

$c = 1, 2$	(Condition)
$l = 1, \dots, L_c$	(ORF)
$m = 1, \dots, M_{cl}$	(Repeat)

$$y_{clm} \sim \text{N}(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$Z_l \sim \text{N}(Z^p, (e^{\sigma^Z})^{-1})$$

$$\nu_l \sim \text{N}(\nu^p, (e^{\sigma^\nu})^{-1})$$

$$\delta_l \sim \text{Bern}(p)$$

$$\sigma^Z \sim \text{N}(\eta^Z, \psi^Z)$$

$$\sigma^\nu \sim \text{N}(\eta^\nu, \psi^\nu)$$

$$\gamma_{cl} = \begin{cases} 0 & \text{if } c = 0; \\ \text{N}(0, (e^{\sigma^\gamma})^{-1}) & \text{if } c = 1. \end{cases}$$

$$\sigma^\gamma = \begin{cases} 0 & \text{if } c = 0; \\ \text{N}(\eta^\gamma, (\psi^\gamma)^{-1}) & \text{if } c = 1. \end{cases}$$

$$\alpha_c = \begin{cases} 0 & \text{if } c = 0; \\ \text{N}(\alpha^\mu, \eta^\alpha) & \text{if } c = 1. \end{cases}$$

$$v_c = \begin{cases} 0 & \text{if } c = 0; \\ \text{N}(v^p, (e^{\sigma^v})^{-1}) & \text{if } c = 1. \end{cases}$$

$$\sigma^v \sim \text{N}(\eta^v, (\psi^v)^{-1})$$

$$Z^p \sim \text{N}(Z^\mu, (\eta^{Z,p})^{-1})$$

$$\nu^p \sim \text{N}(\nu^\mu, (\eta^{\nu,p})^{-1})$$

$$v^p \sim \text{N}(v^\mu, (\eta^{v,p})^{-1})$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$Z_l \sim N(Z^p, (e^{\sigma^Z})^{-1})$$

$$\pi(Z_l|\theta) = \sqrt{\frac{e^{\sigma^Z}}{2\pi}} e^{-\frac{1}{2}(Z_l - Z^p)^2 e^{\sigma^Z}} \prod_{c=1}^2 \prod_{m=1}^{m_{cl}} \sqrt{\frac{e^{v_c + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l}}$$

Taking logs

$$l\pi(Z_l|\theta) = -\frac{1}{2}(Z_l - Z^p)^2 e^{\sigma^Z} - \sum_{c=1}^2 \sum_{m=1}^{m_{cl}} \frac{1}{2}(y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l} + C$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$\nu_l \sim N(\nu^p, (e^{\sigma^\nu})^{-1})$$

$$\pi(\nu_l|\theta) = \sqrt{\frac{e^{\sigma^\nu}}{2\pi}} e^{-\frac{1}{2}(\nu_l - \nu^p)^2 e^{\sigma^\nu}} \prod_{c=1}^2 \prod_{m=1}^{m_{cl}} \sqrt{\frac{e^{v_c + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l}}$$

Taking logs

$$l\pi(\nu_l|\theta) = -\frac{1}{2}(\nu_l - \nu^p)^2 e^{\sigma^\nu} - \sum_{c=1}^2 \sum_{m=1}^{m_{cl}} \frac{1}{2}(\nu_l - (y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l}) + C$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$\delta_l \sim \text{Bern}(p)$$

$$\pi(y_{2lm}|\delta_l = 1, \theta) = (p) \times \prod_{m=1}^{m_{2l}} \sqrt{\frac{e^{v_2 + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{2lm} - e^{\alpha_2 + (Z_l + \gamma_{2l})})^2 e^{v_2 + \nu_l}}$$

$$\pi(y_{2lm}|\delta_l = 0, \theta) = (1 - p) \times \prod_{m=1}^{m_{2l}} \sqrt{\frac{e^{v_2 + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{2lm} - e^{\alpha_2 + Z_l})^2 e^{v_2 + \nu_l}}$$

$$Z_l \sim N(Z^p, (e^{\sigma^Z})^{-1})$$

$$\sigma^Z \sim N(\eta^Z, \psi^Z)$$

$$\pi(\sigma^Z|\theta) = \sqrt{\frac{\psi^Z}{2\pi}} e^{-\frac{1}{2}(\sigma^Z - \eta^Z)^2 \psi^Z} \prod_{l=1}^L \sqrt{\frac{e^{\sigma^Z}}{2\pi}} e^{-\frac{1}{2}(Z_l - Z^p)^2 e^{\sigma^Z}}$$

Taking logs

$$l\pi(\sigma^Z|\theta) = -\frac{1}{2}(\sigma^Z - \eta^Z)^2 \psi^Z + \sum_{l=1}^L \frac{1}{2}(\sigma^Z - (Z_l - Z^p)^2 e^{\sigma^Z}) + C$$

Similarly for σ^ν

$$l\pi(\sigma^\nu|\theta) = -\frac{1}{2}(\sigma^\nu - \eta^\nu)^2 \psi^\nu + \sum_{l=1}^L \frac{1}{2}(\sigma^\nu - (\nu_l - \nu^p)^2 e^{\sigma^\nu}) + C$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$\gamma_{cl} = \begin{cases} 0 & \text{if } c = 0; \\ N(0, (e^{\sigma^\gamma})^{-1}) & \text{if } c = 1. \end{cases}$$

$$\pi(\gamma_{2l}|\theta) = \sqrt{\frac{e^{\sigma^\gamma}}{2\pi}} e^{-\frac{1}{2}(\gamma_{2l})^2 e^{\sigma^\gamma}} \prod_{m=1}^{m_l} \sqrt{\frac{e^{v_2 + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{2lm} - e^{\alpha_2 + (Z_l + \delta_l \gamma_{2l})})^2 e^{v_2 + \nu_l}}$$

Taking logs

$$l\pi(\gamma_{2l}|\theta) = -\frac{1}{2}(\gamma_{2l})^2 e^{\sigma^\gamma} - \sum_{m=1}^{m_l} \frac{1}{2}(y_{2lm} - e^{\alpha_2 + (Z_l + \delta_l \gamma_{2l})})^2 e^{v_2 + \nu_l} + C$$

σ^γ is similar to both σ^Z and σ^ν

$$l\pi(\sigma^\gamma|\theta) = -\frac{1}{2}(\sigma^\gamma - \eta^\gamma)^2 \psi^\gamma + \sum_{m=1}^{m_l} \frac{1}{2}(\sigma^\gamma - (\gamma_l)^2 e^{\sigma^\gamma}) + C$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$\alpha_c = \begin{cases} 1 & \text{if } c = 0; \\ N(\alpha^\mu, \eta^\alpha) & \text{if } c = 1. \end{cases}$$

$$\pi(\alpha_2|\theta) = \sqrt{\frac{\eta^\alpha}{2\pi}} e^{-\frac{1}{2}(\alpha_2 - \alpha^\mu)^2 \eta^\alpha} \prod_{l=1}^L \prod_{m=1}^{m_{2l}} \sqrt{\frac{e^{v_2 + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{2lm} - e^{\alpha_2 + (Z_l + \delta_l \gamma_{2l})})^2 e^{v_2 + \nu_l}}$$

Taking logs

$$l\pi(\alpha_2|\theta) = -\frac{1}{2}(\alpha_2 - \alpha^\mu)^2 \eta^\alpha - \sum_{l=1}^L \sum_{m=1}^{m_{2l}} \frac{1}{2}(y_{2lm} - e^{\alpha_2 + (Z_l + \delta_l \gamma_{2l})})^2 e^{v_2 + \nu_l} + C$$

$$y_{clm} \sim N(e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})}, (e^{v_c + \nu_l})^{-1})$$

$$v_c \sim N(v^p, (e^{\sigma^v})^{-1})$$

$$\pi(v_c|\theta) = \sqrt{\frac{e^{\sigma^v}}{2\pi}} e^{-\frac{1}{2}(v_c - v^p)^2 e^{\sigma^v}} \prod_{l=1}^L \prod_{m=1}^{m_{cl}} \sqrt{\frac{e^{v_c + \nu_l}}{2\pi}} e^{-\frac{1}{2}(y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l}}$$

Taking logs

$$l\pi(v_c|\theta) = -\frac{1}{2}(v_c - v^p)^2 e^{\sigma^v} + \sum_{l=1}^L \sum_{m=1}^{m_{cl}} \frac{1}{2}(v_l - (y_{clm} - e^{\alpha_c + (Z_l + \delta_l \gamma_{cl})})^2 e^{v_c + \nu_l}) + C$$

σ^v is similar to both σ^Z and σ^ν

$$l\pi(\sigma^v|\theta) = -\frac{1}{2}(\sigma^v - \eta^v)^2\psi^v + \sum_{c=1}^2 \frac{1}{2}(\sigma^v - (v_c - v_p)^2 e^{\sigma^v}) + C$$

$$Z_l \sim N(Z^p, (e^{\sigma^Z})^{-1})$$

$$Z^p \sim N(Z^\mu, (\eta^{Z,p})^{-1})$$

$$\pi(Z^p|\theta) = \sqrt{\frac{\eta^{Z,p}}{2\pi}} e^{-\frac{1}{2}(Z^p - Z^\mu)^2 \eta^{Z,p}} \prod_{l=1}^L \sqrt{\frac{e^{\sigma^Z}}{2\pi}} e^{-\frac{1}{2}(Z_l - Z^p)^2 e^{\sigma^Z}}$$

Taking logs

$$l\pi(Z^p|\theta) = -\frac{1}{2}(Z^p - Z^\mu)^2 e^{\sigma^Z} - \sum_{l=1}^L \frac{1}{2}(Z_l - Z^p)^2 e^{\sigma^Z} + C$$

Similarly for ν^p

$$l\pi(\nu^p|\theta) = -\frac{1}{2}(\nu^p - \nu^\mu)^2 e^{\sigma^\nu} - \sum_{l=1}^L \frac{1}{2}(\nu_l - \nu^p)^2 e^{\sigma^\nu} + C$$

And also similarly for v^p

$$l\pi(v^p|\theta) = -\frac{1}{2}(v^p - v^\mu)^2 e^{\sigma^v} - \sum_{l=1}^L \frac{1}{2}(v_l - v^p)^2 e^{\sigma^v} + C$$