$$\mu_Z = \int_{\log S} \left(\int_R \exp(\log S(X_b, X_R)) p(R) \, dR \right) \mathcal{N}(\log S | \mu_{\log S}, \Sigma_{\log S}) \, d\log S$$

$$\approx \int_R \mu_S (1 + \mu_{\Delta_c}) p(R) \, dR, \text{ where } \Delta_c = \mu_{\log S} - \log \mu_S$$