## Online Appendix

Moderate Overlap

Table O1. Estimated Policy Advantage, Tree-based Policy Class (SD)

Panel A: Normal Outcomes									
Moderate Overlap		SETTING	1	SETTING 2			SETTING 3		
•	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
DML	-0.337	-0.304	-0.274	-0.254	-0.203	-0.141	-0.251	-0.197	-0.138
	(0.045)	(0.033)	(0.015)	(0.048)	(0.034)	(0.016)	(0.048)	(0.034)	(0.016)
NDR	-0.334	-0.301	-0.274	-0.250	-0.198	-0.140	-0.245	-0.193	-0.137
	(0.044)	(0.032)	(0.015)	(0.046)	(0.034)	(0.016)	(0.047)	(0.034)	(0.016)
CF	-0.335	-0.302	-0.274	-0.249	-0.199	-0.139	-0.247	-0.193	-0.137
	(0.044)	(0.032)	(0.015)	(0.047)	(0.033)	(0.016)	(0.047)	(0.033)	(0.016)
CFTT	-0.334	-0.302	-0.274	-0.249	-0.199	-0.139	-0.246	-0.193	-0.137
	(0.044)	(0.032)	(0.015)	(0.046)	(0.033)	(0.016)	(0.046)	(0.033)	(0.016)
BART	-0.307	-0.292	-0.274	-0.230	-0.195	-0.140	-0.231	-0.189	-0.138
	(0.040)	(0.031)	(0.016)	(0.043)	(0.033)	(0.017)	(0.043)	(0.033)	(0.017)
Weak Overlap		SETTING		SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
DML	-0.366	-0.326	-0.295	-0.297	-0.238	-0.173	-0.291	-0.233	-0.173
	(0.057)	(0.044)	(0.027)	(0.059)	(0.046)	(0.028)	(0.059)	(0.046)	(0.028)
NDR	-0.350	-0.313	-0.283	-0.277	-0.219	-0.157	-0.270	-0.213	-0.157
	(0.052)	(0.039)	(0.021)	(0.054)	(0.040)	(0.022)	(0.054)	(0.040)	(0.022)
CF	-0.348	-0.313	-0.279	-0.279	-0.222	-0.154	-0.275	-0.220	-0.160
	(0.053)	(0.040)	(0.022)	(0.054)	(0.041)	(0.022)	(0.054)	(0.041)	(0.022)
CFTT	-0.347	-0.312	-0.279	-0.280	-0.223	-0.154	-0.277	-0.220	-0.160
	(0.052)	(0.040)	(0.022)	(0.054)	(0.041)	(0.022)	(0.054)	(0.041)	(0.022)
BART	-0.295	-0.292	-0.303	-0.233	-0.208	-0.179	-0.236	-0.208	-0.181
	(0.046)	(0.040)	(0.035)	(0.048)	(0.042)	(0.034)	(0.047)	(0.041)	(0.034)

Panel B: Rare Outcomes

SETTING 1

SETTING 2

SETTING 3

	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.046	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
DML	-0.069	-0.061	-0.054	-0.037	-0.032	-0.020	-0.037	-0.032	-0.020
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)
NDR	-0.071	-0.062	-0.054	-0.038	-0.032	-0.020	-0.038	-0.032	-0.020
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)
CF	-0.069	-0.061	-0.053	-0.036	-0.031	-0.020	-0.036	-0.031	-0.020
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)
CFTT	-0.071	-0.062	-0.054	-0.036	-0.032	-0.020	-0.036	-0.031	-0.020
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)
BART	-0.061	-0.056	-0.052	-0.034	-0.031	-0.020	-0.034	-0.030	-0.020
	(0.013)	(0.010)	(0.005)	(0.010)	(0.008)	(0.004)	(0.010)	(0.008)	(0.004)
Weak Overlap		SETTING			SETTING			SETTING	3
	N = 500	N = 1000	N = 5000		N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.051	-0.047	-0.047	-0.117	-0.117	-0.047	-0.010	-0.010	-0.010
	-0.051 $(0.005)$	-0.047 (0.003)	-0.047 $(0.001)$	-0.117 $(0.000)$	-0.117 $(0.000)$	-0.047 $(0.000)$	-0.010 $(0.000)$	-0.010 $(0.000)$	-0.010 (0.000)
OR DML	-0.051 $(0.005)$ $-0.087$	-0.047 $(0.003)$ $-0.065$	-0.047 $(0.001)$ $-0.056$	-0.117 $(0.000)$ $-0.038$	-0.117 $(0.000)$ $-0.033$	-0.047 $(0.000)$ $-0.024$	-0.010 $(0.000)$ $-0.037$	-0.010 $(0.000)$ $-0.033$	-0.010 $(0.000)$ $-0.023$
DML	-0.051 $(0.005)$ $-0.087$ $(0.016)$	-0.047 $(0.003)$ $-0.065$ $(0.011)$	-0.047 $(0.001)$ $-0.056$ $(0.006)$	$ \begin{array}{c} -0.117 \\ (0.000) \\ -0.038 \\ (0.012) \end{array} $	-0.117 $(0.000)$ $-0.033$ $(0.009)$	$ \begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \end{array} $	-0.010 $(0.000)$ $-0.037$ $(0.012)$	-0.010 $(0.000)$ $-0.033$ $(0.009)$	-0.010 $(0.000)$ $-0.023$ $(0.005)$
	-0.051 $(0.005)$ $-0.087$ $(0.016)$ $-0.089$	-0.047 $(0.003)$ $-0.065$ $(0.011)$ $-0.067$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \end{array}$	$ \begin{array}{c} -0.117 \\ (0.000) \\ -0.038 \\ (0.012) \\ -0.038 \end{array} $	-0.117 $(0.000)$ $-0.033$ $(0.009)$ $-0.033$	$-0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.037 \\ (0.012) \\ -0.037 \end{array}$	$ \begin{array}{c} -0.010 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \end{array} $	$ \begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \end{array} $
DML NDR	$\begin{array}{c} -0.051 \\ (0.005) \\ -0.087 \\ (0.016) \\ -0.089 \\ (0.015) \end{array}$	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \end{array}$	$\begin{array}{c} -0.117 \\ (0.000) \\ -0.038 \\ (0.012) \\ -0.038 \\ (0.012) \end{array}$	$ \begin{array}{c} -0.117 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \end{array} $	$\begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023 \\ (0.005) \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.037 \\ (0.012) \\ -0.037 \\ (0.012) \end{array}$	$ \begin{array}{c} -0.010 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \end{array} $	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \\ (0.005) \end{array}$
DML	$\begin{array}{c} -0.051 \\ (0.005) \\ -0.087 \\ (0.016) \\ -0.089 \\ (0.015) \\ -0.081 \end{array}$	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \\ -0.060 \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \\ -0.051 \end{array}$	$\begin{array}{c} -0.117 \\ (0.000) \\ -0.038 \\ (0.012) \\ -0.038 \\ (0.012) \\ -0.036 \end{array}$	-0.117 (0.000) -0.033 (0.009) -0.033 (0.009) -0.032	$\begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.037 \\ (0.012) \\ -0.037 \\ (0.012) \\ -0.035 \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \\ -0.031 \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \end{array}$
DML NDR CF	$\begin{array}{c} -0.051 \\ (0.005) \\ -0.087 \\ (0.016) \\ -0.089 \\ (0.015) \\ -0.081 \\ (0.015) \end{array}$	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \\ -0.060 \\ (0.011) \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \\ -0.051 \\ (0.006) \end{array}$	-0.117 (0.000) -0.038 (0.012) -0.038 (0.012) -0.036 (0.011)	-0.117 (0.000) -0.033 (0.009) -0.033 (0.009) -0.032 (0.009)	$\begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.037 \\ (0.012) \\ -0.037 \\ (0.012) \\ -0.035 \\ (0.011) \end{array}$	-0.010 (0.000) -0.033 (0.009) -0.033 (0.009) -0.031 (0.009)	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \end{array}$
DML NDR	-0.051 (0.005) -0.087 (0.016) -0.089 (0.015) -0.081 (0.015) -0.087	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \\ -0.060 \\ (0.011) \\ -0.062 \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \\ -0.051 \\ (0.006) \\ -0.051 \end{array}$	-0.117 (0.000) -0.038 (0.012) -0.038 (0.012) -0.036 (0.011) -0.037	$\begin{array}{c} -0.117 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \\ -0.032 \\ (0.009) \\ -0.032 \end{array}$	$\begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \\ -0.023 \end{array}$	-0.010 (0.000) -0.037 (0.012) -0.037 (0.012) -0.035 (0.011) -0.036	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \\ -0.031 \\ (0.009) \\ -0.032 \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \\ -0.023 \end{array}$
DML NDR CF CFTT	-0.051 (0.005) -0.087 (0.016) -0.089 (0.015) -0.081 (0.015) -0.087 (0.015)	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \\ -0.060 \\ (0.011) \\ -0.062 \\ (0.011) \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \\ -0.051 \\ (0.006) \\ -0.051 \\ (0.006) \end{array}$	$\begin{array}{c} -0.117 \\ (0.000) \\ -0.038 \\ (0.012) \\ -0.038 \\ (0.012) \\ -0.036 \\ (0.011) \\ -0.037 \\ (0.011) \end{array}$	-0.117 (0.000) -0.033 (0.009) -0.033 (0.009) -0.032 (0.009) -0.032 (0.009)	-0.047 (0.000) -0.024 (0.005) -0.023 (0.005) -0.022 (0.005) -0.023 (0.005)	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.037 \\ (0.012) \\ -0.037 \\ (0.012) \\ -0.035 \\ (0.011) \\ -0.036 \\ (0.011) \end{array}$	-0.010 (0.000) -0.033 (0.009) -0.033 (0.009) -0.031 (0.009) -0.032 (0.009)	-0.010 (0.000) -0.023 (0.005) -0.023 (0.005) -0.022 (0.005) -0.023 (0.005)
DML NDR CF	-0.051 (0.005) -0.087 (0.016) -0.089 (0.015) -0.081 (0.015) -0.087	$\begin{array}{c} -0.047 \\ (0.003) \\ -0.065 \\ (0.011) \\ -0.067 \\ (0.011) \\ -0.060 \\ (0.011) \\ -0.062 \end{array}$	$\begin{array}{c} -0.047 \\ (0.001) \\ -0.056 \\ (0.006) \\ -0.056 \\ (0.005) \\ -0.051 \\ (0.006) \\ -0.051 \end{array}$	-0.117 (0.000) -0.038 (0.012) -0.038 (0.012) -0.036 (0.011) -0.037	$\begin{array}{c} -0.117 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \\ -0.032 \\ (0.009) \\ -0.032 \end{array}$	$\begin{array}{c} -0.047 \\ (0.000) \\ -0.024 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \\ -0.023 \end{array}$	-0.010 (0.000) -0.037 (0.012) -0.037 (0.012) -0.035 (0.011) -0.036	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.033 \\ (0.009) \\ -0.033 \\ (0.009) \\ -0.031 \\ (0.009) \\ -0.032 \end{array}$	$\begin{array}{c} -0.010 \\ (0.000) \\ -0.023 \\ (0.005) \\ -0.023 \\ (0.005) \\ -0.022 \\ (0.005) \\ -0.023 \end{array}$
OR	-0.051	-0.047	-0.047	-0.117	-0.117	-0.047	-0.010	-0.010	-0.010

<sup>&</sup>lt;sup>a</sup> This table reports Normalized RMSE of estimated depth-two optimal policy for settings with moderate overlap. RMSE is normalized by the mean advantage of the oracle policy. The top panel depicts normal outcome prevalence, and the bottom panel shows rare outcome prevalence.

TABLE O2. True Policy Advantage, Tree-based Policy Class (SD)

			Panel A:	Normal	Outcomes				
Moderate Overlap		SETTING	1	SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
DML	-0.211	-0.232	-0.247	-0.057	-0.069	-0.097	-0.053	-0.064	-0.094
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.001)	(0.006)	(0.004)	(0.001)
NDR	-0.212	-0.234	-0.247	-0.060	-0.072	-0.097	-0.052	-0.065	-0.094
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.001)	(0.006)	(0.004)	(0.001)
CF	-0.212	-0.232	-0.247	-0.059	-0.071	-0.098	-0.054	-0.066	-0.094
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.001)	(0.006)	(0.004)	(0.001)
CFTT	-0.213	-0.231	-0.247	-0.058	-0.071	-0.098	-0.053	-0.067	-0.095
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.001)	(0.006)	(0.004)	(0.001)
BART	-0.213	-0.232	-0.247	-0.058	-0.069	-0.095	-0.055	-0.063	-0.092
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.001)
Weak Overlap		SETTING	1		SETTING	2	•	SETTING	3
•	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
DML	-0.193	-0.217	-0.238	-0.049	-0.059	-0.082	-0.048	-0.059	-0.084
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.002)
NDR	-0.193	-0.227	-0.243	-0.054	-0.065	-0.086	-0.049	-0.062	-0.087
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.002)
CF	-0.193	-0.212	-0.238	-0.052	-0.061	-0.083	-0.053	-0.065	-0.087
	(0.011)	(0.008)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.002)
CFTT	-0.194	-0.214	-0.239	-0.051	-0.063	-0.083	-0.052	-0.065	-0.086
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.002)
BART	-0.200	-0.214	-0.234	-0.052	-0.062	-0.080	-0.056	-0.060	-0.079
	(0.011)	(0.007)	(0.003)	(0.006)	(0.004)	(0.002)	(0.006)	(0.004)	(0.002)

Panel B: Rare Outcomes

Moderate Overlap		SETTING 1			SETTING	2	SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000			
OR	-0.046	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
$_{\mathrm{DML}}$	-0.031	-0.035	-0.043	-0.002	-0.004	-0.006	-0.003	-0.004	-0.006
	(0.005)	(0.003)	(0.002)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)	(0.000)
NDR	-0.032	-0.036	-0.043	-0.002	-0.004	-0.006	-0.002	-0.004	-0.006
	(0.005)	(0.003)	(0.002)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)	(0.000)
CF	-0.031	-0.035	-0.043	-0.002	-0.004	-0.006	-0.003	-0.004	-0.006
	(0.005)	(0.003)	(0.002)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)	(0.000)
CFTT	-0.032	-0.036	-0.043	-0.003	-0.004	-0.006	-0.003	-0.004	-0.006
	(0.005)	(0.003)	(0.002)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)	(0.000)
BART	-0.031	-0.035	-0.043	-0.002	-0.004	-0.006	-0.002	-0.004	-0.006
	(0.005)	(0.003)	(0.002)	(0.001)	(0.000)	(0.000)	(0.001)	(0.000)	(0.000)
Weak Overlap		SETTING			SETTING			SETTING	3
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR									
Oit	-0.051	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
DML	$(0.005) \\ -0.040$	$(0.003) \\ -0.036$	$(0.001) \\ -0.042$	(0.000) $-0.002$	$(0.000) \\ -0.004$	$(0.000) \\ -0.007$	(0.000) $-0.003$	$(0.000) \\ -0.005$	$(0.000) \\ -0.006$
DML	(0.005)	(0.003) $-0.036$ $(0.003)$	(0.001) $-0.042$ $(0.002)$	$ \begin{array}{c c} (0.000) \\ -0.002 \\ (0.001) \end{array} $	(0.000) $-0.004$ $(0.000)$	(0.000)	(0.000) $-0.003$ $(0.001)$	(0.000) $-0.005$ $(0.000)$	(0.000)
	(0.005) $-0.040$ $(0.005)$ $-0.042$	(0.003) $-0.036$ $(0.003)$ $-0.036$	(0.001) $-0.042$ $(0.002)$ $-0.042$	$ \begin{array}{c} (0.000) \\ -0.002 \\ (0.001) \\ -0.002 \end{array} $	(0.000) $-0.004$ $(0.000)$ $-0.004$	(0.000) $-0.007$ $(0.000)$ $-0.006$	$ \begin{array}{c} (0.000) \\ -0.003 \\ (0.001) \\ -0.002 \end{array} $	(0.000) $-0.005$ $(0.000)$ $-0.004$	(0.000) $-0.006$ $(0.000)$ $-0.006$
DML NDR	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.002 \\ (0.001) \\ -0.002 \\ (0.001) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \end{array} $	$\begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \end{array}$	$ \begin{array}{c} (0.000) \\ -0.003 \\ (0.001) \\ -0.002 \\ (0.001) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \end{array} $	$\begin{array}{c} (0.000) \\ -0.006 \\ (0.000) \\ -0.006 \\ (0.000) \end{array}$
DML	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \\ -0.041 \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.002 \\ (0.001) \\ -0.002 \\ (0.001) \\ -0.003 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.007 \end{array} $	(0.000) -0.003 (0.001) -0.002 (0.001) -0.003	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.006 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.006 \end{array} $
DML NDR CF	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \\ -0.041 \\ (0.005) \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.002 \\ (0.001) \\ -0.002 \\ (0.001) \\ -0.003 \\ (0.001) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.007 \\ (0.000) \end{array} $	(0.000) -0.003 (0.001) -0.002 (0.001) -0.003 (0.000)	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \end{array} $	(0.000) -0.006 (0.000) -0.006 (0.000) -0.006 (0.000)
DML NDR	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \\ -0.041 \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.002 \\ (0.001) \\ -0.002 \\ (0.001) \\ -0.003 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.007 \end{array} $	(0.000) -0.003 (0.001) -0.002 (0.001) -0.003	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.006 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.006 \end{array} $
DML NDR CF CFTT	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \\ -0.041 \\ (0.005) \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \end{array} $	(0.000) -0.002 (0.001) -0.002 (0.001) -0.003 (0.001) -0.002 (0.001)	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \\ -0.005 \\ (0.000) \end{array} $	$ \begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.007 \\ (0.000) \end{array} $	(0.000) -0.003 (0.001) -0.002 (0.001) -0.003 (0.000)	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \end{array} $	(0.000) -0.006 (0.000) -0.006 (0.000) -0.006 (0.000)
DML NDR CF	$ \begin{array}{c} (0.005) \\ -0.040 \\ (0.005) \\ -0.042 \\ (0.005) \\ -0.041 \\ (0.005) \\ -0.041 \end{array} $	$ \begin{array}{c} (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \\ (0.003) \\ -0.036 \end{array} $	$ \begin{array}{c} (0.001) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \\ (0.002) \\ -0.042 \end{array} $	(0.000) -0.002 (0.001) -0.002 (0.001) -0.003 (0.001) -0.002	$ \begin{array}{c} (0.000) \\ -0.004 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \\ -0.005 \end{array} $	$ \begin{array}{c} (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \\ (0.000) \\ -0.007 \\ (0.000) \\ -0.006 \end{array} $	(0.000) -0.003 (0.001) -0.002 (0.001) -0.003 (0.000) -0.003	$ \begin{array}{c} (0.000) \\ -0.005 \\ (0.000) \\ -0.004 \\ (0.000) \\ -0.005 \\ (0.000) \\ -0.005 \end{array} $	(0.000) -0.006 (0.000) -0.006 (0.000) -0.006 (0.000) -0.006

<sup>&</sup>lt;sup>a</sup> This table reports the true advantages of estimated depth-two optimal policy for both overlap settings. Advantage is calculated using the learned policies with the true CATE. The top panel depicts normal outcome prevalence, and the bottom panel shows rare outcome prevalence.

TABLE O3. Estimated Policy Advantage, Plug-in Policy Class (SD)

Panel A: Normal Outcomes									
Moderate Overlap		SETTING	1	SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
NDR	-0.225	-0.242	-0.264	-0.108	-0.110	-0.112	-0.095	-0.101	-0.111
	(0.046)	(0.032)	(0.015)	(0.047)	(0.034)	(0.016)	(0.048)	(0.034)	(0.016)
CF	-0.231	-0.245	-0.265	-0.119	-0.115	-0.113	-0.102	-0.111	-0.113
	(0.046)	(0.032)	(0.015)	(0.048)	(0.034)	(0.016)	(0.048)	(0.034)	(0.016)
CFTT	-0.232	-0.246	-0.265	-0.112	-0.114	-0.113	-0.101	-0.105	-0.113
	(0.045)	(0.032)	(0.015)	(0.047)	(0.034)	(0.016)	(0.047)	(0.034)	(0.016)
BART	-0.250	-0.265	-0.283	-0.125	-0.125	-0.120	-0.125	-0.118	-0.118
	(0.041)	(0.031)	(0.016)	(0.044)	(0.033)	(0.017)	(0.044)	(0.033)	(0.017)
Weak Overlap		SETTING	1		SETTING	2	SETTING 3		
•	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)
NDR	-0.197	-0.233	-0.257	-0.095	-0.103	-0.108	-0.087	-0.089	-0.109
	(0.053)	(0.039)	(0.021)	(0.055)	(0.041)	(0.022)	(0.055)	(0.041)	(0.022)
CF	-0.208	-0.224	-0.246	-0.107	-0.113	-0.111	-0.117	-0.110	-0.117
	(0.055)	(0.041)	(0.022)	(0.056)	(0.042)	(0.022)	(0.055)	(0.042)	(0.022)
CFTT	-0.208	-0.223	-0.246	-0.103	-0.106	-0.109	-0.107	-0.104	-0.117
	(0.054)	(0.041)	(0.022)	(0.055)	(0.042)	(0.022)	(0.055)	(0.041)	(0.022)
BART	-0.222	-0.244	-0.278	-0.114	-0.116	-0.120	-0.121	-0.114	-0.119
	(0.046)	(0.040)	(0.035)	(0.049)	(0.042)	(0.034)	(0.048)	(0.042)	(0.034)

Panel B: Rare Outcomes

Moderate Overlap		SETTING	1		SETTING	2	SETTING 3			
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	
OR	-0.046	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010	
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
NDR	-0.042	-0.041	-0.045	-0.005	-0.006	-0.007	-0.006	-0.006	-0.007	
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)	
CF	-0.043	-0.041	-0.045	-0.008	-0.008	-0.010	-0.009	-0.009	-0.010	
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)	
CFTT	-0.044	-0.042	-0.046	-0.005	-0.007	-0.008	-0.007	-0.007	-0.008	
	(0.015)	(0.010)	(0.005)	(0.011)	(0.008)	(0.004)	(0.011)	(0.008)	(0.004)	
BART	-0.038	-0.037	-0.047	-0.013	-0.011	-0.011	-0.015	-0.012	-0.011	
	(0.013)	(0.010)	(0.005)	(0.010)	(0.008)	(0.004)	(0.010)	(0.008)	(0.004)	
Weak Overlap		SETTING	1		SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	
OR	-0.051	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010	
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
NDR	-0.062	-0.042	-0.044	-0.005	-0.008	-0.007	-0.006	-0.006	-0.006	
	(0.016)	(0.011)	(0.005)	(0.012)	(0.009)	(0.005)	(0.012)	(0.009)	(0.005)	
CF	-0.059	-0.037	-0.041	-0.007	-0.008	-0.010	-0.010	-0.009	-0.010	
	(0.015)	(0.011)	(0.006)	(0.011)	(0.009)	(0.005)	(0.011)	(0.009)	(0.005)	
CFTT	-0.063	-0.038	-0.041	-0.007	-0.008	-0.008	-0.008	-0.008	-0.008	
	(0.015)	(0.011)	(0.006)	(0.011)	(0.009)	(0.005)	(0.011)	(0.009)	(0.005)	
BART	-0.040	-0.035	-0.046	-0.013	-0.012	-0.011	-0.014	-0.013	-0.012	
	(0.013)	(0.010)	(0.007)	(0.010)	(0.008)	(0.006)	(0.010)	(0.008)	(0.006)	

<sup>&</sup>lt;sup>a</sup> This table reports raw estimated Ai of estimated plug-in optimal policy for both overlap settings. Advantage is calculated using the learned policies with the learned CATE. The top panel depicts normal outcome prevalence, and the bottom panel shows rare outcome prevalence.

Table O4. True Policy Advantage, Plug-in Policy Class(SD)

Panel B: Rare Outcomes											
Moderate Overlap		SETTING 1			SETTING 2			SETTING 3			
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000		
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117		
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)		
NDR	-0.229	-0.246	-0.264	-0.101	-0.103	-0.109	-0.095	-0.101	-0.111		
	(0.010)	(0.006)	(0.003)	(0.004)	(0.003)	(0.001)	(0.048)	(0.034)	(0.016)		
CF	-0.241	-0.248	-0.264	-0.108	-0.108	-0.110	-0.102	-0.111	-0.113		
	(0.009)	(0.006)	(0.003)	(0.004)	(0.003)	(0.001)	(0.048)	(0.034)	(0.016)		
CFTT	-0.239	-0.247	-0.264	-0.106	-0.106	-0.111	-0.101	-0.105	-0.113		
	(0.009)	(0.006)	(0.003)	(0.004)	(0.003)	(0.001)	(0.047)	(0.034)	(0.016)		
BART	-0.229	-0.247	-0.269	-0.104	-0.105	-0.109	-0.125	-0.118	-0.118		
	(0.010)	(0.006)	(0.002)	(0.004)	(0.003)	(0.001)	(0.044)	(0.033)	(0.017)		
Weak Overlap		SETTING	1	SETTING 2			SETTING 3				
•	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000		
OR	-0.280	-0.280	-0.281	-0.119	-0.118	-0.119	-0.117	-0.117	-0.117		
	(0.007)	(0.005)	(0.002)	(0.004)	(0.003)	(0.001)	(0.003)	(0.002)	(0.001)		
NDR	-0.207	-0.240	-0.259	-0.091	-0.097	-0.103	-0.089	-0.093	-0.103		
	(0.011)	(0.007)	(0.003)	(0.005)	(0.003)	(0.001)	(0.005)	(0.003)	(0.001)		
CF	-0.215	-0.227	-0.243	-0.098	-0.105	-0.109	-0.099	-0.106	-0.110		
	(0.010)	(0.007)	(0.003)	(0.004)	(0.003)	(0.001)	(0.004)	(0.003)	(0.001)		
CFTT	-0.212	-0.227	-0.244	-0.093	-0.099	-0.108	-0.093	-0.100	-0.109		
	(0.011)	(0.007)	(0.003)	(0.005)	(0.003)	(0.001)	(0.004)	(0.003)	(0.001)		
BART	-0.204	-0.231	-0.259	-0.093	-0.101	-0.107	-0.096	-0.101	-0.109		
	(0.011)	(0.007)	(0.003)	(0.004)	(0.003)	(0.001)	(0.004)	(0.003)	(0.001)		

Panel B: Rare Outcomes

Moderate Overlap		SETTING	1		SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	
OR	-0.046	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010	
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
NDR	-0.042	-0.041	-0.045	-0.005	-0.006	-0.007	-0.005	-0.006	-0.007	
	(0.015)	(0.010)	(0.005)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
CF	-0.043	-0.041	-0.045	-0.006	-0.008	-0.010	-0.006	-0.008	-0.010	
	(0.015)	(0.010)	(0.005)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
CFTT	-0.044	-0.042	-0.046	-0.005	-0.006	-0.008	-0.005	-0.007	-0.008	
	(0.015)	(0.010)	(0.005)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
BART	-0.038	-0.037	-0.047	-0.004	-0.006	-0.008	-0.004	-0.006	-0.008	
	(0.013)	(0.010)	(0.005)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
Weak Overlap		SETTING	1		SETTING 2			SETTING 3		
	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	N = 500	N = 1000	N = 5000	
OR	-0.051	-0.047	-0.047	-0.010	-0.010	-0.010	-0.010	-0.010	-0.010	
	(0.005)	(0.003)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
NDR	-0.044	-0.040	-0.043	-0.005	-0.006	-0.007	-0.005	-0.006	-0.006	
	(0.005)	(0.003)	(0.002)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
CF	-0.044	-0.039	-0.043	-0.004	-0.006	-0.009	-0.005	-0.007	-0.009	
	(0.005)	(0.003)	(0.002)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
CFTT	-0.045	-0.040	-0.043	-0.004	-0.006	-0.007	-0.005	-0.006	-0.007	
	(0.005)	(0.003)	(0.002)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
BART	-0.045	-0.039	-0.042	-0.003	-0.005	-0.007	-0.003	-0.006	-0.007	

<sup>&</sup>lt;sup>a</sup> This table reports true Ai of estimated plug-in optimal policy for both overlap settings. Advantage is calculated using the learned policies with the true CATE. The top panel depicts normal outcome prevalence, and the bottom panel shows rare outcome prevalence.