

```
variables = [var('x'), var('y')] f = sum([randint(-4,4) * prod([v**randint(0,2) for
v in variables]) for i in range(3)]) gradient = [derivative(f, v) for v in variables]
```

**Exercise 1** Let  $\vec{\mathbf{F}}(x, y) = \langle \text{gradient}[0], \text{gradient}[1] \rangle$ . Identify whether  $\vec{\mathbf{F}}$  is a gradient field, and if it is, find a potential function  $F$  such that  $F(0, 0) = 0$ .

**Hint:** You should use the Clairaut gradient test.

**Multiple Choice:**

- (a)  $\vec{\mathbf{F}}$  is a gradient field. ✓
- (b)  $\vec{\mathbf{F}}$  is not a gradient field.

**Exercise 1.1** A potential function  $F$  such that  $F(0, 0) = 0$  is:

$$F(x, y) = \boxed{f - f(x = 0, y = 0)}$$

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