## Udacity Intro To Statistics Problem Set 6

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1 Ratio of Correlation to Regression

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## 1 Ratio of Correlation to Regression

Given:

$$b = \frac{\sum_{i=1}^{n} (x_i - \bar{x}) (y_i - \bar{y})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$
(1)

and:

$$r = \frac{\sum_{i=1}^{n} (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (y_i - \bar{y})^2}}$$
(2)

find a simplified form for  $\frac{b}{r}$  let f(x) =

$$\sum_{i=1}^{n} (x_i - \bar{x}) (y_i - \bar{y}) \tag{3}$$

then  $\frac{b}{r} =$ 

$$\frac{\frac{f(x)}{\sum_{i=1}^{n}(x_{i}-\bar{x})^{2}}}{\frac{f(x)}{\sqrt{\sum_{i=1}^{n}(x_{i}-\bar{x})^{2}\sum_{i=1}^{n}(y_{i}-\bar{y})^{2}}}}$$
(4)

$$\implies \frac{b}{r} = \frac{f(x)}{\sum_{i=1}^{n} (x_i - \bar{x})^2} \frac{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (y_i - \bar{y})^2}}{f(x)}$$
(5)

$$\implies \frac{b}{r} = \frac{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (y_i - \bar{y})^2}}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$
(6)

$$\implies \frac{b}{r} = \frac{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$
(7)

$$\implies \frac{b}{r} = \frac{\left(\sum_{i=1}^{n} (x_i - \bar{x})^2\right)^{\frac{1}{2}} \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$
(8)

$$\implies \frac{b}{r} = \left(\sum_{i=1}^{n} (x_i - \bar{x})^2\right)^{\frac{1}{2}} \left(\sum_{i=1}^{n} (x_i - \bar{x})^2\right)^{-1} \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$
(9)

$$\implies \frac{b}{r} = \left(\sum_{i=1}^{n} (x_i - \bar{x})^2\right)^{-\frac{1}{2}} \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$
 (10)

$$\implies \frac{b}{r} = \frac{\sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}}{\sqrt{\left(\sum_{i=1}^{n} (x_i - \bar{x})^2\right)}}$$
(11)

$$\implies \frac{b}{r} = \sqrt{\frac{\sum_{i=1}^{n} (y_i - \bar{y})^2}{\sum_{i=1}^{n} (x_i - \bar{x})^2}}$$
 (12)