$$X_R = RX_a = \tau(X_{R-r}, r) = \tau(\tau(X_{R-2r}, r), r) = \ldots = \tau^{\left(\frac{R}{r}\right)}(X_a, r)$$