$\begin{aligned} \text{variables} &= [\text{var('x')}, \text{var('y')}] \text{ } \\ \text{f} &= \text{sum}([\text{randint(-4,4)} * \text{prod}([\text{v**randint(0,2)} \text{ } \\ \text{for } \\ \text{in variables}]) \text{ } \\ \text{for } _i \\ \text{range(3)}]) \\ \text{gradient} &= [derivative(f, v) \\ for \\ vinvariables] \end{aligned}$

Exercise 1 Let $\overrightarrow{\mathbf{F}}(x,y) = \langle gradient[0], gradient[1] \rangle$. Identify whether $\overrightarrow{\mathbf{F}}$ is a gradient field, and if it is, find a potential function F such that F(0,0) = 0.

Hint: You should use the Clairaut gradient test.

Multiple Choice:

- (a) $\overrightarrow{\mathbf{F}}$ is a gradient field. \checkmark
- (b) $\overrightarrow{\mathbf{F}}$ is not a gradient field.

Exercise 1.1 A potential function F such that F(0,0) = 0 is:

$$F(x,y) = f(x = 0, y = 0)$$