# DATA624\_Homework7

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### Instructions

In Kuhn and Johnson do problems 6.2 and 6.3. There are only two but they consist of many parts. Please submit a link to your Rpubs and submit the .rmd file as well.

#### Question 6.2

Developing a model to predict permeability (see Sect. 1.4) could save significant resources for a pharmaceutical company, while at the same time more rapidly identifying molecules that have a sufficient permeability to become a drug:

(a) Start R and use these commands to load the data:

```
library(AppliedPredictiveModeling)

## Warning: package 'AppliedPredictiveModeling' was built under R version 4.4.2

data(permeability)
```

The matrix fingerprints contains the 1,107 binary molecular predictors for the 165 compounds, while permeability contains permeability response.

(b) The fingerprint predictors indicate the presence or absence of substructures of a molecule and are often sparse meaning that relatively few of the molecules contain each substructure. Filter out the predictors that have low frequencies using the nearZeroVar function from the caret package. How many predictors are left for modeling?

```
fin_df <- data.frame(fingerprints)
print(nrow(fin_df))#165 rows</pre>
```

```
## [1] 165
```

```
print(nrow(t(fin_df)))#1107 predictors
```

```
## [1] 1107
```

```
## Limiting to those predictors that have variance.
 #Getting those with little variance.
 no var <- nearZeroVar(fin df)</pre>
 filtered_fingerprints<- fin_df[,-no_var]</pre>
 #print(head(filtered_fingerprints))
 print(nrow(filtered_fingerprints))#165
 ## [1] 165
 print(nrow(t(filtered_fingerprints))) #388
 ## [1] 388
 ### There are a total of 388 predictors / columns left for the analysis.
(c) Split the data into a training and a test set, pre-process the data, and tune a PLS model. How
many latent variables are optimal and what is the corresponding resampled estimate of R2?
 ## Joining the permeability vector to the main of before splitting the training data.
 #Confirming it is 165 rows long before adding as columns
 print(length(permeability)) #165
 ## [1] 165
 fin_df <- cbind(filtered_fingerprints, permeability)</pre>
 ## Splitting into training and test. 70 / 30 split
 training_split <- createDataPartition(fin_df$permeability, p = 0.7, list = FALSE)</pre>
 training_data <- fin_df[training_split,]</pre>
 print(nrow(training_data)) #117
 ## [1] 117
 print(nrow(t(training_data))) #389
 ## [1] 389
 test_data <- fin_df[-training_split,]</pre>
 print(nrow(test_data)) #48
 ## [1] 48
```

```
print(nrow(t(test_data))) #389
```

```
## [1] 389
```

#Data is joined and split into training and test groups.

```
set.seed(55)

## kfold cross validation
cros_val <- trainControl(method = "cv", number = 10)

## Now building the pls model with this. Using the pre processing in chapter to center and sc ale.
pls_model <- train(permeability ~ ., data = training_data, method = "pls", preProc = c("cente r", "scale"), tuneLength = 20, trControl = cros_val)

print(pls_model)</pre>
```

```
## Partial Least Squares
##
## 117 samples
## 388 predictors
##
## Pre-processing: centered (388), scaled (388)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 105, 105, 105, 106, 105, 105, ...
## Resampling results across tuning parameters:
##
    ncomp RMSE
##
                     Rsquared
                                 MAE
##
     1
           12.58853 0.3511641
                                 9.356453
                                 8.366885
##
     2
           11.60144 0.4544098
##
     3
           12.05765 0.4393652
                                9.130589
##
     4
           12.27880 0.4394690
                                9.369868
##
     5
           12.27715 0.4449749
                                9.423895
##
           11.79750 0.4773522
     6
                                9.154883
##
     7
           12.15269 0.4673002
                                9.696704
##
     8
           12.34894 0.4608957
                                 9.803761
     9
           12.92097 0.4286110 10.327925
##
##
    10
           13.23454 0.4124511 10.606670
##
           13.32668 0.4060148 10.494620
     11
##
    12
           13.71110 0.3976863 10.548275
##
           13.56240 0.4142326 10.442903
    13
           13.74217 0.4038169 10.603450
##
     14
##
    15
           13.62405 0.4053626 10.456459
           13.43965 0.4238671 10.203302
##
    16
##
    17
           13.83938 0.4147860 10.490994
##
    18
           13.77051 0.4205518 10.426430
##
    19
           13.97746 0.4094807 10.592096
     20
           14.19270 0.4000833 10.718478
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 2.
```

#### Taking a look at the model results above, the latent variables that are optimal for this model are 2. After running the model on the training data, the lowest error values (RMSE 11.7  $\mid$  MAE 8.2) was 2 variables and this also had the highest r^2 value at ~0.512. In short a pls model with 2 components is ideal.

(d) Predict the response for the test set. What is the test set estimate of R2?

```
## Running it on the test data
test_preds <- predict(pls_model, newdata = test_data)
print(postResample(pred = test_preds, obs = test_data$permeability))</pre>
```

```
## RMSE Rsquared MAE
## 12.1647314 0.5202086 8.3202388
```

```
#RMSE Rsquared MAE
#13.6063581 0.2713528 8.5561909
## The r^2 for the test set is 0.27
```

## (e) Try building other models discussed in this chapter. Do any have better predictive performance?

```
## Other models discussed in this chapter were:

# OLS regression
ols_model <- train(permeability ~ ., data = training_data, method = "lm", preProc = c("cente
r", "scale"), trControl = cros_val)</pre>
```

```
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
```

```
print(ols model)
```

```
## Linear Regression
##
## 117 samples
## 388 predictors
##
## Pre-processing: centered (388), scaled (388)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 105, 105, 106, 105, 105, 105, ...
## Resampling results:
##
##
     RMSE
              Rsquared
                         MAE
##
     29.8877 0.2580011 21.10244
##
## Tuning parameter 'intercept' was held constant at a value of TRUE
# RMSE
            Rsquared
                       MAE
  26.08582 0.2149182 17.51395
test_preds_ols <- predict(ols_model, newdata = test_data)</pre>
## Warning in predict.lm(modelFit, newdata): prediction from rank-deficient fit;
## attr(*, "non-estim") has doubtful cases
print(postResample(pred = test_preds_ols, obs = test_data$permeability))
         RMSE
##
                Rsquared
                                 MAE
## 28.9716851 0.1406138 19.5017028
#RMSE
                          MAE
         Rsquared
#33.36353485 0.09437608 17.42874107
# Ridge Regression model
ridge_model <- train(permeability ~ ., data = training_data, method = "ridge", preProc = c("c</pre>
enter", "scale"), tuneLength = 20, trControl = cros_val)
## Warning: model fit failed for Fold05: lambda=0.0000000 Error in if (zmin < gamhat) { : mis</pre>
sing value where TRUE/FALSE needed
## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = train<math>Info,
## : There were missing values in resampled performance measures.
print(ridge_model)
```

```
## Ridge Regression
##
## 117 samples
## 388 predictors
##
## Pre-processing: centered (388), scaled (388)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 105, 106, 105, 105, 105, 107, ...
## Resampling results across tuning parameters:
##
##
     lambda
                   RMSE
                                Rsquared
##
    0.0000000000
                      16.78449
                                0.4010052
                                             11.886117
##
    0.0001000000
                    7432.70364 0.1925270 4035.002624
##
    0.0001467799
                    8649.20983 0.2113661 5392.668059
    0.0002154435
##
                    1646.90596 0.2091461
                                           710.633984
##
    0.0003162278
                    2839.24160 0.1022610 1276.747770
##
    0.0004641589 10681.62792 0.2667660 7243.315800
##
    0.0006812921
                     547.95967 0.2030475
                                            301.325185
##
    0.0010000000
                     335.42721 0.3221792
                                            172.942270
##
    0.0014677993
                    2837.00493 0.2929745 1502.741819
##
    0.0021544347
                      27.27480 0.3492623
                                             21.111022
##
    0.0031622777
                      56.01914 0.3208350
                                             39.397471
##
    0.0046415888
                      14.31350 0.3893171
                                             10.767258
##
    0.0068129207
                      13.81930 0.4059457
                                             10.452938
##
    0.0100000000
                    1276.76490 0.4230961
                                            726.528869
##
    0.0146779927
                      13.12967 0.4276944
                                             10.058409
##
    0.0215443469
                      12.90388 0.4335900
                                              9.984634
##
    0.0316227766
                      12.62272 0.4450382
                                              9.748127
##
    0.0464158883
                      12.46719 0.4525066
                                              9.599264
##
    0.0681292069
                      12.42141 0.4575246
                                              9.548504
                      12.34554 0.4632535
##
    0.1000000000
                                              9.574879
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was lambda = 0.1.
```

```
#Lambda RMSE Rsquared MAE
#0.1000000000 12.20011 0.4841976 9.502962e+00

test_preds_ridge <- predict(ridge_model, newdata = test_data)
print(postResample(pred = test_preds_ridge, obs = test_data$permeability))</pre>
```

```
## RMSE Rsquared MAE
## 13.0256479 0.4791969 9.0590933
```

```
# RMSE Rsquared MAE
#13.4624090 0.3555569 9.4449031

# Lasso Regression model
lasso_model <- train(permeability ~ ., data = training_data, method = "lasso", preProc = c("c enter", "scale"), tuneLength = 20, trControl = cros_val)
print(lasso_model)</pre>
```

```
## The lasso
##
## 117 samples
## 388 predictors
##
## Pre-processing: centered (388), scaled (388)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 105, 105, 106, 105, 105, 105, ...
## Resampling results across tuning parameters:
##
##
    fraction
               RMSE
                          Rsquared
                                    MAE
##
    0.1000000 11.03291 0.5004920
                                     8.017154
    0.1421053 11.01264 0.4815066
##
                                     7.900521
##
    0.1842105 11.23266 0.4447080
                                     8.099254
##
    0.2263158 11.31899 0.4328353
                                     8.167599
##
    0.2684211 11.28798 0.4317873
                                     8.178458
##
    0.3105263 11.34393 0.4257644
                                     8.220985
##
    0.3526316 11.49308 0.4142110
                                     8.352751
    0.3947368 11.66008 0.4003222
##
                                     8.553292
    0.4368421 11.82742 0.3881127
##
                                     8.746691
##
    0.4789474 11.96278 0.3804394
                                     8.909622
    0.5210526 12.08143 0.3753035
##
                                     9.039031
##
    0.5631579 12.18870 0.3708012
                                     9.146026
    0.6052632 12.27187 0.3672951
##
                                     9.235108
##
    0.6473684 12.38499 0.3628674
                                     9.329889
##
    0.6894737 12.48411 0.3586532
                                     9.419492
##
    0.7315789 12.68825 0.3503381
                                     9.597973
##
    0.7736842 12.93145 0.3394492
                                     9.808901
##
    0.8157895 13.13502 0.3307069
                                     9.979756
##
    0.8578947 13.33402 0.3230556
                                    10.129946
##
    0.9000000 13.54018 0.3145848
                                    10.285269
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was fraction = 0.1421053.
```

```
#fraction RMSE Rsquared MAE
# 0.1842105 10.53842 0.5652147 7.571420

test_preds_lasso <- predict(lasso_model, newdata = test_data)
print(postResample(pred = test_preds_lasso, obs = test_data$permeability))</pre>
```

```
## RMSE Rsquared MAE
## 12.8780797 0.4632927 9.5707901
```

```
# RMSE Rsquared MAE
#14.2522321 0.1930075 9.2703352
```

(f) Would you recommend any of your models to replace the permeability laboratory experiment?

Of all the models I ran, when performed on the test set the ridge regression model had the highest r^2 for the test data at 0.355, while the PLS had a r^2 of 0.27. I would choose the ridge model here as a result.

#### Question 6.3

A chemical manufacturing process for a pharmaceutical product was discussed in Sect. 1.4. In this problem, the objective is to understand the relationship between biological measurements of the raw materials (predictors), measurements of the manufacturing process (predictors), and the response of product yield. Biological predictors cannot be changed but can be used to assess the quality of the raw material before processing. On the other hand, manufacturing process predictors can be changed in the manufacturing process. Improving product yield by 1 % will boost revenue by approximately one hundred thousand dollars per batch:

(a) Start R and use these commands to load the data:

```
library(AppliedPredictiveModeling)
data(ChemicalManufacturingProcess)
```

The matrix processPredictors contains the 57 predictors (12 describing the input biological material and 45 describing the process predictors) for the 176 manufacturing runs. 'yield' contains the percent yield for each run.

(b) A small percentage of cells in the predictor set contain missing values. Use an imputation function to fill in these missing values (e.g., see Sect. 3.8).

print(summary(ChemicalManufacturingProcess))

```
##
        Yield
                    BiologicalMaterial01 BiologicalMaterial02 BiologicalMaterial03
##
   Min.
                                           Min.
                                                  :46.87
                                                                 Min.
                                                                        :56.97
           :35.25
                    Min.
                            :4.580
   1st Qu.:38.75
                    1st Qu.:5.978
                                           1st Qu.:52.68
                                                                 1st Qu.:64.98
##
   Median :39.97
                    Median :6.305
                                           Median :55.09
                                                                 Median :67.22
##
##
   Mean
           :40.18
                            :6.411
                                                  :55.69
                                                                        :67.70
                    Mean
                                           Mean
                                                                 Mean
   3rd Qu.:41.48
                    3rd Qu.:6.870
                                           3rd Qu.:58.74
##
                                                                 3rd Qu.:70.43
##
   Max.
           :46.34
                    Max.
                            :8.810
                                           Max.
                                                  :64.75
                                                                 Max.
                                                                        :78.25
##
##
   BiologicalMaterial04 BiologicalMaterial05 BiologicalMaterial06
   Min.
          : 9.38
                          Min.
                                 :13.24
                                                Min.
##
                                                       :40.60
##
   1st Qu.:11.24
                          1st Qu.:17.23
                                                1st Qu.:46.05
##
   Median :12.10
                          Median :18.49
                                                Median :48.46
   Mean
          :12.35
                                                Mean
                                                       :48.91
##
                          Mean
                                 :18.60
##
   3rd Qu.:13.22
                          3rd Qu.:19.90
                                                3rd Qu.:51.34
##
   Max.
           :23.09
                          Max.
                                 :24.85
                                                Max.
                                                       :59.38
##
##
   BiologicalMaterial07 BiologicalMaterial08 BiologicalMaterial09
##
           :100.0
                          Min.
                                 :15.88
                                                Min.
                                                       :11.44
##
   1st Qu.:100.0
                          1st Qu.:17.06
                                                1st Qu.:12.60
   Median :100.0
                          Median :17.51
                                                Median :12.84
##
##
   Mean
           :100.0
                          Mean
                                 :17.49
                                                Mean
                                                       :12.85
##
   3rd Ou.:100.0
                          3rd Ou.:17.88
                                                3rd Ou.:13.13
##
   Max.
           :100.8
                          Max.
                                 :19.14
                                                Max.
                                                       :14.08
##
   BiologicalMaterial10 BiologicalMaterial11 BiologicalMaterial12
##
   Min.
           :1.770
                          Min.
                                 :135.8
                                                Min.
##
                                                       :18.35
   1st Qu.:2.460
                          1st Qu.:143.8
                                                1st Qu.:19.73
##
##
   Median :2.710
                          Median :146.1
                                                Median :20.12
##
   Mean
           :2.801
                          Mean
                                 :147.0
                                                Mean
                                                       :20.20
   3rd Ou.:2.990
                          3rd Qu.:149.6
                                                3rd Qu.:20.75
##
   Max.
           :6.870
                          Max.
                                 :158.7
                                                       :22.21
##
                                                Max.
##
   ManufacturingProcess01 ManufacturingProcess02 ManufacturingProcess03
##
##
   Min.
           : 0.00
                            Min.
                                   : 0.00
                                                    Min.
                                                            :1.47
##
   1st Qu.:10.80
                            1st Qu.:19.30
                                                    1st Qu.:1.53
   Median :11.40
                            Median :21.00
                                                    Median :1.54
##
##
   Mean
          :11.21
                            Mean
                                  :16.68
                                                    Mean
                                                          :1.54
##
   3rd Qu.:12.15
                            3rd Qu.:21.50
                                                    3rd Qu.:1.55
##
   Max.
           :14.10
                            Max.
                                   :22.50
                                                    Max.
                                                           :1.60
   NA's
           :1
                            NA's
                                   :3
                                                    NA's
                                                            :15
##
##
   ManufacturingProcess04 ManufacturingProcess05 ManufacturingProcess06
##
   Min.
           :911.0
                            Min.
                                   : 923.0
                                                    Min.
                                                            :203.0
                            1st Qu.: 986.8
   1st Qu.:928.0
                                                    1st Qu.: 205.7
##
##
   Median :934.0
                            Median : 999.2
                                                    Median :206.8
##
   Mean
           :931.9
                            Mean
                                   :1001.7
                                                    Mean
                                                           :207.4
   3rd Qu.:936.0
                            3rd Qu.:1008.9
                                                    3rd Qu.:208.7
##
##
   Max.
           :946.0
                            Max.
                                   :1175.3
                                                    Max.
                                                            :227.4
##
   NA's
           :1
                            NA's
                                   :1
                                                    NA's
                                                            :2
##
   ManufacturingProcess07 ManufacturingProcess08 ManufacturingProcess09
##
   Min.
           :177.0
                            Min.
                                   :177.0
                                                    Min.
                                                            :38.89
##
   1st Qu.:177.0
                            1st Qu.:177.0
                                                    1st Qu.:44.89
```

```
##
   Median :177.0
                          Median :178.0
                                                 Median :45.73
   Mean :177.5
                                                 Mean :45.66
##
                          Mean
                                :177.6
##
   3rd Qu.:178.0
                          3rd Qu.:178.0
                                                 3rd Qu.:46.52
##
   Max.
         :178.0
                          Max.
                                 :178.0
                                                 Max.
                                                        :49.36
   NA's
                          NA's
##
          :1
                                 :1
   ManufacturingProcess10 ManufacturingProcess11 ManufacturingProcess12
##
         : 7.500
##
   Min.
                          Min.
                                 : 7.500
                                                 Min.
                                                            0.0
   1st Qu.: 8.700
                          1st Ou.: 9.000
                                                 1st Ou.:
##
                                                            0.0
   Median : 9.100
                          Median : 9.400
                                                 Median :
##
                                                            0.0
##
   Mean : 9.179
                          Mean : 9.386
                                                 Mean : 857.8
   3rd Qu.: 9.550
                          3rd Qu.: 9.900
                                                 3rd Qu.:
##
                                                            0.0
##
   Max.
         :11.600
                          Max.
                                :11.500
                                                 Max.
                                                        :4549.0
   NA's
                          NA's
                                                 NA's
                                                        :1
##
          :9
                                 :10
##
   ManufacturingProcess13 ManufacturingProcess14 ManufacturingProcess15
                                                        :5904
   Min.
                          Min.
                                 :4701
                                                 Min.
##
         :32.10
   1st Qu.:33.90
##
                          1st Qu.:4828
                                                 1st Qu.:6010
##
   Median :34.60
                          Median:4856
                                                 Median :6032
##
   Mean :34.51
                          Mean
                                 :4854
                                                 Mean :6039
                          3rd Qu.:4882
##
   3rd Qu.:35.20
                                                 3rd Qu.:6061
   Max. :38.60
                          Max.
                                :5055
                                                 Max. :6233
##
##
                          NA's
                                 :1
##
   ManufacturingProcess16 ManufacturingProcess17 ManufacturingProcess18
                                                      :
##
   Min.
                          Min.
                                :31.30
                                                 Min.
##
   1st Qu.:4561
                          1st Qu.:33.50
                                                 1st Qu.:4813
   Median:4588
                          Median :34.40
                                                 Median:4835
##
   Mean :4566
                                                 Mean :4810
##
                          Mean :34.34
                          3rd Qu.:35.10
##
   3rd Qu.:4619
                                                 3rd Qu.:4862
##
   Max. :4852
                          Max. :40.00
                                                 Max. :4971
##
   ManufacturingProcess19 ManufacturingProcess20 ManufacturingProcess21
##
##
   Min.
          :5890
                          Min.
                                : 0
                                                 Min.
                                                        :-1.8000
                                                 1st Qu.:-0.6000
   1st Qu.:6001
                          1st Qu.:4553
##
   Median :6022
                          Median :4582
                                                 Median :-0.3000
##
   Mean :6028
                          Mean :4556
                                                 Mean :-0.1642
##
   3rd Qu.:6050
                                                 3rd Qu.: 0.0000
##
                          3rd Qu.:4610
##
   Max. :6146
                          Max.
                                 :4759
                                                 Max. : 3.6000
##
##
   ManufacturingProcess22 ManufacturingProcess23 ManufacturingProcess24
   Min. : 0.000
##
                          Min.
                                 :0.000
                                                 Min. : 0.000
##
   1st Qu.: 3.000
                          1st Qu.:2.000
                                                 1st Qu.: 4.000
   Median : 5.000
                          Median :3.000
                                                 Median : 8.000
##
##
   Mean
         : 5.406
                          Mean
                                :3.017
                                                 Mean : 8.834
   3rd Qu.: 8.000
                          3rd Qu.:4.000
                                                 3rd Qu.:14.000
##
                          Max.
                                                 Max. :23.000
##
   Max. :12.000
                                :6.000
##
   NA's
         :1
                          NA's
                                 :1
                                                 NA's
                                                        :1
##
   ManufacturingProcess25 ManufacturingProcess26 ManufacturingProcess27
##
   Min. : 0
                          Min.
                               :
                                                 Min. :
##
   1st Qu.:4832
                          1st Qu.:6020
                                                 1st Qu.:4560
                          Median:6047
##
   Median :4855
                                                 Median:4587
   Mean :4828
                                                 Mean :4563
##
                          Mean
                                 :6016
   3rd Qu.:4877
                          3rd Qu.:6070
                                                 3rd Qu.:4609
```

```
##
    Max.
           :4990
                            Max.
                                   :6161
                                                    Max.
                                                           :4710
                            NA's
                                                    NA's
##
    NA's
           :5
                                   :5
                                                           :5
##
    ManufacturingProcess28 ManufacturingProcess29 ManufacturingProcess30
                                   : 0.00
                                                    Min.
##
    Min.
           : 0.000
                            Min.
                                                           : 0.000
    1st Qu.: 0.000
                            1st Qu.:19.70
                                                    1st Qu.: 8.800
##
    Median :10.400
                            Median :19.90
                                                    Median : 9.100
##
##
    Mean
          : 6.592
                            Mean
                                   :20.01
                                                    Mean
                                                          : 9.161
                            3rd Ou.:20.40
                                                    3rd Ou.: 9.700
##
    3rd Qu.:10.750
##
    Max.
           :11.500
                            Max.
                                   :22.00
                                                    Max.
                                                           :11.200
##
    NA's
           :5
                            NA's
                                   :5
                                                    NA's
                                                           :5
   ManufacturingProcess31 ManufacturingProcess32 ManufacturingProcess33
##
##
   Min.
           : 0.00
                            Min.
                                   :143.0
                                                    Min.
                                                           :56.00
    1st Qu.:70.10
                            1st Qu.:155.0
                                                    1st Ou.:62.00
##
##
   Median :70.80
                            Median :158.0
                                                    Median :64.00
##
           :70.18
                            Mean
                                   :158.5
   Mean
                                                    Mean
                                                           :63.54
##
    3rd Qu.:71.40
                            3rd Qu.:162.0
                                                    3rd Qu.:65.00
##
   Max.
          :72.50
                            Max.
                                   :173.0
                                                    Max.
                                                           :70.00
##
    NA's
           :5
                                                    NA's
                                                           :5
##
   ManufacturingProcess34 ManufacturingProcess35 ManufacturingProcess36
##
   Min.
          :2.300
                            Min.
                                   :463.0
                                                    Min.
                                                           :0.01700
##
    1st Qu.:2.500
                            1st Qu.:490.0
                                                    1st Qu.:0.01900
##
   Median :2.500
                            Median :495.0
                                                    Median :0.02000
##
   Mean
          :2.494
                            Mean
                                   :495.6
                                                    Mean :0.01957
##
    3rd Qu.:2.500
                            3rd Qu.:501.5
                                                    3rd Qu.:0.02000
                                   :522.0
##
   Max.
          :2.600
                            Max.
                                                    Max.
                                                           :0.02200
                                                    NA's
    NA's
                            NA's
##
           :5
                                   :5
                                                           :5
##
   ManufacturingProcess37 ManufacturingProcess38 ManufacturingProcess39
##
   Min.
           :0.000
                            Min.
                                   :0.000
                                                    Min.
                                                           :0.000
                                                    1st Qu.:7.100
##
    1st Qu.:0.700
                            1st Ou.:2.000
   Median :1.000
                            Median :3.000
##
                                                    Median :7.200
##
    Mean
          :1.014
                            Mean
                                   :2.534
                                                    Mean
                                                           :6.851
    3rd Qu.:1.300
                            3rd Qu.:3.000
                                                    3rd Qu.:7.300
##
           :2.300
                                   :3.000
##
    Max.
                            Max.
                                                    Max.
                                                           :7.500
##
   ManufacturingProcess40 ManufacturingProcess41 ManufacturingProcess42
##
##
   Min.
           :0.00000
                            Min.
                                   :0.00000
                                                    Min.
                                                           : 0.00
    1st Qu.:0.00000
                            1st Qu.:0.00000
                                                    1st Qu.:11.40
##
##
   Median :0.00000
                            Median :0.00000
                                                    Median :11.60
##
   Mean
           :0.01771
                            Mean
                                   :0.02371
                                                    Mean :11.21
##
    3rd Ou.:0.00000
                            3rd Ou.:0.00000
                                                    3rd Ou.:11.70
##
   Max.
           :0.10000
                            Max.
                                   :0.20000
                                                    Max.
                                                           :12.10
##
   NA's
           :1
                            NA's
                                   :1
   ManufacturingProcess43 ManufacturingProcess44 ManufacturingProcess45
##
##
   Min.
          : 0.0000
                            Min.
                                   :0.000
                                                    Min.
                                                           :0.000
##
    1st Qu.: 0.6000
                            1st Qu.:1.800
                                                    1st Qu.:2.100
##
   Median : 0.8000
                            Median :1.900
                                                    Median :2.200
##
    Mean
          : 0.9119
                            Mean
                                   :1.805
                                                    Mean :2.138
##
    3rd Qu.: 1.0250
                            3rd Qu.:1.900
                                                    3rd Qu.:2.300
##
    Max.
           :11.0000
                            Max.
                                   :2.100
                                                    Max.
                                                           :2.600
##
```

```
## Columns that contain null/ NA values.
#ManufacturingProcess01 ManufacturingProcess02 ManufacturingProcess03 ManufacturingProcess04
ManufacturingProcess05 ManufacturingProcess06 ManufacturingProcess07
#ManufacturingProcess08 ManufacturingProcess10 ManufacturingProcess11 ManufacturingProcess12
ManufacturingProcess14 ManufacturingProcess22 ManufacturingProcess23
#ManufacturingProcess24 ManufacturingProcess25 ManufacturingProcess26 ManufacturingProcess27
ManufacturingProcess28 ManufacturingProcess29 ManufacturingProcess30
#ManufacturingProcess31 ManufacturingProcess33 ManufacturingProcess34 ManufacturingProcess35
ManufacturingProcess36 ManufacturingProcess40 ManufacturingProcess41
## Imputing the values.
chem_df <- data.frame(ChemicalManufacturingProcess)</pre>
## Keeping it simple with taking the median values of each of the columns, as most columns th
at have NA only have one NA
imputed <- preProcess(chem_df, method = "medianImpute")</pre>
chem df imputed <- predict(imputed, chem df)</pre>
print(summary(chem df imputed)) # No more nulls
```

```
BiologicalMaterial01 BiologicalMaterial02 BiologicalMaterial03
##
        Yield
##
    Min.
           :35.25
                    Min.
                            :4.580
                                           Min.
                                                  :46.87
                                                                 Min.
                                                                         :56.97
    1st Qu.:38.75
                     1st Qu.:5.978
                                           1st Qu.:52.68
                                                                 1st Qu.:64.98
##
    Median :39.97
                    Median :6.305
                                           Median :55.09
                                                                 Median :67.22
##
##
    Mean
           :40.18
                    Mean
                            :6.411
                                           Mean
                                                  :55.69
                                                                 Mean
                                                                         :67.70
    3rd Qu.:41.48
                     3rd Qu.:6.870
                                           3rd Qu.:58.74
                                                                 3rd Qu.:70.43
##
##
    Max.
           :46.34
                    Max.
                            :8.810
                                           Max.
                                                  :64.75
                                                                 Max.
                                                                         :78.25
    BiologicalMaterial04 BiologicalMaterial05 BiologicalMaterial06
##
           : 9.38
                                 :13.24
                                                Min.
##
    Min.
                          Min.
                                                        :40.60
    1st Qu.:11.24
                          1st Qu.:17.23
                                                1st Qu.:46.05
##
##
    Median :12.10
                          Median :18.49
                                                Median :48.46
##
    Mean
           :12.35
                          Mean
                                 :18.60
                                                Mean
                                                        :48.91
    3rd Qu.:13.22
                          3rd Qu.:19.90
                                                3rd Qu.:51.34
##
##
    Max.
           :23.09
                          Max.
                                 :24.85
                                                Max.
                                                        :59.38
##
    BiologicalMaterial07 BiologicalMaterial08 BiologicalMaterial09
    Min.
           :100.0
                          Min.
                                 :15.88
##
                                                Min.
                                                        :11.44
##
    1st Qu.:100.0
                          1st Qu.:17.06
                                                1st Qu.:12.60
    Median :100.0
##
                          Median :17.51
                                                Median :12.84
##
    Mean
           :100.0
                          Mean
                                 :17.49
                                                Mean
                                                        :12.85
    3rd Qu.:100.0
                          3rd Qu.:17.88
##
                                                3rd Qu.:13.13
##
    Max.
           :100.8
                          Max.
                                 :19.14
                                                Max.
                                                        :14.08
##
    BiologicalMaterial10 BiologicalMaterial11 BiologicalMaterial12
##
    Min.
           :1.770
                          Min.
                                 :135.8
                                                Min.
                                                        :18.35
    1st Qu.:2.460
                          1st Qu.:143.8
                                                1st Qu.:19.73
##
    Median :2.710
                          Median :146.1
                                                Median :20.12
##
    Mean
           :2.801
                          Mean
                                 :147.0
                                                Mean
                                                        :20.20
##
    3rd Qu.:2.990
                          3rd Qu.:149.6
                                                3rd Qu.:20.75
##
##
    Max.
           :6.870
                          Max.
                                 :158.7
                                                Max.
                                                        :22.21
##
    ManufacturingProcess01 ManufacturingProcess02 ManufacturingProcess03
                                                    Min.
##
    Min.
           : 0.00
                            Min.
                                   : 0.00
    1st Qu.:10.80
                            1st Qu.:19.30
                                                     1st Qu.:1.53
##
                                                    Median :1.54
##
    Median :11.40
                            Median :21.00
    Mean
           :11.21
                            Mean
                                   :16.76
                                                    Mean :1.54
##
##
    3rd Qu.:12.12
                            3rd Qu.:21.50
                                                     3rd Qu.:1.55
##
    Max.
           :14.10
                            Max.
                                   :22.50
                                                    Max.
                                                            :1.60
##
    ManufacturingProcess04 ManufacturingProcess05 ManufacturingProcess06
    Min.
           :911.0
                            Min.
                                   : 923.0
                                                    Min.
                                                            :203.0
##
##
    1st Qu.:928.0
                            1st Qu.: 986.8
                                                    1st Qu.:205.7
    Median :934.0
                            Median : 999.2
                                                    Median :206.8
##
    Mean
           :931.9
                            Mean
                                   :1001.7
                                                    Mean
                                                            :207.4
##
    3rd Ou.:936.0
                            3rd Ou.:1008.7
                                                     3rd Ou.:208.7
##
##
    Max.
           :946.0
                            Max.
                                   :1175.3
                                                    Max.
                                                            :227.4
    ManufacturingProcess07 ManufacturingProcess08 ManufacturingProcess09
##
##
    Min.
           :177.0
                            Min.
                                   :177.0
                                                    Min.
                                                            :38.89
##
    1st Qu.:177.0
                            1st Qu.:177.0
                                                    1st Ou.:44.89
    Median :177.0
                            Median :178.0
                                                    Median :45.73
##
##
    Mean
           :177.5
                            Mean
                                   :177.6
                                                    Mean
                                                            :45.66
##
    3rd Ou.:178.0
                            3rd Qu.:178.0
                                                     3rd Qu.:46.52
##
    Max.
           :178.0
                            Max.
                                   :178.0
                                                    Max.
                                                            :49.36
##
    ManufacturingProcess10 ManufacturingProcess11 ManufacturingProcess12
##
    Min.
           : 7.500
                            Min.
                                   : 7.500
                                                    Min.
                                                                0.0
```

```
##
   1st Qu.: 8.700
                           1st Qu.: 9.000
                                                  1st Qu.:
                                                             0.0
   Median : 9.100
                          Median : 9.400
                                                  Median :
##
                                                             0.0
##
   Mean : 9.175
                          Mean : 9.386
                                                  Mean : 852.9
   3rd Qu.: 9.500
                           3rd Qu.: 9.825
                                                  3rd Ou.:
##
                                                             0.0
   Max.
                                                  Max.
##
         :11.600
                          Max.
                                 :11.500
                                                         :4549.0
   ManufacturingProcess13 ManufacturingProcess14 ManufacturingProcess15
##
                                                        :5904
##
   Min.
          :32.10
                           Min.
                                  :4701
                                                  Min.
   1st Qu.:33.90
                           1st Ou.:4828
                                                  1st Ou.:6010
##
   Median :34.60
                          Median :4856
                                                  Median :6032
##
##
   Mean :34.51
                          Mean
                                :4854
                                                  Mean :6039
   3rd Qu.:35.20
                           3rd Ou.:4882
                                                  3rd Qu.:6061
##
##
   Max.
          :38.60
                          Max.
                                  :5055
                                                  Max.
                                                         :6233
##
   ManufacturingProcess16 ManufacturingProcess17 ManufacturingProcess18
##
                          Min.
                                :31.30
                                                  Min. :
   1st Qu.:4561
                           1st Ou.:33.50
                                                  1st Ou.:4813
##
##
   Median:4588
                          Median :34.40
                                                  Median:4835
##
   Mean :4566
                          Mean
                                :34.34
                                                  Mean :4810
                           3rd Ou.:35.10
##
   3rd Qu.:4619
                                                  3rd Qu.:4862
         :4852
##
   Max.
                          Max.
                                :40.00
                                                  Max. :4971
   ManufacturingProcess19 ManufacturingProcess20 ManufacturingProcess21
##
##
   Min.
          :5890
                          Min.
                                : 0
                                                  Min.
                                                        :-1.8000
   1st Qu.:6001
                           1st Qu.:4553
                                                  1st Ou.:-0.6000
##
                          Median:4582
##
   Median:6022
                                                  Median :-0.3000
##
   Mean :6028
                           Mean
                                :4556
                                                  Mean :-0.1642
   3rd Qu.:6050
                                                  3rd Qu.: 0.0000
##
                           3rd Qu.:4610
                                 :4759
##
   Max.
          :6146
                          Max.
                                                  Max. : 3.6000
##
   ManufacturingProcess22 ManufacturingProcess23 ManufacturingProcess24
         : 0.000
                                                  Min. : 0.00
##
   Min.
                          Min.
                                :0.000
   1st Ou.: 3.000
                           1st Ou.:2.000
                                                  1st Ou.: 4.00
##
   Median : 5.000
                          Median :3.000
                                                  Median: 8.00
##
##
   Mean : 5.403
                          Mean
                                :3.017
                                                  Mean : 8.83
   3rd Qu.: 8.000
                           3rd Qu.:4.000
                                                  3rd Qu.:14.00
##
                                                  Max. :23.00
##
   Max.
         :12.000
                           Max.
                                  :6.000
   ManufacturingProcess25 ManufacturingProcess26 ManufacturingProcess27
##
   Min. : 0
                          Min. :
                                                  Min. :
##
   1st Ou.:4834
                           1st Ou.:6021
                                                  1st Ou.:4563
##
   Median:4855
                          Median:6047
##
                                                  Median:4587
##
   Mean :4829
                          Mean
                                :6016
                                                  Mean :4563
                           3rd Qu.:6069
   3rd Qu.:4876
                                                  3rd Qu.:4609
##
##
   Max.
          :4990
                          Max.
                                  :6161
                                                  Max.
                                                        :4710
   ManufacturingProcess28 ManufacturingProcess29 ManufacturingProcess30
##
                          Min.
                                  : 0.00
##
   Min. : 0.0
                                                  Min. : 0.00
   1st Qu.: 0.0
                           1st Qu.:19.70
                                                  1st Qu.: 8.80
##
##
   Median :10.4
                          Median :19.90
                                                  Median: 9.10
##
   Mean : 6.7
                           Mean
                                 :20.01
                                                  Mean : 9.16
                                                  3rd Qu.: 9.70
##
   3rd Qu.:10.7
                           3rd Qu.:20.40
##
   Max.
         :11.5
                          Max.
                                :22.00
                                                  Max. :11.20
##
   ManufacturingProcess31 ManufacturingProcess32 ManufacturingProcess33
##
   Min. : 0.0
                          Min. :143.0
                                                  Min.
                                                        :56.00
   1st Qu.:70.1
##
                           1st Qu.:155.0
                                                  1st Qu.:62.00
   Median:70.8
                          Median :158.0
                                                 Median :64.00
```

```
##
           :70.2
                                    :158.5
                                                             :63.56
    Mean
                            Mean
                                                     Mean
##
    3rd Qu.:71.4
                             3rd Qu.:162.0
                                                     3rd Qu.:65.00
    Max.
           :72.5
                            Max.
                                    :173.0
                                                     Max.
                                                             :70.00
##
##
    ManufacturingProcess34 ManufacturingProcess35 ManufacturingProcess36
           :2.300
    Min.
                             Min.
                                    :463.0
                                                     Min.
                                                             :0.01700
##
    1st Qu.:2.500
                             1st Qu.:490.0
                                                     1st Qu.:0.01900
##
##
    Median :2.500
                            Median :495.0
                                                     Median :0.02000
                                                             :0.01959
##
    Mean
           :2.494
                            Mean
                                    :495.6
                                                     Mean
                             3rd Qu.:501.0
##
    3rd Qu.:2.500
                                                     3rd Qu.:0.02000
##
    Max.
            :2.600
                             Max.
                                    :522.0
                                                     Max.
                                                             :0.02200
    ManufacturingProcess37 ManufacturingProcess38 ManufacturingProcess39
##
##
    Min.
            :0.000
                            Min.
                                    :0.000
                                                     Min.
                                                             :0.000
                                                     1st Qu.:7.100
##
    1st Qu.:0.700
                             1st Ou.:2.000
##
    Median :1.000
                            Median :3.000
                                                     Median :7.200
##
    Mean
           :1.014
                            Mean
                                    :2.534
                                                     Mean
                                                             :6.851
##
    3rd Qu.:1.300
                             3rd Qu.:3.000
                                                     3rd Qu.:7.300
##
           :2.300
                             Max.
                                    :3.000
                                                     Max.
                                                             :7.500
    Max.
    ManufacturingProcess40 ManufacturingProcess41 ManufacturingProcess42
##
                                    :0.00000
##
    Min.
           :0.00000
                            Min.
                                                     Min.
                                                             : 0.00
    1st Qu.:0.00000
                             1st Qu.:0.00000
                                                     1st Qu.:11.40
##
##
    Median :0.00000
                            Median :0.00000
                                                     Median :11.60
           :0.01761
                                    :0.02358
                                                             :11.21
##
    Mean
                            Mean
                                                     Mean
    3rd Qu.:0.00000
                             3rd Qu.:0.00000
                                                     3rd Qu.:11.70
##
##
    Max.
            :0.10000
                             Max.
                                    :0.20000
                                                     Max.
                                                             :12.10
    ManufacturingProcess43 ManufacturingProcess44 ManufacturingProcess45
##
    Min.
           : 0.0000
                            Min.
                                    :0.000
                                                     Min.
                                                             :0.000
##
    1st Qu.: 0.6000
                             1st Qu.:1.800
                                                     1st Qu.:2.100
##
    Median : 0.8000
                            Median :1.900
                                                     Median :2.200
##
    Mean
           : 0.9119
                            Mean
                                    :1.805
                                                     Mean
                                                             :2.138
    3rd Qu.: 1.0250
                             3rd Qu.:1.900
                                                     3rd Qu.:2.300
##
##
    Max.
            :11.0000
                             Max.
                                    :2.100
                                                     Max.
                                                             :2.600
```

(c) Split the data into a training and a test set, pre-process the data, and tune a model of your choice from this chapter. What is the optimal value of the performance metric?

```
## Splitting the same way in previous question with 70 / 30 train/test
training_split <- createDataPartition(chem_df_imputed$Yield, p = 0.7, list = FALSE)
training_data <- chem_df_imputed[training_split,]
print(nrow(training_data)) #124</pre>
```

```
## [1] 124
```

```
print(nrow(t(training_data))) #58
```

```
## [1] 58
```

```
test_data <- chem_df_imputed[-training_split,]
print(nrow(test_data)) #52</pre>
```

```
## [1] 52
```

```
print(nrow(t(test_data))) #58
```

```
## [1] 58
```

```
#Data is joined and split into training and test groups.

### Model Start

## crossvalidation

cross_val <- trainControl(method = "cv", number = 10)

## Choosing PLS as before because a lot of predictors

pls_model <- train(Yield ~ ., data = training_data, method = "pls", preProc = c("center", "sc ale"), tuneLength = 20, trControl = cros_val)</pre>
```

```
## Warning in preProcess.default(thresh = 0.95, k = 5, freqCut = 19, uniqueCut = 10, : These variables have zero variances: BiologicalMaterial07
```

```
print(pls_model)
```

```
## Partial Least Squares
##
## 124 samples
   57 predictor
##
##
## Pre-processing: centered (57), scaled (57)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 111, 112, 111, 110, 112, 112, ...
  Resampling results across tuning parameters:
##
     ncomp RMSE
##
                      Rsquared
                                 MAE
##
     1
            1.743454 0.3848032 1.265995
     2
            2.090435 0.4483916 1.299609
##
##
      3
            1.684349 0.4884593 1.137722
##
     4
            1.917514 0.4703228 1.200486
      5
##
            2.164873 0.4822886 1.290156
##
      6
            2.194309 0.4662026 1.302664
##
      7
            2.398166 0.4509602 1.393619
##
     8
            2.503817 0.4398075 1.462878
     9
##
            2.603515 0.4302625 1.511631
##
     10
            2.640057 0.4299287 1.531501
##
            2.523398 0.4362536 1.486035
     11
##
     12
            2.407645 0.4283151 1.469341
##
     13
            2.394987 0.4193345 1.484479
##
     14
            2.280194 0.4175881 1.472641
##
     15
            2.345575 0.4154113 1.508872
##
            2.430022 0.4096232 1.556598
     16
##
     17
            2.600111 0.4043572 1.641440
##
     18
            2.882322 0.4036897 1.749258
##
     19
            3.098463 0.4029102 1.826827
     20
            3.361116 0.4023438 1.925809
##
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was ncomp = 3.
```

```
#ncomp RMSE Rsquared MAE
# 3 1.319743 0.5803008 1.050852
## The model chose three components from the PLS predictors as the optimal value.
```

(d) Predict the response for the test set. What is the value of the performance metric and how does this compare with the resampled performance metric on the training set?

```
## Running it on the test data
test_preds <- predict(pls_model, newdata = test_data)
print(postResample(pred = test_preds, obs = test_data$Yield))</pre>
```

```
## RMSE Rsquared MAE
## 1.1703978 0.6537831 0.9595592
# RMSE Rsquared MAE
```

```
# RMSE Rsquared MAE
#1.9545288 0.2765253 1.1098108

## The r^2 opn the test data from the Pls model trained on the trainingdata is lower than the training data. The R^2 on the test data is 0,27 with a RMSE of 1.95, while on the training data it the r^2 was 0.58 with a root mean sqrd error of ~1.3. The model performed more poorly on the test data.
```

(e) Which predictors are most important in the model you have trained? Do either the biological or process predictors dominate the list?

```
# Checking the varibles for what is important
print(varImp(pls_model))

## Warning: package 'pls' was built under R version 4.4.3

##
## Attaching package: 'pls'

## The following object is masked from 'package:caret':
##
## R2

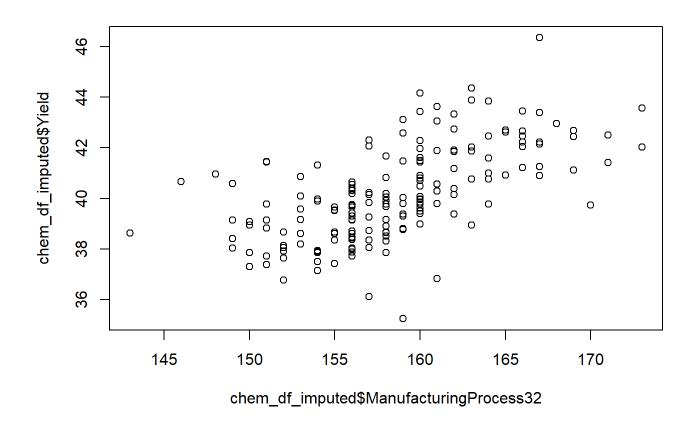
## The following object is masked from 'package:stats':
##
## loadings
```

```
pls variable importance
##
##
     only 20 most important variables shown (out of 57)
##
##
                           Overall
##
                           100.00
## ManufacturingProcess32
## ManufacturingProcess09
                             87.65
## ManufacturingProcess13
                            83.75
## ManufacturingProcess17
                            77.10
## ManufacturingProcess36
                            73.43
## ManufacturingProcess06
                            70.85
## ManufacturingProcess11
                             58.80
## ManufacturingProcess12
                             55.36
## BiologicalMaterial02
                             52.80
## BiologicalMaterial08
                             51.68
## ManufacturingProcess33
                             50.41
## BiologicalMaterial06
                             50.32
## BiologicalMaterial03
                             46.88
## ManufacturingProcess34
                            45.70
## ManufacturingProcess37
                            45.26
## BiologicalMaterial12
                            44.87
## BiologicalMaterial11
                            43.38
## BiologicalMaterial01
                            43.36
## BiologicalMaterial04
                            42.93
## ManufacturingProcess28
                             39.26
```

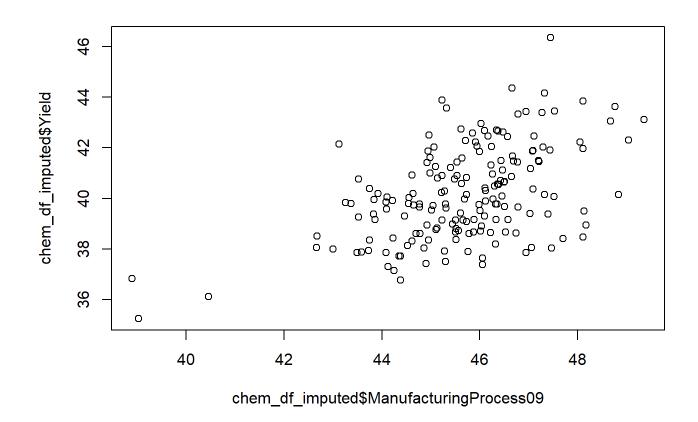
## The top 6 predictors in this model are the Manufacturing / Process predictors. So the answ er would be the process predictors as those that are dominating the list. While there are 3 b iological predictors in the top 10 variables, 70% are manufacturing / process predic

(f) Explore the relationships between each of the top predictors and the response. How could this information be helpful in improving yield in future runs of the manufacturing process?

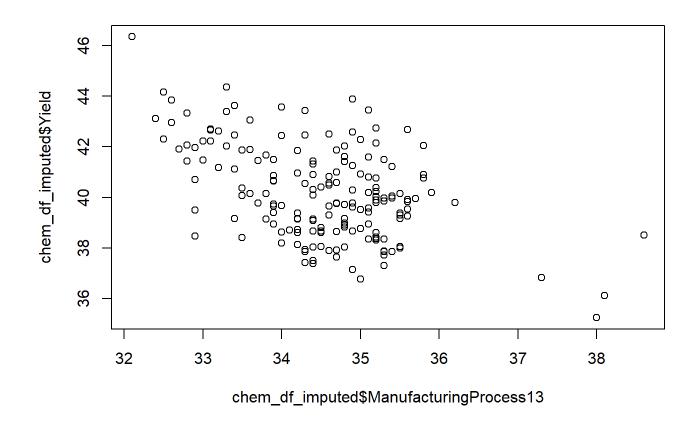
```
## Looking at the top 5 predictors.
print(plot(chem_df_imputed$ManufacturingProcess32, chem_df_imputed$Yield))
```



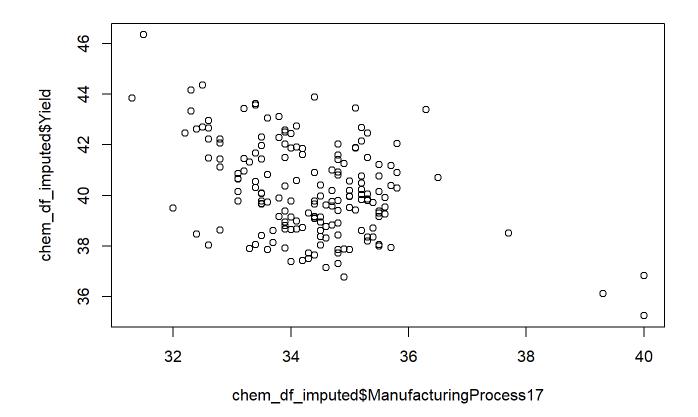
print(plot(chem\_df\_imputed\$ManufacturingProcess09, chem\_df\_imputed\$Yield))



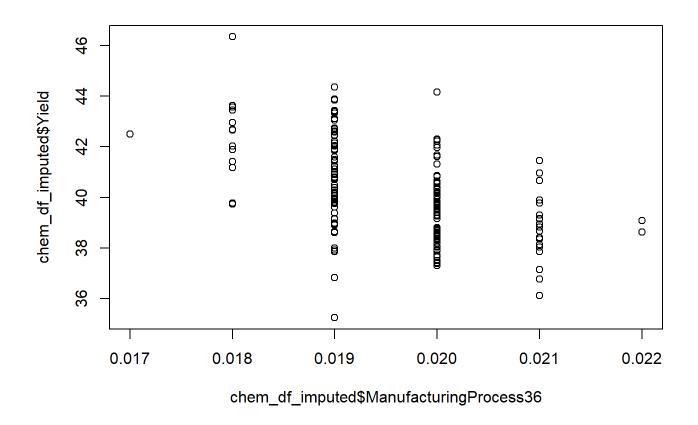
print(plot(chem\_df\_imputed\$ManufacturingProcess13, chem\_df\_imputed\$Yield))



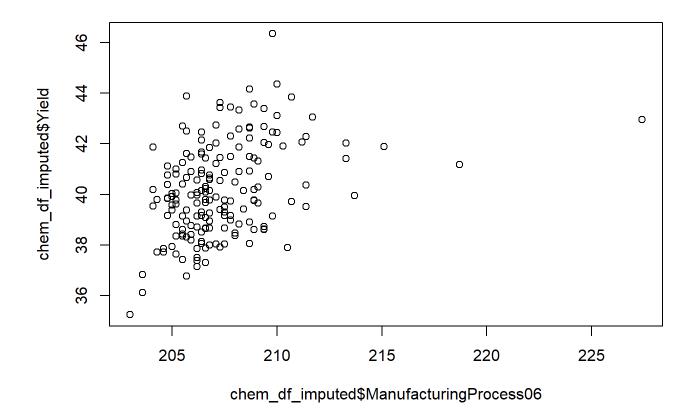
print(plot(chem\_df\_imputed\$ManufacturingProcess17, chem\_df\_imputed\$Yield))



print(plot(chem\_df\_imputed\$ManufacturingProcess36, chem\_df\_imputed\$Yield))



print(plot(chem\_df\_imputed\$ManufacturingProcess06, chem\_df\_imputed\$Yield))



## The predictors ManufacturingProcess32, ManufacturingProcess09, and ManufacturingProcess06 all have positive correlations with yield. These would be the processes that if improved would have the strongest return on yield. ManufacturingProcess36 seems to be impacted by another third variable, but also seems to have a bit of a negative relationship with yield.Lastly, ManufacturingProcess13 has little to negative relationship with yield based on the plot. Overall the first three predictors listed would be the most impactful if improved when looking at a ttempting to increase yield.