

Point Source Approximation For Simulating Extracellular Recording

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% Written by Jesse Hurtado
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% Simulation of two neurons firing in proximity to an electrode array.  
% This simulation includes two functions, PSA1 and PSA2, point source  
approximation 1 and 2.
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```
% PSA1 will simulate an EXTRACELLULAR POTENTIAL RECORDING using a POINT  
% SOURCE APPROXIMATION based on the Hodgkin-Huxley model, which assumes the  
current source acts as a point and  
% the potential at a distance  $r$  away from the source can be approximated  
% using a simple linear equation based on Koch, Buzaki, and Gold Point  
Source Approximation.
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```
% This PSA assumes the extracellular medium  
% is homogeneous in conductivity. PSA takes three arguments, 1 = current  
% amplitude (in pA) stimulating the distant neuron, 2 = distance from the  
% recording electrode in microns, and 3 = noise that will cause variable  
% spiking.
```

```
% PSA2 will simulate EXTRACELLULAR POTENTIAL RECORDING using a POINT SOURCE  
% APPROXIMATION (PSA) based on the Connors Stevens model.
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```
% Increasing the distance  $r$  (microns) from the electrode will, as proposed,  
% decrease the recorded extracellular potential, and the amplitude of the  
% overall trace changes as a function of  $r$ . This can be demonstrated by  
% varying the parameter  $r$ .
```

```
% Using PSA, we can simulate extracellular  
% recording, and sum their voltage traces to produce a simulated recording  
that models what a Utah array recording electrode might detect.
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```
% This simulation works best with a slight difference in applied currents  
% as the frequency of spikes will be slightly out of phase and more  
individual spikes  
% will appear in the summed trace.
```

```
% Finally, noise can be added to the trace to simulate LFP. Adding noise  
% this way does not affect excitability of either neurons.
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% Each time the simulation is run, a unique trace will be produced.
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% PSA can be adapted to other dynamic models
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```
% SIMULATE UTAH RECORDING OF TWO HH NEURONS
```

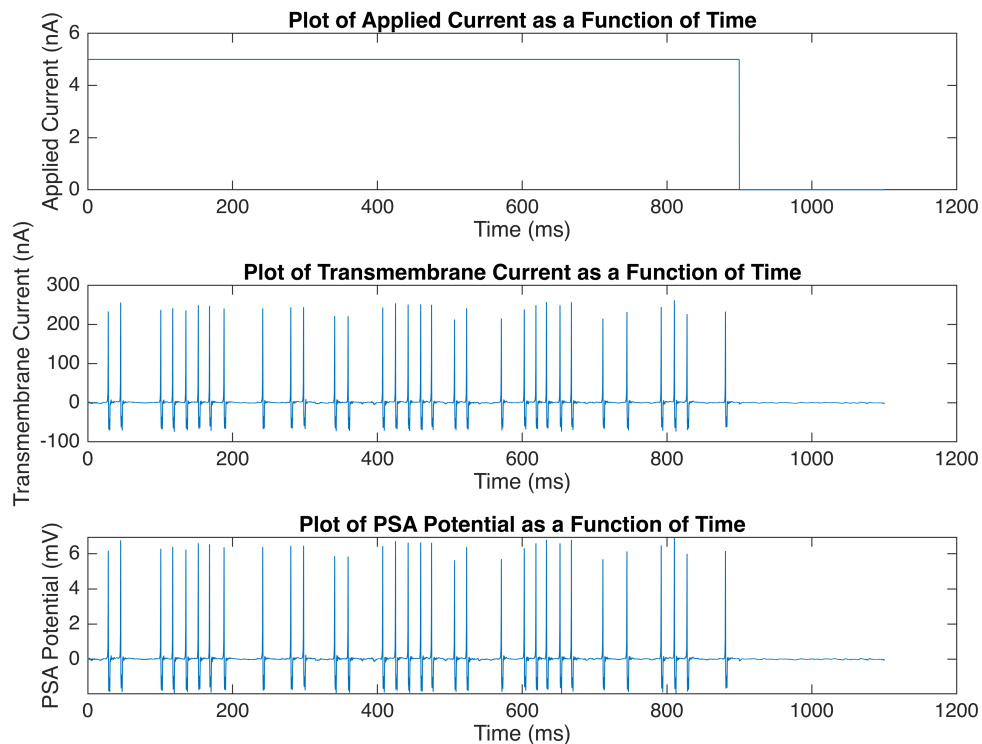
% Time Vector

```
dt=0.00002;           % time step (s)
tmax=1.1;              % max time value 1 second (s)
tvect= 0:dt:tmax;      % time vector, a second
```

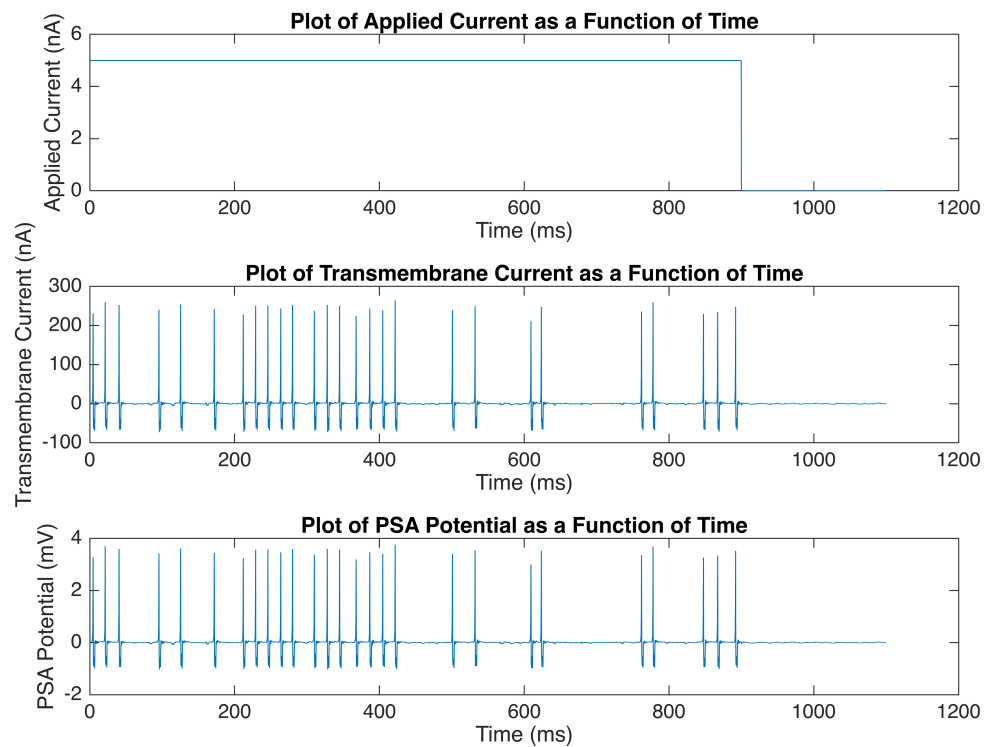
% LFP Noise Vector

```
hi = 16;
LFP_vec = randn(1, length(tvect));
LFP_vec = LFP_vec*hi;
```

```
T1 = PSA1(5,7,0.0002); % Simulate the PSA of a neuron with applied current
of 5 nA, 7 microns away from recording electrode, with added noise to vary
spiking.
```



```
T2 = PSA1(5,13,0.0002); % Simulate the PSA of a neuron with applied current
of 5 nA, 13 microns away from recording electrode, with added noise.
```



```

T3 = T1+T2; % Sum the voltage trace outputs

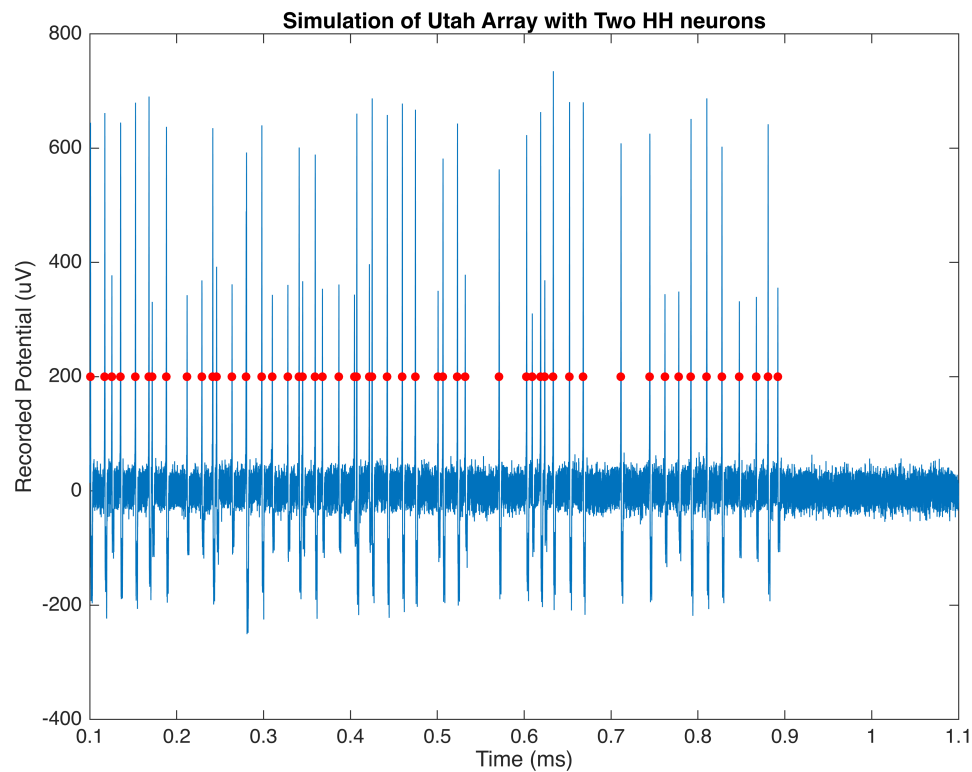
T3 = T3*100 + LFP_vec; % Add LFP noise, final trace

% This is done to remove artifacts present at the time of the start of the
% pulse

start_time = 0.1; % Start time to remove (in seconds)
start_index = find(tvect >= start_time, 1); % Find the index corresponding
to the start time
T3 = T3(start_index:end);
tvect = tvect(start_index:end); % Remove the time values
before the start index
spikeTimes = detectSpikes(T3,tvect,200); % Detect spikes

%Plot
figure;
plot(tvect,T3);
hold on
plot(spikeTimes, 200*ones(size(spikeTimes)), 'r.', 'MarkerSize', 15);
title('Simulation of Utah Array with Two HH neurons')
xlabel('Time (ms)');
ylabel('Recorded Potential (uV)');
hold off

```



```
% SIMULATE UTAH RECORDING OF TWO CONNORS STEVENS NEURONS
```

```
clear
```

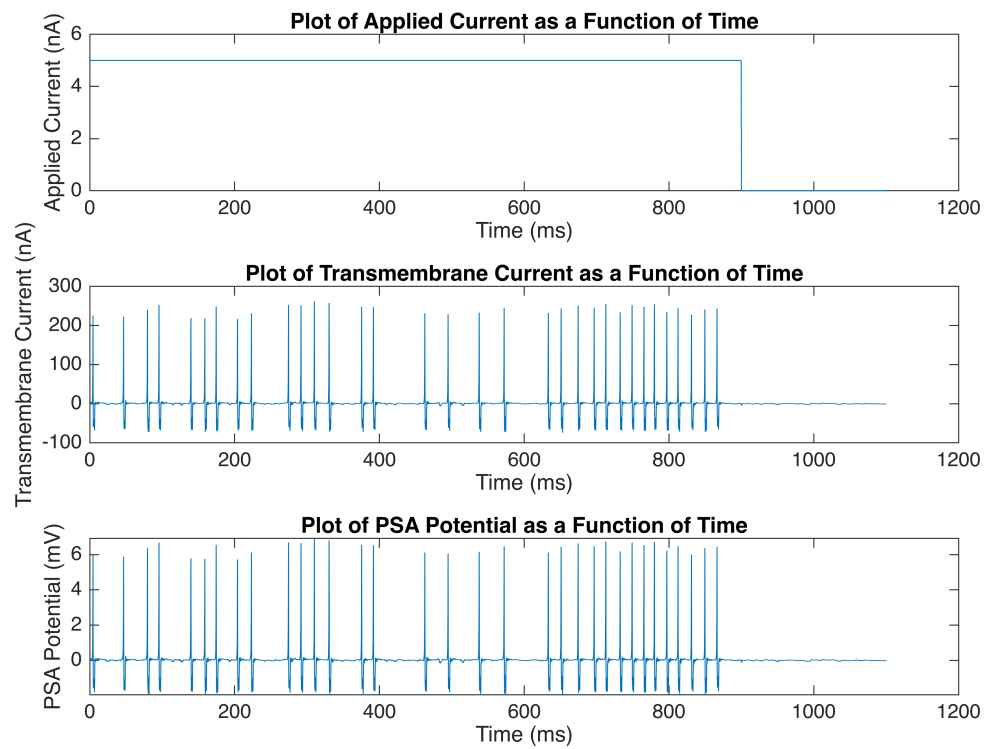
```
% Time Vector
```

```
dt=0.00002;           % time step (s)
tmax=1.1;              % max time value 1 second (s)
tvect= 0:dt:tmax;      % time vector, a second
```

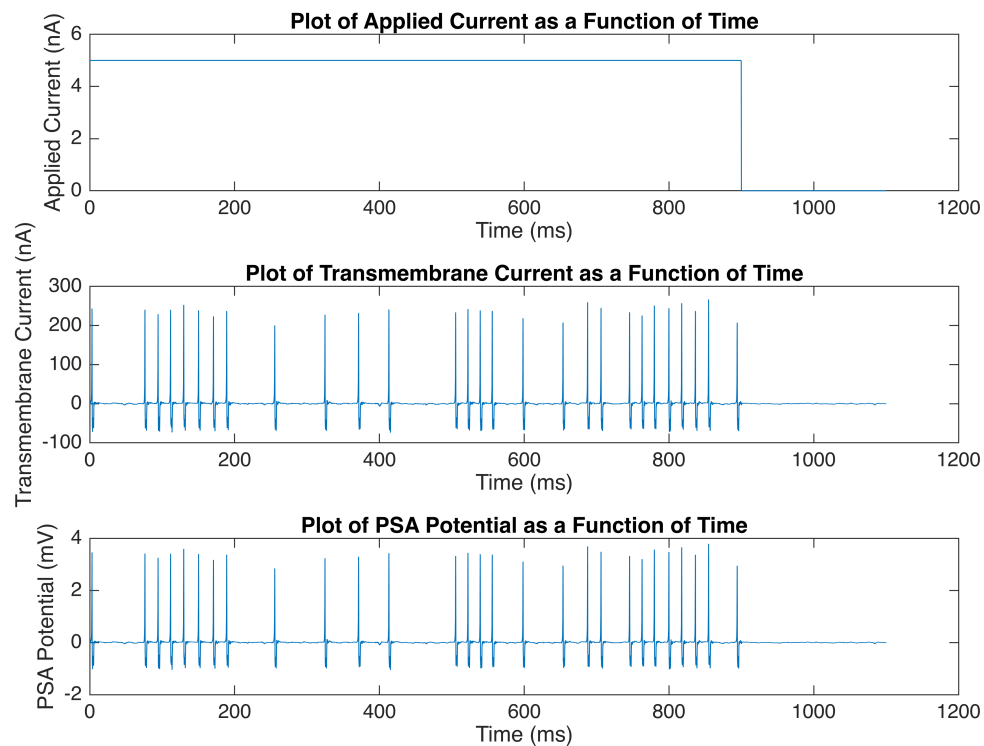
```
% LFP Noise Vector
```

```
hi = 16;               % noise scalar
LFP_vec = randn(1, length(tvect)); % empty LFP vector
LFP_vec = LFP_vec*hi;  % scaled LFP vector
```

```
V1 = PSA2(5,7,0.0002); % run PSA2 (Connors Stevens) simulation for a
neuron 7 microns away with a 5 nA applied current with noise.
```



```
V2 = PSA2(5,13,0.0002); % run PSA2 (Connors Stevens) simulation for a
neuron 15 microns away with a 5 nA applied current with noise.
```



```

V3 = V1+V2; % Sum the voltage trace outputs

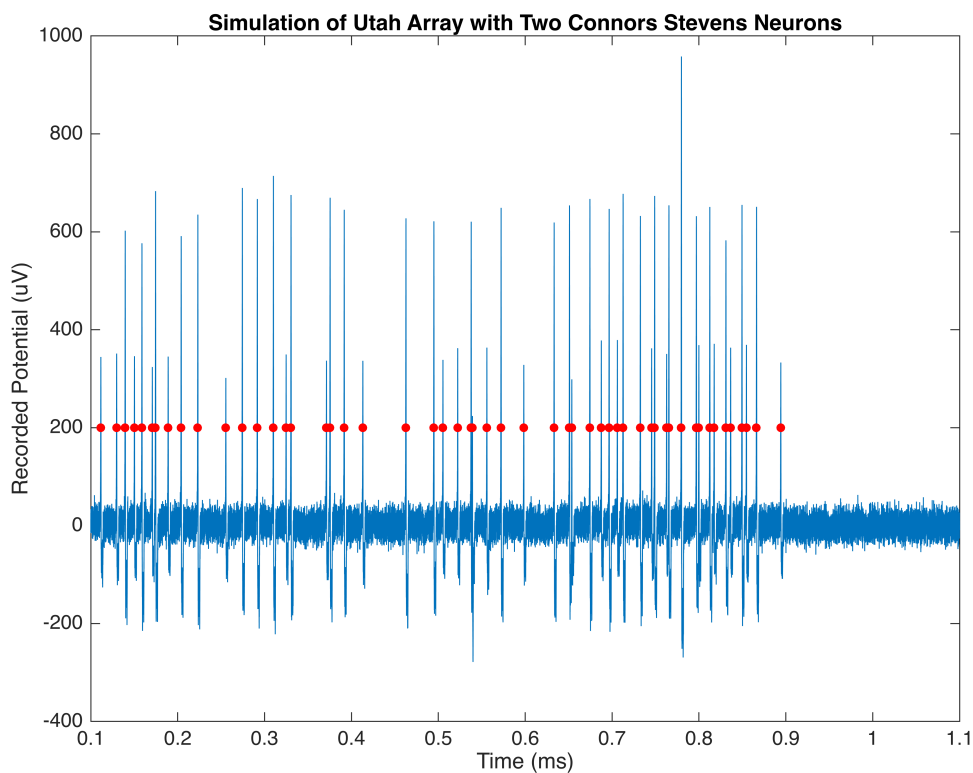
V3 = V3*100 + LFP_vec; % Add LFP noise, final trace

start_time = 0.1; % Start time to remove (in seconds)
start_index = find(tvect >= start_time, 1); % Find the index corresponding
to the start time
V3 = V3(start_index:end);
tvect = tvect(start_index:end); % Remove the time values before the start
index

spikeTimes = detectSpikes(V3,tvect,200); % Detect spikes

%Plot
figure;
plot(tvect,V3);
hold on
plot(spikeTimes, 200*ones(size(spikeTimes)), 'r.', 'MarkerSize',
15);title('Simulation of Utah Array with Two Connors Stevens Neurons')
xlabel('Time (ms)');
ylabel('Recorded Potential (uV)');

```



```

function [j] = PSA1(I,r,noise)
% Point Source Approximation based on HODGKIN-HUXLEY
% inputs are I in nA and r (distance from recording electrode) in microns,

% HH Parameters

Gmax_Na=12e-6;      % maximum sodium conductance (S)
Gmax_K=3.6e-6;      % maximum delayed rectifier conductance (S)
G_L=30e-9;          % leak conductance (S)
E_Na=45e-3;         % sodium reversal potential (V)
E_K=-82e-3;         % potassium reversal potential (V)
E_L=-60e-3;         % leak reversal potential (V)
Cm=100e-12;         % membrane capacitance (F)

% Point Source Approximation Values

sigma = 0.43;       % Siemens / m^2 medium conductivity
R = r * 10^-7;      % in meters (one micron = 1e-6 meters)
q = noise;          % noise scalar

dt=0.00002;         % time step (s)
tmax=1.1;           % max time value (s)
tvect=0:dt:tmax;    % time vector (s)
Vm=zeros(size(tvect)); % membrane potential Vm vector
Vm(1)=-0.065;       % set initial condition (V)
m=zeros(size(tvect)); % gating variable m vector
m(1)=0.05;          % set initial condition
h=zeros(size(tvect)); % gating variable h vector
h(1)=0.5;           % set initial condition
n=zeros(size(tvect)); % gating variable n vector
n(1)=0.35;          % set initial condition

dVmdt = zeros(size(tvect)); % store value of dVdt for PSA
Im = zeros(size(tvect));    % empty vector for transmembrane current
theta = zeros(size(tvect)); % point source approximation for EXTRACELLULAR
POTENTIAL

step_time=0.9;        % step duration (s)
start_time=0;         % start time of the step (s)
step_Iapp= I * 10^-10; % applied current value (A)
Iapp_vect=zeros(size(tvect)); % applied current vector (A)
step_indices = tvect >= start_time & tvect < (start_time + step_time); %
find indices corresponding to step duration
Iapp_vect(step_indices)=step_Iapp; % set step current for the specified
duration

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for i=2:length(tvect) % integrate over time
    dVmdt=(1/Cm) * (G_L*(E_L-Vm(i-1)) +
    Gmax_Na*((m(i-1))^3)*h(i-1)*(E_Na-Vm(i-1)) + Gmax_K*((n(i-1))^4)*(E_K-
    Vm(i-1)) + Iapp_vect(i-1)); % define Vm rate of change
    Vm(i)=Vm(i-1)+dVmdt*dt +randn()*noise; % update Vm

    dmdt=((10^5)*(-Vm(i-1)-0.045))/(exp(100*(-Vm(i-1)-0.045))-1)*(1-
    m(i-1)) - (4*(10^3)*exp((-Vm(i-1)-0.070)/0.018))*m(i-1); % define m rate
of change
    m(i)=m(i-1)+dmdt*dt; % update m

    dhdt=(70*exp(50*(-Vm(i-1)-0.070)))*(1-h(i-1)) - ((10^3)/(1+exp(100*(-
    Vm(i-1)-0.040))))*h(i-1); % define h rate of change
    h(i)=h(i-1)+dhdt*dt; % update h

    dndt=((10^4)*(-Vm(i-1)-0.060))/(exp(100*(-Vm(i-1)-0.060))-1)*(1-
    n(i-1)) - (125*exp((-Vm(i-1)-0.070)/0.08))*n(i-1); % define n rate of
change
    n(i)=n(i-1)+dndt*dt; % update n

    Im(i-1) = dVmdt(i-1)*Cm; % calculate Im
    theta(i-1) = Im(i-1)/(4*pi*sigma*R); %calculate PSA potential

end

% Plot
figure;
subplot(3,1,2);
plot(tvect*10^3,Im*10^10);
title('Plot of Transmembrane Current as a Function of Time')
xlabel('Time (ms)');
ylabel('Transmembrane Current (nA)');

subplot(3,1,1);
plot(tvect*10^3,Iapp_vect*10^10);
title('Plot of Applied Current as a Function of Time')
xlabel('Time (ms)');
ylabel('Applied Current (nA)');

subplot(3,1,3);
plot(tvect*10^3,theta*10^3);
title('Plot of PSA Potential as a Function of Time')
xlabel('Time (ms)')
ylabel('PSA Potential (mV)')
j = theta*10^3;
end

function [V] = PSA2(I,r,noise)
% Point Source Approximation based on Connors Stevens Model
% inputs are I in nA and r (distance from recroding electrode) in microns,

```



```

% and noise

% Connors Stevens Parameters
Gmax_Na=12e-6;      % maximum sodium conductance (S)
Gmax_K=3.6e-6;     % maximum delayed rectifier conductance (S)
G_L=30e-9;         % leak conductance (S)
E_Na=45e-3;        % sodium reversal potential (V)
E_K=-82e-3;        % potassium reversal potential (V)
E_L=-60e-3;        % leak reversal potential (V)
Cm=100e-12;        % membrane capacitance (F)

Gmax_A=25e-9;      % A-current conductance (S)
E_A=-70e-3;        % A-current reversal potential (V)

% Initialize Vectors
dt=0.00002;        % time step (s)
tmax=1.1;          % max time value (s)
tvect=0:dt:tmax;   % time vector (s)
Vm=zeros(size(tvect)); % membrane potential Vm vector
Vm(1)=-0.065;      % set initial condition (V)
m=zeros(size(tvect)); % gating variable m vector
m(1)=0.05;         % set initial condition
h=zeros(size(tvect)); % gating variable h vector
h(1)=0.5;          % set initial condition
n=zeros(size(tvect)); % gating variable n vector
n(1)=0.35;         % set initial condition
a=zeros(size(tvect)); % gating variable a vector
a(1)=0.05;         % set initial condition
b=zeros(size(tvect)); % gating variable b vector
b(1)=0.05;         % set initial condition

%PSA Values
sigma = 0.43;      % Siemens / m^2 medium conductivity
R = r * 10^-7;     % in meters (one micron = 1e-6 meters)
w = noise;         % noise scalar

step_time=0.9;      % step duration (s)
start_time=0;       % start time of the step (s)
step_Iapp= I * 10^-10; % applied current value (A)
Iapp_vect=zeros(size(tvect)); % applied current vector (A)
step_indices = find(tvect >= start_time & tvect < (start_time +
step_time)); % find indices corresponding to step duration
Iapp_vect(step_indices)=step_Iapp; % set step current for the specified
duration

dVmdt = zeros(size(tvect)); % store value of dVdt for PSA
Im = zeros(size(tvect));    % empty vector for transmembrane current

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```

theta = zeros(size(tvect)); % point source approximation for EXTRACELLULAR
POTENTIAL

for i=2:length(tvect) % integrate over time

    dVmdt(i-1)=(1/Cm) * (G_L*(E_L-Vm(i-1)) +
Gmax_Na*((m(i-1))^3)*h(i-1)*(E_Na-Vm(i-1)) + Gmax_K*((n(i-1))^4)*(E_K-
Vm(i-1)) + Gmax_A*((a(i-1))^3)*b(i-1)*(E_A-Vm(i-1)) + Iapp_vect(i-1)); %
define Vm rate of change
    Vm(i)=Vm(i-1)+dVmdt(i-1)*dt + randn()*w; % update Vm

    dmdt=(( (10^5)*(-Vm(i-1)-0.045))/(exp(100*(-Vm(i-1)-0.045))-1))*(1-
m(i-1)) - (4*(10^3)*exp((-Vm(i-1)-0.070)/0.018))*m(i-1); % define m rate
of change
    m(i)=m(i-1)+dmdt*dt; % update m

    dhdt=(70*exp(50*(-Vm(i-1)-0.070)))*(1-h(i-1)) - ((10^3)/(1+exp(100*(-
Vm(i-1)-0.040))))*h(i-1); % define h rate of change
    h(i)=h(i-1)+dhdt*dt; % update h

    dndt=(( (10^4)*(-Vm(i-1)-0.060))/(exp(100*(-Vm(i-1)-0.060))-1))*(1-
n(i-1)) - (125*exp((-Vm(i-1)-0.070)/0.08))*n(i-1); % define n rate of
change
    n(i)=n(i-1)+dndt*dt; % update n

    dadt=((0.3)-a(i-1))/0.0005; % define h rate of change
    a(i)=a(i-1)+dadt*dt; % update a

    dbdt=((0.2)-b(i-1))/0.0005; % define n rate of change
    b(i)=b(i-1)+dbdt*dt; % update b

    Im(i-1) = dVmdt(i-1) * Cm; % calculate Im
    theta(i-1) = Im(i-1)/(4*pi*sigma*R); %calculate PSA potential

end

% Plot
figure;
subplot(3,1,2);
plot(tvect*10^3,Im*10^10);
title('Plot of Transmembrane Current as a Function of Time')
xlabel('Time (ms)');
ylabel('Transmembrane Current (nA)');

subplot(3,1,1);
plot(tvect*10^3,Iapp_vect*10^10);
title('Plot of Applied Current as a Function of Time')
xlabel('Time (ms)');
ylabel('Applied Current (nA)');

```

```

subplot(3,1,3);
plot(tvect*10^3,theta*10^3);
title('Plot of PSA Potential as a Function of Time')
xlabel('Time (ms)')
ylabel('PSA Potential (mV)')
V = theta*10^3;
end

function [spikeTimes] = detectSpikes(V,tvect,t)

% spike detection

spikeThreshold = t;    % Threshold for detecting spikes

isSpiking = false;    % Initialize spike detection flag
spikeTimes = [];      % Initialize spike times array
spikeAmplitudes = []; % Initialize spike amplitudes array

for i = 1:length(V)
    if V(i) > spikeThreshold && ~isSpiking
        isSpiking = true;
        spikeTimes = [spikeTimes, tvect(i)]; % Store spike time
    elseif V(i) < -30e-3 && isSpiking
        isSpiking = false;
    end
end
end
end

```