_moving_average(hon[1:100], weights)
```

With this calculated, the linear model can be fit for the remaining periods.

```
apl_trend <- lm(Value ~ Period, data = apl_train)
```

```
hon_trend <- lm(Value ~ Period, data = hon_train)
```

And predictions can be made.

```
> apl_forecasts_253_257
      253      254      255      256      257
128.0162 128.4151 128.8139 129.2128 129.6117
> hon_forecasts_253_257
      253      254      255      256      257
176.0496 176.3539 176.6582 176.9625 177.2668
```

And these predictions can be compared with the actual closing values

Date	Period	APPL Forecast	APPL Actual	HON Forecast	HON Actual
11/9/2020	253	128.02	116.32	176.05	196.99
11/10/2020	254	128.42	115.97	176.35	201.98
11/11/2020	255	128.81	119.49	176.66	199.29
11/12/2020	256	129.21	119.21	176.96	197.24
11/13/2020	257	129.61	119.26	177.27	201.54

The forecast for periods 101-257 can be found in the appendix.

## ii. Mean Absolute Percentage Error (MAPE)

To evaluate the performance of this model, the MAPE is calculated for each company.

```
> # Display MAPE results for long-term forecasts
> apl_long_mape
[1] 4.778476
> hon_long_mape
[1] 3.052453
```

In both cases, these MAPE values for the 3-period weighted average are higher than those seen in the exponential smoothing or adjusted exponential smoothing forecast. This is a foreseeable outcome as the starting point of the linear regression was in the depths of the Covid market crash, a period that was a historic outlier to nearly all publicly traded companies.

## Part 3: Regression

### i. Simple Regression

For further comparison, a simple regression model is fit for each company and the predictions are made to period 257.

```
# Perform simple regression for AAPL
apl_regression <- lm(`AAPL (Apple Inc) / $` ~ Period, data = data)
apl_regression_forecast <- predict(apl_regression, newdata = data.frame(Period = 1:257))

# Perform simple regression for HON
hon_regression <- lm(`HON (Honeywell Inc) / $` ~ Period, data = data)
hon_regression_forecast <- predict(hon_regression, newdata = data.frame(Period = 1:257))
```

With the predictions made, the MAPE can be evaluate for both companies.

```
> # Display MAPE results for regression forecasts
> apl_regression_mape
[1] 10.56076
> hon_regression_mape
[1] 9.758568
>
```

Company	Exponential Smoothing	Adj Exponential Smoothing	3-Period Weighted Average	Simple Regression
Apple	1.9691	2.0260	4.7785	10.5608
Honeywell	1.8958	2.0634	3.5245	9.7586

Predictably, the linear regression model has the worst performance of all techniques. This technique has no ability to measure the complicated nuances seen in the performance data.



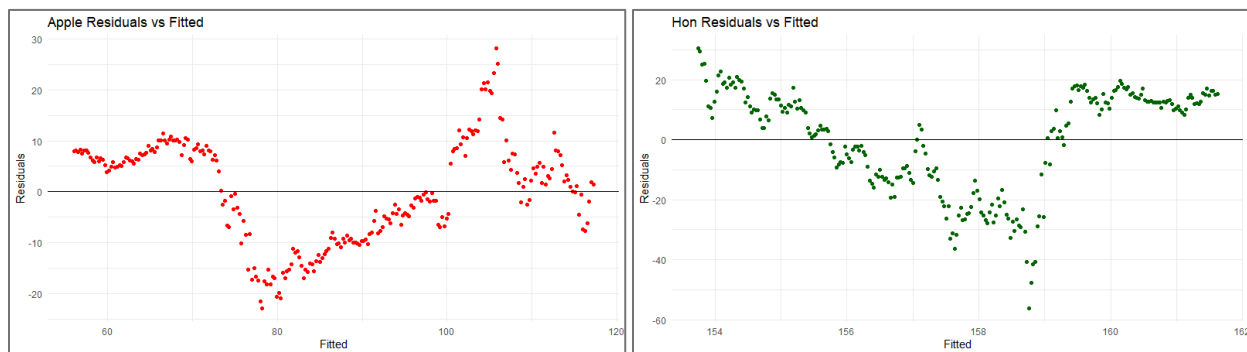
## ii. Appropriateness of Regression Model

To further evaluate the use of the regression model, tests will be conducted to determine if the

- The residuals are independent
- The residuals are homoscedastic
- The residuals are normally distributed (both through a Q-Q plot and a statistical test)

### Independent residuals

To test for the independence of the residuals, they are plotted against the fitted values. If the residuals are independent, there would be not discernible pattern in the plot.



In this case, there are clear patterns for both Apple and Honeywell in the plot.

### Homoscedasticity

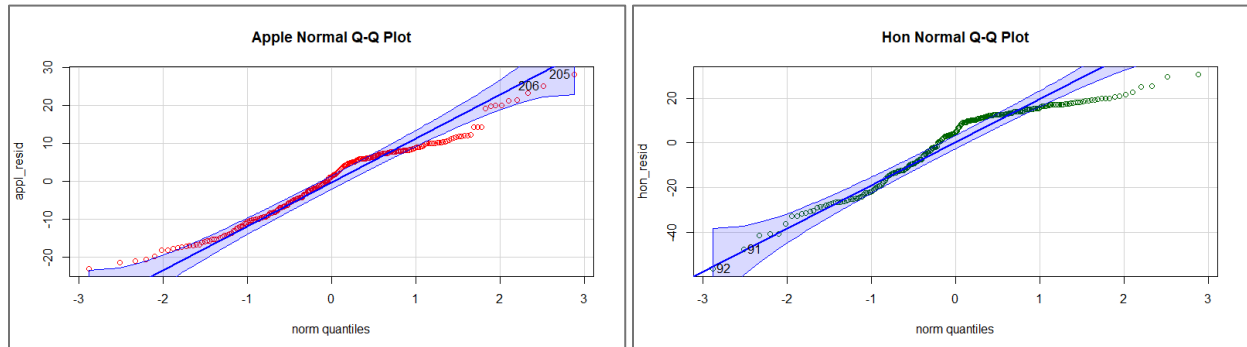
To test for homoscedasticity, the `ncvTest` is deployed. This uses the Breusch-Pagen test for non-constant variance in the residuals of the liner regression model.

```
> ncvTest(appl_regression)
Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 0.0001407281, Df = 1, p = 0.99054
> ncvTest(hon_regression)
Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 1.241827, Df = 1, p = 0.26512
```

While both results display p-values greater than 0.05, the Apple results are particularly strong. In both cases, the null hypothesis of constant variance in the residuals is accepted.

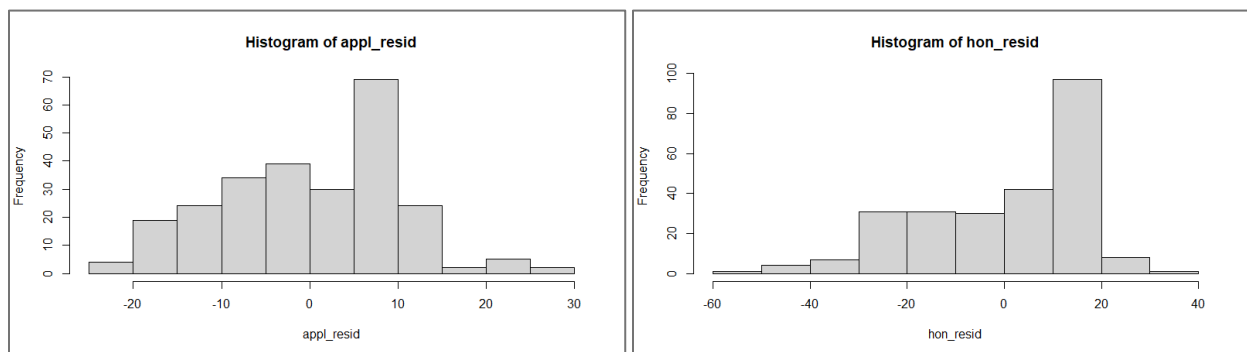
## Normal Distribution

To test for a normal distribution of the residuals, first a Q-Q Plot is created for each model.



In each of these plots, considerable deviation from the normal distribution can be seen, especially at the right side of plots.

Also looking at histograms for each, they do not match the normal distribution.



To confirm the deviation from a normal distribution, the Shapiro-Wilk test is conducted on each model. This test is similar to the Chi-Squared goodness of fit test but is better suited for continuous data, such as the results of the linear regression model.

```
> shapiro.test(appl_resid)

      Shapiro-Wilk normality test
```

```
data:  appl_resid
W = 0.97284, p-value = 9.674e-05
```

```
> shapiro.test(hon_resid)

      Shapiro-Wilk normality test
```

```
data:  hon_resid
W = 0.92097, p-value = 2.591e-10
```

Both results of both the w and p-value scores indicate a rejection of the null hypothesis that the residuals are normally distributed. However, the large w values, especially for the Honeywell model, indicate that the deviation is not severe.

## Conclusion

After examining the data from Apple and Honeywell in the given period, the prediction model with the best performance has been the exponential smoothing model. Given the nature of stock performance and the specific time of consideration, this does seem like a likely outcome. The exponential smoothing method is best suited for short-term predictions and best categorizes short-term momentum over long-term trends.

If considering a new stock portfolio, only containing these two stocks, the recommendation would be 70/30 split in favor of Apple. Many of the models in this study unduly punished the Apple stock due to the massive dip in performance around period 90, but this was due to the unprecedented global impact of Covid-19. Rarely in stock performance can such a large dip be easily explained by short-term (in hindsight) external factors. In the period after the Covid dip, the Apple growth has far exceeded Honeywell. Maintaining the 30% investment in Honeywell is a nod to the stable growth seen in the company after the 2020 dip, and future predictions of performance mirror that slow, steady growth.

## References

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<https://sscc.wisc.edu/sscc/pubs/RegDiag-R/homoscedasticity.html>
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[http://www.statistics4u.com/fundstat\\_eng/cc\\_normality\\_test.html](http://www.statistics4u.com/fundstat_eng/cc_normality_test.html)

# Appendix

## Apple Forecast

```
> setNames(appl_forecasts[101:257], 101:257)
```

101	102	103	104	105	106	107	108	109	110	111
67.38491	67.78380	68.18269	68.58158	68.98047	69.37936	69.77824	70.17713	70.57602	70.97491	71.37380

112	113	114	115	116	117	118	119	120	121	122
71.77269	72.17158	72.57047	72.96936	73.36825	73.76714	74.16603	74.56492	74.96381	75.36270	75.76159

123	124	125	126	127	128	129	130	131	132	133
76.16048	76.55937	76.95826	77.35715	77.75604	78.15493	78.55382	78.95271	79.35160	79.75049	80.14938

134	135	136	137	138	139	140	141	142	143	144
80.54827	80.94716	81.34605	81.74494	82.14383	82.54272	82.94161	83.34050	83.73939	84.13828	84.53717

145	146	147	148	149	150	151	152	153	154	155
84.93606	85.33495	85.73384	86.13273	86.53162	86.93051	87.32940	87.72829	88.12718	88.52607	88.92496

156	157	158	159	160	161	162	163	164	165	166
89.32385	89.72274	90.12163	90.52052	90.91941	91.31830	91.71719	92.11608	92.51497	92.91386	93.31275

167	168	169	170	171	172	173	174	175	176	177
93.71164	94.11053	94.50942	94.90831	95.30720	95.70609	96.10498	96.50387	96.90276	97.30165	97.70054

178	179	180	181	182	183	184	185	186	187	188
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

98.09943 98.49832 98.89721 99.29610 99.69499 100.09387 100.49276 100.89165 101.29054  
101.68943 102.08832

189 190 191 192 193 194 195 196 197 198 199  
102.48721 102.88610 103.28499 103.68388 104.08277 104.48166 104.88055 105.27944  
105.67833 106.07722 106.47611

200 201 202 203 204 205 206 207 208 209 210  
106.87500 107.27389 107.67278 108.07167 108.47056 108.86945 109.26834 109.66723  
110.06612 110.46501 110.86390

211 212 213 214 215 216 217 218 219 220 221  
111.26279 111.66168 112.06057 112.45946 112.85835 113.25724 113.65613 114.05502  
114.45391 114.85280 115.25169

222 223 224 225 226 227 228 229 230 231 232  
115.65058 116.04947 116.44836 116.84725 117.24614 117.64503 118.04392 118.44281  
118.84170 119.24059 119.63948

233 234 235 236 237 238 239 240 241 242 243  
120.03837 120.43726 120.83615 121.23504 121.63393 122.03282 122.43171 122.83060  
123.22949 123.62838 124.02727

244 245 246 247 248 249 250 251 252 253 254  
124.42616 124.82505 125.22394 125.62283 126.02172 126.42061 126.81950 127.21839  
127.61728 128.01617 128.41506

255 256 257  
128.81395 129.21284 129.61173

## Honeywell Forecast

101 102 103 104 105 106 107 108 109 110 111 112 113  
129.7957 130.1000 130.4043 130.7086 131.0129 131.3172 131.6215 131.9258 132.2301  
132.5344 132.8387 133.1430 133.4473

114	115	116	117	118	119	120	121	122	123	124	125	126
133.7516	134.0559	134.3602	134.6645	134.9688	135.2731	135.5774	135.8817	136.1860				
136.4903	136.7946	137.0989	137.4032									
127	128	129	130	131	132	133	134	135	136	137	138	139
137.7075	138.0118	138.3161	138.6204	138.9247	139.2290	139.5333	139.8376	140.1419				
140.4462	140.7505	141.0548	141.3591									
140	141	142	143	144	145	146	147	148	149	150	151	152
141.6634	141.9677	142.2721	142.5764	142.8807	143.1850	143.4893	143.7936	144.0979				
144.4022	144.7065	145.0108	145.3151									
153	154	155	156	157	158	159	160	161	162	163	164	165
145.6194	145.9237	146.2280	146.5323	146.8366	147.1409	147.4452	147.7495	148.0538				
148.3581	148.6624	148.9667	149.2710									
166	167	168	169	170	171	172	173	174	175	176	177	178
149.5753	149.8796	150.1839	150.4882	150.7925	151.0968	151.4011	151.7054	152.0097				
152.3140	152.6183	152.9226	153.2269									
179	180	181	182	183	184	185	186	187	188	189	190	191
153.5312	153.8355	154.1398	154.4441	154.7485	155.0528	155.3571	155.6614	155.9657				
156.2700	156.5743	156.8786	157.1829									
192	193	194	195	196	197	198	199	200	201	202	203	204
157.4872	157.7915	158.0958	158.4001	158.7044	159.0087	159.3130	159.6173	159.9216				
160.2259	160.5302	160.8345	161.1388									
205	206	207	208	209	210	211	212	213	214	215	216	217
161.4431	161.7474	162.0517	162.3560	162.6603	162.9646	163.2689	163.5732	163.8775				
164.1818	164.4861	164.7904	165.0947									
218	219	220	221	222	223	224	225	226	227	228	229	230

165.3990 165.7033 166.0076 166.3119 166.6162 166.9205 167.2248 167.5292 167.8335  
168.1378 168.4421 168.7464 169.0507

231 232 233 234 235 236 237 238 239 240 241 242 243

169.3550 169.6593 169.9636 170.2679 170.5722 170.8765 171.1808 171.4851 171.7894  
172.0937 172.3980 172.7023 173.0066

244 245 246 247 248 249 250 251 252 253 254 255 256

173.3109 173.6152 173.9195 174.2238 174.5281 174.8324 175.1367 175.4410 175.7453  
176.0496 176.3539 176.6582 176.9625

257

177.2668