Given matrix x, b, and arbitrary c (x.c <> 0), find a such that ax=b

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$$b \cdot c^{T} = \begin{bmatrix} 2 & -1 & 1 \\ 4 & -2 & 2 \\ 6 & -3 & 3 \end{bmatrix}$$

$$a := \frac{\mathbf{b} \cdot \mathbf{c}^{\mathsf{T}}}{\mathbf{x} \cdot \mathbf{c}}$$

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(Check solution ax=b)

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$$\mathbf{b} \cdot \mathbf{c}^{\mathrm{T}} = \begin{bmatrix} 1 & -2 & 3 \\ 2 & -4 & 6 \\ 3 & -6 & 9 \end{bmatrix}$$

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