

**FractionalKnapsack Growth Rate Investigation**  
**CS4310 - Design & Analysis of Algorithms**  
**Spring 2017**  
**John Harvey**  
**04/09/2017**

**Hypothesis:**

The FractionalKnapsack algorithm has a time complexity of  $O(n \log n)$

**Test Design:**

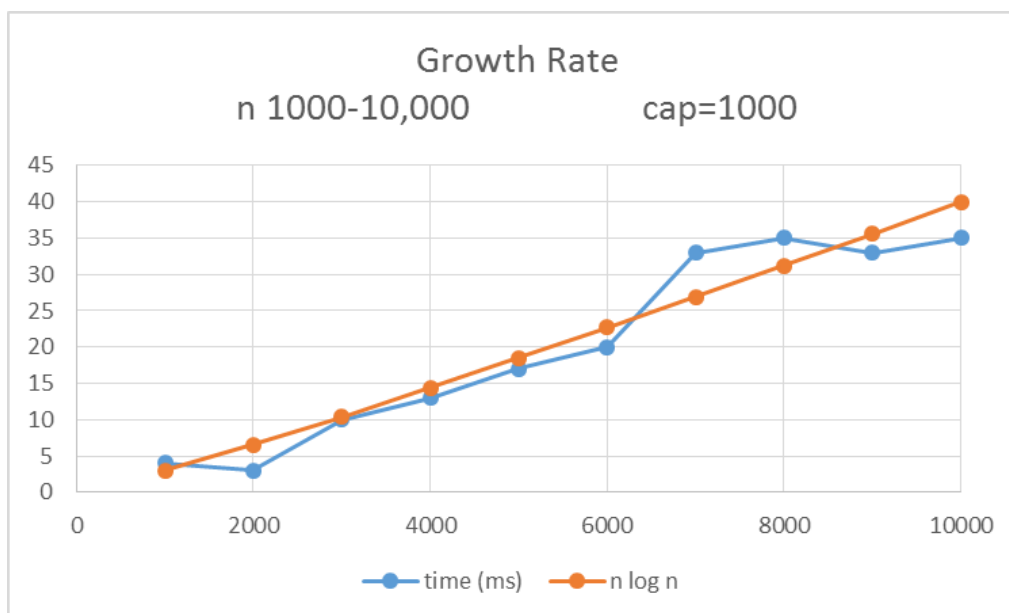
In order to test the hypothesis involved, I have taken the following steps:

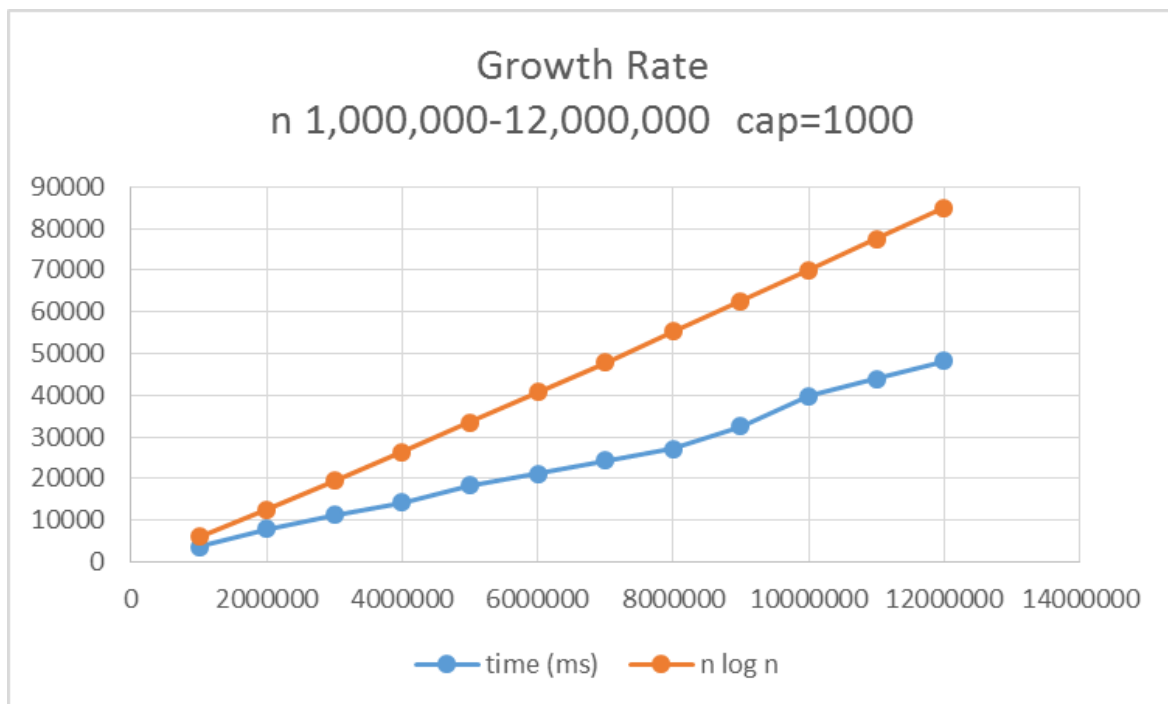
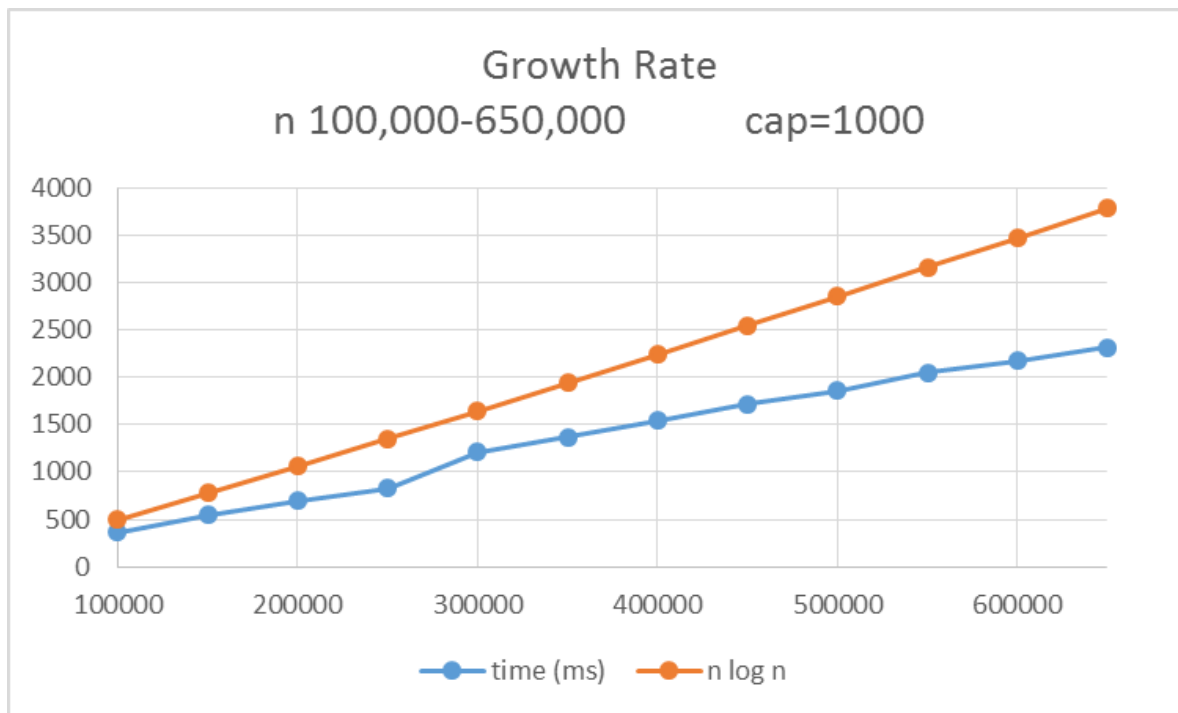
- 1) Implement the FractionalKnapsack algorithm in Ruby
- 2) Run the code for multiple amounts of  $n$  items
  - a) Test with various maximum capacities
  - b) Analyze all data on individual graphs
  - c) Analyze all data on a single graph
- 3) Inspect the graphs and compare the growth to an  $n \log n$  growth rate
- 4) Examine code and make changes if results do not seem right

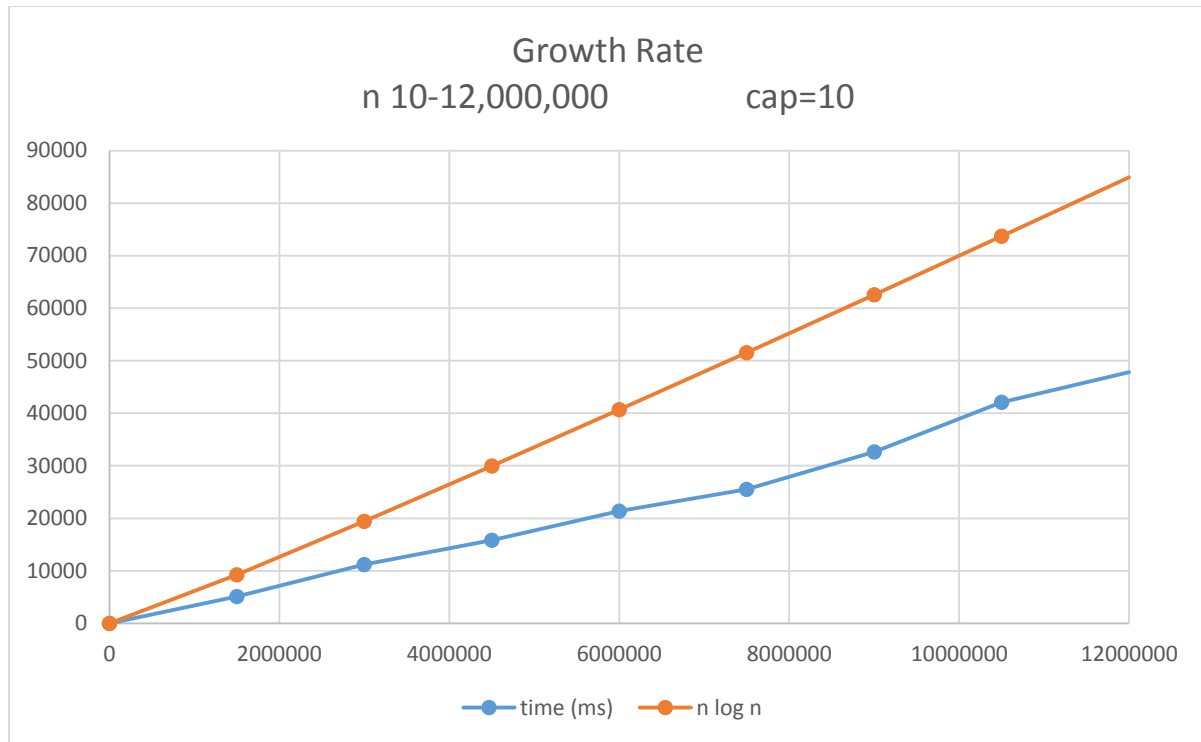
**Evaluation of Data:**

All files will be included in the submission .zip.

**Visual Inspection:**







The graphs above show each simulation given different size inputs of  $n$ . Each run is plotted against the  $n \log n$  line. By looking at each one, we can easily reject the exponential possibility for all. We can see that each simulation comes fairly close to the  $n \log n$  trend line. Actually, our simulation line comes up below the  $n \log n$  trend line in each one except for the first. The time for each one is in milliseconds.

## Conclusion:

The growth of the fractional knapsack algorithm is very close to  $n \log n$ . As I pushed the boundaries, my computer would fail to allocate memory.