### Microeconometrics Using Stata

### NONLINEAR OPTIMIZATION METHODS

### JHON R. ORDOÑEZ 1 2 3

- <sup>1</sup> National University of San Cristóbal de Huamanga
- <sup>2</sup> Faculty of Economic, Administrative and Accounting Sciences
- <sup>3</sup> Professional School of Economics

RESEARCH ASSISTANT

September 20, 2024



#### OUTLINE

- 1 Exercise 1
- 2 Exercise 2
- 3 Exercise 3
- 4 Exercise 4
- 5 Exercise 5
- 6 Exercise 6
- 7 Exercise 7
- 8 Exercise 8
- 9 Exercise 9
- 10 Exercise 10
- 11 Exercise 11

#### Exercise 1

Consider estimation of the logit model covered in section 10.5 and chapter 17. Then  $Q(\beta) = \sum_i \{y_i \ln \Lambda_i + (1-y_i)\Lambda_i\}$ , where  $\Lambda_i = \Lambda(\mathbf{x}_i'\beta) = \exp(\mathbf{x}_i'\beta)/\{1+\mathbf{x}_i'\beta\}$ . Show that  $g(\beta) = \sum_i (y_i - \Lambda_i)\mathbf{x}_i$  and  $H(\beta) = \sum_i -\Lambda_i (1-\Lambda_i)\mathbf{x}_i\mathbf{x}_i'$ . Hint:  $\partial \Lambda(z)/\partial z = \Lambda(z)\{1-\Lambda(z)\}$ . Use the data on **docvis** to generate the binary variable  $\mathbf{d}_-\mathbf{d}\mathbf{v}$  for whether there are any doctor visits. Using just 2002 data, as in this chapter, use **logit** to perform logistic regression of the binary variable  $\mathbf{d}_-\mathbf{d}\mathbf{v}$  on **private**, **chronic**, **female**, **income**, and an intercept. Obtain robust estimates of the standard errors. You should find that the coefficient of **private**, for example, equals 1.27266 , with a robust standard error of 0.0896928.

#### Exercise 2

Adapt the code of section 16.2.3 to fit the logit model of exercise 1 using NR iterations coded in Mata. Hint: In defining an  $n \times 1$  column vector with entries  $\Lambda_i$ , you may find it helpful to use the fact that J(n,1,1) creates an  $n \times 1$  vector of 1s.

### Exercise 3

Adapt the code of section 16.5.3 to fit the logit model of exercise 1 using the ml command method If.

 $\cdot$  |

#### Exercise 4

Generate 100,000 observations from the following logit model  $\mathbf{DGP}$ ,  $y_i=1$  if  $\beta_1+\beta_2x_i>0$  and  $y_i=0$  otherwise;  $(\beta_1,\beta_2)=(0,1)$ ;  $x_i\sim N(0,1)$  where  $u_i$  is logistically distributed. Using the inverse transformation method, you can compute a draw u from the logistic distribution as  $u=-\ln\{(1-r)/r\}$ , where r is a draw from the uniform distribution. Use data from this  $\mathbf{DGP}$  to check the consistency of your estimation method in **exercise 3** or, more simply, of the **logit** command.

#### Exercise 5

Consider the **NLS** example in **section 16.5.5** with an exponential conditional mean. Fit the model using the **ml** command and the **lfnls** program. Also, fit the model using the **nl** command, given in **section 13.3.6**. Verify that these two methods give the same parameter estimates but, as noted in the text, the robust standard errors differ.

#### Exercise 6

Continue the preceding exercise. Fit the model using the **ml** command and the **lfnls** program with default standard errors. These implicitly assume that the **NLS** model error has a variance of  $\sigma^2 = 1$ . Obtain an estimate of

$$s^{2} = \left(\frac{1}{N - K}\right) \sum_{i} \left\{ y_{i} - \exp\left(\mathbf{x}_{i}'\hat{\boldsymbol{\beta}}\right) \right\}^{2}$$
 (1)

, using the **predictnl** postestimation command to obtain  $\exp\left(\mathbf{x}_i'\hat{\boldsymbol{\beta}}\right)$ . Then, obtain an estimate of the **VCE** by multiplying the stored result  $\mathbf{e}(\mathbf{V})$  by  $s^2$ . Obtain the standard error of  $\hat{\boldsymbol{\beta}}_{private}$ , and compare this with the standard error obtained when the **NLS** model is fit using the **nl** command with a default estimate of the **VCE**.

#### Exercise 7

Consider a Poisson regression of **docvis** on the regressors **private**, **chronic**, **female**, and **income** and the programs given in **section 16.7**. Run the **ml model d0 d0pois** command, and confirm that you get the same output as produced by the code in **section 16.7.3**. Confirm that the nonrobust standard errors are the same as those obtained using **poisson** with default standard errors. Run **ml model d1 d1pois**, and confirm that you get the same output as produced by the code in **section 16.7.3**. Run **ml model d2 d2pois**, and confirm that you get the same output as that given in **section 16.7.3**.

1.

### Exercise 8

Adapt the code of section 16.7.3 to fit the logit model of exercise 1 by using ml command method d0.

### Exercise 9

Adapt the code of section 16.7.2 to fit the logit model of exercise 1 by using ml command method If1 with robust standard errors reported.

#### Exercise 10

Adapt the code of section 16.7.3 to fit the logit model of exercise 1 by using ml command method d2.

11 | 1

### Exercise 11

Consider the negative binomial example given in section 16.5.4. Fit this same model by using the ml command method d0. Hint: See the Weibull example in [R] ml.

### References I



A. Colin Cameron, P. K. T. (2022a).

Microeconometrics Using Stata, Second Edition, Volume I: Cross-Sectional and Panel Regression Models.

Stata Press, 2 edition.



A. COLIN CAMERON, P. K. T. (2022B).

Microeconometrics Using Stata, Second Edition, Volume II: Nonlinear Models and Casual Inference Methods.

Stata Press, 2 edition.

### Microeconometrics Using Stata

### NONLINEAR OPTIMIZATION METHODS

### JHON R. ORDOÑEZ 1 2 3

- <sup>1</sup> National University of San Cristóbal de Huamanga
- <sup>2</sup> Faculty of Economic, Administrative and Accounting Sciences
- <sup>3</sup> Professional School of Economics

RESEARCH ASSISTANT

SEPTEMBER 20, 2024

