

#### HW4 (Due 2018/04/02)

1. Every positive integer greater than 1 can be expressed as product of prime numbers. This factorization is unique and is called the **prime factorization**. For example, the number 60 can be decomposed into the factors  $2 \times 2 \times 3 \times 5$ , each of which is prime. Note that the same prime can appear more than once in the factorization. Write a C++ program to display the prime factorization of a given integer  $n$ , where  $2 \leq n \leq 32767$ .

Sample I/O : (The italics for program output and boldfaces for user input)

```
Please input an integer: 60
The prime factorization of 60:
6 = 2*2*3*5.
```

#### **Bonus:**

1. Write a function ***int MinFact(int n)*** that returns the minimum prime factor of  $n$ . Use this function in your program.
2. A point  $(a, b)$  in the plane is said to **dominate** point  $(c, d)$  in the plane if  $a > c$  and  $b > d$ . Given a set  $S = \{(x_1, y_1), (x_2, y_2), (x_3, y_3), \dots, (x_n, y_n)\}$  of  $n$  points in the plane, the **rank** of a point  $p \in S$  is the number of points in  $S$  which are dominated by  $p$ . For instance, If  $S = \{(1, 0), (2, 1), (3, 1), (4, 3), (3, 4)\}$ , the rank of point  $(4, 3)$  is 3 and the rank of  $(3, 1)$  is 1. Write a C++ program to find the ranks of a set  $\{(x_1, y_1), (x_2, y_2), (x_3, y_3), \dots, (x_n, y_n)\}$  of  $n$  points in the plane, where  $1 \leq n \leq 32767$  and  $-32768 \leq x_i, y_i \leq 32767$  for  $1 \leq i \leq n$ .

Sample I/O : (The italics for program output and boldfaces for user input)

```
Please input n: 5
Please input 5 points:
1 0
2 1
3 1
4 3
3 4
The rank of point (1, 0): 0
The rank of point (2, 1): 1
The rank of point (3, 1): 1
The rank of point (4, 3): 3
The rank of point (3, 4): 2
```

#### **Bonus:**

List the results in the non-increasing order.

Sample I/O : (The italics for program output and boldfaces for user input)

*Please input n:* **5**

*Please input 5 points:*

**1 0**

**2 1**

**3 1**

**4 3**

**3 4**

*The rank of point (4, 3): 3*

*The rank of point (3, 4): 2*

*The rank of point (2, 1): 1*

*The rank of point (3, 1): 1*

*The rank of point (1, 0): 0*