

# Intermediate Programming

## Day 23

# Outline

- Templates and the STL
- `std::vector`
- Iterators
- Review questions

# Templates (overview)

Q: What is a *template*?

A: Consider an example:

- What needs to change if I want to make the **payload** member a **float/string/etc.** instead of an **int**?

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

# Templates (overview)

Q: What is a *template*?

A: Templates are a way of writing a generic class (**Node**) or function (**print**) and allowing it to work with a parameterized family of types<sup>\*</sup>

⇒ Instead of defining a single class / function, we provide the compiler with a recipe for generating the class / function for whichever type we need

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

<sup>\*</sup>More on this later

# Templates (overview)

In this example:

- `Node` is now a *template* class, parameterized by a type referred to as `PType`

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

# Templates (overview)

In this example:

- **Node** is now a *template* class, parameterized by a type referred to as **PType**
  - We declare **payload** to be of generic type **PType**

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

# Templates (overview)

In this example:

- **Node** is now a *template* class, parameterized by a type referred to as **PType**
- When declaring a variable of type **Node**, we specify the **payload** type, in angle brackets

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

# Templates (overview)

In this example:

- **Node** is now a *template* class, parameterized by a type referred to as **PType**
- When declaring a variable of type **Node**, we specify the **payload** type, in angle brackets
- When defining a function with a generic **Node** argument, the function is templated by **Node's** parameter
  - We are creating a recipe for the function
  - Note:  
We do not need to use the same parameter name  
 $T \neq PType$

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```



# Templates (overview)

In this example:

- **Node** is now a *template* class, parameterized by a type referred to as **PType**
- When declaring a variable of type **Node**, we specify the **payload** type, in angle brackets
- When defining a function with a generic **Node** argument, the function is templated by **Node's** parameter
  - We specify **Node's** parameter to be the generic type **T**

```
...
using std::cout;
using std::endl;

template< class PType >
struct Node
{
    PType payload;
    Node* next;
};

template< class T >
void print( const Node< T >* n )
{
    cout << n->payload << " ";
    if( next ) print( n->next );
    else      cout << endl;
}

int main( void )
{
    Node< int >* n;
    ...
    print( n );
}
```

# The Standard Template Library

- The Standard Template Library (STL) is C++'s compendium of useful data structures and algorithms
  - `pair` – pair of values (possibly of different types)
  - `tuple` – a tuple of values (possibly of different types and arbitrary long)
  - `list` – linked list!
  - `vector` – dynamically-sized array
  - `array` – fixed-length array (not as useful as vector)
  - `map` – associative list, i.e. dictionary
  - `stack` – last-in first-out (LIFO)
  - `deque` – double-ended queue, flexible combo of LIFO/FIFO
  - and many more

# Outline

- Templates and the STL
- **`std::vector`**
- Iterators
- Review questions

# std::vector

A dynamically sized array of elements:

- The template parameter specifies the element type

*main.cpp*

```
#include <iostream>
#include <vector>
using std::vector;
using std::cin;
using std::cout;
int main( void )
{
    vector< float > grades;
    float grade;
    while( cin >> grade ) grades.push_back( grade );
    grades.insert( grades.begin() , 100 );
    cout << "First grade was " << grades[1] << endl;
    cout << "Last grade was " << grades[ grades.size()-1 ] << endl;
    return 0;
}
```

# std::vector

- **push\_back:**
  - inserts an element at the end
- **insert**
  - Insert an element before the prescribed position
- **[ ] operator:**
  - gives access to an element at a prescribed index
- **size:**
  - returns the number of elements in the **vector**

*main.cpp*

```
#include <iostream>
#include <vector>
using std::vector;
using std::cin;
using std::cout;
int main( void )
{
    vector< float > grades;
    float grade;
    while( cin >> grade ) grades.push_back( grade );
    grades.insert( grades.begin() , 100 );
    cout << "First grade was " << grades[1] << endl;
    cout << "Last grade was " << grades[ grades.size()-1 ] << endl;
    return 0;
}
```

# `std::vector`

- `back`:
  - returns the last element
- `pop_back`:
  - removes the last element
- `resize`:
  - resizes the vector to be able to store a specified number of elements
- `erase`
- `clear`
- `at`
- `empty`

See:

<http://www.cplusplus.com/reference/vector/vector/>  
for more `std::vector` functionality

# std::vector

Using the `[ ]` operator and the `size` method, we can iterate over the entries of a `vector`

*main.cpp*

```
#include <iostream>
#include <vector>
using std::vector;
using std::cout;
using std::endl;
int main( void )
{
    vector< int > values;
    values.push_back( 1 );
    values.push_back( 3 );
    values.push_back( 2 );
    for( int i=0 ; i<values.size() ; ++i )
        cout << values[i] << " ";
    cout << endl;
    return 0;
}
```

```
>> ./a.out
1 3 2
>>
```

# std::vector

Using the [ ] operator and the **size** method, we can iterate over the entries of a **vector**

Or we can use **iterators**

*main.cpp*

```
#include <iostream>
#include <vector>
using std::vector;
using std::cout;
using std::endl;
int main( void )
{
    vector< int > values;
    values.push_back( 1 );
    values.push_back( 3 );
    values.push_back( 2 );
    for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it )
        cout << *it << " ";
    cout << endl;
    return 0;
}
```

```
>> ./a.out
1 3 2
>>
```



# std::vector

Using the `[ ]` operator and the `size` method, we can iterate over the entries of a `vector`

Or we can use `iterators`:

- Iterators are “clever pointers” that know how to move over elements of a container
  - Container could be simple (e.g. array) or more complicated (e.g. linked list) or very complicated (e.g. tree)

*main.cpp*

```
#include <iostream>
#include <vector>
using std::vector;
using std::cout;
using std::endl;
int main( void )
{
    vector< int > values;
    values.push_back( 1 );
    values.push_back( 3 );
    values.push_back( 2 );
    for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it )
        cout << *it << " ";
    cout << endl;
    return 0;
}
```

```
>> ./a.out
1 3 2
>>
```

# Outline

- Templates and the STL
- `std::vector`
- Iterators
- Review questions

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**
- The container defines a **T::begin** method
  - Returns an iterator to the first element in the container

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**
- The container defines a **T::begin** method
- The container defines a **T::end** method
  - Returns an iterator to the element just past the last element in the container

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**
- The container defines a **T::begin** method
- The container defines a **T::end** method
- The iterator overloads the pre-increment operator **++**
  - Advances the iterator to the next element

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**
- The container defines a **T::begin** method
- The container defines a **T::end** method
- The iterator overloads the pre-increment operator **++**
- The iterator overloads the inequality operator **!=**
  - Checks if two iterators are different

# Forward iterators

```
vector< int > values;  
...  
for( vector< int >::iterator it=values.begin() ; it!=values.end() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The forward iterator has type **T::iterator**
- The container defines a **T::begin** method
- The container defines a **T::end** method
- The iterator overloads the pre-increment operator **++**
- The iterator overloads the inequality operator **!=**
- The iterator overloads the dereference operator **\***
  - Returns the contents of what the iterator is “pointing to”



# Reverse iterators

```
vector< int > values;  
...  
for( vector< int >::reverse_iterator it=values.rbegin() ; it!=values.rend() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The reverse iterator has type **T::reverse\_iterator**
- The container defines a **T::rbegin** method
- The container defines a **T::rend** method

# Reverse iterators

```
vector< int > values;
```

```
...
```

```
for( vector< int >::reverse
```

For an STL container

- The reverse iterator
- The container default
- The container default

```
#include <iostream>
```

```
#include <vector>
```

```
using std::vector;
```

```
using std::cout;
```

```
using std::endl;
```

```
int main( void )
```

```
{
```

```
    vector< int > values;
```

```
    values.push_back( 1 );
```

```
    values.push_back( 3 );
```

```
    values.push_back( 2 );
```

```
    for( vector< int >::reverse_iterator it=values.rbegin() ; it!=values.rend() ; ++it )
```

```
        cout << *it << " ";
```

```
    cout << endl;
```

```
    return 0;
```

```
}
```

*main.cpp*

```
>> ./a.out
```

```
2 3 1
```

```
>>
```

# Constant iterators

```
vector< int > values;
```

```
...
```

```
for( vector< int >::const_iterator it=values.cbegin() ; it!=values.cend() ; ++it ) cout << *it << " ";
```

For an STL container of type **T** (in this example , **vector<int>**):

- The constant iterator has type **T::const\_iterator**
  - The contents of the container cannot be modified
- The container defines a **T::cbegin** method
- The container defines a **T::cend** method

# Constant iterators

```
vector< int > values;
```

```
...
```

```
for( vector< int >::const_iterator it = values.cbegin(); it != values.cend(); ++it )
```

For an STL container

- The constant iterator
- The contents of the container do not change
- The container does not change
- The container does not change

```
#include <iostream>
```

```
#include <vector>
```

```
using std::vector;
```

```
using std::cout;
```

```
using std::endl;
```

```
int main( void )
```

```
{
```

```
    vector< int > values;
```

```
    values.push_back( 1 );
```

```
    values.push_back( 3 );
```

```
    values.push_back( 2 );
```

```
    for( vector< int >::const_iterator it=values.cbegin(); it!=values.cend(); ++it )
```

```
        cout << *it << " ";
```

```
    cout << endl;
```

```
    return 0;
```

```
}
```

*main.cpp*

```
>> ./a.out
```

```
1 3 2
```

```
>>
```

# Iterators

In general, iterators act like “smart” pointers, allowing us to iterate through the contents of a container and get its values.

For iterators *iter1* and *iter2*, supported operations include:

- Increment: *iter1++* or *++iter1*
- Dereference: *\*iter*
- Assignment: *iter1=iter2*
- Comparison: *iter1!=iter2* or *iter1==iter2*

# Random access iterators

Like pointers, some iterators also support arithmetic (random access).

For iterators *iter1* and *iter2* and integer *n* supported operations include:

- Arithmetic:  $\text{iter1} = \text{iter2} + n$  or  $\text{iter1} = \text{iter2} - n$
- Compound arithmetic:  $\text{iter1} += n$  or  $\text{iter1} -= n$
- Comparison:  $\text{iter1} < \text{iter2}$ ,  $\text{iter1} > \text{iter2}$ , etc.
- Differencing:  $n = \text{iter2} - \text{iter1}$

## Note:

Not all iterators support random access:

- ✓ Iterators for vectors do
- ✗ Iterators for linked lists do not

# Outline

- Templates and the STL
- `std::vector`
- Iterators
- Review questions

# Review questions

1. What is a template in C++?

A way of writing an object (generalization of a struct) so that they can work with any type



# Review questions

2. What is the standard template library?

A collection of standardly used, templated objects and functions

# Review questions

3. How do you iterate a `std::vector` and print out its elements?

```
for( int i=0 ; i<v.size() ; i++ ) std::cout << v[i] << std::endl;
```

or

```
for( vector<type>::iterator it=v.begin() ; it!=v.end() ; it++ )  
    std::cout << *it << std::endl;
```

# Review questions

4. What is an iterator in C++?

Clever pointers that know how to move over the components of a data structure (e.g. support increment and dereferencing)

# Review questions

5. How do you add an element to an existing `std::vector`?

Use the `push_back` or `insert` method.

# Review questions

6. (Bonus) What is the output of this program?

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

v = {}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=1

v = {0.5}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=2

v = {0.5, 4.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```



# Review questions

6. (Bonus) What is the output of this program?

i=3

v = {1.5, 0.5, 4.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=4

v = {1.5, 0.5, 4., 8.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=5

v = {2.5, 1.5, 0.5, 4., 8.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=6

v = {2.5, 1.5, 0.5, 4., 8., 12.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

$i=7$

$v = \{3.5, 2.5, 1.5, 0.5, 4., 8., 12.\}$

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=8

v = {3.5, 2.5, 1.5, 0.5, 4., 8., 12., 16.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=9

v = {4.5, 3.5, 2.5, 1.5, 0.5, 4., 8., 12., 16.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Review questions

6. (Bonus) What is the output of this program?

i=10

v = {4.5, 3.5, 2.5, 1.5, 0.5, 4., 8., 12., 16., 20.}

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```



# Review questions

6. (Bonus) What is the output of this program?

v = {4.5, 3.5, 2.5, 1.5, 0.5, 4., 8., 12., 16., 20.}

↑  
it

↑   ↑  
it+4 it+5

↑  
it+9

```
#include <iostream>
#include <vector>
using std::cin;
using std::cout;
using std::endl;
using std::vector;
int main( void )
{
    vector< double > v;
    for( int i=1 ; i<=10 ; i++ )
    {
        if( i%2==1 ) v.insert( v.begin() , i/2.0 );
        else v.push_back( i*2.0 );
    }
    vector< double >::iterator it = v.begin();
    cout << "first == " << *it << endl;
    cout << "middle1 == " << *(it + 4) << endl;
    cout << "middle2 == " << *(it + 5) << endl;
    cout << "last == " << *(it + 9) << endl;
}
```

# Exercise 8-1

- Website -> Course Materials -> ex8-1

# Exercise 8-1

- Website -> Course Materials -> ex8-1

Merge Sort:

Given an array of values

$\{1, 27, 7, 5, -2, 6, 5, 3, 13\}$

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

$\{1, 27, 7, 5, -2, 6, 5, 3, 13\}$

- Split in two

$\{1, 27, 7, 5, -2\} \{6, 5, 3, 13\}$

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

$\{1, 27, 7, 5, -2, 6, 5, 3, 13\}$

- Split in two

$\{1, 27, 7, 5, -2\}$   $\{6, 5, 3, 13\}$

- Sort the two halves independently

$\{-2, 1, 5, 7, 27\}$   $\{3, 5, 6, 13\}$

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{ }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

## Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

$$\{1, 27, 7, 5, -2, 6, 5, 3, 13\}$$
$$\{1, 27, 7, 5, -2\} \{6, 5, 3, 13\}$$
$$\{-2, \overset{\downarrow}{1}, 5, 7, 27\} \quad \{3, \overset{\downarrow}{5}, 6, 13\}$$
$$\{-2 \quad \quad \quad \}$$

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

## Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

$$\{1, 27, 7, 5, -2, 6, 5, 3, 13\}$$
$$\{1, 27, 7, 5, -2\} \{6, 5, 3, 13\}$$
$$\{-2, 1, \downarrow 5, 7, 27\} \quad \{3, \downarrow 5, 6, 13\}$$
$$\{-2, 1\}$$



# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3, 5 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3, 5, 5 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3, 5, 5, 6 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓ ↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3, 5, 5, 6, 7 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

- Split in two
- Sort the two halves independently
- Merge the two sorted halves into a single sorted array

{1, 27, 7, 5, -2, 6, 5, 3, 13}

{1, 27, 7, 5, -2} {6, 5, 3, 13}

↓  
{-2, 1, 5, 7, 27} {3, 5, 6, 13}

{-2, 1, 3, 5, 5, 6, 7, 13 }

# Exercise 8-1

- Website -> Course Materials -> ex8-1

## Merge Sort:

Given an array of values

{1, 27, 7, 5, -2, 6, 5, 3, 13}

- Split in two

{1, 27, 7, 5, -2} {6, 5, 3, 13}

- Sort the two halves independently

{-2, 1, 5, 7, 27} {3, 5, 6, 13}

- Merge the two sorted halves into a single sorted array

{-2, 1, 3, 5, 5, 6, 7, 13, 27}