

Populating Occupancy Grids from LIDAR Scan Data

Course 4, Module 2, Lesson 2 – Part 2



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Learning Objectives

- Create a simple Inverse Measurement Model
- Discuss an improvement using Bresenham line algorithm

Inverse Measurement Module

$$l_{t,i} = \text{logit}\left(p(m^i|y_t)\right) + l_{t-1,i} - l_{0,i}$$

- State of the occupancy grid given a measurement
- So far we have only seen the following measurement model:

$$p(y_t|m^i)$$

- State of the occupancy grid given a measurement
- A inverse measurement model is needed!

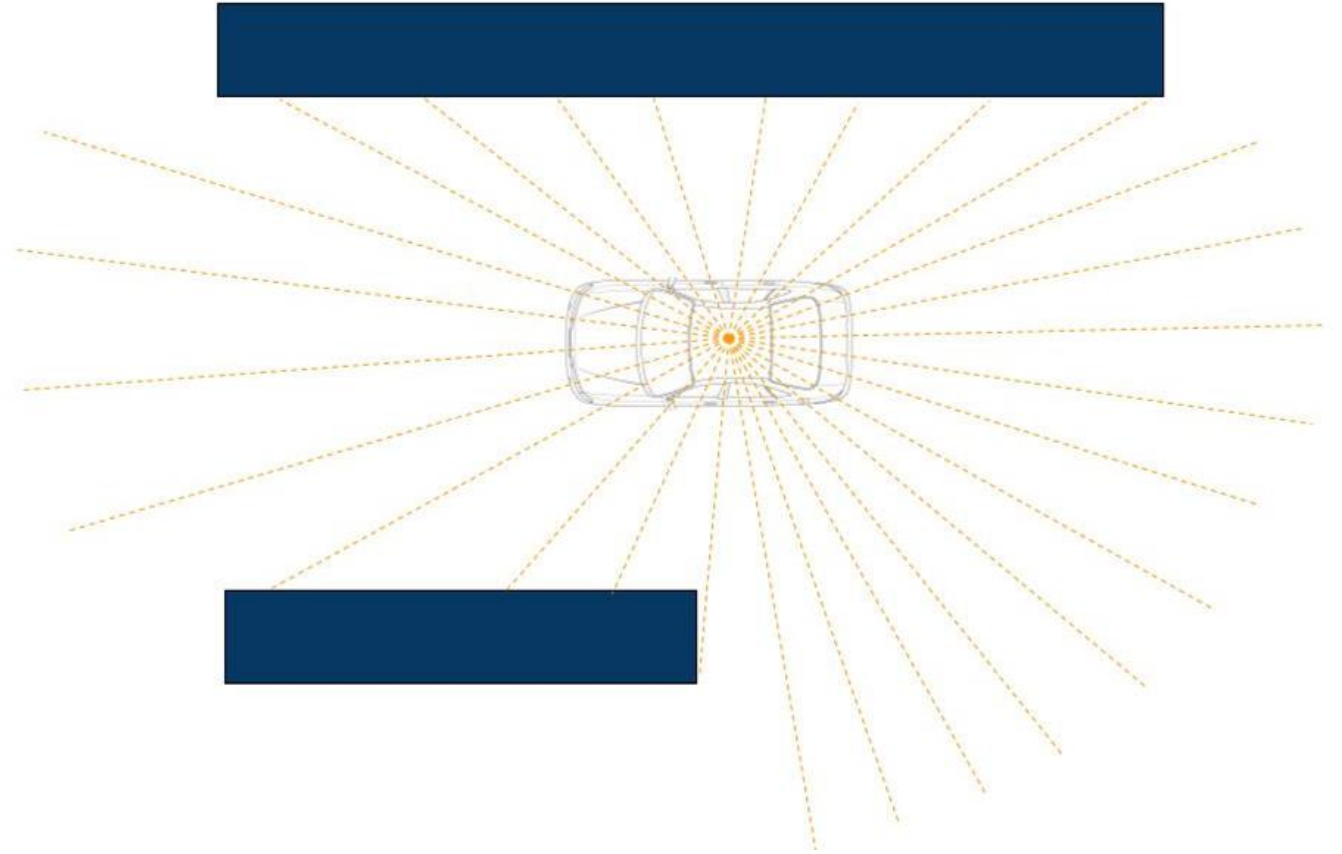
Inverse Measurement Module

- Scanner bearing:

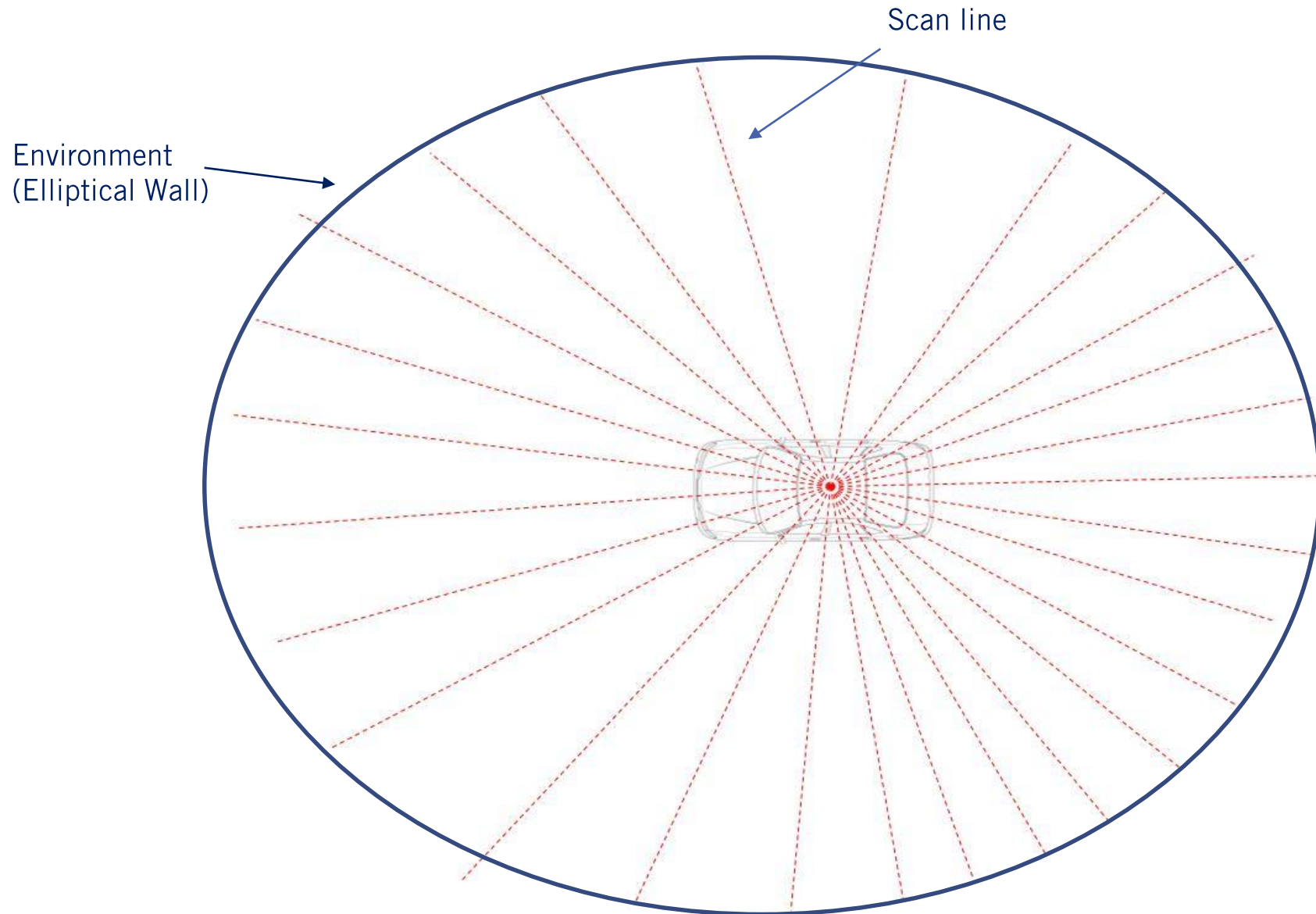
$$\phi^s = [-\phi_{max}^s \quad \dots \quad \phi_{max}^s] \quad \phi_j^s \in \phi^s$$

- Scanner ranges:

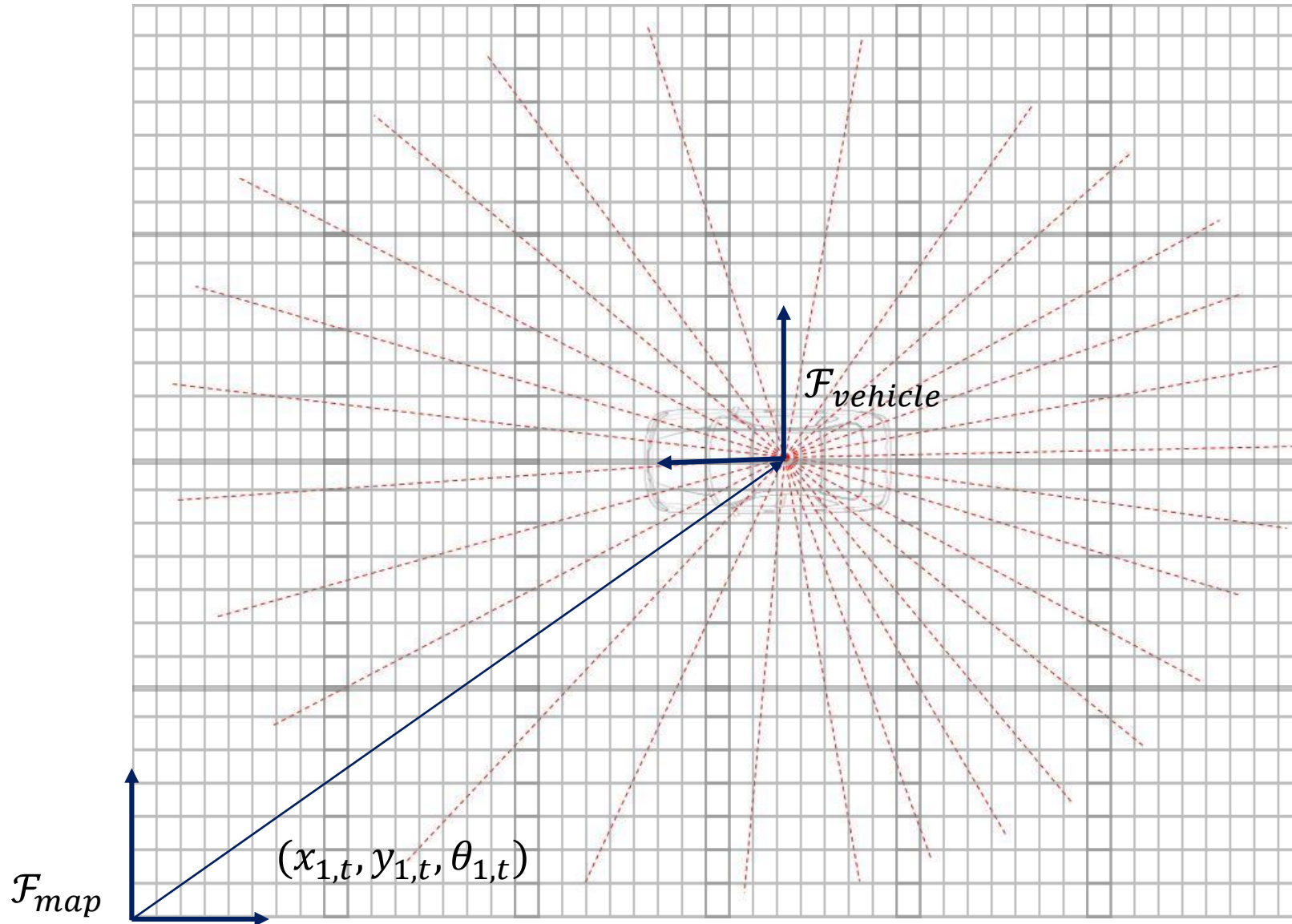
$$r^s = [r_1^s \quad \dots \quad r_j^s] \quad r_j^s \in [0, r_{max}^s]$$



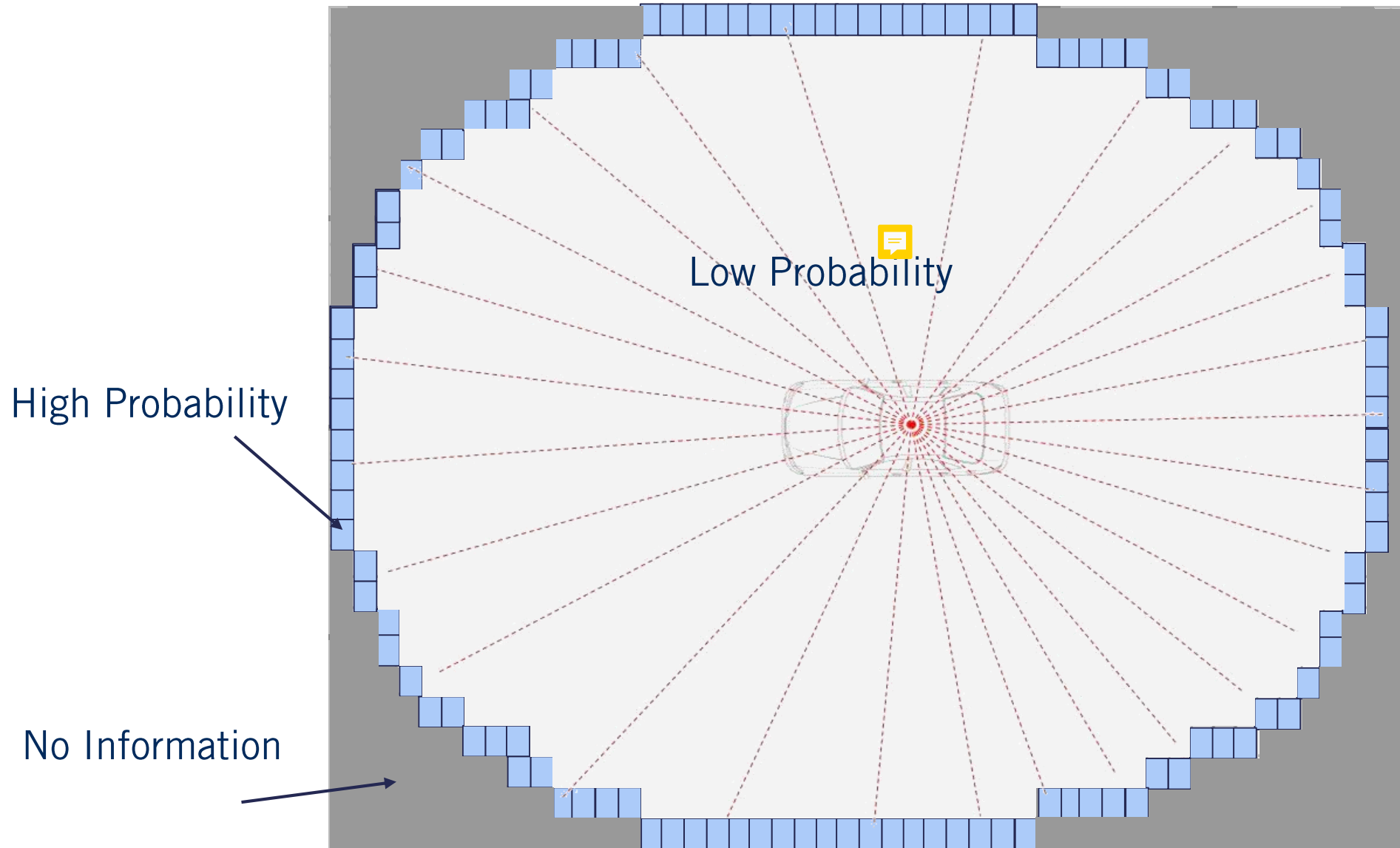
Inverse Measurement Module



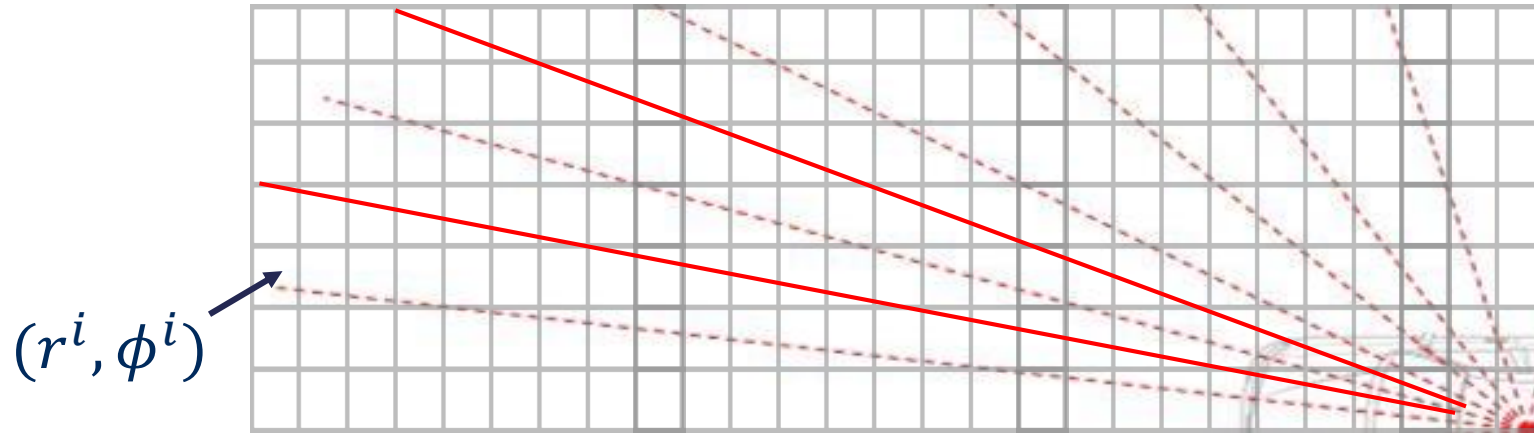
Inverse Measurement Module



Inverse Measurement Module



Inverse Measurement Module – To be fixed



Closest relative bearing:

$$k = \operatorname{argmin}(|\phi^i - \phi_j^s|)$$

Relative range:

$$r^i = \sqrt{\underbrace{(m_x^i - x_{1,t})^2}_{\text{grid location}} + \underbrace{(m_y^i - x_{2,t})^2}_{\text{sensor location}}}$$

grid location

sensor
location

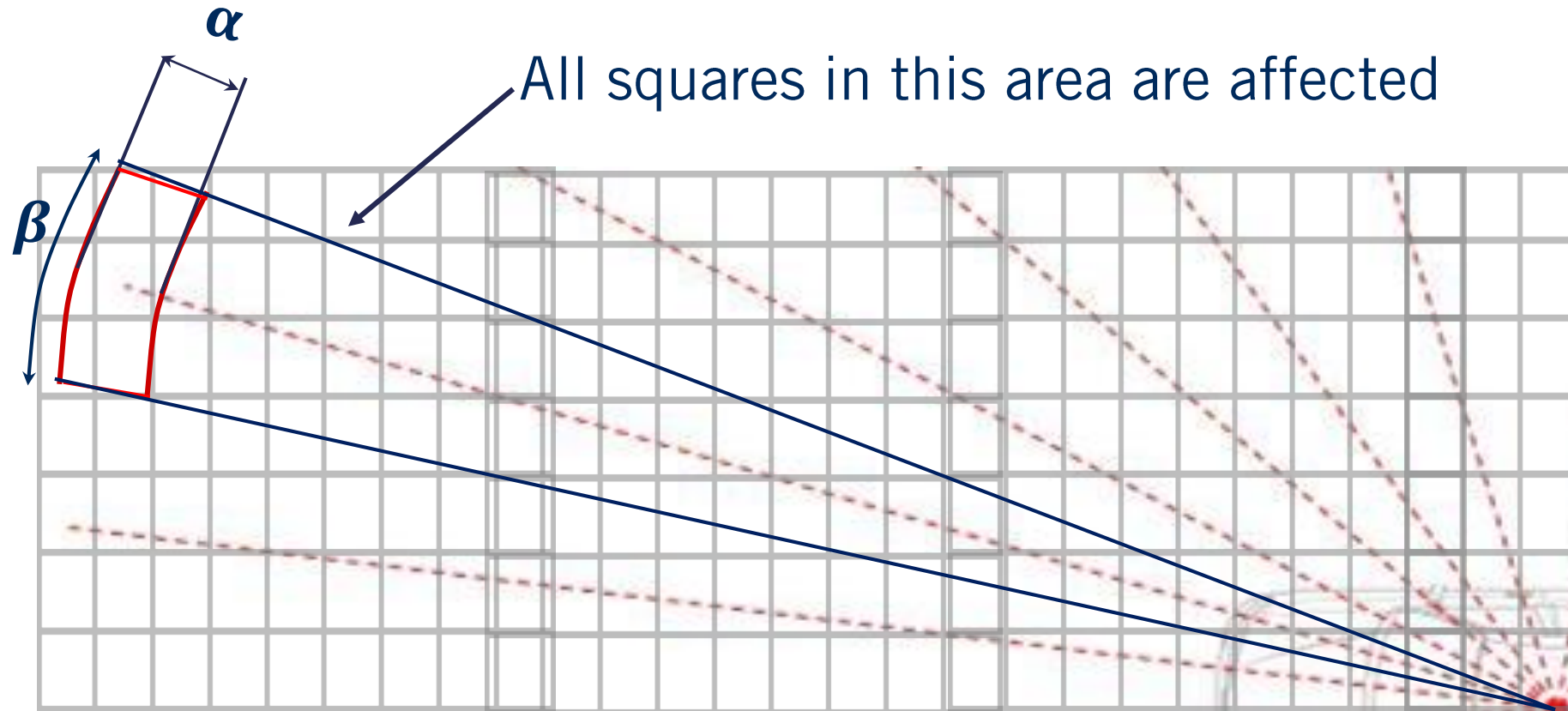
Relative bearing:

$$\phi^i = \tan^{-1} \left(\frac{m_y^i - x_{2,t}}{m_x^i - x_{1,t}} \right) - x_{3,t}$$

Phi identifies the bearing to the given cell in reference to the sensor's coordinate frame.

Inverse Measurement Module

- α - defines the affected range for high probability
- β - defines the affected angle for low and high probability



Inverse Measurement Module - Algorithm

- No Information

$$\text{if } r^i > \min(r_{max}^s) \text{ or } |\phi^i - \phi_k^s| > \beta/2$$

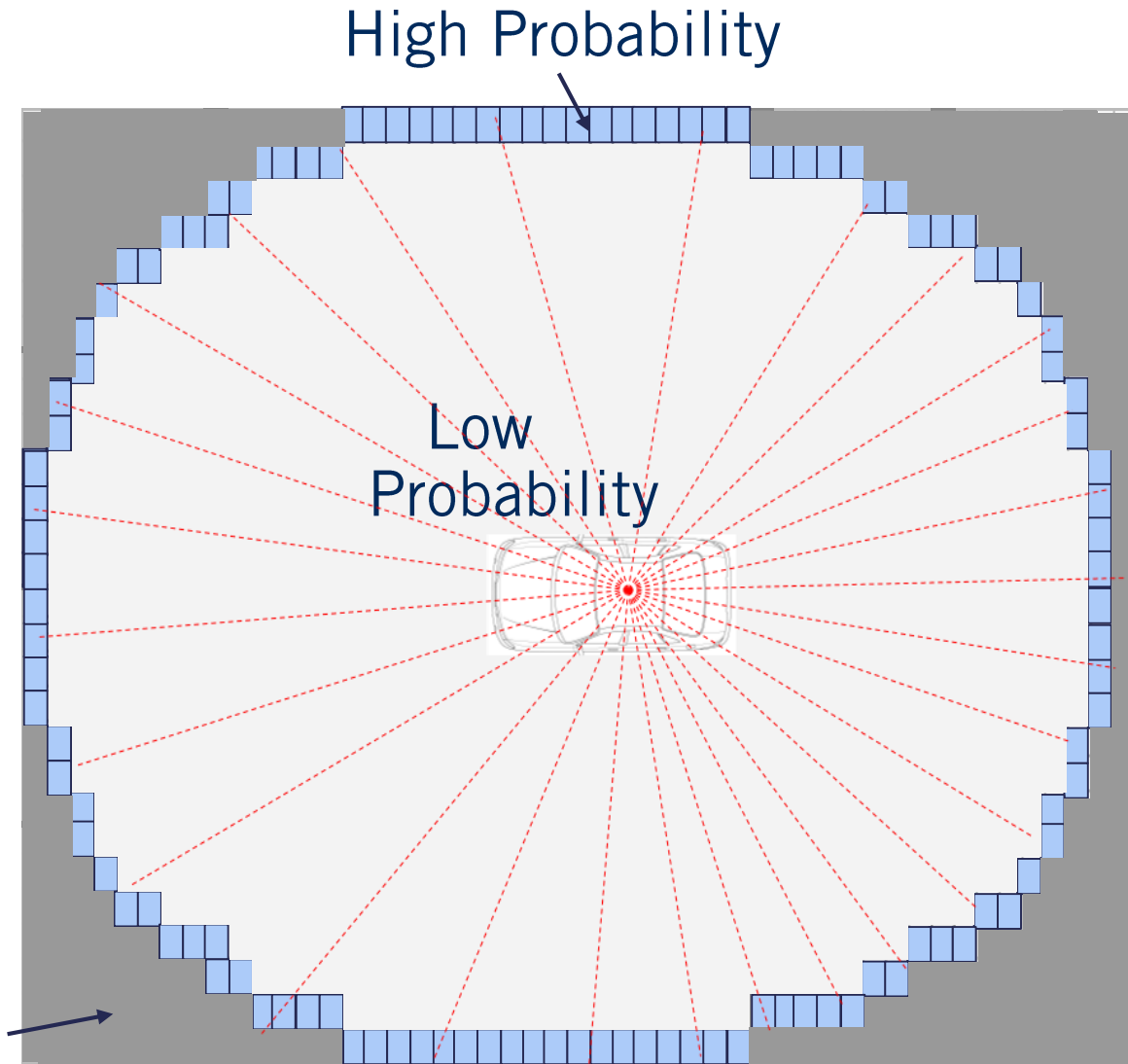
- High probability

$$\text{if } r_k^s < r_{max}^s \text{ and } |r^i - r_k^s| > \alpha/2$$

- Low probability

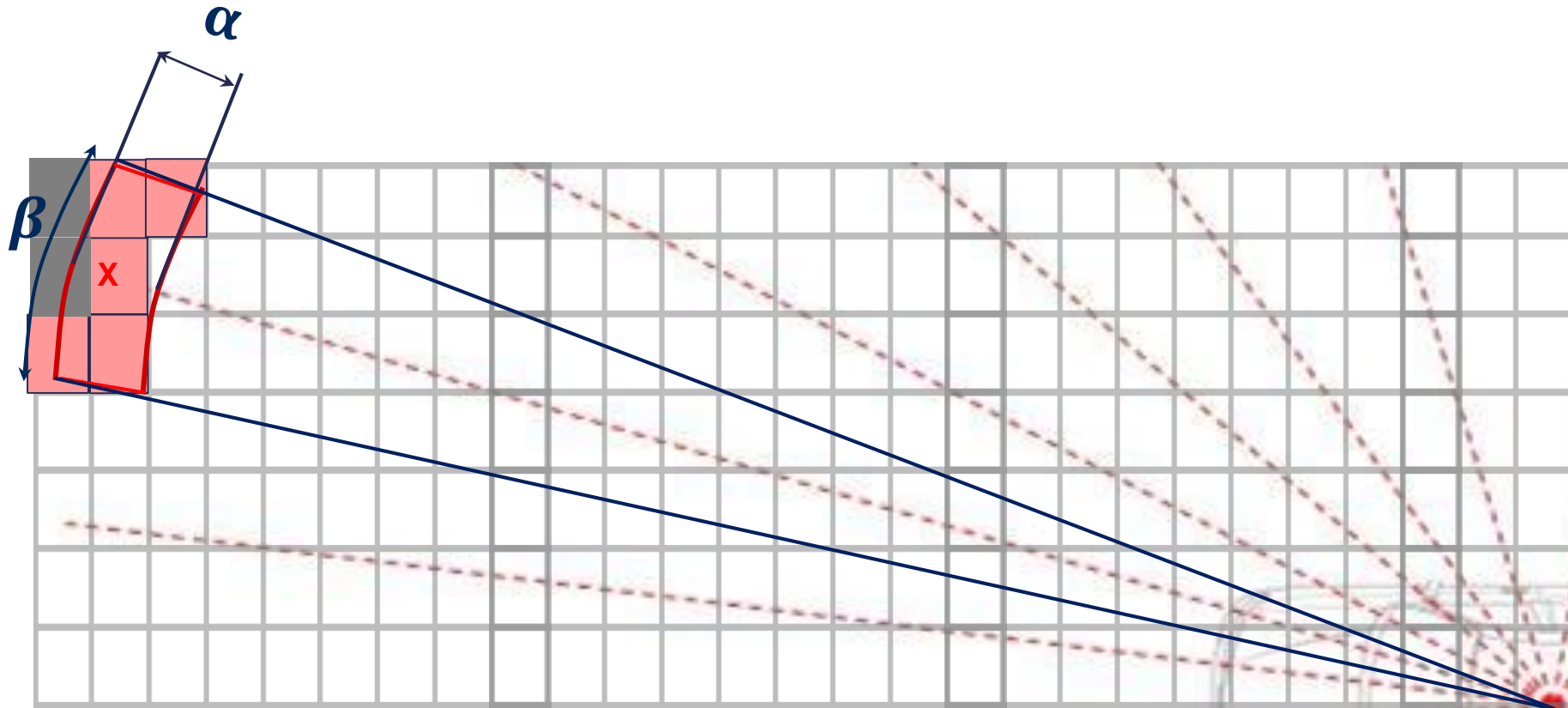
$$\text{if } r^i < r_k^s$$

No Information



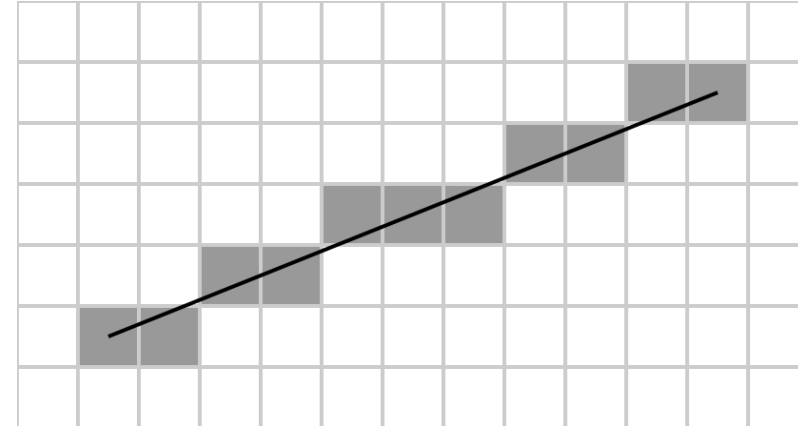
Inverse Measurement Module

- Example – red cells denote high probability of occupied, given measurement denoted by red x.



Inverse Measurement Module With Ray Tracing

- Ray tracing algorithm using Bresenham's line algorithm
 - Rasterized line algorithm
 - Uses very cheap fixed point operations for fast calculations
- Perform update on each beam from the LIDAR rather than each cell on the grid
 - Performs far fewer updates (ignores no information zone)
 - Much cheaper per operation



Summary

- Create a simple Inverse Measurement Model
- Discuss an improvement using Bresenham line algorithm