

# Course Project 2 Guidelines

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## Overview

You will give solutions to four problems on the topic of fitting observed data to models. You can submit your solutions by (1) uploading them to your GitHub repository *ude-ecomod-hw* or (2) emailing me the solutions at [jelena.pantel@uni-due.de](mailto:jelena.pantel@uni-due.de). The solutions can either be (1) a fully executable RMarkdown file (.Rmd) or (2) an R script (.R).

Please note that the following R packages should be installed to get everything I do here to work:

```
library(ggplot2)
library(palmerpenguins)
library(gauseR)
library(vegan)
library(mapsFinland)
```

## Problem 1. Fitting, interpreting, and predicting from a linear model

**Description:** We recall that in our ‘normal’ statistical lives, we may use a *linear regression* to model the relationship between two continuous variables. I made the point that a regression is a mathematical model! Let’s work with a linear regression in R, and how to interpret the output (you will have more of this later in a proper statistics class, but let’s review for now).

**Data / Problem:** Imagine we are researchers studying penguins in Antarctica, more specifically penguins observed at the Palmer Station inhabiting Biscoe, Dream, and Torgersen islands.

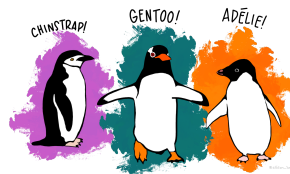
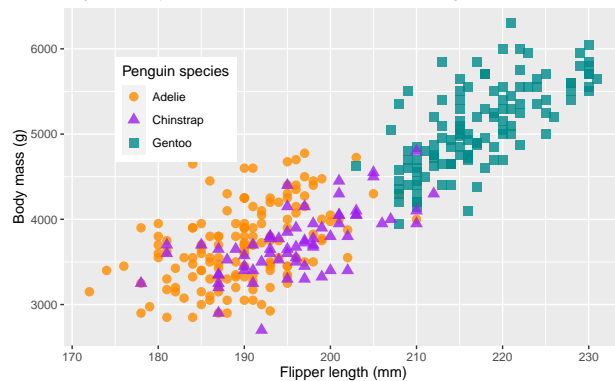


Figure 1: Meet the Palmer penguins! (Artwork by @allison\_horst)

We have access to camera data that allows us to measure penguin flipper length (mm), and we would like to use that to predict penguin body mass (g). This would save a lot of effort by not having to weigh new penguins! We use an existing dataset with observed values for penguin flipper length and body mass, fit a linear model to predict mass from flipper length, and then use the fitted model to make predictions for new cases.

Penguin size, Palmer Station LTER  
Flipper length and body mass for Adelle, Chinstrap and Gentoo Penguins



The data can be found here:

```
data(package = "palmerpenguins")
```

- Please use the `lm` command to fit a linear model to estimate  $y$  `body_mass_g` as a function of  $x$  `flipper_length_mm`:  $y = mx + b$ . Tell me the model estimates for the parameters  $b$  (*y-intercept*) and  $m$  (*slope*). Then, use the `predict` command to tell me the model-predicted values for penguin body mass when the flipper lengths are 190, 215, and 230 mm.

## Problem 2. Fitting, interpreting, and predicting from a logistic growth model using `nls`

**Description:** We considered a model for logistic growth:

$$\frac{dN}{dt} = rN\left(1 - \frac{N}{K}\right)$$

where  $r$  is the population growth rate,  $K$  is the population carrying capacity, and  $N$  is the population size. We would like to evaluate some population data, fit it to a logistic growth model, and estimate parameters in that logistic growth model.

**Data / Problem:** We will use data for a *Paramecium* from Gause's experiments.



Figure 2: *Paramecium aurelium* (Artwork from PhyloPic, by Emily Jane McTavish, from <http://chestofbooks.com/animals/Manual-Of-Zoology/images/I-Order-Ciliata-41.jpg>)

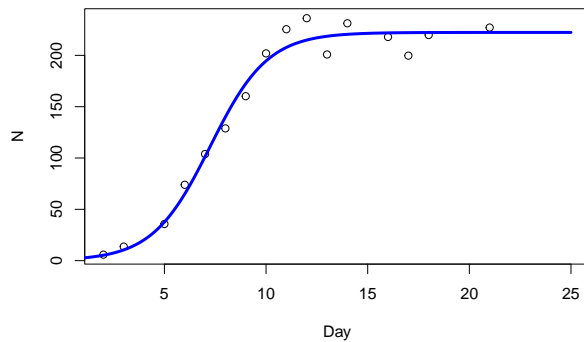
```
# load data
data(gause_1934_book_f22)
dat <- gause_1934_book_f22[gause_1934_book_f22$Treatment == "Pa",
]
```

- Create a plot of the population size over time (`dat$Days`) for species 2 only (`dat$Volume_Species2`). Then I would like you to use the `nls` command to fit this observed data to a logistic growth model (`Volume_Species2 ~ Day`).

- Recall that `nls` has some built-in models, and one of the was for logistic growth. You can find that via the function `SSlogis`. This will work similarly to the Michaelis-Menten (`SSmicmen`) example we did in class January 19.
- There is one very important consideration!! R's `nls` command does not use the exact same logistic model I show you above. Instead it fits the model as:

$$\frac{dN}{dt} = \frac{r}{1 + e^{(-K(N-N_m))}}$$

- This form is a bit different than what you are used to, but it still considers exponential growth at a rate  $r$ , then population size limitation by the carrying capacity  $K$ . There is a new parameter,  $N_m$  - this is the value of  $N$  at the inflection point of the logistic curve. So in this logistic model, there are **three** parameters you need to estimate. Please use the `nls` command to estimate the parameters  $r$ ,  $K$ , and  $N_m$ .
- Report the parameter values given by the model fit.
- Please make a plot of the original data, and the curve fit by the logistic model produced by the `nls` command. Mine looks like this:



### Problem 3. Fitting, interpreting, and predicting from a logistic growth model using `gauseR`

**Data / Problem:** For the same Paramecium dataset, use the function `gause_wrapper` in the R package `gauseR` to fit the data for Species 2 (the same data as above). This is yet another version of the logistic growth model. Instead of using carrying capacity  $K$ , it uses an *intraspecific competition coefficient*  $\alpha_{ii}$ :

$$\frac{dN_i}{dt} = \frac{r}{1 + \alpha_{ii}N_i}$$

- So please estimate the values of  $r$  and  $\alpha_{ii}$ , and show the plot with the raw data and curve fit. You will use the command `gause_wrapper`- note from the example last week that you don't need to do much to get this to work!
- Please give me the model estimates for  $r$  (given in the output variable as `r1`) and for  $\alpha_{ii}$  (given in the output variable as `a11`). Note that you can access this using the name of the output variable, then adding `$parameter_intervals`. So for example, if I assign the results of the `gause_wrapper` command to a variable called `gause_out`, then I can get the parameter values by typing `gause_out$parameter_intervals`. The values are given in the `mu` column.

#### Problem 4. Fitting, interpreting, and predicting from a species-area curve using `vegan` and `nls`

**Description:** A reliable pattern we can observe in nature is the relationship between area (of habitat) and number of species observed. You can read more about that in this paper, **Lomolino 2000**. The exact shape of this curve can take a few different forms. For example, here is a plot showing the number of terrestrial isopods on the central Aegean islands:

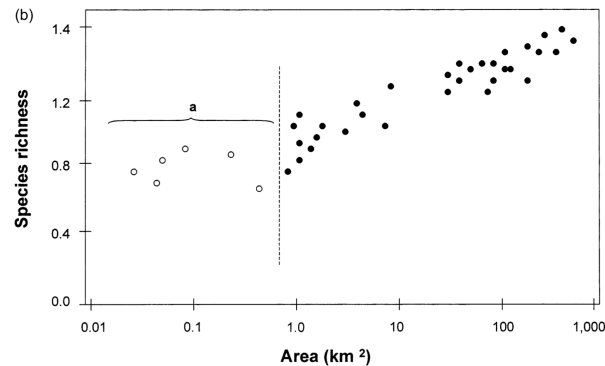


Figure 3: Species-area curve, terrestrial isopods, central Aegean islands. From Lomolino 2000.



One curve that can often describe the species-area relationship is an *Arrhenius curve*. The function for this is:

$$Species = k * area^z$$

Where parameter  $z$  is the steepness of the species-area curve, and  $k$  is the expected number of species in a unit area.

**Data / Problem:** We have some data for bird species on the Sipoo island archipelago (a district of Finland) (the data is using 'hectares' as units, a hectare is equal to 10,000 square meters).

```
data("seutukunnat2019")
ggplot(seutukunnat2019) + geom_sf() + ggtitle("Finland: Maps in R!")
```



```
## Get species area data: sipoo.map gives the areas of
## islands
data(sipoo, sipoo.map)
S <- specnumber(sipoo)
plot(S ~ area, sipoo.map, xlab = "Island Area (ha)", ylab = "Number of Bird Species",
     ylim = c(1, max(S)))
```



- An R package, **vegan** has some nls models included that are commonly used in ecology! After loading `library(vegan)`, please use the `nls` command and the `SSarrhenius` model to fit the model  $S \sim \text{area}$  and estimate the parameters  $k$  and  $z$ . Add the curve to the plot. Mine looks like this:



- Please give me the values for the estimated model parameters (you can use `summary` or `coef` on the fit nls model object to get these).