



COMP 412  
FALL 2010

*Code Shape, Part II*  
*Addressing Arrays, Aggregates, & Strings*  
*Comp 412*

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# Last Lecture

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## Code Generation for Expressions

- Simple treewalk produces reasonable code
  - Execute most demanding subtree first
  - Generate function calls inline
  - Can implement treewalk explicitly, with an AG or ad hoc SDT ...
- Handle assignment as an operator
  - Insert conversions according to language-specific rules
  - If compile-time checking is impossible, check tags at runtime
  - Talked about reference counting as alternative to GC

## Today

- Addressing arrays and aggregates
- Next Time: Booleans & Relationals



# How does the compiler handle $A[i,j]$ ?

First, must agree on a storage scheme

## *Row-major order*

(most languages)

Lay out as a sequence of consecutive rows

Rightmost subscript varies fastest

$A[1,1]$ ,  $A[1,2]$ ,  $A[1,3]$ ,  $A[2,1]$ ,  $A[2,2]$ ,  $A[2,3]$

## *Column-major order*

(Fortran)

Lay out as a sequence of columns

Leftmost subscript varies fastest

$A[1,1]$ ,  $A[2,1]$ ,  $A[1,2]$ ,  $A[2,2]$ ,  $A[1,3]$ ,  $A[2,3]$

## *Indirection vectors*

(Java)

Vector of pointers to pointers to ... to values

Takes much more space, trades indirection for arithmetic

Not amenable to analysis



# Laying Out Arrays

## The Concept

A

|     |     |     |     |
|-----|-----|-----|-----|
| 1,1 | 1,2 | 1,3 | 1,4 |
| 2,1 | 2,2 | 2,3 | 2,4 |

These can have distinct & different cache behavior

### Row-major order

A

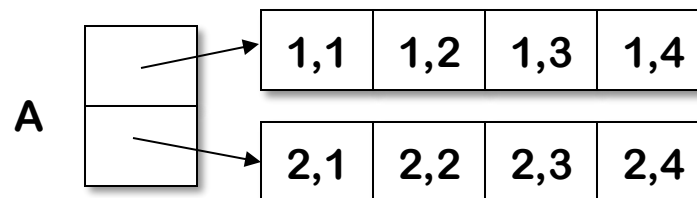
|     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 1,1 | 1,2 | 1,3 | 1,4 | 2,1 | 2,2 | 2,3 | 2,4 |
|-----|-----|-----|-----|-----|-----|-----|-----|

### Column-major order

A

|     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 1,1 | 2,1 | 1,2 | 2,2 | 1,3 | 2,3 | 1,4 | 2,4 |
|-----|-----|-----|-----|-----|-----|-----|-----|

### Indirection vectors





# Computing an Array Address

$A[i]$

- $@A + (i - \text{low}) \times \text{sizeof}(A[1])$
- In general:  $\text{base}(A) + (i - \text{low}) \times \text{sizeof}(A[1])$

Color Code:  
Invariant  
Varying

Depending on how  $A$  is declared,  $@A$  may be

- an offset from the ARP,
- an offset from some global label, or
- an arbitrary address.

The first two are compile time constants.



# Computing an Array Address

$A[i]$

- $@A + (i - \text{low}) \times \text{sizeof}(A[1])$
- In general:  $\text{base}(A) + (i - \text{low}) \times \text{sizeof}(A[1])$

$\text{int } A[1:10] \Rightarrow \text{low is 1}$   
Make low 0 for faster  
access (saves a - )

Almost always a power of  
2, known at compile-time  
 $\Rightarrow$  use a shift for speed



# Computing an Array Address

$A[i]$

- $@A + (i - \text{low}) \times \text{sizeof}(A[1])$
- In general:  $\text{base}(A) + (i - \text{low}) \times \text{sizeof}(A[1])$

What about  $A[i_1, i_2]$ ?

This stuff looks expensive!  
Lots of implicit +, -, x ops

*Row-major order, two dimensions*

$$@A + ((i_1 - \text{low}_1) \times (\text{high}_2 - \text{low}_2 + 1) + i_2 - \text{low}_2) \times \text{sizeof}(A[1])$$

*Column-major order, two dimensions*

$$@A + ((i_2 - \text{low}_2) \times (\text{high}_1 - \text{low}_1 + 1) + i_1 - \text{low}_1) \times \text{sizeof}(A[1])$$

*Indirection vectors, two dimensions*

$*(A[i_1])[i_2]$  — where  $A[i_1]$  is, itself, a 1-d array reference

e.g.,  $@A + (i_1 - \text{low}) \times \text{sizeof}(A[1])$



# Optimizing Address Calculation for $A[i,j]$

In row-major order

$$@A + (i - \text{low}_1) \times (\text{high}_2 - \text{low}_2 + 1) \times w + (j - \text{low}_2) \times w$$

Which can be factored into

$$\begin{aligned} & @A + i \times (\text{high}_2 - \text{low}_2 + 1) \times w + j \times w \\ & - (\text{low}_1 \times (\text{high}_2 - \text{low}_2 + 1) \times w) - (\text{low}_2 \times w) \end{aligned}$$

where  $w = \text{sizeof}(A[1,1])$

If  $\text{low}_i$ ,  $\text{high}_i$ , and  $w$  are known, the last term is a constant

Define  $@A_0$  as

$$@A - (\text{low}_1 \times (\text{high}_2 - \text{low}_2 + 1) \times w - \text{low}_2 \times w)$$

If  $@A$  is known,  $@A_0$  is a known constant.

And  $\text{len}_2$  as  $(\text{high}_2 - \text{low}_2 + 1)$

Then, the address expression becomes

$$@A_0 + (i \times \text{len}_2 + j) \times w$$

Compile-time constants

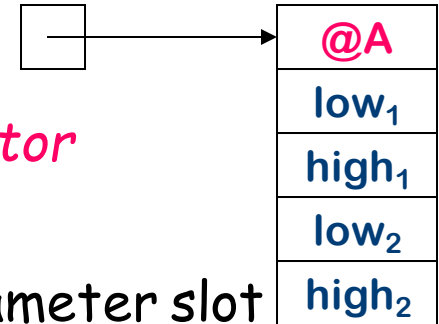




# Array References

## What about arrays as actual parameters?

Whole arrays, as call-by-reference parameters



- Need dimension information → build a *dope vector*
- Store the values in the calling sequence
- Pass the address of the dope vector in the parameter slot
- Generate complete address polynomial at each reference

Some improvement is possible

- Save **len<sub>i</sub>** and **low<sub>i</sub>** rather than **low<sub>i</sub>** and **high<sub>i</sub>**
- Pre-compute the fixed terms in prologue sequence

What about call-by-value?

- Most c-b-v languages pass arrays by reference
- This is a language design issue



# Array References

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What about `A[12]` as an actual parameter?

If corresponding parameter is a scalar, it's easy

- Pass the address or value, as needed
- Must know about both formal & actual parameter
- Language definition must force this interpretation

What if corresponding parameter is an array?

- Must know about both formal & actual parameter
- Meaning must be well-defined and understood
- Cross-procedural checking of conformability

⇒ Again, we're treading on language design issues



# Array References

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## What about variable-sized arrays?

Local arrays dimensioned by actual parameters

- Same set of problems as parameter arrays
  - Requires dope vectors (or equivalent)
    - dope vector at fixed offset in activation record
- Different access costs for textually similar references

This presents a lot of opportunity for a good optimizer

- Common subexpressions in the address polynomial
- Contents of dope vector are fixed during each activation
- Should be able to recover much of the lost ground

⇒ Handle them like parameter arrays



# Array Address Calculations

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Array address calculations are a major source of overhead

- Scientific applications make extensive use of arrays and array-like structures
  - Computational linear algebra, both dense & sparse
- Non-scientific applications use arrays, too
  - Representations of other data structures
    - *Hash tables, adjacency matrices, tables, structures, ...*

Array calculations tend iterate over arrays

- Loops execute more often than code outside loops
- Array address calculations inside loops make a huge difference in efficiency of many compiled applications

Reducing array address overhead has been a major focus of optimization since the 1950s.



# Example: Array Address Calculations in a Loop

A, B are declared as conformable  
floating-point arrays

```
DO J = 1, N
  A[I,J] = A[I,J] + B[I,J]
END DO
```

Naïve: Perform the address calculation twice

```
DO J = 1, N
  R1 = @A0 + (J × len1 + I) × sizeof(A[1,1])
  R2 = @B0 + (J × len1 + I) × sizeof(A[1,1])
  MEM(R1) = MEM(R1) + MEM(R2)
END DO
```

Code generated by a  
translator will almost  
certainly work this way.  
(treewalk code generator)  
Imagine a 5 point stencil:

$$A[I,J] = 0.2 * (A[I-1,J] + A[I,J] + A[I+1,J] \\ + A[I,J-1] + A[I,J+1])$$



## Example: Array Address Calculations in a Loop

```
DO J = 1, N
  A[I,J] = A[I,J] + B[I,J]
END DO
```

**More sophisticated:** Move common calculations out of loop

```
R1 = I × sizeof(A[1,1])
c = len1 × sizeof(A[1,1])  ! Compile-time constant
R2 = @A0 + R1
R3 = @B0 + R1
DO J = 1, N
  a = J × c
  R4 = R2 + a
  R5 = R3 + a
  MEM(R4) = MEM(R4) + MEM(R5)
END DO
```



## Example: Array Address Calculations in a Loop

```
DO J = 1, N  
  A[I,J] = A[I,J] + B[I,J]  
END DO
```

Very sophisticated: Convert multiply to add

```
R1 = I × sizeof(A[1,1])  
c = len1 × sizeof(A[1,1])  ! Compile-time constant  
R2 = @A0 + R1 ; R3 = @B0 + R1  
DO J = 1, N  
  R2 = R2 + c  
  R3 = R3 + c  
  MEM(R2) = MEM(R2) + MEM(R3)  
END DO
```

J is now bookkeeping  
A good compiler  
would rewrite the  
end-of-loop test to  
operate on R2 or R3  
(Linear function test  
replacement)



# Structures and Records

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Structures and records have two complications

Each declared structure has a set of fields

- Size and offset
- Compute base + offset for field
- Use size to choose load width and register width

Structures and records can have dimensions

- Arrays of structures
- Fields that are arrays or arrays of structures
- Use array address calculation techniques, as needed

Structures and records require compile-time support in the form of a table that maps field names to  $\langle \text{offset}, \text{size} \rangle$  tuples.





# Representing and Manipulating Strings

Character strings differ from scalars, arrays, & structures

- Fundamental unit is a character
  - Typical sizes are one or two bytes
  - Target ISA may (or may not) support character-size operations
- Set of supported operations on strings is limited
  - Assignment, length, concatenation, translation (?)
- Efficient string operations are complex on most RISC ISAs
  - Ties into representation, linkage convention, & source language

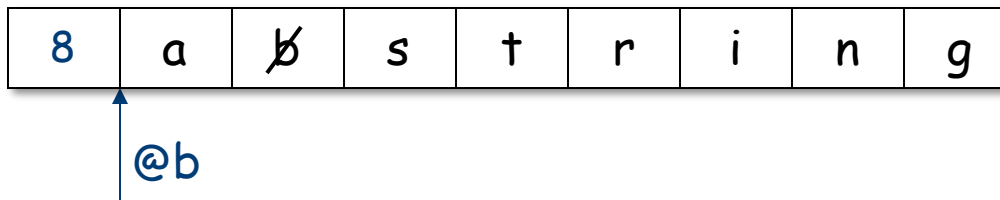
Subword data



# Representing and Manipulating Strings

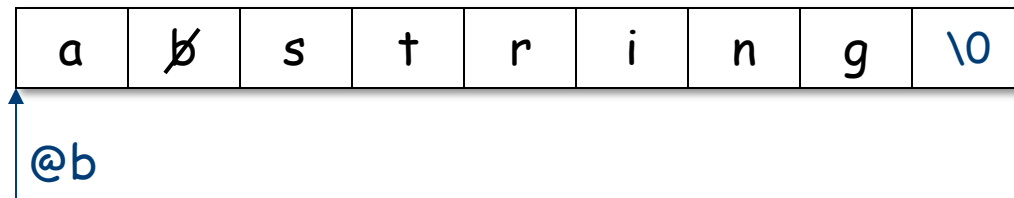
Two common representations

- Explicit length field



Length field may take more space than terminator

- Null termination



- Language design issue
  - Fixed-length versus varying-length strings *(1 or 2 length fields)*



# Representing and Manipulating Strings

Each representation as advantages and disadvantages

| Operation          | Explicit Length  | Null Termination               |
|--------------------|------------------|--------------------------------|
| Assignment         | Straightforward  | Straightforward                |
| Checked Assignment | Checking is easy | Must count length <sup>1</sup> |
| Length             | $O(1)$           | $O(n)$                         |
| Concatenation      | Must copy data   | Length + copy data             |

Unfortunately, null termination is almost considered normal

- Hangover from design of C
- Embedded in OS and API designs

<sup>1</sup> Checked assignment requires both a current length for the string and an allocated length for the buffer.



# Manipulating Strings

## Single character assignment

- With character operations
  - Compute address of rhs, load character
  - Compute address of lhs, store character
- With only word operations *(>1 char per word)*
  - Compute address of word containing rhs & load it
  - Move character to destination position within word
  - Compute address of word containing lhs & load it
  - Mask out current character & mask in new character
  - Store lhs word back into place



# Manipulating Strings

## Multiple character assignment

### Two strategies

1. Wrap a loop around the single character code, or
2. Work up to a word-aligned case, repeat whole word moves, and handle any partial-word end case

### With character operations

1. Easy to generate; inefficient use of resources
2. Harder to generate; better use of resources

Requires explicit code to check for buffer overflow ( $\Rightarrow$  length)

### With only word operations

1. Lots of complication to generate; inefficient at runtime, too
2. Fold complications into end case; reasonable efficiency

Source & destination aligned differently  
 $\Rightarrow$  much harder cases for word operations



# Manipulating Strings

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## Concatenation

- String concatenation is a length computation followed by a pair of whole-string assignments
  - Touches every character
- Exposes representation issues
  - Is string a descriptor that points to text?
  - Is string a buffer that holds the text?
  - Consider `a = b || c`
    - Compute `b || c` and assign descriptor to `a`?
    - Compute `b || c` into a temporary & copy it into `a`?
    - Compute `b || c` directly into `a`?
- What about a call to `free( b || c )`?



# Manipulating Strings

## Length Computation

- Representation determines cost
  - Explicit length turns `length(b)` into a memory reference
  - Null termination turns `length(b)` into a loop of memory references and arithmetic operations
- Length computation arises in other contexts
  - Whole-string or substring assignment
  - Checked assignment (buffer overflow)
  - Concatenation
  - Evaluating call-by-value actual parameter or concatenation as an actual parameter