

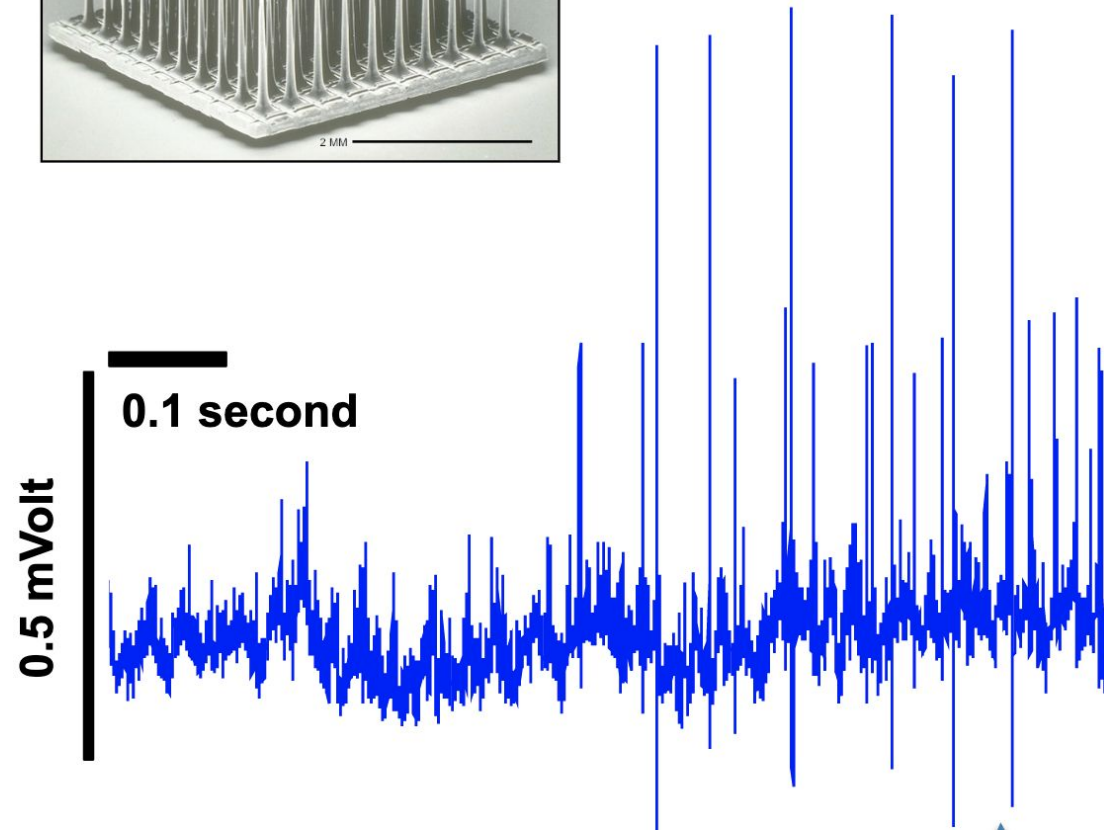
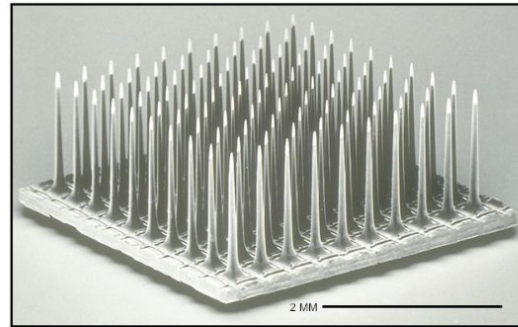
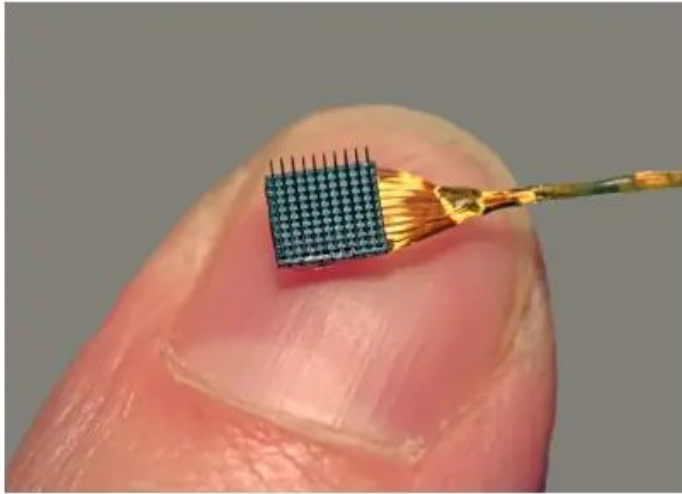
# Array Recording Simulation and Neuron Spike Clustering

Jesse Hurtado

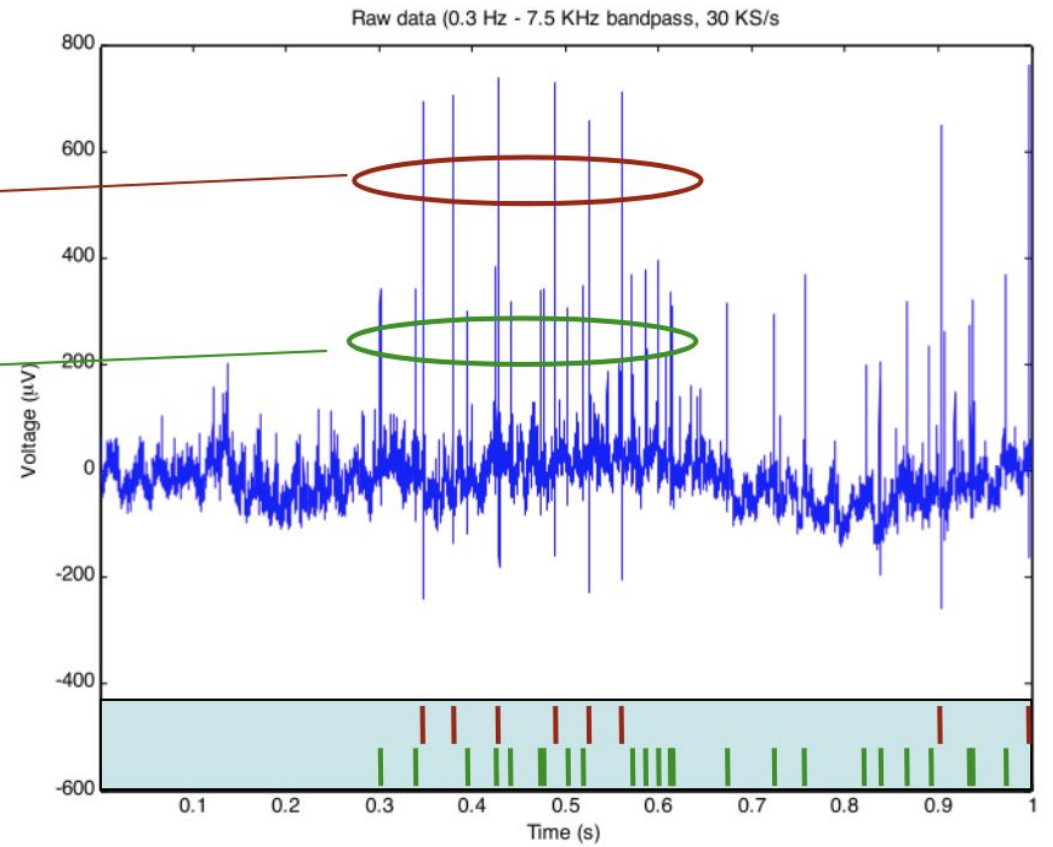
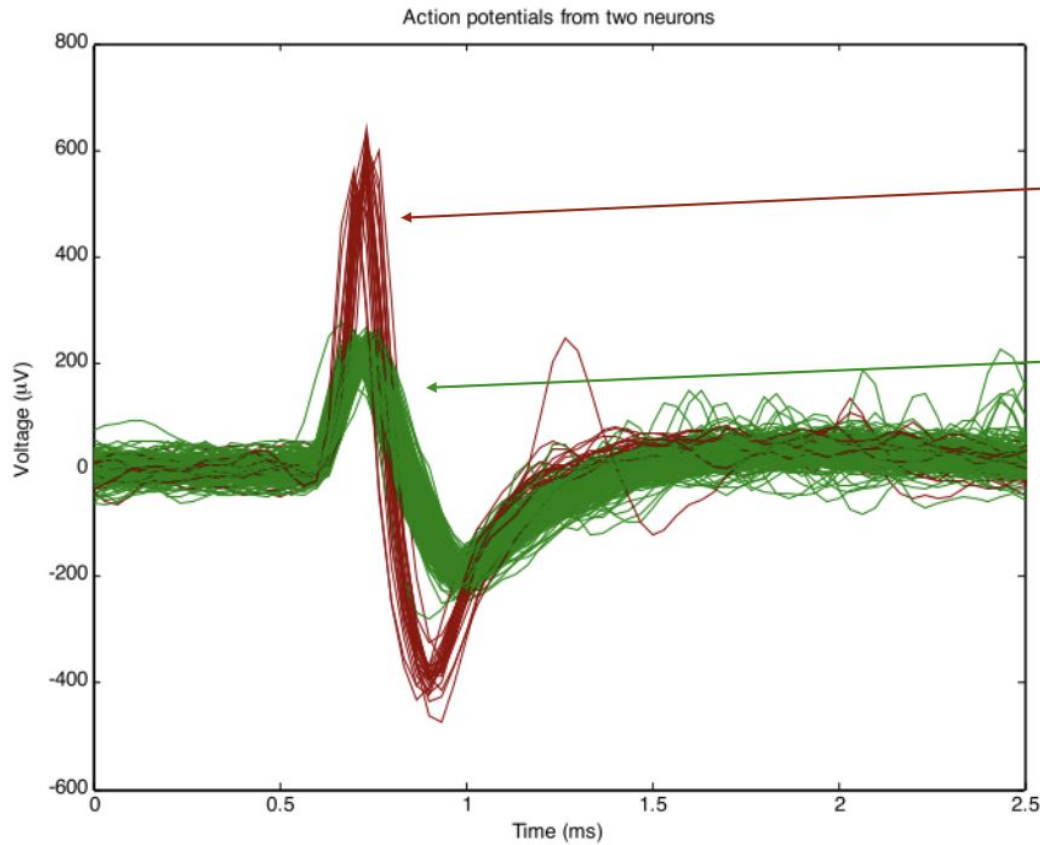
# INTRODUCTION

## Array Recordings, Aims, and Hypothesis

# Background



# Aims and Hypothesis



# METHODS

## Array Recording Simulation: 2 Methods

## Method 1: Simulating Extracellular Recording of 2 Hodgkin-Huxley Neurons

$$\begin{aligned}
 \frac{dm}{dt} &= \alpha_m(1-m) - \beta_m m \\
 \frac{dh}{dt} &= \alpha_h(1-h) - \beta_h h \\
 \frac{dn}{dt} &= \alpha_n(1-n) - \beta_n n
 \end{aligned}
 \quad
 \begin{aligned}
 C_m \frac{\partial V_m}{\partial t} &= G_L(E_L - V_m) + G_{Na} m^3 h (E_{Na} - V_m) + G_K n^4 (E_K - V_m) + \\
 I_{app} & \\
 V_m(i) &= V_m(i-1) + \partial V_m \partial t + NOISE
 \end{aligned}$$

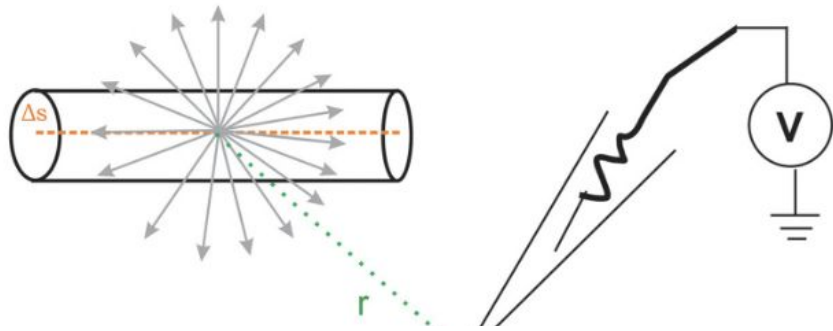
## Method 2: Simulating Extracellular Recording of 2 Connors-Stevens Neurons

$$\begin{aligned}
 \frac{dm}{dt} &= \alpha_m(1-m) - \beta_m m \\
 \frac{dh}{dt} &= \alpha_h(1-h) - \beta_h h \\
 \frac{dn}{dt} &= \alpha_n(1-n) - \beta_n n \\
 \frac{da}{dt} &= \frac{a_\infty - a}{\tau_a} \\
 \frac{db}{dt} &= \frac{b_\infty - b}{\tau_b}
 \end{aligned}
 \quad
 \begin{aligned}
 C_m \frac{dV_m}{dt} &= G_L(E_L - V_m) + G_{Na}^{(max)} m^3 h (E_{Na} - V_m) + G_K^{(max)} n^4 (E_K - V_m) \\
 &+ G_A^{(max)} a^3 b (E_A - V_m) + I_{app} \\
 V_m(i) &= V_m(i-1) + \partial V_m \partial t + NOISE
 \end{aligned}$$

# Point Source Approximation to Generate Voltage Traces

GOAL: Simulate the recorded activity of two neurons using PSA to generate individual voltage traces and sum them to make the final simulated recording

## Point Source Approximation



$$I_{transmembrane} = I_{ionic} + c_m \frac{\partial V_m}{\partial t}$$

$$\sigma \nabla \Phi = J_m$$

$\Phi$  = approximated extracellular potential

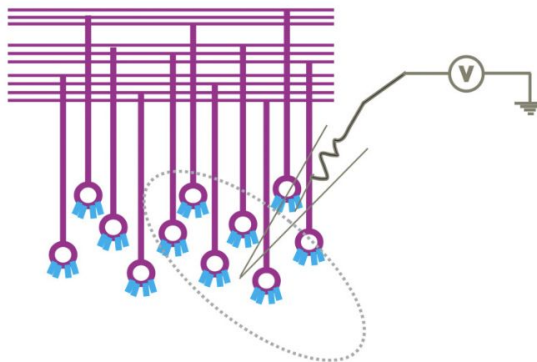
$\sigma$  = conductance of extracellular medium

$r$  = distance between neuron point source and recording electrode

This approximation is based on Ohm's Law

$$\Phi_{LFP} = \sum_{i=1}^{n_{sources}} \frac{I_i}{4\pi\sigma r_i}$$

Here,  $\Phi_{LFP}$  is the summed approximation of extracellular potentials from point sources, to be clear we are not generating LFP, but rather using a method to generate LFP to instead simulate the activity of two spiking neurons



$$J = \frac{I}{A}$$

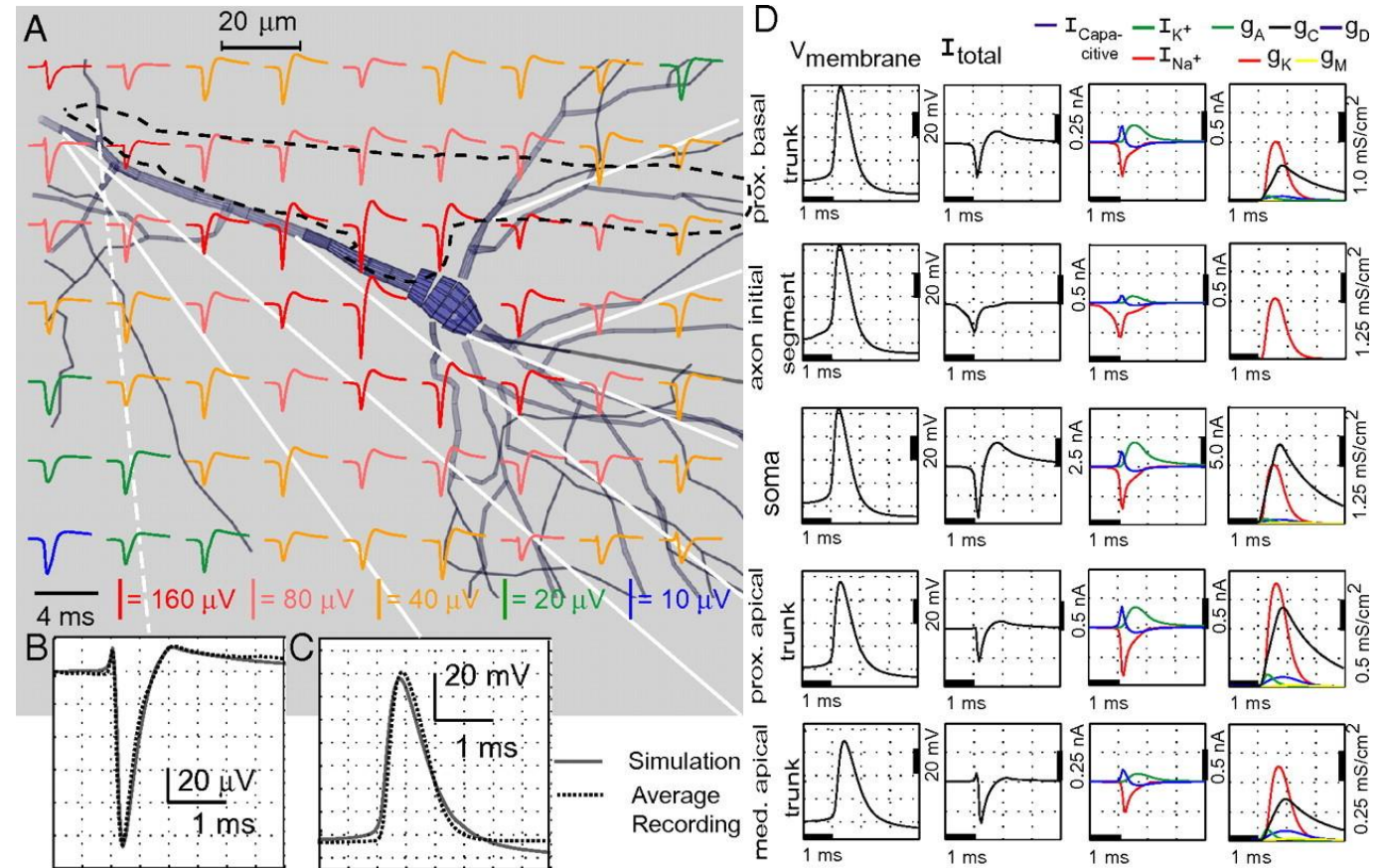
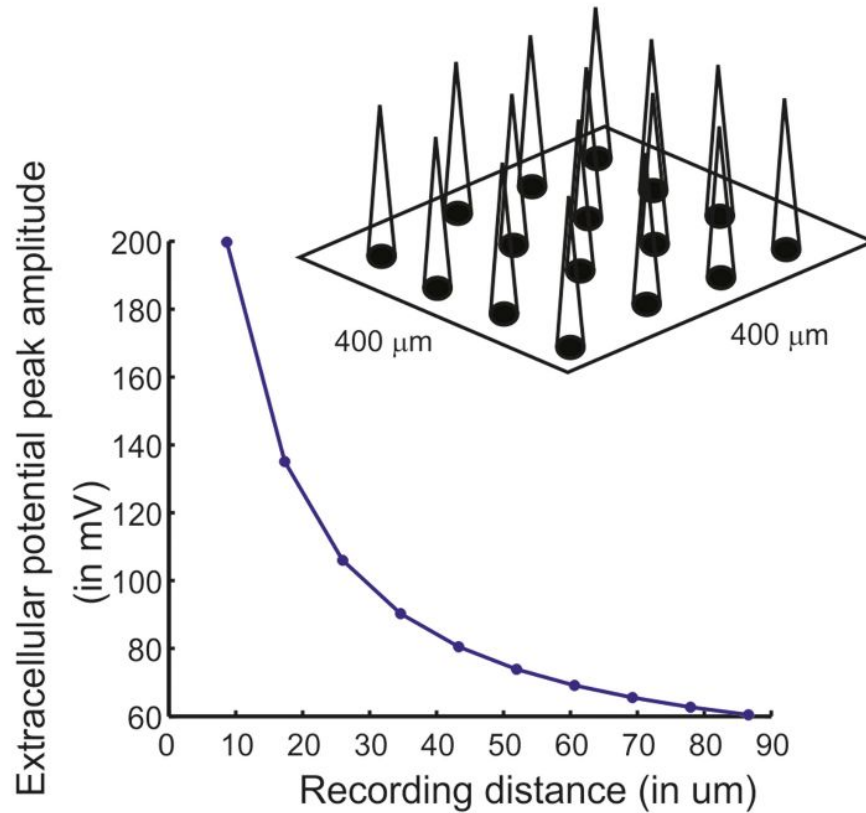
$$V = IR$$

$$\Phi = \frac{I}{4\pi\sigma r}$$

$$J = \sigma E$$



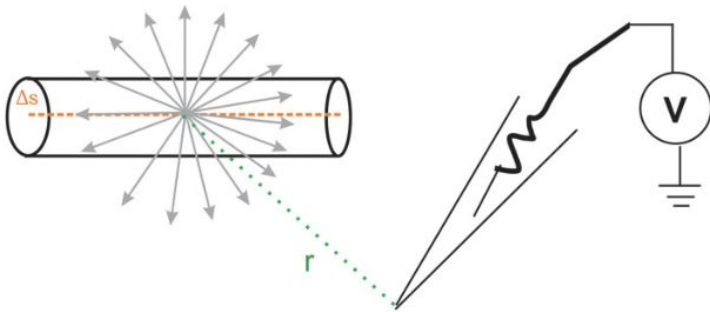
# Point Source Approximation





# Simulating 2 Neurons Using Point Source Approximation to Calculate Extracellular Potential

## Point Source Approximation



$$\Phi_{LFP} = \sum_{i=1}^{n\_sources} \frac{I_i}{4\pi\sigma r_i}$$

$$\Phi = \frac{I}{4\pi\sigma r}$$

$$V = IR$$

### Key assumptions:

1. Homogenous extracellular medium
2. Purely ohmic conductance through the medium
3. Current dissipates linearly as a function of  $r$
4. Treats  $I$  as a POINT SOURCE, and calculations can be done on a simple sum of all currents across the neuron acting as a point source
5. A linear relationship is assumed between the transmembrane current density and the electric potential at a distance  $r$ . ( Ohm's Law)

$$C_m \frac{\partial V_m}{\partial t} = G_L (E_L - V_m) + G_{Na} m^3 h (E_{Na} - V_m) + G_K n^4 (E_K - V_m) + I_{app}$$

$$C_m \frac{dV_m}{dt} = G_L (E_L - V_m) + G_{Na}^{(max)} m^3 h (E_{Na} - V_m) + G_K^{(max)} n^4 (E_K - V_m) + G_A^{(max)} a^3 b (E_A - V_m) + I_{app}$$

$$V_m(i) = V_m(i-1) + \partial V_m \partial t + NOISE$$

# The Model: PSA1(HH) and PSA2 (CS)

```
function [V] = PSA2(I,r,noise)
% Point Source Approximation based on Connors Stevens Model
% inputs are I in nA and r (distance from recoding electrode) in
% and noise

% Connors Stevens Parameters
Gmax_Na=12e-6;      % maximum sodium conductance (S)
Gmax_K=3.6e-6;      % maximum delayed rectifier conductance (S)
G_L=30e-9;          % leak conductance (S)
E_Na=45e-3;          % sodium reversal potential (V)
E_K=-82e-3;          % potassium reversal potential (V)
E_L=-60e-3;          % leak reversal potential (V)
Cm=100e-12;          % membrane capacitance (F)

Gmax_A=25e-9;        % A-current conductance (S)
E_A=-70e-3;          % A-current reversal potential (V)

% Initialize Vectors
dt=0.0002;           % time step (s)
tmax=1.1;            % max time value (s)
tvect=0:dt:tmax;      % time vector (s)
Vm=zeros(size(tvect)); % membrane potential Vm vector
Vm(1)=-0.065;         % set initial condition (V)
m=zeros(size(tvect)); % gating variable m vector
m(1)=0.05;            % set initial condition
h=zeros(size(tvect)); % gating variable h vector
h(1)=0.5;            % set initial condition
n=zeros(size(tvect)); % gating variable n vector
n(1)=0.35;            % set initial condition
a=zeros(size(tvect)); % gating variable a vector
a(1)=0.05;            % set initial condition
b=zeros(size(tvect)); % gating variable b vector
b(1)=0.05;            % set initial condition

%PSA Values
sigma = 0.43;         % Siemens / m^2 medium conductivity
R = r * 10^-7;        % in meters (one micron = 1e-6 meters)
w = noise;            % noise scalar
```

```
for i=2:length(tvect)      % integrate over time
    dVmdt=(1/Cm) * (G_L*(E_L-Vm(i-1)) + Gmax_Na*(m(i-1))^3*h(i-1)*(E_Na-Vm(i-1)) + Gmax_K*(n(i-1))^4*(E_K-Vm(i-1)) + Gmax_A*(a(i-1))^3*b(i-1)*(E_A-Vm(i-1)) + Iapp_vect(i-1)); %
    Vm(i)=Vm(i-1)+dVmdt*(i-1)*dt + randn()*w; % update Vm

    dmdt=((10^5)*(-Vm(i-1)-0.045))/(exp(100*(-Vm(i-1)-0.045))-1)*(1-m(i-1)) - (4*(10^3)*exp((-Vm(i-1)-0.070)/0.018))*m(i-1); % define m rate of change
    m(i)=m(i-1)+dmdt*dt; % update m

    dhdt=(70*exp(50*(-Vm(i-1)-0.070)))*(1-h(i-1)) - ((10^3)/(1+exp(100*(-Vm(i-1)-0.040))))*h(i-1); % define h rate of change
    h(i)=h(i-1)+dhdt*dt; % update h

    dndt=((10^4)*(-Vm(i-1)-0.060))/(exp(100*(-Vm(i-1)-0.060))-1)*(1-n(i-1)) - (125*exp((-Vm(i-1)-0.070)/0.08))*n(i-1); % define n rate of change
    n(i)=n(i-1)+dndt*dt; % update n

    dadt=((0.3)-a(i-1))/0.0005; % define a rate of change
    a(i)=a(i-1)+dadt*dt; % update a

    dbdt=((0.2)-b(i-1))/0.0005; % define b rate of change
    b(i)=b(i-1)+dbdt*dt; % update b

    Iionic(i-1) = (G_L*(E_L-Vm(i-1)) + Gmax_Na*(m(i-1))^3*h(i-1)*(E_Na-Vm(i-1)) + Gmax_K*(n(i-1))^4*(E_K-Vm(i-1)) + Gmax_A*(a(i-1))^3*b(i-1)*(E_A-Vm(i-1)));
    Im(i-1) = (dVmdt(i-1) * Cm) + Iionic(i-1); % calculate Im
    theta(i-1) = Im(i-1)/(4*pi*sigma*R); %calculate PSA potential
end
```

Features of the functions:

1. PSA1 runs point source approximation based on Hodgkin Huxley model
2. PSA2 runs point source approximation based on Connors Stevens model

# The Model: PSA1 and PSA2

```
% SIMULATE UTAH RECORDING OF TWO CONNORS STEVENS NEURONS
clear

% Time Vector
dt=0.00002;      % time step (s)
tmax=1.1;        % max time value 1 second (s)
tvect= 0:dt:tmax; % time vector, a second

% LFP Noise Vector
hi = 16;          % noise scalar
LFP_vec = randn(1, length(tvect)); % empty LFP vector
LFP_vec = LFP_vec*hi; % scaled LFP vector

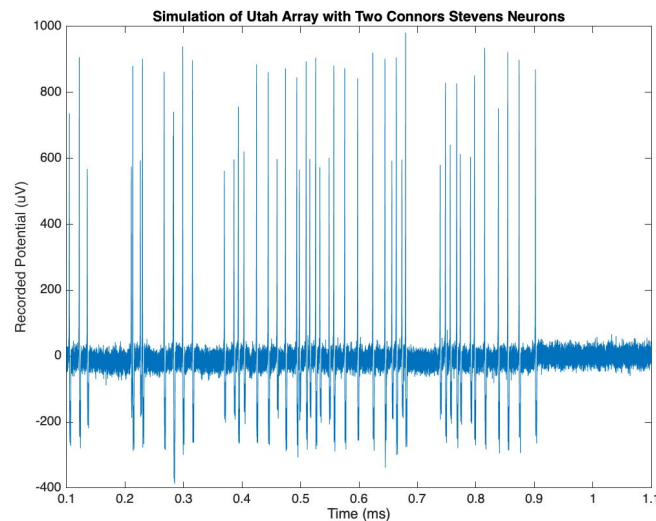
V1 = PSA2(5,10,0.0002); % run PSA2 (Connors Stevens) simulation for a neuron 7 microns away with a 5 nA applied current with noise.
V2 = PSA2(5,15,0.0002); % run PSA2 (Connors Stevens) simulation for a neuron 15 microns away with a 5 nA applied current with noise.

V3 = V1+V2;        % Sum the voltage trace outputs

V3 = V3*100 + LFP_vec; % Add LFP noise, final trace

start_time = 0.1; % Start time to remove (in seconds)
start_index = find(tvect >= start_time, 1); % Find the index corresponding to the start time
V3 = V3(start_index:end);
tvect = tvect(start_index:end); % Remove the time values before the start index

%Plot
figure;
plot(tvect,V3);
title('Simulation of Utah Array with Two Connors Stevens Neurons')
xlabel('Time (ms)');
ylabel('Recorded Potential (uV)');
```



```
% SIMULATE UTAH RECORDING OF TWO HH NEURONS
% Time Vector
dt=0.00002;      % time step (s)
tmax=1.1;        % max time value 1 second (s)
tvect= 0:dt:tmax; % time vector, a second

% LFP Noise Vector
hi = 16;          % noise scalar
LFP_vec = randn(1, length(tvect)); % empty LFP vector
LFP_vec = LFP_vec*hi; % scaled LFP vector

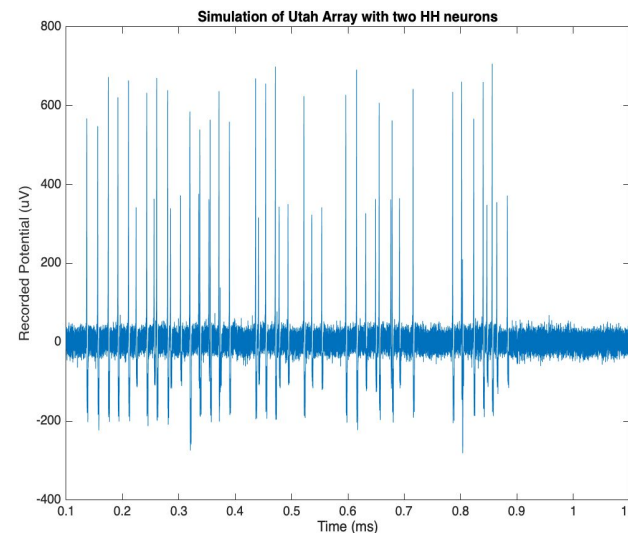
T1 = PSA1(5,7,0.0002); % Simulate the PSA of a neuron with applied current of 5 nA, 7 microns away from recording electrode, with added noise
T2 = PSA1(5,13,0.0002); % Simulate the PSA of a neuron with applied current of 5 nA, 13 microns away from recording electrode, with added noise
T3 = T1+T2;           % Sum the voltage trace outputs

T3 = T3*100 + LFP_vec; % Add LFP noise, final trace

% This is done to remove artifacts present at the time of the start of the
% pulse

start_time = 0.1; % Start time to remove (in seconds)
start_index = find(tvect >= start_time, 1); % Find the index corresponding to the start time
T3 = T3(start_index:end);
tvect = tvect(start_index:end); % Remove the time values before the start index

%Plot
figure;
plot(tvect,T3);
title('Simulation of Utah Array with two HH neurons')
xlabel('Time (ms)');
ylabel('Recorded Potential (uV)');
hold off
```



Features of the functions:

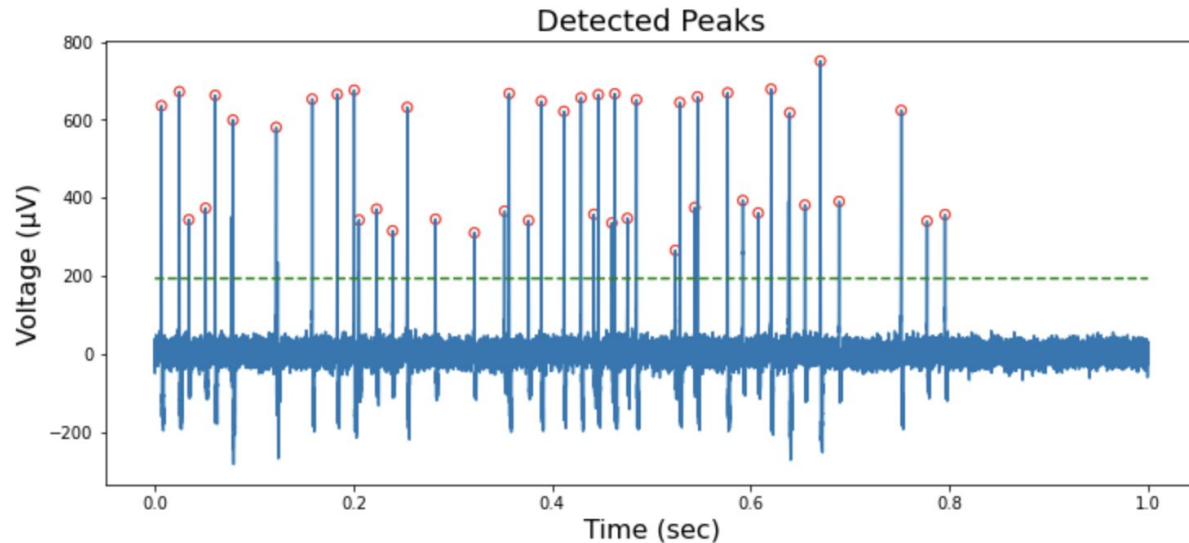
1. Initialize Parameters
2. Generate Step Pulse
3. Forward Euler's Method
4. Calculate PSA
5. Plot Traces

# METHODS

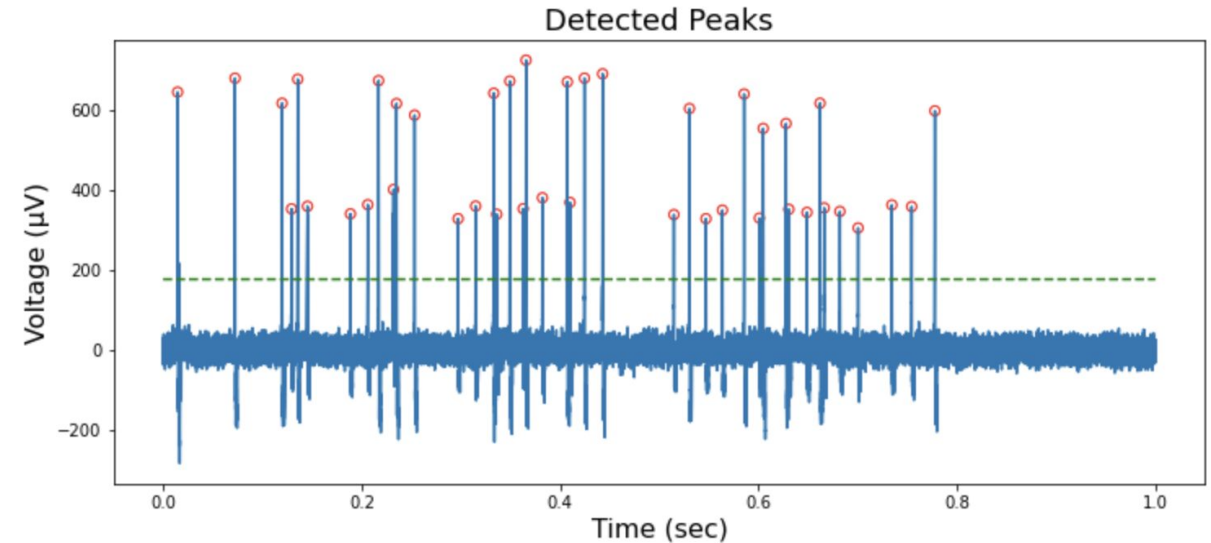
## Neuron Spike Clustering

# Spike Detection: Height Threshold of $3 \times \text{RMS}$ and Time Threshold of 2 ms

## Hodgkin-Huxley Model

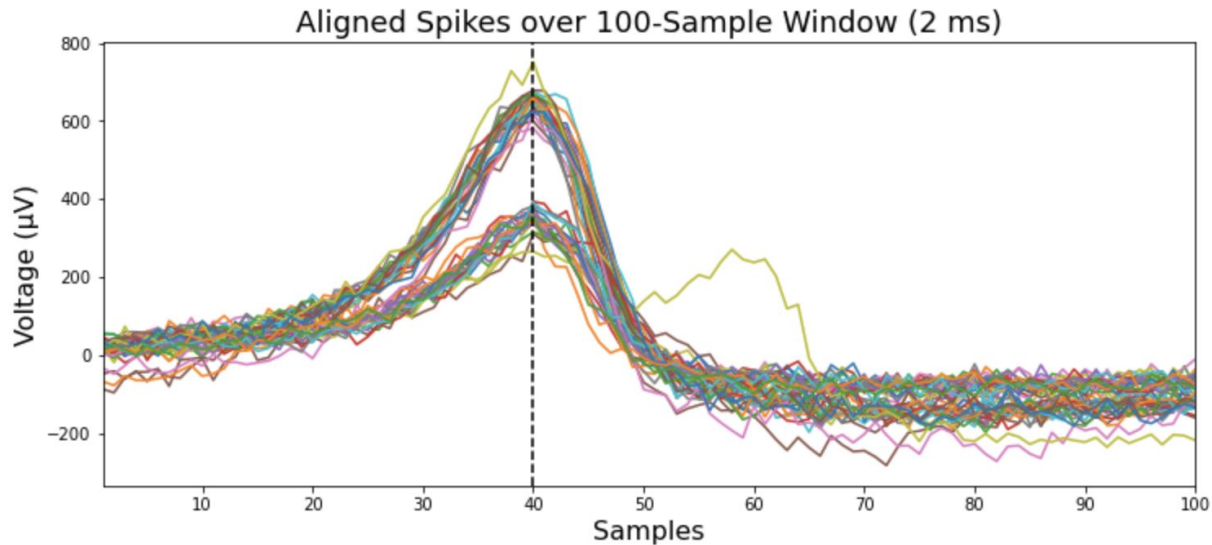


## Connor-Stevens Model

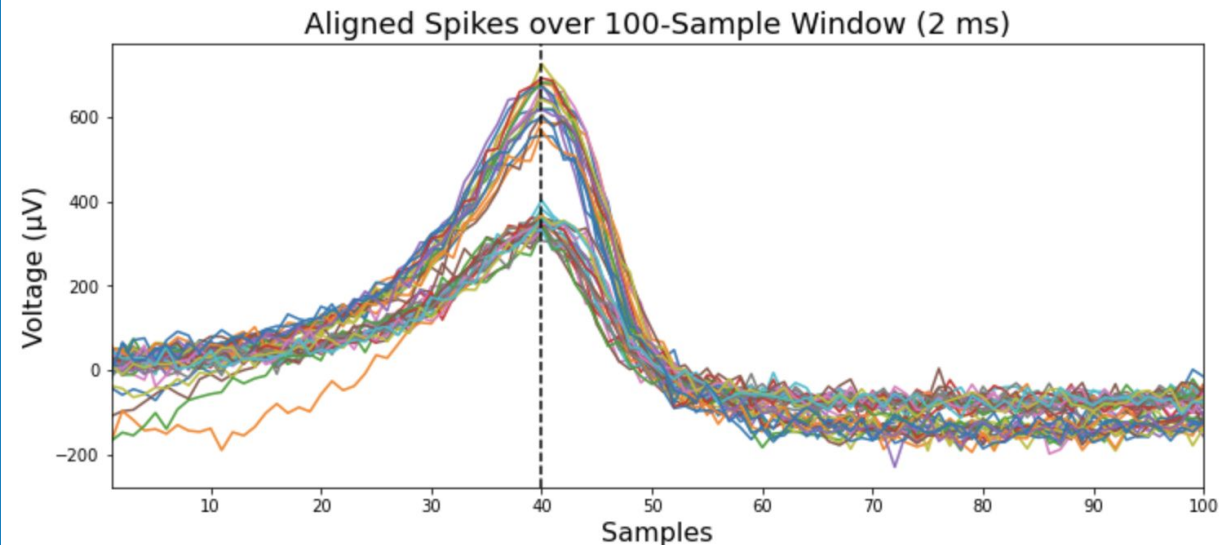


# Spike Alignment: 2-ms Segments with Centered around the Detected Peak

## Hodgkin-Huxley Model



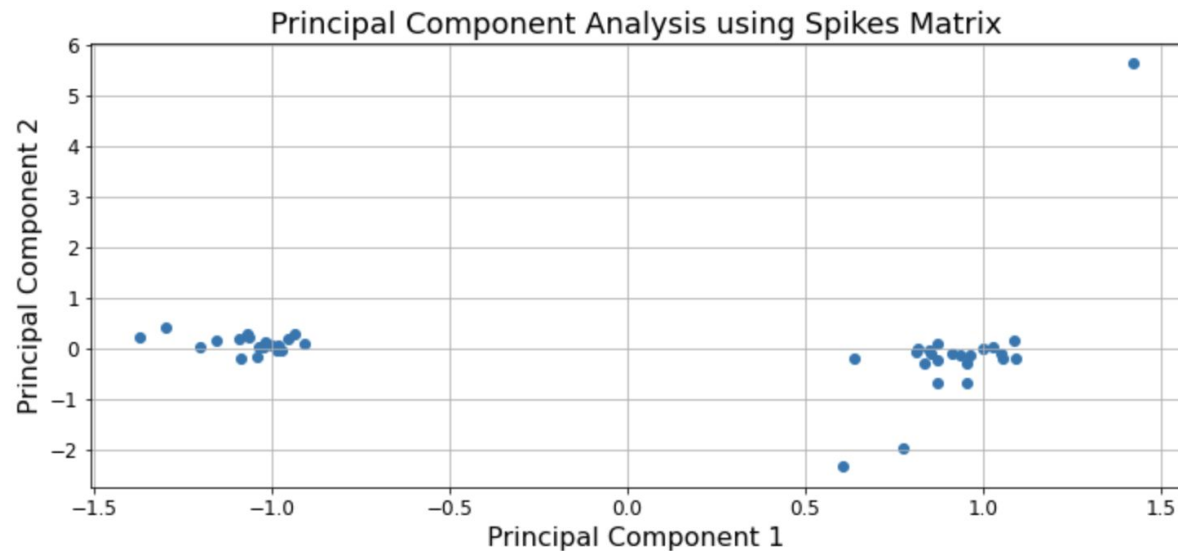
## Connor-Stevens Model



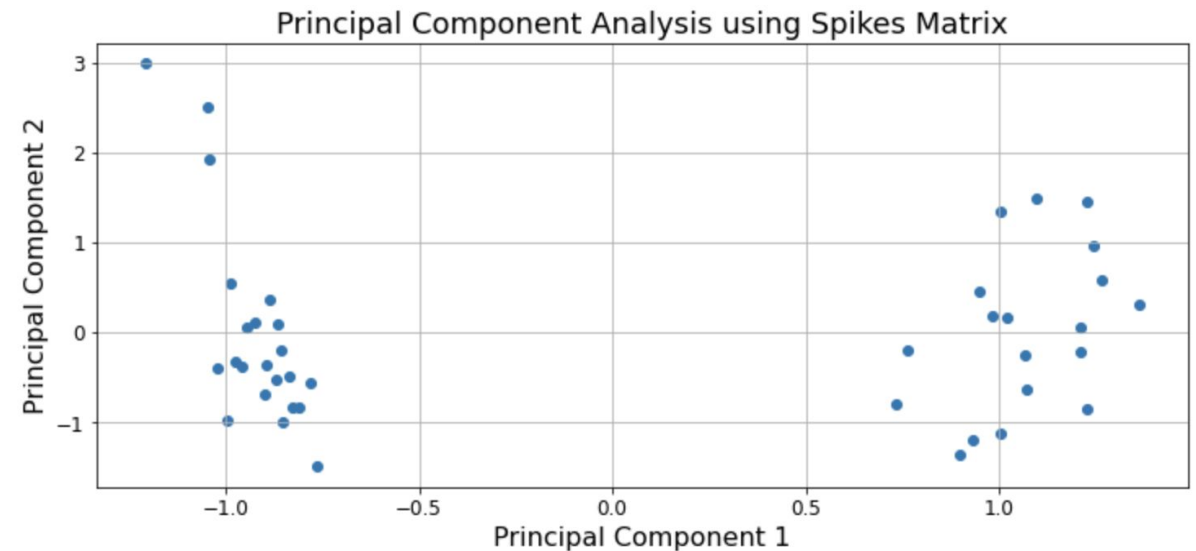


# Feature Extraction: 2 First Principal Components

Hodgkin-Huxley Model



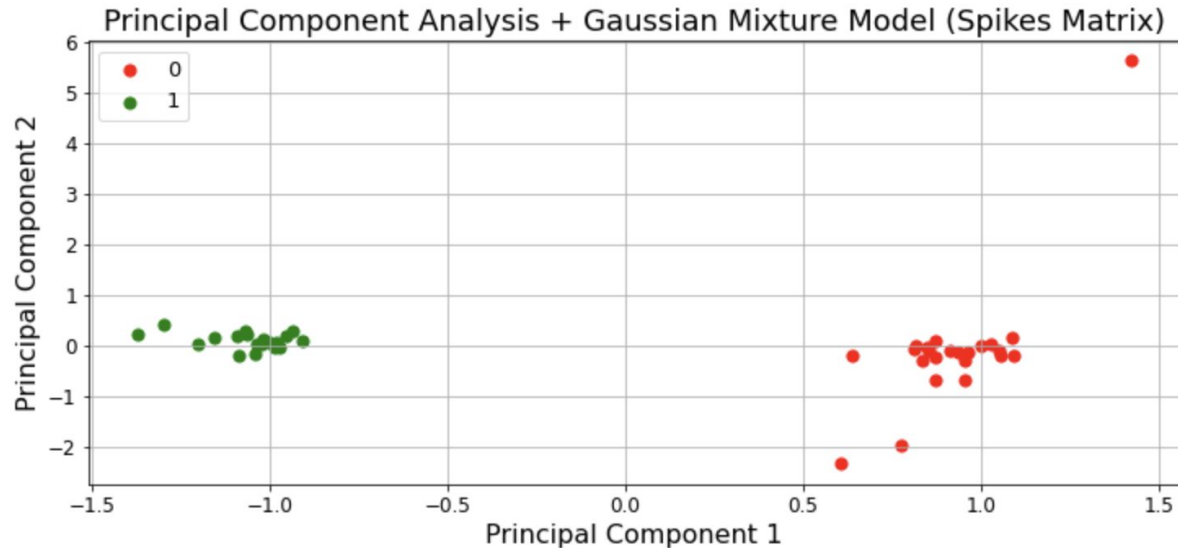
Connor-Stevens Model



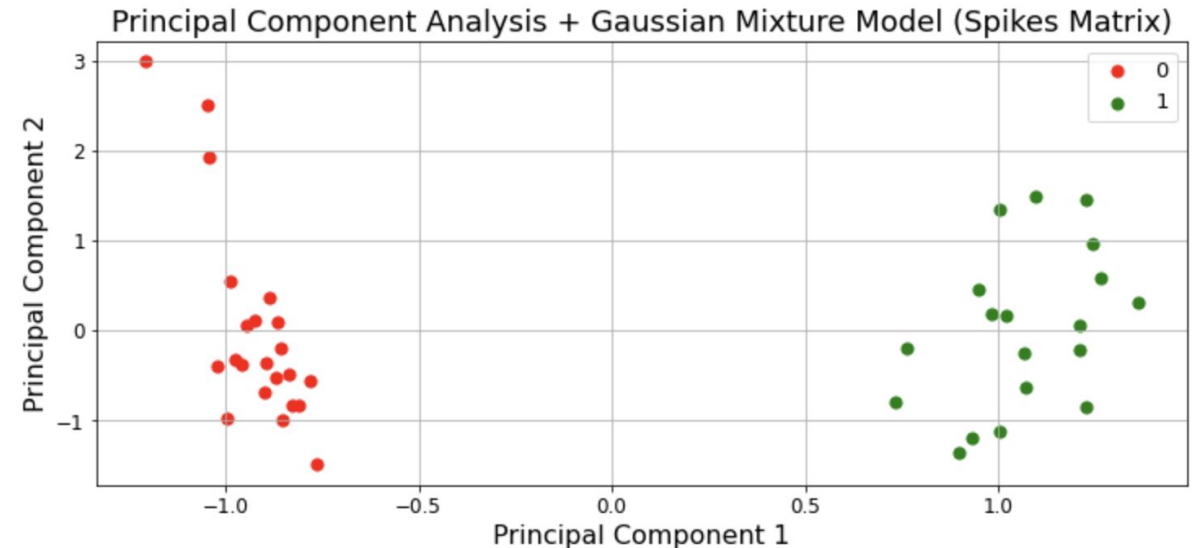


# Spike Classification: Gaussian Mixture Model (GMM)

## Hodgkin-Huxley Model

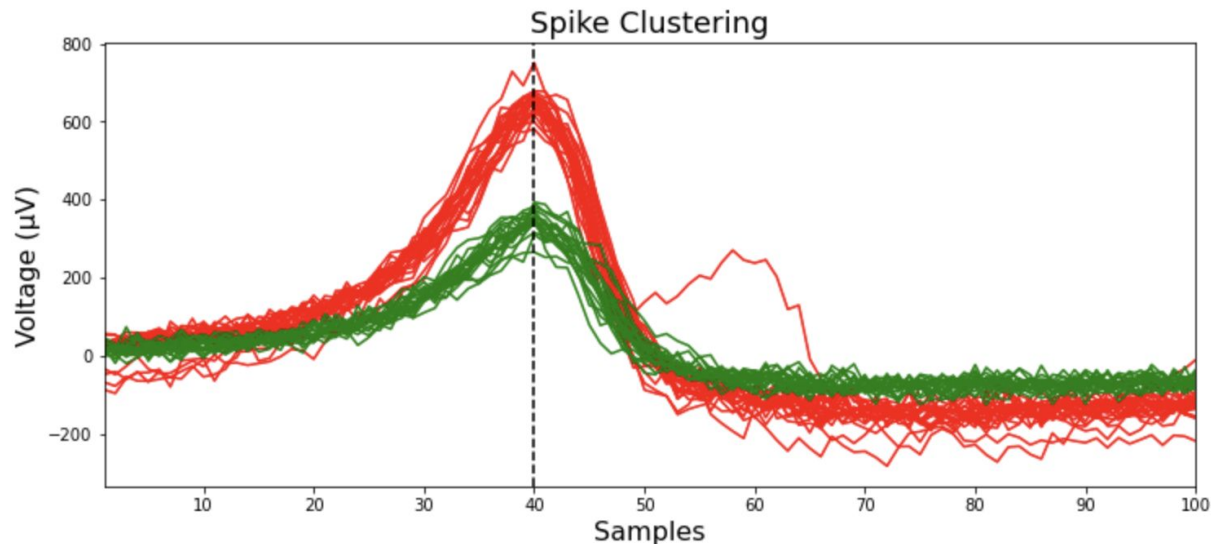


## Connor-Stevens Model

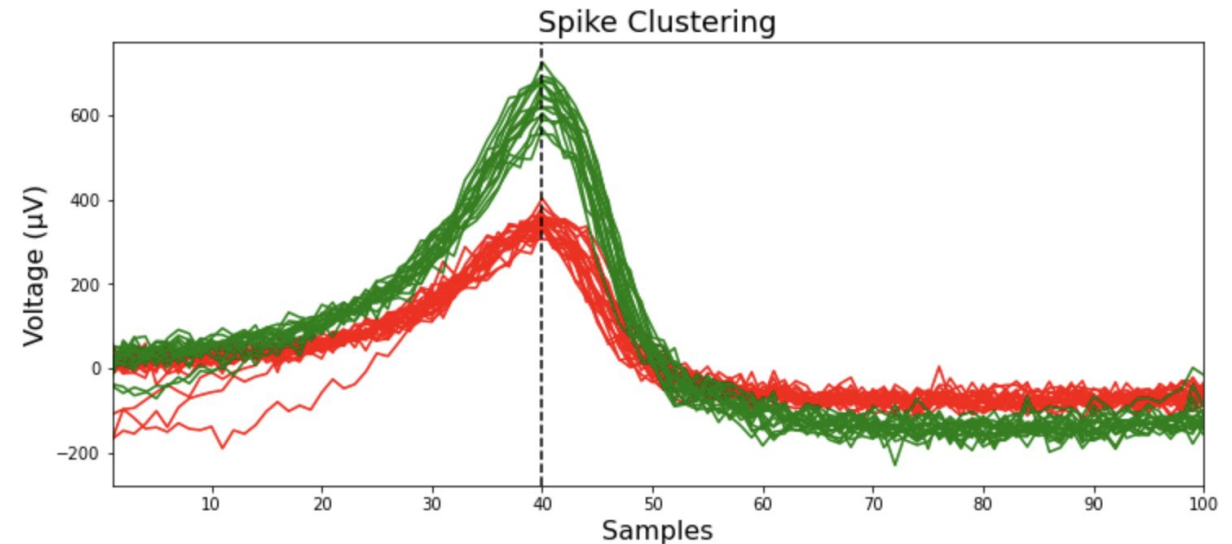


# Spike Clustering: 2-ms Spike Segments with GMM Labels

## Hodgkin-Huxley Model

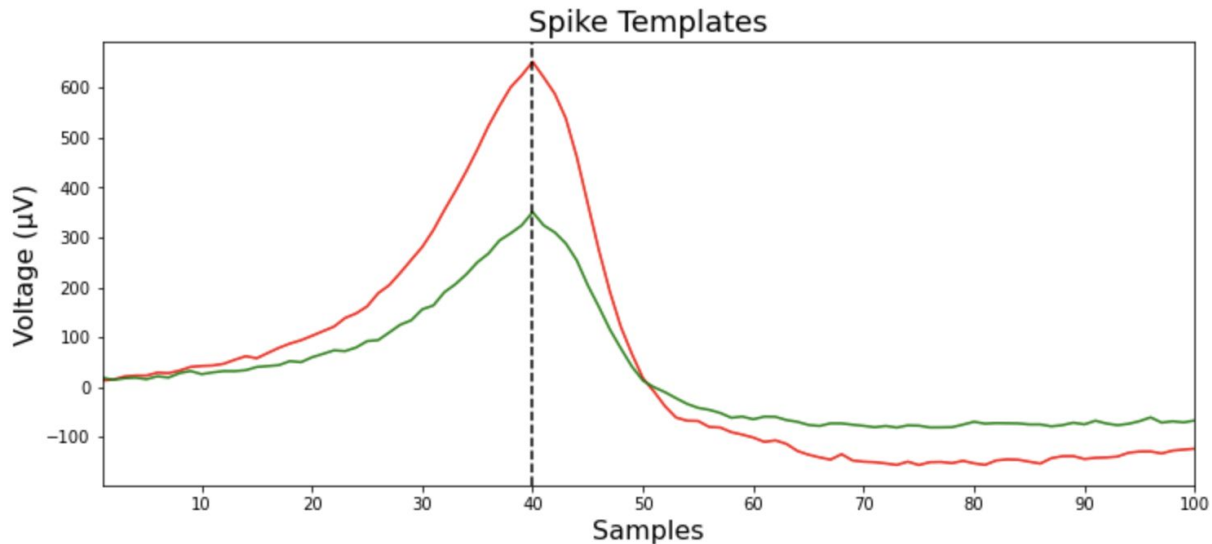


## Connor-Stevens Model

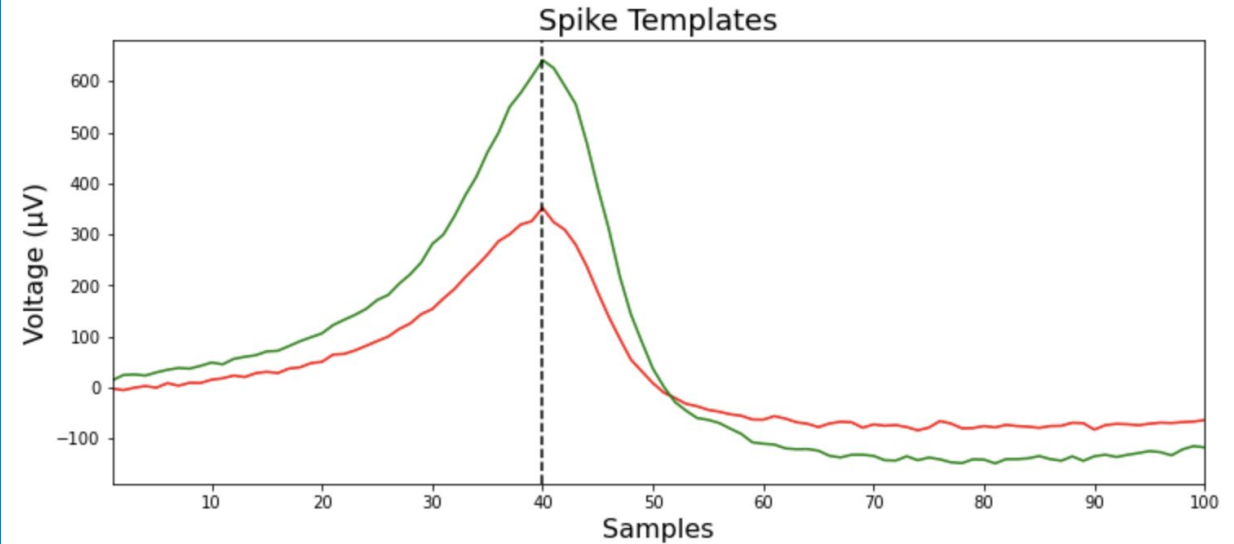


# Spike Templates: 2-ms Mean of GMM Labeled Spike Segments

## Hodgkin-Huxley Model

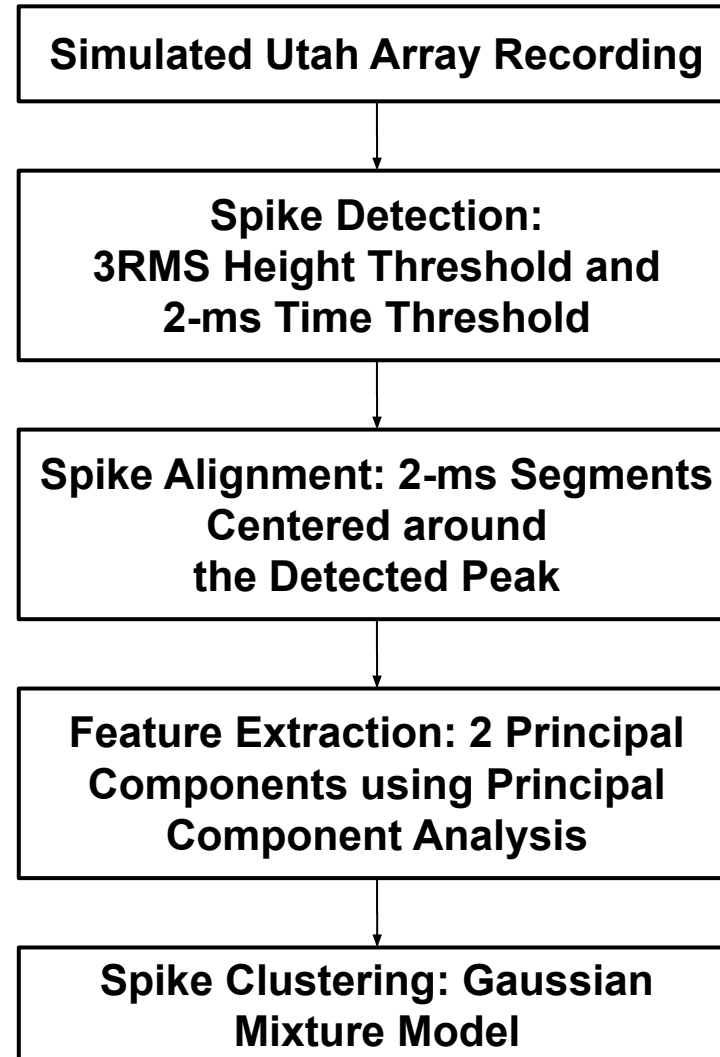


## Connor-Stevens Model



# Flowchart of Neuron Spike Sorting Model

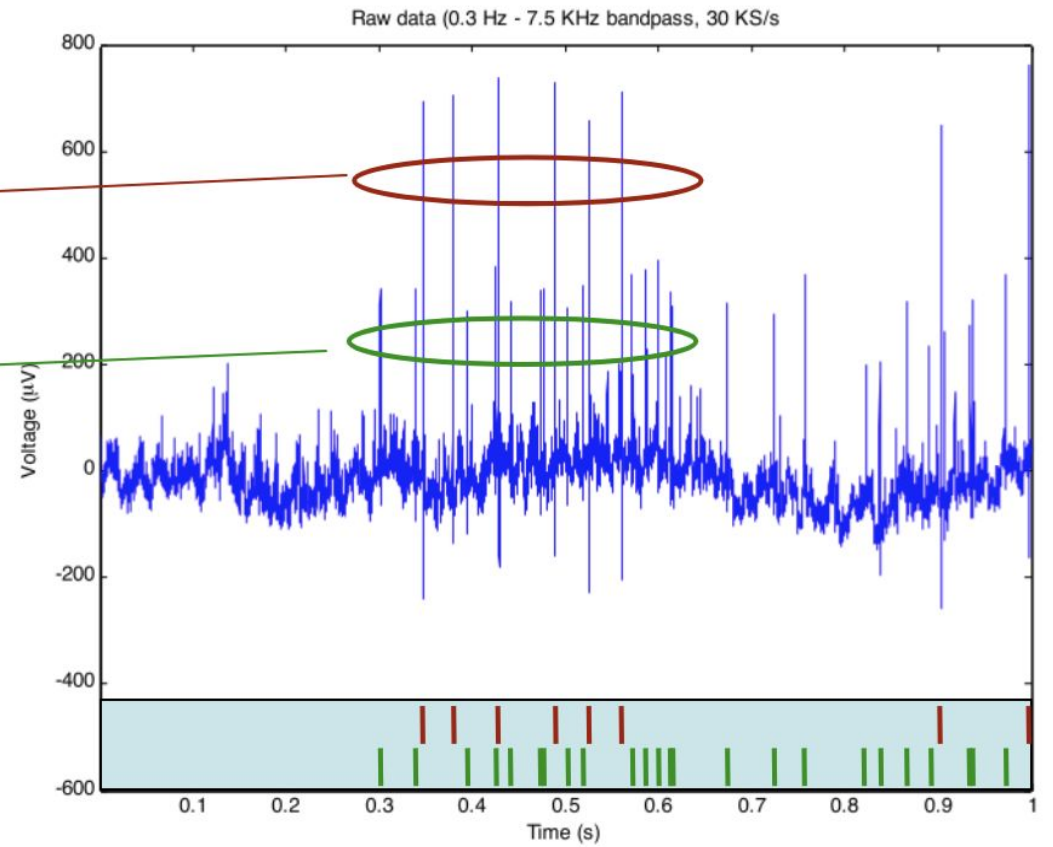
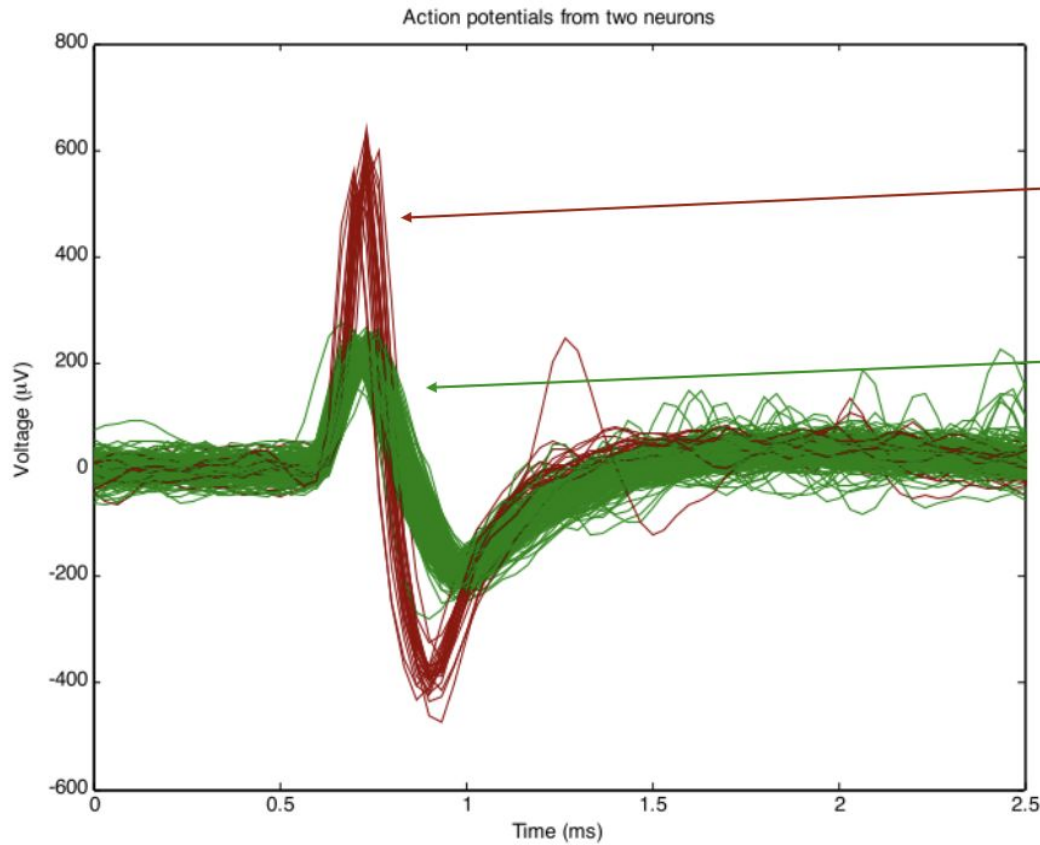
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# RESULTS

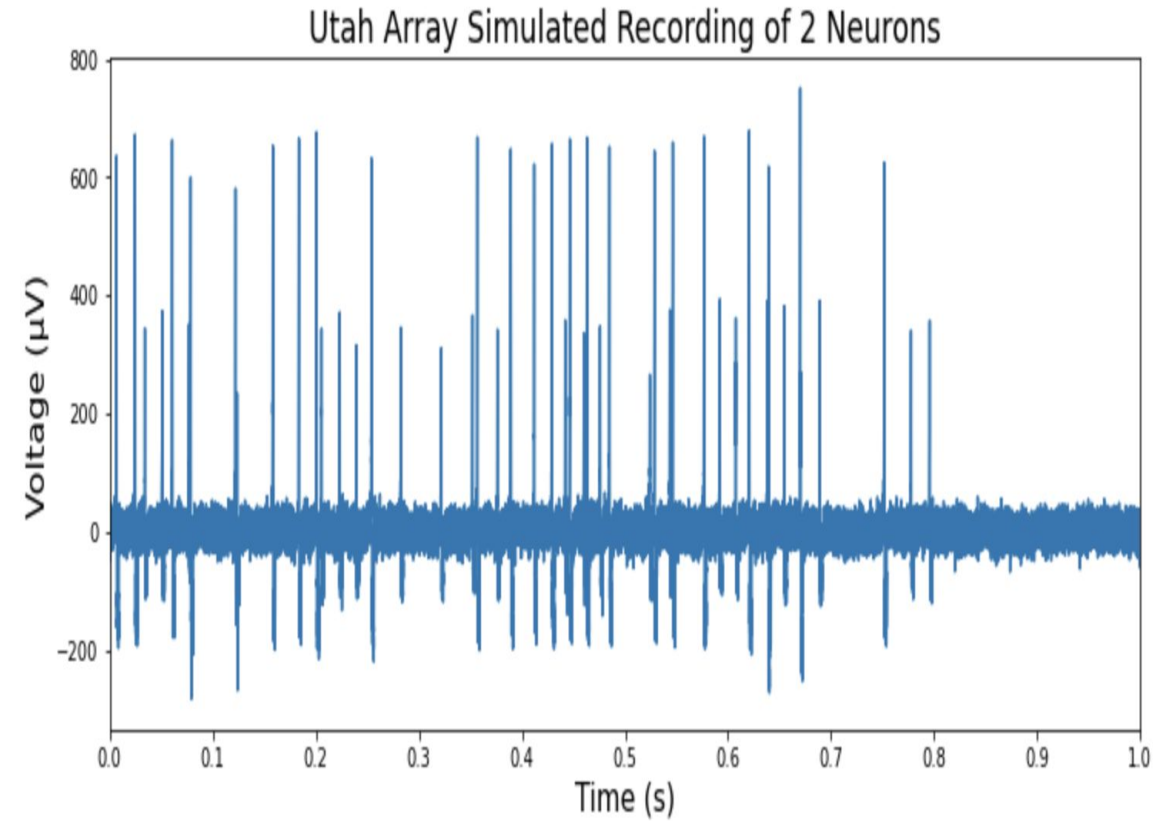
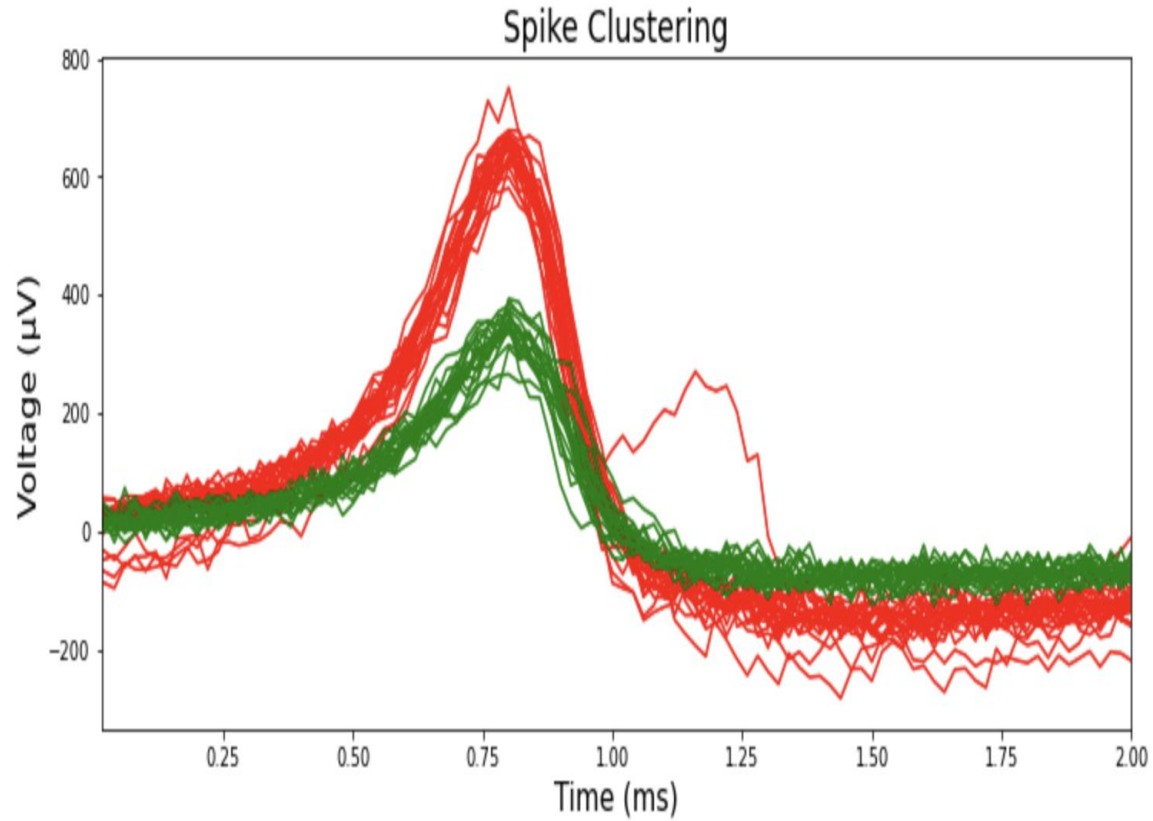
## Utah Array Recordings

# Aim: Replicate this



# Look at this!

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# CONCLUSION

## It is possible!

To make simulation even more realistic, we can add several neurons at a very large distance from the electrode. The goal is to make their action potentials small enough that they would only contribute to the LFP baseline to make it variable rather than constant at 0.

# References

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- Toosi, R., Akhaee, M. A., & Dehaqani, M.-R. A. (2021). An automatic spike sorting algorithm based on adaptive spike detection and a mixture of skew-T distributions. Scientific Reports, 11(1). <https://doi.org/10.1038/s41598-021-93088-w>
- Reaz, M. B., et al. “Techniques of EEG Signal Analysis: Detection, Processing, Classification and Applications.” Biological Procedures Online, vol. 8, no. 1, 2006, pp. 11–35., <https://doi.org/10.1251/bpo115>.
- Yang, Zhi, et al. “1/F Neural Noise Reduction and Spike Feature Extraction Using a Subset of Informative Samples.” Annals of Biomedical Engineering, vol. 39, no. 4, 2010, pp. 1264–1277., <https://doi.org/10.1007/s10439-010-0201-5>
- Gold, C., Henze, D. A., Koch, C., Buzsáki, G., and Buzsaki, G. (2006). On the origin of the extracellular action potential waveform: a modeling study. J. Neurophysiol. 95, 3113–3128. <https://journals.physiology.org/doi/full/10.1152/jn.00979.2005>
- Parasuram H, Nair B, D'Angelo E, Hines M, Naldi G and Diwakar S (2016) Computational Modeling of Single Neuron Extracellular Electric Potentials and Network Local Field Potentials using LFPsim. Front. Comput. Neurosci. 10:65. <https://www.frontiersin.org/articles/10.3389/fncom.2016.00065/full#B22>