

The University of Texas at Austin  
Mechanical Engineering Department  
**MODELING OF PHYSICAL SYSTEMS**

J.J. Beaman  
Assigned 2/24/2022

ME 383Q.4  
**Assignment 3**

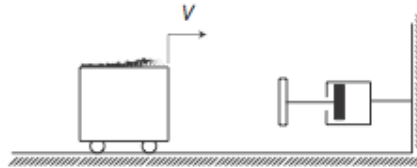
Spring 2022  
Due 3/3/2022

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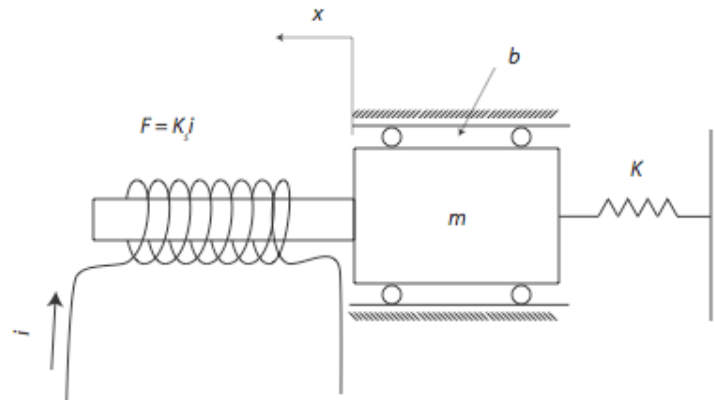
Read Chapter 4 and Chapter sections 5.1 and 5.2

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- 1) Shown below is a cart containing a load of scrap. You have been hired to design a damper to stop this cart in 10 seconds if the initial velocity of the cart is .5 m/s and the cart has a mass of 1,000 kg.
  - (a) Calculate the necessary damping coefficient  $b$ .
  - (b) How long does the damper stroke have to be?
  - (c) How much heat is generated?



- 2) Shown below is a portion of a positioning mechanism in a machine. The parameters in the model have the values  $K_s = 1 \text{ N/A}$ ,  $k = 100 \text{ N/m}$ ,  $m = 1 \text{ kg}$ ,  $b = 10 \text{ N-sec/m}$ .



- (a) Develop a bond graph model for this system.
- (b) Obtain state equations for your model.
- (c) Obtain a 2<sup>nd</sup> order differential equation  $x$ .
- (d) Is the system over damped or under damped?
- (e) For a step input in current,  $i = 1 \text{ A}$ , find the maximum value of the position  $x$ .
- (f) At what time after the step does the maximum occur?
- (g) What is the steady state position of  $x$ ?
- (h) It is desired that the maximum value of  $x$  never exceed the steady state value. Find the smallest value of  $b$  to achieve this result.

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- The figure consists of two parts. The top part is a schematic diagram of a piezoelectric sensor for measuring the pressure in a pipe. It shows a cross-section of a pipe with a piezoelectric sensor (m) and electrodes connected to a circuit with a spring (K) and a load resistor (R<sub>load</sub>). A magnetic field B is applied perpendicular to the electrodes. The bottom part is a free-body diagram of the pipe section with forces F<sub>R</sub>, F<sub>p</sub>, F<sub>T</sub>, F<sub>L</sub>, F<sub>Q</sub>, F<sub>elect</sub>, F<sub>R</sub>, and F<sub>I</sub>, and moments M<sub>R</sub>, M<sub>Q</sub>, M<sub>elect</sub>, M<sub>R</sub>, and M<sub>I</sub>.

$$\begin{aligned} P_o(t) \\ v &= R_{load} i \\ P_R &= R_{pipe} Q_{pipe} \\ Q_{pipe} &= \Gamma/I \\ Q_L &= P_L/R_L \\ V &= p/m \\ F_K &= Kx \\ P_{elect} &= Bli/A \end{aligned}$$

Obtain a set of state equations for this bond graph model.