

1 The Title

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4 *AN ESSAY PRESENTED TO AIMS RWANDA IN PARTIAL FULFILMENT OF THE REQUIREMENTS FOR THE AWARD OF*
5 *MASTER OF SCIENCE IN MATHEMATICAL SCIENCES*



DECLARATION

This work was carried out at AIMS Rwanda in partial fulfilment of the requirements for a Master of Science Degree.

I hereby declare that except where due acknowledgement is made, this work has never been presented wholly or in part for the award of a degree at AIMS Rwanda or any other University.

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ACKNOWLEDGEMENTS

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- 15 This is optional and should be at most half a page. Thanks Ma, Thanks Pa. One paragraph in
16 normal language is the most respectful.
- 17 Do not use too much bold, any figures, or sign at the bottom.

¹⁸ DEDICATION

¹⁹ This is optional.

Abstract

A short, abstracted description of your essay goes here. It should be about 100 words long. But write it last.

An abstract is not a summary of your essay: it's an abstraction of that. It tells the readers why they should be interested in your essay but summarises all they need to know if they read no further.

The writing style used in an abstract is like the style used in the rest of your essay: concise, clear and direct. In the rest of the essay, however, you will introduce and use technical terms. In the abstract you should avoid them in order to make the result comprehensible to all.

You may like to repeat the abstract in your mother tongue.

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1. Introduction

In today's world where the most popular and convenient way of storing information is the electronic storage. Electronic storage provides an effective way to process this form of data storage with less human effort. As the stored information increases the difficulty it turns we face in trying access and extract what we need. For the purpose of easily understanding the contents of the data or know what it talks about, topic models serves as a tool for handling this task. Topic models were discovered by researchers in machine learning (ML). It is a statistical tool with a collection of algorithms that reveals the key components to understanding a document. Huge magnitude of unlabelled text can be analysed with a topic model. Topic model algorithms provides the environment that allows users to explore the text in details and summarize it irrespective their size. Topic model is very useful in identifying the patterns of words in a document and in the event that more than one document is involved in the ML, documents with similar patterns can be related. Topic models are unsupervised method of ML, through various algorithms is able to produce cluster of words that represent somewhat a summary of a document. They are applied in search engines to recommend to users what they are interested . A typical summary for a collection of documents is for the analysis of web search, producing results for users in further search Turpin et al (2007). This research focuses on summarizing reports from the international federation of red cross and crescent societies (IFRC). The summary provides a representative topic for each document or in other words best cluster of words that summarize the document. Mathematically, it can be perceived as a function that takes a large text and converts to small one, in a way that thematic structure of the large or original document is preserved. This can be represented as :

$$f : L \longrightarrow S, \quad \text{Such that} \quad |L| \ll |S|$$

Where L = Large text or document and S = Summarized document or small document. Intuitively the size of S is smaller than L . Manually going through the reports and trying to understand what each is talking about can be time consuming and challenging. The IFRC is a Non governmental organization that provides humanitarian assistance to victims who suffers a disaster event. Through this aid the IFRC generates data of the occurrences of disaster world-wide. Large volumes of complex information are locked in the reports and it hard extracting them going by the manual approach.. This research will employ the Latent Dirichlet Algorithm (LDA) the Latent Semantic Algorithm (LSA). Both models extract the contextual meaning from a given large text. This research is divided into five chapters, the second chapter elaborates some key concepts of topic modelling, IFRC and similar work. The third chapter discuss explicitly LDA, LSA and the tools that were also used to arrive at the final results. The fourth chapter covers results and discussions. Chapter five presents conclusion and recommendation.

2. Literature Review

2.1 Topic Model

A topic model is a statistical tool that produce a short description of an original document. Topic models can be applied on a single document or a collection of documents. Blei (2012) described topic models as algorithms that discovers the main themes existing in a large text or document and otherwise the combination of two or more documents. He further reveal that the development of probabilistic topic modelling by ML researchers as a set of algorithms that is geared towards revealing and describing large archives of documents with thematic information. Topic models analyses words in the large text document to discover the themes that pervades them, the connection that exist between the words and their with time. In topic modelling the stress of having to label the documents prior to annotations is saved as it is been done in supervised learning. from the analysis of the original document the topics are obtained. Given an very large volume of electronic archives that is impossible for human annotations, topic modelling can help to summarize and organize it.

2.2 Topic Model methods

Topic modelling techniques have been developed to automatically summarize document or large text. These techniques are: latent semantic indexing/allocation (LSI/LSA), the latent dirichlet allocation (LDA) and the probabilistic latent semantic analysis (PLSA) . This research will narrow between LDA and LSA.

2.3 Latent Semantic Analysis

Also known as the latent semantic indexing (LSI) is a topic model method that transforms documents of high dimension to low dimension of words. One useful role played by LSI in topic modelling is its ability to deal with polysemy (Griffiths, Steyvors, 2006). Polysemy is a term that describes words with multiple meaning.

2.4 How The LSA Works

Preliminarily it constructs a matrix $M \in \mathbb{R}^{k \times n}$, from the documents d_1, d_2, \dots, d_k of words w_1, w_2, \dots, w_n . The rows represents the different words and the columns can be viewed as different documents. For example from (??), m_{ij} shows the position and the frequency of the word w_j in document d_i . .To achieve reduction in the dimension of the matrix M the truncated Singular Value Decomposition is applied, given as $M \approx A_t \sum B_t^T$. A_t and B^T are orthogonal

matrices, whilst Σ is a diagonal matrix. Reducing the dimension leads to reduction of noise (Deerwester et al, 1990). To achieve document similarity computing the dot product of the row vectors yields desired results.

Table 2.1: Corpus of documents

	d_1	d_2	d_3
food	0	0	2
food	2	5	0
cash	0	1	0
automobile	1	0	4

2.5 The Idea Latent Dirithchet Allocation

Blei(2012) referred to LDA as the simplest topic model . The ideas underlying this model is every document has several topics existing in it.He defined topic to be a distribution over a fixed a topic.Each topic is made up of words that are very related to the topic. Considering an article with a title "Seeking Life's Bare (Genetic) Necessities," for which data analysis was used to determine the number of genes an organism needs to survive. By hand words pertaining to three different vocabularies were highlighted with different colours. Words such as computer, prediction linked to the topic data analysis highlighted blue, life and evolve about evolutionary biology highlighted pink and words like gene, DNA describing the topic genetics is highlighted yellow. Stop words that occur frequently in the article are removed. The LDA as a statistical tool uses this idea with the assumption that topics are generated prior to words assignment. All words in each vocabulary has a probability value and depending on the topic each word finds itself would be high or low. For example the word "gene" will have a low probability value if it is in the domain of the vocabulary "data analysis" compared to when it belongs to the topic "genetics".He described the process of assigning words in the document to each vocabulary as:

1. From the documents a random distribution over topics is chosen.
2. for each word in the documents:
 - 2a. Randomly choose a topic from the distribution over topics in step 1.
 - 2b. Randomly choose a word from the corresponding distribution over the vocabulary.

The LDA model reflects the idea of multiple topics exhibited by documents. Figure gives a picture of the whole intuition of this generative probabilistic process:

In short description of Figure (2.1) the idea underlying LDA is that, first of all some number of topics that are distribution over words is assumed (far left). In generating for each document, firstly choose a distribution over topics (far right ie. histogram), then the circles of different colours are topic assignment for which words drawn from the document corresponds to.

Figure (2.2) shows real inference with LDA, using 17000 articles from the journal of science. Genetics, Evolution, Disease and Computers represents the topics from one article and the words below each are top 15 most frequent words. The graph on the left shows the probability values for each topic. The probability values for this article for a given set of topics may be different from

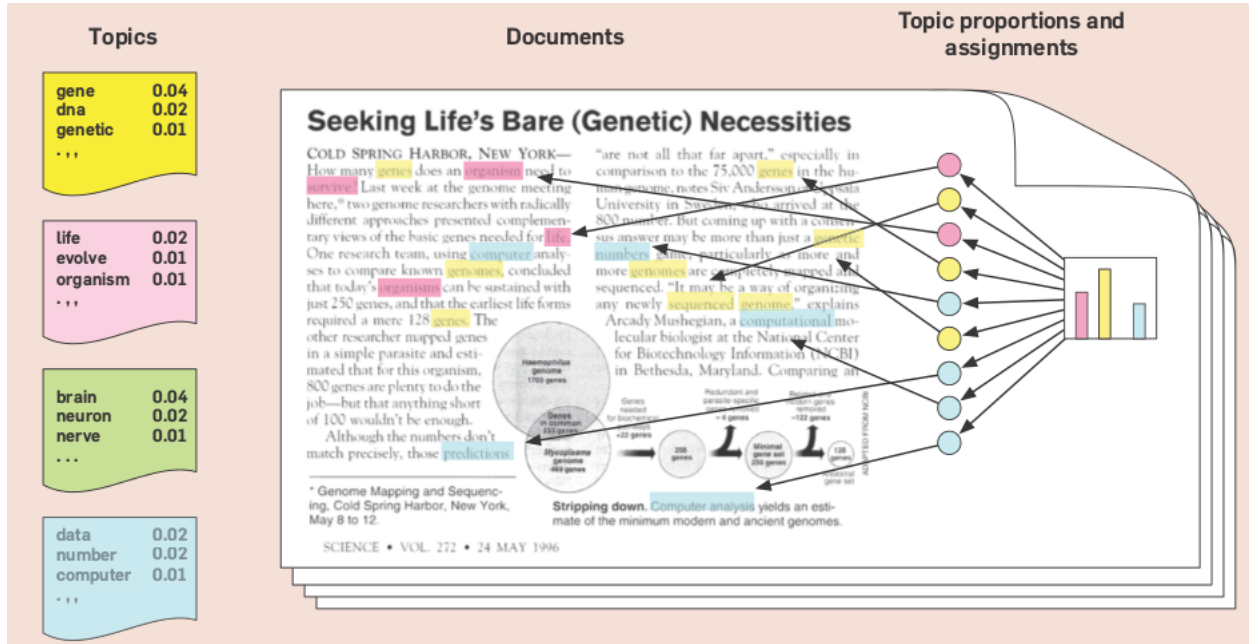


Figure 2.1: Generative intuition of LDA model

another article. in effect, even though some documents or articles may share the same topics, each article exhibits the topics in different proportions.

2.6 Graphical Model of LDA

Figure (2.3) provides a graphical representation, showing the both the observed and latent variables involved in the generative process. The only observed part is the shaded circle $W_{d,n}$, α and η are parameters from the Dirichlet distribution. What the notations stands for:

- D : the number of documents
- N : number of words in each document
- K : number of topics
- θ_d : the topic proportion for each document d .
- $Z_{d,n}$: is the topic assignment for word n in document d .
- $W_{d,n}$: is the observed word n in document d ,
- β_K : topics

From (2.3) the joint distribution or the total probability of both latent and observed variables is given by:

$$P(\beta, \theta, Z, W, \alpha, \beta) = \prod_{k=1}^K P(\beta_k) \prod_{d=1}^D P(\theta_d) \prod_{n=1}^N P(Z_{d,n} | \theta_d) P(W_{d,n} | \beta_k, Z_{d,n}) \quad (2.6.1)$$

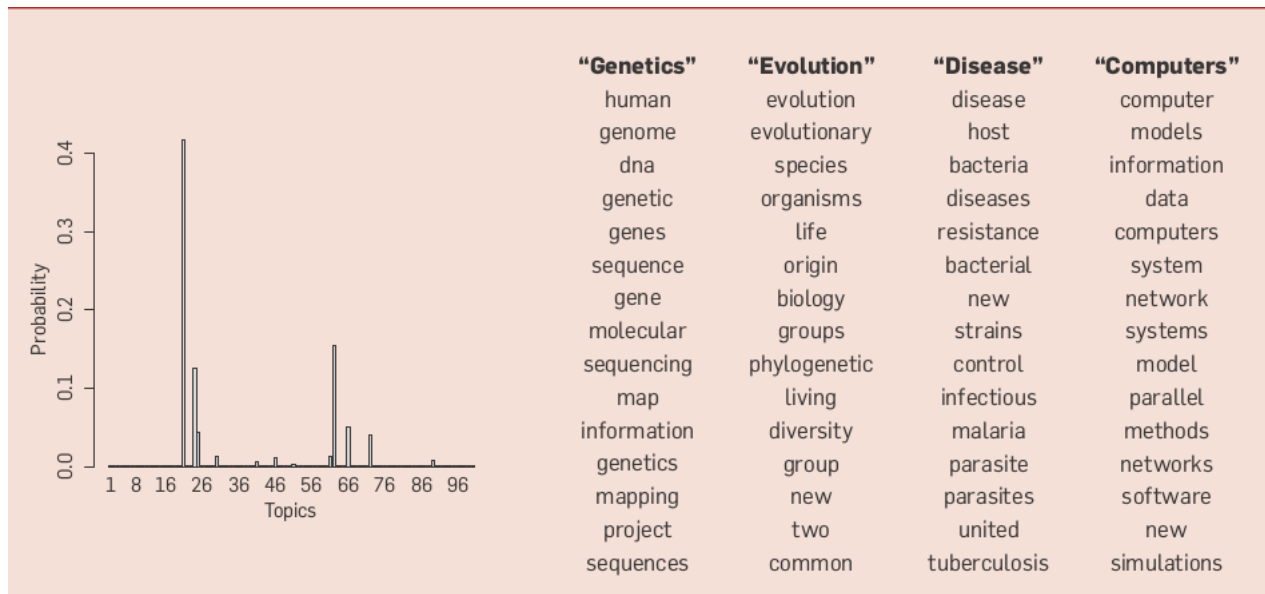


Figure 2.2: Inferred topics from one article of the 17000 articles from the journal of science.

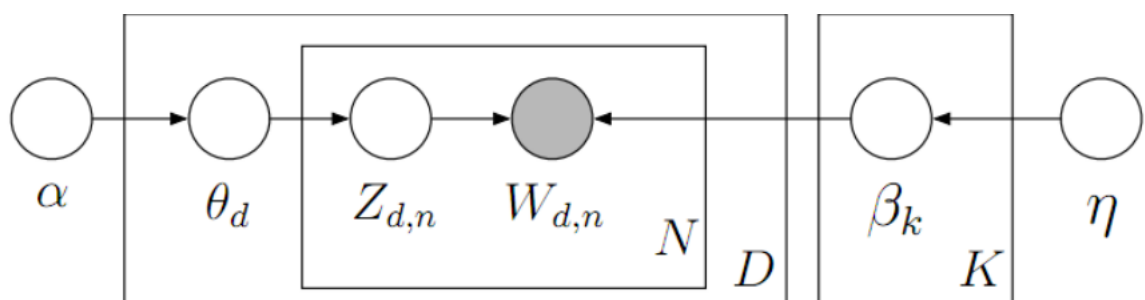


Figure 2.3: Graphical representation of LDA model

2.7 Dirichlet Distribution

It is from the exponential family of continuous multivariate probability with the parameter α of positive real. It is denoted by $D(\alpha)$. Let $S = [S_1, S_2, \dots, S_d]$ as probability mass function, implies $S_i \leq 0$ for $i = 0, 1, 2, \dots, d$ and $\sum_{i=1}^d S_i$. Also suppose $\alpha = [\alpha_1, \alpha_2, \dots, \alpha_d]$ with $\alpha_i > 0$ for each i , and let $\alpha_0 = \sum_{i=1}^d \alpha_i$. Then S is said to have a Dirichlet distribution with parameter α , which is denoted by $S \sim \text{Dir}(\alpha)$, if it has $f(s, \alpha) = 0$, if s is not a pmf and if s is a pmf then,

$$f(s, \alpha) = \frac{\Gamma(\alpha_0)}{\prod_{i=1}^d \Gamma(\alpha_i)} \prod_{i=1}^d s^{\alpha_i - 1} \quad (2.7.1)$$

where $\Gamma(\cdot)$ is the Gamma distribution.

2.8 Advantages of LDA

LDA can be used as a module in other complex models to achieve undertake complicated tasks. The LDA model is used in other applications, not only in text. In recent work we have used pairs of LDA modules to model relationships between images and their corresponding descriptive captions (Blei and Jordan, 2002). But also include problems involving collections of data, including data from domains such as collaborative filtering, content-based image retrieval and bioinformatics.

2.9 Disadvantages of LDA

The bag of words assumption (the order words in a document does not matter) of LDA makes it unrealistic, however it is reasonable if only our task is to uncover the coarse thematic structure of the texts (Blei, 2012).

2.10 Extensions of LDA

Wallach (2006) developed a model that does not ignore the assumption that the order of words does not matter (bag of words). His work uses the combination of the n -gram statistic and latent topic variable by extension of the uni-gram topic model to include properties of a hierarchical Dirichlet language model. Griffiths et al (2005) combined the idea of syntactic and semantics to produce a generative model. This model is capable of simultaneously finding syntactic classes and semantic topics despite having no knowledge of syntax or semantics beyond statistical dependency.

3. Methodology

3.1 Unsupervised Learning (SL)

This is a machine learning task of inferring a function to describe hidden structure from unlabelled data. This type of ML does not require any prior manual categorization of observations in the data. The distinction between supervised learning and unsupervised learning (UL) is that in supervised learning there is evaluation of accuracy of the algorithm used, because data fed to the learner is unlabelled. Also one advantage of UL over SL is that time and cost is saved in labelling as required in SL.

3.2 Natural Language Processing (NLP)

It is a multidisciplinary area that deals with the automatic processing of human language. This automation allows communication between humans and computers. The computer accept input in the form of text or speech and then produces structured representations showing the meaning of those strings as their output.

3.3 Vector Space

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5. Testing

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